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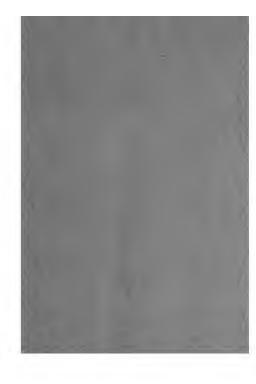
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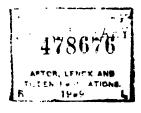
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FORMERLY PROPESSOR OF NATURAL PHILOSOPHY AND ASTRONOMY
IN UNIVERSITY COLLEGE, LONDON.

WITH THIRTY-SEVEN PLATES, AND UPWARDS OF TWO HUNDRED ILLUSTRATIONS ON WOOD.

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AUTHOR'S PREFACE.

To supply the means of acquiring a competent knowledge of the methods and results of the physical sciences, without any unusual acquaintance with mathematics, has been the purpose of the Author in the composition of this series of treatises. The methods of demonstration and illustration have been adopted with this view. It is, however, neither possible nor desirable invariably to exclude the use of mathematical symbols.

Some of these, expressing mere arithmetical operations effected upon numbers, are easily understood by all persons to whom such a work as the present is addressed, and, as they express in many cases the relations of quantities and the laws which govern them with greater brevity and clearness than ordinary language, to exclude the use of them altogether would be to deprive the reader of one of the most powerful aids to the comprehension of the laws of nature.

Nevertheless such symbols are used sparingly, and never without ample explanation of their signification. The principles of the sciences are in the main developed and demonstrated in ordinary and popular language. The series has been compiled with the view of affording that amount of information on the several subjects comprised in it which is demanded by the student in law and in medicine, by the engineer and artisan, by the superior classes in schools, and by those who, having already entered on the active business of life, are still desirous to sustain and extend their knowledge of the general truths of physics, and of those laws by which the order and stability of the material world are maintained.

It is well known that many students who enter the Universities in. (vii)

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those of Saturn by MM. Dawes and Schmidt; among cometary objects to the magnificent drawings of Enckés comet by Struve, and those of Halley's comet by MM. Struve, Maclear, and Smith; and among stellar objects to the splendid selection of stellar clusters and nebulæ which are reproduced from the originals of the Earl of Rosse and Sir John Herschel. In fine, among the illustrations now produced for the first time in an elementary work, the remarkable drawings of solar spots by Pastorff and Capocci ought not to be passed without notice.

To have entered into the details of the business of the observatory, beyond those explanations which are necessary and sufficient to give the reader a general notion of the processes by which the principal astronomical data are obtained, would not have been compatible with the popular character and limited dimensions of such a treatise as the present.

It has, nevertheless, been thought advisable to append to this volume a short notice of the most remarkable instruments of observation, accompanied by well executed drawings of them, the originals for some of which have been either supplied by or made under the superintendence of the eminent astronomers under whose direction the instruments are placed.

In the composition of this part of the series, it has been the good fortune of the author to detect several errors of considerable importance which have been hitherto almost universally disseminated in elementary works and under the authority of the most eminent names. Several examples of this will be noticed by the reader, among which we may refer more particularly to the Uranography of Saturn, a subject which has been hitherto completely misapprehended, phenomena being described as manifested on that planet which are demonstrably impossible.* The correction of other errors less striking, though of great scientific importance, will be found in the chapter on Perturbations, and in other parts of the treatise.

This series of elementary treatises consists of three courses, which are saleable separately, and are as independent each of the others as the nature of the subject allows.

[•] See a Memoir, by the Author, on the Uranography of Saturn, in Vol. XXII. of the Memoirs of the Royal Astronomical Society, London, Sept. 1853.

erences in it are made to the numbers of the to those of the pages, and it will be found con that the first paragraph of the second course is the third 2160. The paragraphs being number roughout the three courses, it has not been necessed make any reference to the courses or volumes. Il be found that this Index, combined with the Contents, will give to the entire series all the unpendious Encyclopædia of Natural Philosophy

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HAND-BOOK

OF

NATURAL PHILOSOPHY

AND

ASTRONOMY.

THIRD COURSE. >

BOOK THE FIRST.

METEOROLOGY.

CHAPTER I.

TERRESTRIAL HEAT.

2160. Insufficiency of thermal observations. — To ascertain the laws which regulate the distribution of heat and the periodical vicissitudes of temperature on and below the surface of the earth and in the superior strata of the atmosphere, is a problem of which the complete solution would require a collection of exact thermal observations, made not only in every part of the earth, but for a long series of years, not to say ages. Experimental research has not yet supplied such data. Observations on temperature made at periods even so recent as those within which physical science has been cultivated with more or less ardour and success, were in general scattered and unconnected, and marked neither by system nor precision. It was only since the commencement of the present century that observations on terrestrial heat were accumulated in sufficient quantity, and directed with the skill and precision indispensable to render them the source from which the laws of temperature could be evolved.

The exteriments and observations of Humboldt, and the profound the states of Fourier and Laplace, supplied at once the state of Fourier and Laplace, supplied at once the state of the whole of the state of physics, the state of the whole others have been carried to the state of the document of the state of the state

The superficial temperature.—The superficial temperature of the corn wards with the latitude, gradually decreasing in

price in gift in the equator towards the poles.

It is some with the elevation of the point of observation, decrees and the second of t

At a given actuals at in given elevation the temperature varies with the commerce of the surface, according as the place of observation is an scalar lamit and if on land, according to the nature, predictions of the surface, such as its inclination or aspect.

21/2 At a given place the temperature undergoes two principal periodic variations, diurnal and

The temperature falling to a minimum at a certain moment near sources, augments until it attains a maximum, at a certain moment after the sun has passed the meridian. The temperature then gradually falls until it returns to the minimum in the morning.

This diurnal thermometric period varies with the latitude, the elevation of the place, the character of the surface, and with a great variety of local conditions, which not only affect the hours of the maximum, minimum, and mean temperatures, but also the difference between the maximum and minimum, or the extent of the variation.

2163. Annual thermometric period. — The annual thermometric period also varies with the latitude, and with all the other conditions

that affect the thermal phenomena.

In order to be enabled to evolve the general thermal laws from phenomena so complicated and shifting, it is above all things necessary to define and ascertain those mean conditions or states, round which the thermometric oscillations take place.

2164. The mean diarnal temperature.—This is a temperature so taken between the extremes, that all those temperatures which are superior to it shall exceed it by exactly as much as those which are inferior in shall fall short of it.

To render this more clear, let us suppose that the temperature is observed every second in twenty-four hours. This would give 86,400 observed temperatures. Suppose, that of these 43,000 are above, and 43,400 below the mean temperature. If, then, the mean temperature be subtracted from each of those above it, and if each of those below it be subtracted from it, the sum of the remainders in the one case must be equal to the sum of the remainders in the otber.

This is equivalent to stating that the mean temperature, multiplied by 86,400, will give the same result as would be obtained by adding

together all the 80,400 observed temperatures.

But the thermometric column is not subject to such rapid changes as to show any observable difference of elevation from second to second, nor even from minute to minute. If its height be observed every hour, the mean diurnal temperature will be obtained by adding together the twelve horary temperatures, and dividing their sum by But even this is not necessary, and the same result is more easily obtained, either by taking the sum of the temperatures at sunrise, at 2 P. M., and at sunset, and dividing the result by 3, or more simply still by adding together the maximum and minimum temperatures, and taking half their sum. Whichever of these methods be adopted, the same result very nearly will be obtained. [The second is the method adopted at the Observatory of Paris.]

2165. The mean temperature of the month. — This is found by dividing the sum of the mean diurnal temperature by the number

of days.

2166. The mean temperature of the year. — This may be found

by dividing the sum of the mean monthly temperatures by 12.

2167. Month of mean temperature.—It is found that in each climate there is a certain month of which the mean temperature is identical with the mean temperature of the year, or very nearly so. This circumstance, when the month is known, supplies an easy method of observing the mean temperature of the year. In the climate of Paris, this month is October.

[The mean temperature of the year may also be found by taking the mean of the temperatures corresponding to a single hour of the

day, which, for the latitude of Paris, is 9 o'clock, A. M.]

2168. The mean temperature of the place. — The mean annual temperature being observed in a given place for a series of years, the comparison of these means, one with another, will show whether the mean annual temperature is subject to variation, and, if so, whether the variation is periodic or progressive. All observations hitherto made and recorded tend to support the conclusion, that the variations of the mean annual temperature are, like all other cosmical phenomena, periodic, and that the oscillations are made within definite limits and definite intervals. There exists, therefore, for every place, another mean temperature superior to the annual, and which is called the mean temperature of the place. This is obtained by adding together the mean annual temperatures of all the years which constitute the thermometric period, and dividing the sum thus obtained by the number of years.

But even though the period of the variation of the mean annual temperature be not known, a near approximation to the mean temperature of the place may be obtained by adding together any attainable number of mean annual temperatures and dividing their sum The probable accuracy of the result will be by their number. greater, the less the difference between the temperatures computed.

Thus it was found by a comparison of thirty mean annual temperatures at Paris, that the mean was 51° 44, and that the difference between the greatest and least of the mean annual temperatures was It may therefore be assumed that 51°.44 does not differ by so much as two-tenths of a degree from the true mean tempera-

ture of that place.

Observation, however, has been hitherto so limited, both as to extent and duration, that this thermal character has been determined for a very limited number of places. Indications, nevertheless, have been obtained sufficiently clear and satisfactory to enable Humboldt to arrive at some general conclusions, which we shall now briefly state.

2169. Isothermal lines. — In proceeding successively along the same meridian from the equator towards the pole, the mean temperature decreases generally, but not regularly nor uniformly. some points it even happens that the mean temperature augments, instead of decreasing. These irregularities are caused partly by the varying character of the surface, over which the meridian passes, and partly by the atmospheric effects produced by adjacent regions, and a multitude of other causes, local and accidental. As these causes of irregularity in the rate of decrease of the mean temperature, proceeding from the equator to the poles, are different upon different meridians, it is evident that the points of the meridians which surround the globe, at which the mean temperatures are equal, do not lie upon a parallel of latitude, as they would if the causes which affect the distribution of heat were free from all such irregularities and accidental influences.

If, then, a series of points be taken upon all the meridians surrounding the globe, having the same mean temperature, the line upon which such points are placed is called an isothermal line.

Each isothermal line is therefore characterized by the uniform mean temperature, which prevails upon every part of it.

2170. Isothermal zones. — The space included between two isothermal lines of given temperatures is called an isothermal zone.

The northern hemisphere has been distributed in relation to its

thermal condition into six zones, limited by the seven isothermal lines, characterized by the mean temperatures, 86°, 74°, 68°, 59°, 50°, 41° and 32°.

2171. The first thermal or torrid zone. - This zone is a space surrounding the globe, included between the equator and the isother-

mal line, whose temperature is 74°.

The mean temperature of the terrestrial equator is subject to very little variation, and it may therefore be considered as very nearly an isothermal line. Its mean temperature varies between the narrow limits of 811° and 821°. [This mean, however, is modified by the great extent of the equatorial seas; under the line, the continents occupy only a sixth of the earth's circumference. Hence, in approaching the tropics, and particularly the tropic of Cancer, we must not be surprised at finding mean temperatures which sensibly exceed that of the terrestrial equator; at Pondicherry, for example, in lat. 11° 55' N., the mean is 85° 28, and at Kouka, in Africa, lat. 13° 10', the mean is 87°-26.7

2172. Thermal equator. - If, upon each meridian, the point of greatest mean temperature be taken, the series of such points will follow a certain course round the globe, which has been designated as the thermal equator. This line departs from the terrestrial equator, to the extent of ten or twelve degrees on the north and about eight degrees on the south side, following a sinuous and irregular course, intersecting the terrestrial equator at about 100°, and 160°, east longitude. - It attains its greatest distances north at Jamaica, and at a point in Central Africa, having a latitude of 15°, and east longitude 10° or 12°. The greatest mean temperature of the thermal equator is 86°.

The isothermal line having the temperature of 74° is not very singous in its course, and does not much depart from the tropies.

2173. The second thermal zone. — This zone, which is included between the isothermal parallels characterized by the mean temperatures of 74° and 68° is much more sinuous, and includes very various latitudes. At the points where it intersects the meridians of Europe, it is convex towards the north, and attains its greatest latitude in Algeria.

2174. The third thermal zone.—This zone, included between the isothermal parallels which have the mean temperatures of 68° and 59°, passes over the coasts of France upon the Mediterranean, about the latitude 43°, and from thence bends southwards, both east and west, on the east towards Nangasaki and the coasts of Japan, and on the west to Natchez on the Mississippi.

2175. The fourth thermal zone. - This zone is included between the parallels of mean temperatures 59° and 50°. It is convex to the north in Europe, including the chief part of France, and thence falls to the south on both sides, including Pekin on the east, and Philadelphia, New York, and Cincinnati on the west. It is evident from this arrangement of the fourth thermal zone, that the climate of Europe is warmer than that of those parts of the eastern and western continents which have the same latitude.

2176. The fifth thermal zone. — The fifth zone, included between the mean temperatures of 50° and 41°, is more sinuous, and includes latitudes more various even than the preceding. [By comparing the mean temperatures of Fayetteville and of Copenhagen, of Quebec and of Stockholm, of Kendal and of Berlin, we may see more and more the difference which exists between the climate of the Paris meridian, and the climates to the east and west of this meridian.]

[2176.* The sixth thermal zone. — The sixth zone is included between the mean temperatures of 41° and 32°; and it is to be regretted that we do not possess in this zone several series of observations in Siberia and the north of America. These observations would be so much the more interesting as they would enable us to trace, with some precision, the limits to which vegetation extends. However, this zone appears to be comprised between the latitudes of 60° and 70°.1

2177. The polar regions. — The circle whose area is comprised within the isothermal parallel whose mean temperature is 32°, is still less known. Nevertheless, the results of the observations made by arctic voyagers within the last twenty years, afford ground for inferring that the mean temperature of the pole itself must be somewhere from 13° to 36° below the zero of Fahrenheit, or 45° to 68° below the temperature of melting ice.

2178. Climate varies on the same isothermal line. — When it is considered how different are the vegetable productions of places situate upon the same isothermal line, it will be evident that other thermal conditions besides the mean temperature must be ascertained before the climate of a place can be known. Thus London, New York, and Pekin are nearly on the same isothermal line, yet their climates and vegetable productions are extremely different.

2179. Constant, variable, and extreme climates. — One of the circumstances which produce the most marked difference in the climates of places having the same mean temperature is the difference between the extreme temperatures. In this respect climates are

classed as constant, variable, and extreme.

Constant climates are those in which the maximum and minimum monthly temperatures differ but little; variable climates are those in which the difference between these extremes is more considerable, and extreme climates are those in which this difference is very great.

Constant climates are sometimes called insular, because the effect of the ocean in equalising the temperature of the air is such as to rive this character to the climates of islands.

180. Examples of the classification of climates.—The following ples will illustrate this classification of climates:

Places.	Mean Tempera- ture of the year.	Highest mean Monthly Tempe- rature.	Lowest mean Monthly Tempe- rature.	Difference.
	•	•		0
Funchal	68.54	75.56	62.96	12.60
London	50.86	66-92	41.72	25.20
Paris	51·08	65.80	86.14	29.16
St. Malo	54-14	64.40	87.76	26.64
New York	53.78	80-78	25.84	55.44
Pekin	54.86	84.38	24.62	59.76

Funchal offers the example of a constant or insular climate; London, Paris, and St. Malo, of a variable; and New York and Pekin of an extreme climate.

2181. Climatological conditions. — A complete analysis of those conditions on which climate depends, requires also that the epochs of the extreme temperature, and, in a word, the general distribution of heat through the seasons, should be stated. For this purpose we should have an exact record, not only of the extreme temperatures and the mean annual and monthly temperatures, but also the mean diurnal. The importance of such data in any climatological inquiries will be perceived, when it is considered that a few degrees difference in the lowest temperature will decide the question of the possibility of certain vegetable productions continuing to live, and the difference of a few degrees in the highest temperature will render it possible or not for certain fruits to ripen.

2182. Table of Paris temperatures. — The following table, published by M. Arago, shows the extremes of the temperature of the air in Paris for more than a century:—

Greatest Heat.			Greatest Cold.			
Year.	Month.	Temperature Fahrenheit.	Year.	Month.	Temperature Fahrenheit.	
	•				0	
1706	August 8.	95.5	1709	January 13.	- 9.6	
1753	July 7.	96-1	1716	" 13.	1.7	
1754	. 14.	95.0	1754	" 8.	+ 6.6	
1755	" 14.	94.5	1755	" 8.	+ 30	
1793	" 8.	101.1	1768	" 8.	+1.2	
1793	" 16.	99-1	1776	" 29.	_ 24	
1800	August 18.	95.9	1783	December 30.	- 2.1	
1802	8.	97.5	1788	" 31.	- 8:1	
1803	8.	98 1	1795	January 25.	10 3	
1808	July 15.	97.2	1798	- December 26.	+ 03	
1818	" 24.	94.1	1823	January 14.	6.6 + 1	

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Observer.	Lat.	Place.	Height in Feet.	Mean Tem'- rat're
All the second	0			0
Humboldt	0 to 10	Rueupichineha	15,730	34.7
**	**	Huaupinehineha	**	84.
" minerelianies	- 16	Antisana	44	
* 4		Corazon		EL.
. "	-44	Cotopaxi	44	44
	- "	Chimborazo		54
Pentland	14 to 19	Eastern Cordilleras of Upper Peru	17.060	
	*	Western ditto ditto	16,830	
Humboldt	19 to 20	Oribaza	15.026	1
11 10 mmmm		Popocatepetl	44	
* n		Femmeblanche	66	
********	ec .	Nevado de Toluca		
Webb	27 to 36	Himalaya (south side)	12,630	
44		" (north side)	16,400	
Engelhardt and Parrot	42 to 43	Caucasus	10,550	38-3
Ramond		Pyrenees	8950	54
**	45 to 46	Alps	8760	39-2
Wahlenberg	40	Carpathlans	8500	100
Leopold de Buch	61	Peak of Saletind	5540	42-8
**	70	The Storvans-Field	3480	41.0

2188. Further results of Himboldt's and Pentland's researches.

To these general results may be added the following observations of M. Humboldt*:—

"1. The snow-line on the Andes does not vary more than 70 to 100

feet in its elevation.

"The plains of Antisana, at an elevation of 13,800 feet, clothed with a rich vegetation of aromatic herb, are covered with a depth of three or four feet of snow for five or six weeks.

"In Quito, mean temperature 48°, snow is never seen below the

elevation of 12,000 feet.

"Hail falls in the tropical regions at elevations of from 2000 to 3000 feet, but is never witnessed on the lower plateauf. It falls once in five or six years.

"No mountains have been observed in tropical Africa which rise to

the snow-line.

"2. Pentland found that from 14° to 19° lat. S. the snow-line is higher than upon the Line. This might probably be explained by the nature and configuration of the surface.

"3. Between the Line and 20° lat. N. the snow-line falls only 700 feet. The variation of the height of the snow-line increases with

the latitude.

"The summit of Mowna Roa (Owhyhee), Sandwich Islands, whose height exceeds 16,000 feet, is sometimes divested of snow.

"4. The elevation of the snow-line on the southern declivity of the Himalaya agrees with observations made in Mexico; but the northern declivity presents a singular anomaly, the snow-line rising

[&]quot; Notice on the Snow-line," Ann. de Ch. et Phys. tom. xiv. p. l.

- to 16,000 feet, a greater elevation than upon the Line. [The explanation of this phenomenon must be sought in the immenso extent of the plateaux, and in the configuration of the surface.]
- "5. The snow-line on the Caucasus is higher by 1300 feet than on the Pyrenees, which are, nevertheless, in the same latitude.
- "6. The snow-line on the chain of mountains which extends along Norway, from 58° to 70° lat., is at an elevation of 5000 feet. This great elevation in latitudes so high is probably explicable by local atmospheric phenomena, and the proximity of the sea."
- 2189. Thermal phenomena below the surface.—At a given place the surface of the ground undergoes a periodical variation of temperature, attaining a certain maximum in summer, and a minimum in winter, and gradually, but not regularly or uniformly, augmenting from the minimum to the maximum, and decreasing from the maximum to the minimum.

The question then arises as to whether this periodic variation of temperature is propagated downwards through the crust of the earth, and if so, whether in its descent it undergoes any and what modifications?

To explain the phenomena which have been ascertained by observation, let us express the mean temperature by M, and let the maximum and minimum temperatures be T and t.

If we penetrate to depths more or less considerable, we shall find that the mean temperature M of the strata will be very nearly the same as at the surface. The extreme temperatures T and t, will, however, undergo a considerable change, T decreasing, and t increasing. Thus the extremes gradually approach each other as the depth increases, the mean M remaining nearly unaltered.

2190. Stratum of invariable temperature. — A certain depth will therefore be attained at length, when the maximum temperature T, by its continual decrease, and the minimum temperature t, by its continual increase, will become respectively equal to the mean temperature M. At this depth, therefore, the periodical variations at the surface disappear; and the mean temperature M is maintained permanently without the least change.

This mean temperature, however, though nearly is not precisely equal to the mean temperature at the surface. In descending M undergoes a slight increase, and at the depth where T and t become equal to M, and the variation disappears, the mean temperature is a little higher than the mean temperature of the surface.

little higher than the mean temperature of the surface.

2191. Its depth varies with the latitude.—The depth at which the superficial vicissitudes of temperature disappear varies with the latitude, with the nature of the surface, and other circumstances. In our climates it varies from 80 to 100 feet. It diminishes in proceeding towards the equator, and increases towards the pole. The

excess of the permanent temperature at this depth above the mean

temperature at the surface, increases with the latitude.

2192. Its depth and temperature at Paris.—The same thermometer which has been kept for sixty years in the vaults of the Observatory at Paris, at the depth of eighty-eight feet below the surface, has shown, during that interval, the temperature of 11°82 Cent., which is equal to 53‡° Fahr., without varying more than half a degree of Fahr.; and even this variation, small as it is, has been explained by the effects of currents of air produced by the quarrying operations in the neighbourhood of the Observatory.

[This phenomenon was first observed by Cassini, in 1671.]

2193. Its form.—We must therefore infer, that within the surface of the earth there exists a stratum of which the temperature is invariable, and so placed that all strata superior to it are more or less affected by the thermal vicissitudes of the surface, and the more so the nearer they are to the surface, and that this stratum of invariable temperature has an irregular form, approaching nearer to the surface at some places, and receding further from it at others; the nature and character of the surface, mountains, valleys, and plains, seas, lakes, and rivers, the greater or less distance from the equator or poles, and a thousand other circumstances, imparting to it variations of form, which it will require observations and experiments much more long continued and extensive than have hitherto been made, to render manifest.

2194. Thermal phenomena between the surface and the stratum of invariable temperature. — The thermometric observations on the periodical changes which take place above the stratum of invariable temperature are not so numerous as could be desired; [and even these observations generally extend only to a depth of about 25 feet:] nevertheless, the following general conditions have been ascertained, especially in the middle latitudes of the northern hemi-

sphere:—

1. The diurnal variations of temperature are not sensible to a

greater depth than 31 feet.

[2. The mean annual temperatures of the different strata differ

little from the mean annual temperature of the air.]
3. The difference $\mathbf{r} - t$ between the extreme temperatures of the strata decreases in geometrical progression for depths measured in

arithmetical progression, or nearly so. 4. At the depth of 25 feet, $\mathbf{r} - t = 2^{\circ}$. At 50 feet $\mathbf{r} - t = 0^{\circ}$:

and at 60 to 80 feet, $T - t = 0^{\circ} \cdot 02$.

5. Since the effects of the superficial variation must require a certain time to penetrate the strata, it is evident that the epoch at which each stratum attains its maximum and minimum temperatures will be different from those at which the other strata and the surface attain them. The lower the strata the greater will be the difference

etween the times of attaining those limits, as compared with the arface. Thus, it is found, that at the depth of twenty-five feet the maximum is not attained until the surface has attained its minimum. The seasons, therefore, at this depth are reversed, the temperature of July being manifested in January, and vice versa.

2195. Thermal phenomena below the stratum of uniform temperature.—The same uniformity of temperature which prevails in the invariable stratum is also observed at all greater depths; but the temperature increases with the depth. Thus, each successive stratum, in descending, has a characteristic temperature, which never changes. The rate at which this temperature augments with the depth below the invariable stratum is extremely different in different localities. In some there is an increase of one degree for every thirty feet, while in others the same increase corresponds to a depth of 100 feet. It may be assumed, in general, that an increase of one degree of temperature will take place for every fifty or sixty feet of lepth.

The existence of a sensible heat in deep mines had long attracted the attention of observers; but there was more eagerness to explain the facts than to observe them accurately. It was explained variously; some, as Boyle, attributed it to the decomposition of pyrites, we rather, to a kind of fermentation to which recourse was often had to explain embarrassing facts; others regarded it as a confirmation or a consequence of the famous hypothesis of the central fire—an hypothesis which had been framed in the most ancient times, and which had been in turn adopted or rejected by philosophers. Genmanne appears to be the first observer who carried the thermometer to gradually increasing depths, and who discovered the important fact that the temperature augments with the depth. These experiments go back to 1740, and were made in the lead-mines of Giromagny, at three leagues from Béfort.]

2196. Temperature of springs.—The permanency of the temperatures of the inferior strata is rendered manifest by the uniformity of the temperature of springs, of which the water rises from any considerable depths. At all seasons of the year the water of such springs maintains [very nearly] the same uniform temperature; [it attains its maximum about the month of September, and its minimum in March; the difference between these two epochs reaching from 2° to 4°.]

It may be assumed that the [mean] temperature of the water proceeding from such springs is that of the strata from which they rise. In these latitudes it is found in general to be a little above the mean temperature of the air for ordinary springs; that is from those which probably rise from strata not below the invariable stratum. In higher latitudes the excess of temperature is greater [from 6° to III]

8°]; a fact which is in accordance with what has been already explained.

It has not been certainly ascertained whether the hot springs, some of which rise to a temperature little less than that of boiling water, derive their heat from the great depth of the strata from which they rise, or from local conditions affecting the strata. The uniformity of the temperature of many of them appears to favour the former hypothesis; but it must not be forgotten that other geological conditions besides mere depth may operate with the same permanency

and regularity.

2197. Thermal conditions of seas and lakes.—The anomalous quality manifested in the dilatation of water when its temperature falls below 38°8 Fahr. (1395), and its consequent maximum density at that temperature, is attended with most remarkable and important consequences in the phenomena of the waters of the globe, and in the economy of the tribes of organised creatures which inhabit them. It is easy to show that, but for this provision, exceptional and anomalous as it seems, disturbances would take place, and changes ensue, which would be attended with effects of the most injurious description in the economy of nature.

If a large collection of water, such as an ocean, a sea, or a lake, be exposed to continued cold, so that its superficial stratum shall have its temperature constantly reduced, the following effects will be

manifested.

The superficial stratum falling in temperature, will become heavier, volume for volume, than the strata below it, and will therefore sink, the inferior strata rising and taking its place. These in their turn being cooled will sink, and in this manner a continual system of downward and upward currents will be maintained, by means of which the temperature of the entire mass of liquid will be continually equalized and rendered uniform from the surface to the bottom. This will continue so long as the superficial stratum is rendered heavier, volume for volume, than those below it, by being lowered in temperature. But the superficial stratum, and all the inferior strata, will at length be reduced to the uniform temperature of 38°-8. After this the system of currents upwards and downwards will cease. The several strata will assume a state of repose. When the superficial stratum is reduced to a temperature lower than 38°8 (which is that of the maximum density of water), it will become lighter. volume for volume, instead of being heavier than the inferior strata. It will therefore float upon them. The stratum immediately below it, and in contact with it, will be reduced in temperature, but in a less degree; and in like manner a succession of strata, one below the other, to a certain depth, will be lowered in temperature by the cold of those above them, but each stratum being lighter than those below, will remain at rest, and no interchange by currents will take

see between stratum and stratum. If water were a good conctor of heat, the cooling effect of the surface would extend downands to a considerable depth. But water being, on the contrary, extremely imperfect conductor, the effect of the superficial temrature will extend only to a very limited depth; and at and below at limit, the uniform temperature of 38°-8, that of the greatest nsity, will be maintained.

This state of repose will continue until the superficial stratum falls 82°,* after which it will be congealed. When its surface is solified, if it be still exposed to a cold lower than 32°, the temperare of the surface of the ice will continue to fall, and this reduced mperature will be propagated downward, diminishing, however, in gree, so as to reduce the temperature of the stratum on which the rests to 32°, and therefore to continue the process of congelation, id to thicken the ice.

If ice were a good conductor of heat, this downward process of ngelation would be continued indefinitely, and it would not be possible that the entire mass of water from the surface to the botm, whatever be the depth, might be solidified. Ice, however, is arly as bad a conductor of heat as water, so that the superficial imperature can be propagated only to a very inconsiderable depth; d it is found accordingly, that the crust of ice formed even on the rface of the polar seas, does not exceed the average thickness of enty feet.

[2197*. Temperature and congelation of rivers.—In rivers, the stribution of heat follows other laws, on account of the motion of inslation of the liquid molecules. There results from this, in fact, continual mixture of the upper and lower strata, which tends to tablish a uniform temperature in the whole mass. Nevertheless. this motion is different at the surface and at the bottom, in the iddle of the river and near the shores, we should expect many acdental phenomena determined by these circumstances. Among ese phenomena, those of congelation alone have been observed ith any care. It has been established, by decisive experiments, at, in certain cases, congelation commences at the surface, and at, in other cases, on the contrary, it commences at the bottom.

When rivers are covered with floating ice, we may say, in general. at all these blocks, which dash against each other, and consezently assume rounded or angular forms, were originally formed at a surface: some were detached from the shores; but others were, first, only small particles, which gained size as they floated on the iter.

The formation of the first pieces is not doubtful, since we see the ores covered with a layer of ice which is constantly beaten and

^{*} For sea-water the freezing point is 284°.

broken by the waves. It is then that congelation commences, because generally the water is there less deep, and because it is in contact with the shore, which is constantly cooled by the air and radiation. The ice which is attached thereto, is cooled in its turn by this double cause, and becomes then, as the shore itself, a cold body, capable of chilling what touches it. The lump or even imperceptible fragments, into which this mass is broken, float by their specific levity: they become cooler than the water, and the drops which fall on their borders congeal instantly.

The formation of pieces of ice at the surface, and far from the shores and all solid bodies, has been called in question by some physicists: and it is difficult to prove it directly, for it may be said that the pieces which are found there were detached from the shores by the waves. But it must be admitted that the free surface of the water may be indefinitely cooled below 32°, and that thus finally, notwithstanding the agitation, it must give birth to needles of ice which subsequently grow on cooling, by contact of the air and radi-

ation.

The formation of ice at the very bottom of the water was long contested; but able observers have obtained direct proof of it, and it remains only to seek the cause. The agitated waters of rivers may doubtless fall several degrees below 32° without freezing; and when the depth is not great, the whole thickness of the liquid stratum may participate in this depression of temperature. The solid substances at the bottom at length participate in it themselves by their prolonged contact with the water, and the agitation at the bottom is less than at the surface. The inequalities of the bed form a multitude of little hollows where the water is only feebly agitated; and in them we may conceive congelation to take place, and even more rapidly than at the surface.]

2198. Thermal condition of a frozen sea.—The thermal condition, therefore, of a frozen sea, is a state of molecular repose, as absolute as if the whole mass of liquid were solid. The temperature at the surface of the ice being below the freezing point, increases in descending until it rises to the freezing point, at the stratum where the ice ceases, and the liquid water commences. Below this the temperature still augments until it reaches 38°-8, the temperature of maximum density of water, and this temperature is continued

uniform to the bottom.

2199. Process of thawing.—Let us now consider what effects will be produced, if the superficial strata be exposed to an increase of temperature. After the fusion of the ice, the temperature of the surface will gradually rise from 32° to 38°8, the temperature of greatest density. When the superficial stratum rises above 32°, it will become heavier than the stratum under it, and an interchange by currents, and a consequent equalisation of temperature, will take

place, and this will continue until the superficial stratum attains the temperature of 38°.8, when the temperature of the whole mass of water from the surface to the bottom will become uniform.

After this a further elevation of the temperature of the superficial stratum will render it lighter than those below it, and no currents will be produced, the liquid remaining at rest; and this state of repose will continue so long as the temperature continues to rise.

Every fall of the superficial temperature, so long as it continues above 38°-8, will be attended with an interchange of currents between the superficial and those inferior strata whose temperature is

above 38°.8, and a constant equalization of temperature.

2200. Depth of stratum of constant temperature in oceans and seas. — It appears, therefore, to result as a necessary consequence from what has been explained, and this inference is fully confirmed by experiment and observations, that there exists in oceans, seas, and other large and deep collections of water, a certain stratum, which retains permanently, and without the slightest variation, the temperature of 38°-8, which characterizes the state of greatest density, and that all the inferior strata equally share this temperature. At the lower latitudes, the superior strata have a higher, at the higher latitudes a lower temperature, and at a certain mean latitude the stratum of invariable temperature coincides with the surface.

In accordance with this, it has been found by observation that in the torrid zone, where the superficial temperature of the sea is about 83°, the temperature decreases with the depth until we attain the stratum of invariable temperature, the depth of which, upon the Line, is estimated at about 7000 feet. The depth of this stratum gradually diminishes as the latitude increases, and the limit at which it coincides with the surface is somewhere between 55° and 60°. Above this the temperature of the sea increases as the depth of the stratum increases, until we sink to the stratum of invariable temperature, the depth of which at the highest latitudes (at which obser-

vations have been made) is estimated at about 4500 feet.

2201. Effect of superficial agitation of the sea extends to only a small depth.—It might be imagined that the temperature of the surface would be propagated downwards, and that a thermal equalization might therefore be produced by the intermixture of the superior with the inferior strata, arising from the agitation of the surface of the waters by atmospheric commotions. It is found, however, that these effects, even in the case of the most violent storms and hurricanes, extend to no great depth, and that while the surface of the ocean is furrowed by waves of the greatest height and extent, the inferior strata are in the most absolute repose.

2202. Destructive effects which would be produced if water had not a point of maximum density above its point of congelation.—

If water followed the general law, in virtue of which all bodies become

more dense as their temperature is lowered, a continued frost might congeal the ocean from its surface to the bottom; and certainly would do so in the polar regions; for in that case the system of vertical currents, passing upwards and downwards and producing an equalization of temperature, which has been shown to prevail above 38°-8, would equally prevail below that point, and consequently the same equalization of temperature would be continued, until the entire mass of water, from the surface to the bottom, would be reduced to the point of congelation, and would consequently be converted into a solid mass, all the organized tribes inhabiting the waters being destroyed.

The existence of a temperature of maximum density at a point of the thermometric scale above the point of congelation of water, combined with the very feeble conducting power of water, whether in the liquid or solid state, renders such a catastrophe impossible.

2203. Variations of the temperature of the air at sea and on land.—The air is subject to less extreme changes of temperature at sea than on land. Thus, in the torrid zone, while the temperature on land suffers a diurnal variation amounting to 10° , the extreme diurnal variation at sea does not exceed $3\frac{1}{2}^{\circ}$. In the temperate zone the diurnal variation at sea is limited generally to about $5\frac{1}{3}^{\circ}$, while on continents it is very various and everywhere considerable. In different parts of Europe it varies from 20° to 25° .

At sea as on land the time of lowest temperature is that of sunrise, but the time of greatest heat is about noon, while on land it is

at two or three hours after noon.

On comparing the temperature of the air at sea with the superficial temperature of the water, it has been found that between the tropics the air, when at its highest temperature, is warmer than the water, but that its mean diurnal temperature is lower than that of the water. [The temperature of the air and water was observed every 4 hours by Captain Duperrey; and in 1850 observations made between 0° and 20° lat. N. and S., during his voyage round the world, the sea was found warmer than the air 1371 times, and the air warmer than the sea only 479 times.]

In latitudes between 25° and 50° the temperature of the air is very rarely higher than that of the water, and in the polar regions the air is never found as warm as the surface of the water. It is,

on the contrary, in general at a very much lower temperature.

2204. Interchange of equatorial and polar waters. — Much uncertainty prevails as to the thermal phenomena manifested in the vast collections of water which cover the greater part of the surface of the globe. It appears, however, to be admitted that the currents caused by the difference of the pressures of strata at the same level in the polar and equatorial seas, produce an interchange of waters, which contributes in a great degree to moderate the extreme thermal

effects of these regions, the current from the pole reducing the temperature of the equatorial waters, and that from the line raising the temperature of the polar waters and contributing to the fusion of the ice. A superficial current directed from the line towards the poles carries to the colder regions the heated waters of the tropics, while a counter current in the inferior strata carries from the poles towards the line the colder waters. Although the prevalence of these currents may be regarded as established, they are nevertheless modified, both in their intensity and direction, by a multitude of causes connected with the depth and form of the bottom, and the local influence of winds and tides.

2205. Polar ice. — The stupendous mass of water in the solid state which forms an eternal crust encasing the regions of the globe immediately around the poles, presents one of the grandest and most imposing classes of natural phenomena. The observations and researches of Captain Scoresby have supplied a great mass of valuable information in this department of physical geography.

2206. Extent and character of the ice fields. — Upon the coasts of Spitzbergen and Greenland vast fields of ice are found, the extent of which amounts to not less than thirty to fifty hundred square miles, the thickness varying from twenty to twenty-five feet. [Some of the fields of ice observed by Captain Scoresby were nearly a hundred miles in length, and more than half that breadth.] The surface is sometimes so even that a sledge can run without difficulty for an hundred miles in the same direction. It is, however, in some places, on the contrary, as uneven as the surface of land, the masses of ice collecting in columns and eminences of a variety of forms, rising to heights of from twenty to thirty feet, and presenting the most striking and picturesque appearances. These prodigious crystals sometimes exhibit gorgeous tints of greenish blue, resembling the topaz, and sometimes this is varied by a thick covering of snow upon their summits, which are marked by an endless variety of form and outline.

2207. Production of icebergs by their fracture. — These vast ice fields are sometimes suddenly broken, by the pressure of the subjacent waters, into fragments presenting a surface of from 100 to 200 square yards. These being dispersed, are carried in various directions by currents, and sometimes by the effect of intersecting currents they are brought into collision with a fearful crash. A ship which might chance in such a case to be found between them could no more resist their force than could a glass vessel the effect of a cannon ball. Terrible disasters occur from time to time from this cause. It is by the effects of these currents upon the floating masses of broken ice that these seas are opened to the polar navigators. It is thus that whalers are enabled to reach the parallels from 70° to

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80°, which are the favourite resort of those monsters of the deep

which they pursue.

2208. Their forms, and magnitude.— Sometimes after such collisions new icebergs arise from the fragments which are heaped one upon another, "Pelion on Ossa," more stupendous still than those which have been broken. In such cases the masses which result assume forms infinitely various, rising often to an elevation of thirty to fifty feet above the surface of the water; and since the weight of ice is about four-fifths of the weight of its own bulk of water (787), it follows that the magnitude of these masses submerged is four times as great as that which is above the surface. The total height of these floating icebergs, therefore, including the part submerged, must be from 150 to 250 feet.

2209. Sunken icebergs. — It happens sometimes that two such icebergs resting on the extremities of a fragment of ice 100 or 120 feet in length, keep it sunk at a certain depth below the surface of the water. A vessel in such cases may sail between the icebergs and over the sunken ice; but such a course is attended with the greatest danger, for if any accidental cause should detach either of the icebergs which keep down the intermediate mass while the ship is passing, the latter by its buoyancy will rise above the surface, and

will throw up the ship with irresistible force.

2210. Singular effects of their superficial fusion.—Icebergs are observed in Baffin's Bay of much greater magnitude than off the coast of Greenland. They rise there frequently to the height of 100 to 130 feet above the surface, and their total height, including the part immersed, must therefore amount to 500 or 650 feet. masses appear generally of a beautiful blue colour, and having all the transparency of crystals. During the summer months, when the sun in these high latitudes never sets, a superficial fusion is produced, which causes immense cascades, which, descending from their summit and increasing in volume as they descend, are precipitated into the sea in parabolic curves. Sometimes, on the approach of the cold season, these liquid arches are seized and solidified by the intensity of the cold without losing their form, and seem as if caught in their flight between the brink from which they were projected and the surface, and suddenly congealed. These stupendous arches, however, do not always possess cohesion in proportion to their weight, and after augmenting in volume to a certain limit, sink under their weight, and, breaking with a terrific crash, fall into the sea.

2211. Depth of polar seas.—The depth of the seas off the coast of Greenland is not considerable. Whales, being harpooned, often plunge in their agony to the bottom, carrying with them the harpoon and line attached to it. When they float they bear upon their bodies evidence of having reached the bottom by the impression they retain of it; and the length of line they carry with them in such cases

at the depth does not exceed 3000 or 4000 feet. About the f the space between Spitzbergen and Greenland the sound-

a reached 8000 feet without finding bottom.

Cold of the polar regions.— The degree of cold of the gions, like the temperature of all other parts of the globe, on the extent and depth of the seas. If there be extensive surface not covered by water, or covered only by a small se influence of the water in moderating and equalizing the are is greatly diminished. Hence it is that the temperature rath polar regions is more moderate than that of the north. ssing the latitude of the New Orcades and the New Shethich form a barrier of ice, the navigator enters an open sea, coording to all appearance, extends to the pole. Much, howll remains to be discovered respecting the physical condition regions.

Solar and celestial heat. — Whatever may be the sources and heat, the globe of the earth would, after a certain time, sed to a state of absolute cold, if it did not receive from expurces the quantity of heat necessary to repair its losses. If e were suspended in space, all other bodies from which heat supplied to it being removed, the heat which now pervades he and its surrounding atmosphere would be necessarily dissipation; and would thus escape into the infinite depths of The temperature of the atmosphere, and those of the suctrata, extending from the surface to the centre of the globe,

rus be continually and indefinitely diminished.

o such fall of temperature takes place, and as, on the conmean temperature of the globe is maintained at an invaandard, the variations incidental to season and climate being dical, and producing in their ultimate result a mutual comn, it remains to be shown from what sources the heat is which maintains the mean temperature of the globe at this le standard, notwithstanding the large amount of heat which by radiation into the surrounding space.

he bodies of the material universe, which are distributed in s numbers throughout the infinitude of space, are sources of d centres from which that physical agent is radiated in all is. The effect produced by the radiation of each of these is in the same proportion as the square of its distance in-

The fixed stars are bodies analogous to our sun, and at dispenormous that the effect of the radiation of any individual ltogether insensible. When, however, it is considered that titude of these stars spread over the firmament is so prodiat in some places many thousand are crowded together within no greater than that occupied by the disc of the full moon, of the matter of surprise that the feebleness of thermal influence, due to their immense distances, is compensated to a great extent by their countless number; and that, consequently, their calorific effects in those regions of space through which the earth passes in its annual course is, as will presently appear, not only far from being insensible, but is very little inferior to the calorific power of the sun itself.

We are, then, to consider the waste of heat which the earth suffers by radiation as repaired by the heat which it receives from two sources, the sun and the stellar universe; and it remains to explain what is the actual quantity of heat thus supplied to the earth, and

what proportion of it is due to each of these causes.

2214. Quantity of heat emitted by the sun.—An elaborate series of experiments were made by M. Pouillet, and concluded in 1838, with the view of obtaining, by means independent of all hypothesis as to the physical character of the sun, an estimate of the actual calorific power of that luminary. A detailed report of these observations and experiments, and an elaborate analysis of the results derived from them, appeared in the Transactions of the Academy of Sciences of Paris for that year.

It would be incompatible with the elementary nature and the consequent limits of this work, to enter into the details of these researches. We shall, therefore, confine ourselves here briefly to state their results.

When the firmament is quite unclouded, the atmosphere absorbs about one-fourth of the heat of those solar rays which enter it vertically. A greater absorption takes place for rays which enter it obliquely, and the absorption is augmented in a certain ascertained proportion, with the increase of obliquity. It results from the analysis of the results obtained in the researches of M. Pouillet, that about forty per cent. of all the heat transmitted by the sun to the earth, is absorbed by the atmosphere, and that consequently only sixty per cent. of this heat reaches the surface. It must, however, be observed that a part of the radiant heat, intercepted by the atmosphere, raising the temperature of the air, is afterwards transmitted, as well by radiation as by contact, from the atmosphere to the earth.

By means of direct observation and experiment made with instruments contrived by him, called pyrheliometers, by means of which the heat of the solar radiation was made to affect a known weight of water at a known temperature, M. Pouillet ascertained the actual quantity of heat which the solar rays would impart per minute to a surface of a given magnitude, on which they would fall vertically. This being determined, it was easy to calculate the quantity of heat imparted by the sun in a minute to the hemisphere of the earth which is presented to it, for that quantity is the same which would be imparted to the surface of the great circle which forms the base of that hemisphere, if the solar rays were incident perpendicularly upon it.

2215. Solar heat at the earth would melt a shell of ice 100 feet thick in a year.—In this manner it was ascertained by M. Pouillet, that if the total quantity of heat which the earth receives from the sun in a year were uniformly diffused over all parts of the surface, and were completely absorbed in the fusion of a shell of ice encrusting the globe, it would be sufficient to liquefy a depth of 100 feet of such shell.

Since a cubic foot of ice weighs 54 lbs., it follows that the average annual supply of heat received from the sun per square foot of the earth's surface would be sufficient to dissolve 5400 lbs. weight of ice.

2216. Calculation of the actual quantity of heat emitted by the sun. — This fact being ascertained supplies the means of calculating the quantity of heat emitted from the surface of the sun, independ-

ently of any hypothesis respecting its physical constitution.

It is evident from the uniform calorific effects produced by the solar rays at the earth, while the sun revolves on its axis, exposing successively every side to the earth in the course of about twenty-five days, that the calorific emanation from all parts of the solar surface is the same. Assuming this, then, it will follow, that the heat which the surface of a sphere surrounding the sun at the distance of the earth would receive would be so many times more than the heat received by the earth as the entire surface of such sphere would be greater than that part of it which the earth would occupy. The calculation of this is a simple problem of elementary geometry.

But such a spherical surface surrounding the sun and concentrical with it, would necessarily receive all the heat radiated by that luminary, and the result of the calculation proves that the quantity of heat emitted by the sun per minute is such as would suffice to dissolve a shell of ice enveloping the sun, and having a thickness of 38 40 feet; and that the heat emitted per day would dissolve such a

shell, having a thickness of 55748 feet, or about 101 miles.

2217. Heat at sun's surface seven times as intense as that of a blast furnace.—The most powerful blast furnaces do not emit for a given extent of fire surface more than the seventh part of this quantity of heat. It must therefore be inferred that each square foot of the surface of the sun emits about seven times as much heat as is issued by a square foot of the fire surface of the fiercest blast furnace.

2218. Temperature of the celestial spaces.—When the surface of the earth during the night is exposed to an unclouded sky, an interchange of heat takes place by radiation. It radiates a certain part of the heat which pervades it, and it receives, on the other hand, the heat radiated from two sources, 1st, from the strata of atmosphere, extending from the surface of the earth to the summit of the atmospheric column, and 2d, from the celestial spaces, which lie outside this limit, and which receive their heat from the radiation

of the countless numbers of suns which compose the stellar universe. M. Pouillet, by a series of ingeniously contrived experiments and observations, made with the aid of an apparatus contrived by him, called an actinometer, has been enabled to obtain an approximate estimate of the proportion of the heat received by the earth which is due to each of these two sources, and thereby to determine the actual temperature of the region of space through which the earth and planets move. The objects and limits of this work do not permit us to give the details of these researches, and we must therefore confine ourselves here to the statement of their results.

It appears from the observations, that the actual temperature of space is included between the minor limit of 315°, and the major limit of 207° below the temperature of melting ice, or between —283° and —175° Fahr. At what point between these limits the real temperature lies, is not yet satisfactorily ascertained, but M. Pouillet

thinks that it cannot differ much from -224° Fahr.

2219. Heat received by earth from celestial space would melt, in a year, eighty-five feet thick of ice.—It is proved from those results, that the quantity of heat imparted to the earth in a year, by the radiation of the celestial space, is such as would liquefy a spherical shell of ice, covering the entire surface of the earth, the thickness of which would be eighty-five feet, and that forty per cent. of this quantity is absorbed by the atmosphere.

Thus the total quantity of heat received annually by the earth is such as would liquefy a spherical shell of ice 185 feet thick, of which 100 feet are due to the sun, and 85 feet to the heat which emanates

from the stellar universe.

The fact that the celestial spaces supply very little less heat to the earth annually than the sun, may appear strange, when the very low temperature of these spaces is considered, a temperature 180° lower than the cold of the pole during the presence of the sun. It must, however, be remembered that while the space from which the solar radiation emanates is only that part of the firmament occupied by the disc of the sun, that from which the celestial radiation proceeds is the entire celestial sphere, the area of which is about two hundred thousand times greater than the solar disc. It will therefore cease to create surprise, that the collective effect of an area so extensive should be little short of that of the sun.

The caloric effect due to the solar radiation, according to the calculations and observations of M. Pouillet, exceeds that which resulted from the formulæ of Poisson. These formulæ were obtained from the consideration of the variation of the temperature of the strata of the earth at different depths below the surface. M. Pouillet thinks that the results proceeding from the two methods would be brought into accordance if the influence of the atmosphere on solar heat, which, as appears from what has been explained, is very con-

siderable, could be introduced in a more direct manner into Poisson's formulæ.

2220. Summary of the thermal effects.—In fine, therefore, the researches of M. Pouillet give the following results, which must be received as mere approximations, subject to correction by future observation:

1st. That the sun supplies the earth annually with as much heat as would liquefy 100 feet thick of ice covering the entire globe.

2d. That the celestial spaces supply as much as would liquefy 85

feet thick.

8d. That 40 per cent. of the one and the other supply is absorbed by the atmosphere, and 60 per cent. received by the earth.

4th. That of the heat radiated by the earth, 90 per cent. is inter-

cepted by the atmosphere, and 10 per cent. dispersed in space.

5th. That the heat evolved on the surface of the sun in a day would liquefy a shell of ice 101 miles thick, enveloping the sun, and the intensity of the solar fire is seven times greater than that of the fiercest blast furnace.

6th. That the temperature of space outside the atmosphere of the

earth is -224° Fahr., or 256° below that of melting ice.

7th. That the solar heat alone constitutes only two-thirds of the entire quantity of heat supplied to the earth to repair its thermal losses by terrestrial radiation; and that without the heat supplied by stellar radiation, the temperature of the earth would fall to a point which would be incompatible with organic life.

CHAP. IL.

THE AIR AND ATMOSPHERIC VAPOURS.

2221. Periodical changes in the atmospheric pressure. — The periodical changes to which the pressure of the atmosphere is subject, and the principal causes which produce them, have been already briefly indicated (719. et seq.). We shall now explain more fully some of the more important of these phenomena.

It has been customary in these climates to observe and register the height of the barometric column four times a day, at 9 A. M., at noon,

at 3 P. M., and at 9 P. M.

The mean monthly and mean annual heights are obtained from a comparison of the noon observations. The diurnal period is obtained from a comparison of the morning and afternoon observations.

2222. Mean annual height of barometer. — The mean height of the barometer at Paris, obtained from observations continued from

1816 to 1836, has been ascertained to be 29.764 inches [756--]. The mean annual height during this period did not vary so much as twelve hundredths of an inch.

2223. Effect of winds on the barometric column.—It has been found that the barometric column is affected by the direction and continuance of the wind, but these effects are not the same in all localities. At Paris, the height is greatest when the wind blows from the north or north-east, and least when from the south and south-west. The extreme difference of the mean heights during such winds was found to be twenty-seven hundredths of an inch. Observations made at Metz [for nine years] by Schuster gave a like result, but with a little less difference. At Marseilles, however, no such effect has been observed, but rather a tendency to a contrary change, the height being generally above the mean in southerly winds, and below it in north-westerly.

2224. Diurnal variations of the barometer. — A long series of observations on the diurnal changes in the barometer establish the existence of two periods, a period of decrease from 9 A. M. to 8 P. M., and a period of increase from 3 P. M. to 9 P. M. The mean amount of the former, taken from eleven years' observation at Paris, was 0.0294 in., and of the latter 0.0146 in. The decrease from 9 A. M. to 3 P. M. is therefore less than the thirtieth of an inch, and the increase from 3 P. M. to 9 P. M. less than the sixtieth of an inch.

A comparison of these variations in different seasons of the year shows that the increase of the evening is subject to very minute and irregular changes, but that the changes of the decrease in the morning are both more considerable and more regular, the amount of the decrease being always least in November, December, and January, and greatest in February, March, and April, [and of an intermediate and variable value during the remaining six months of the year.]

During the night the barometer falls from 9 P. M. to 4 A.M., and

rises from 4 A. M. to 9 A. M., [when it attains its maximum.]

2225. The winds. — No meteorological phenomenon has had so many observers, and there is none of which the theory is so little understood, as the winds. The art of navigation has produced in every seaman an observer, profoundly interested in the discovery of the laws which govern a class of phenomena, upon the knowledge of which depends not only his professional success but his personal security, and the lives and property committed to his charge.

The chief part of the knowledge which has been collected respecting the causes which produce these atmospheric currents is derived, nevertheless, much more from the comparison of the registers of

observatories than from the practical experience of mariners.

2226. Winds propagated by compression and rarefaction.—Winds are propagated either by compression or by rarefaction. In the former case they are developed in the same direction in which they

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blow; in the latter case they are developed in the contrary direction. To render this intelligible, let us imagine a column of air included in a tube. If a piston inserted in one end of the tube be driven from the mouth inwards, the air contiguous to it will be compressed, and this portion of air will compress the succeeding portion, and so on; the compression being propagated from the end at which the piston enters toward the opposite end. The remote end being open, the air will flow in a current driven before the piston in the same direction in which the compression is propagated.

If we imagine, on the other hand, a piston inserted in the tube at some distance from its mouth, to be drawn outwards toward the mouth, the air behind it will expand into the space deserted by the piston, and a momentary rarefaction will be produced. The next portion of air will in like manner follow that which is next the piston, the rarefaction which begins at the piston being propagated backwards through the tube in a direction contrary to the motion of

the viston and that of the current of air which follows it.

What is here supposed to take place in the tube is exhibited on a larger scale in the atmosphere. Any physical cause which produces a compression of the atmosphere from north to south will produce a north wind; and any cause which produces a rarefaction from north

to south will produce a south wind.

2227. Effect of sudden condensation of vapour. — Of all the causes by which winds are produced, the most frequent is the sudden condensation of vapour suspended in the atmosphere. In general the atmosphere above us consists of a mixture of air properly so called, and water, either in the state of vapour, or in a vesicular state, the nature and origin of which has not yet been clearly ascertained. In either case its sudden conversion into the liquid state, and its consequent precipitation to the earth, leaves the space it occupied in the atmosphere a vacuum, and a corresponding rarefaction of the air previously mixed with the vapour cusues. The adjacent strata immediately rush in to re-establish the equilibrium of pneumatic pressure, and winds are consequently produced.

The propagation of winds by rarefaction manifested in directions contrary to that of the winds themselves, is common in the North of Europe. Wargentin gives various examples of this. When a west wind springs up, it is felt, he observes, at Moscow before it reaches Abo, although the latter city is four hundred leagues west of Moscow, and it does not reach Sweden until after it has passed

over Finland.

[Dr. Franklin appears to have been the first to observe this mode of propagation of winds and storms. He relates, in his letters, that, having wished to observe an eclipse of the moon at Philadelphia, he was prevented by a north-casterly storm, which commenced about 7 o'clock, P. M. He was surprised, some days after, to learn that at

Boston, situated about 800 miles to the north-east of Philadelphia, the storm did not commence until 11 o'clock, P. M., long after the observation of the first phases of the eclipse; and, comparing together the reports collected in the different colonies, he found that this

north-easterly storm was propagated for the south-west.]
2228. Hurricanes. — The intertropical regions are the theatre of It is there only that these atmospheric commotions are displayed in all their terrors. In the temperate zone tempests are not only more rare in their occurrence but much less violent in their In the circumpolar zone the winds seldom acquire the force which would justify the title of a storm.

The hurricanes of the warm climates spread over a considerable width, and extend through a still more considerable length. are recorded which have swept over a distance of four or five hun-

dred leagues, with a nearly uniform violence.

It is only by recounting the effects produced by these vast commotions of the atmospheric ocean, that any estimate can be formed of the force which air, attenuated and light as that fluid is, may acquire when a great velocity is given to it. In hurricanes such as that which took place at Guadaloupe on the 25th July, 1825, houses the most solidly constructed were overthrown. A new building erected in the most durable manner by the government was rased to the Tiles carried from the roof were projected against thick doors with such force as to pass through them like a cannon ball. A plank of wood 31 feet long, 9 inches wide, and an inch thick, was projected with such force as to cut through a branch of palm wood 18 inches in diameter. A piece of wood 15 feet long and 8 inches square in its cross section, was projected upon a hard paved road, and buried to a depth of more than three feet in it. A strong iron gate in front of the governor's house was carried away, and three twenty-four pounders erected on the fort were dismounted.

2229. The probable causes explained. — These effects, prodigious as they are, all arise from mechanical causes. There is no as engaged in hurricanes more subtle than the mechanical force of air in motion, and since the weight and density of the air suffer no important change, the vast momentum manifested by such effects as those described above, must be ascribed altogether to the extraordinary velocity imparted to the air by the magnitude of the local vacuum produced, as already stated, by the sudden condensation of To form some approximate estimate of this it may be stated that, in the intertropical regions, a fall of rain often takes place over a vast extent of surface, sufficient in quantity to cover it with a stratum of water more than an inch in depth. If such a fall of rain were to take place over the extent of a hundred square leagues, as sometimes happens, the vapour from which such a quantity of liquid would be produced by condensation would, at the temperature of

ily 50°, occupy a volume 100,000 times greater than that of the quid; and, consequently, in the atmosphere over the surface of 00 square leagues it would fill a space 9000 feet, or nearly two iles in length. The extent of the vacuum produced by its condention would be a volume nearly equal to 200 cubic miles, or to the plume of a column whose base is a square mile and whose height 200 miles.

2230. Water spouts and land spouts.—These phenomena, called atter or land spouts according as they are manifested at sea or on and, consist apparently of dense masses of aqueous vapour and air, aving at once a gyratory and progressive motion, and resembling in a conical cloud, the base of which is presented upwards, and to vertex of which generally rests upon the ground, but sometimes saumes a contrary position. This phenomenon is attended with a rund like that of a waggon rolling on a rough pavement.

Violent mechanical effects sometimes attend these meteors. Large rest torn up by the roots, stripped of their leaves, and exhibiting I the appearances of having been struck by lightning, are proceed to great distances. Houses are often thrown down, unroofed, and otherwise injured or destroyed, when they lie in the course of the meteors. Rain, hail, and frequently globes of fire, like the

il lightning, also accompany them.



Fig. 669.

The various appearances exhibited by water spouts are represented in fig. 669.

No satisfactory theory has yet connected these phenomena with the

general laws of physics.

2231. Evaporation from the surface of water.—If the surface of a sea, lake, or other large collection of water, were exposed to the atmosphere consisting of pure air without any admixture of vapour, evaporation would immediately commence, and the vapour developed at the surface of the water would ascend into and mix with the atmosphere. The

ressure of the atmosphere would then be the sum of the pressures f the atmosphere, properly so called, and of the vapour suspended it, since neither of these elastic fluids can augment or diminish be pressure of the other.

The vapour developed from the surface of the water thus minling with the atmosphere, acquires a common temperature with it. his vapour, therefore, receiving thus from the air with which it is intermixed more or less heat, after having passed into the vaporous state, is superheated vapour (1496.) It has, therefore, a greater temperature than that which corresponds to its density, or, what is the same, it has a less density than that which corresponds to its temperature. Such vapour may therefore lose temperature to a certain extent without being condensed.

2232. Air may be saturated with vapour. — But if the same atmosphere continue to be suspended over the surface of water, the process of evaporation being continued, the quantity of vapour which rises into the air and mingles with it will be continually increased until it acquires the greatest density which is compatible with its temperature. Evaporation must then cease, and the air is said

to be saturated with vapour.

If the temperature of the air in such case rise, evaporation will recommence and will continue until the vapour shall acquire the greatest density compatible with the increased temperature, and will

then cease, the air being, as before, saturated.

2233. If the temperature of saturated air fall, condensation will take place.—But if the temperature fall, the greatest density of vapour compatible with it being less than at the higher temperature, a part of the vapour must be condensed, and this condensation must continue until the vapour suspended in the air shall be reduced to that state of density which is the greatest compatible with the reduced temperature.

2234. Atmosphere rarely saturated. — A fluid so light and mobile as the atmosphere, can never remain long in a state of repose, and the column of air suspended over the surface of any collection of water, however extensive, is subject to frequent change. In general, therefore, before any such portion of the atmosphere become saturated by evaporation, it is removed and replaced by another portion. It happens, consequently, that the atmosphere rarely becomes saturated.

rated by the immediate effect of evaporation.

2235. May become so by reduced temperature or intermingling strata. — The state of saturation is, however, often attained either by loss of temperature, or by the intermixture of strata of air of different temperatures and differently charged with vapours. Thus, if air which is below the point of saturation suffer a loss of heat, its temperature may fall to that point which is the highest compatible with the density of the vapour actually suspended in it. The air will then become saturated, not only by receiving any increased quantity of vapour, but by losing that caloric by which the vapour it-contained was previously superheated.

If two strata of air at different temperatures, and both charged with vapour to a point below saturation, be intermingled, they will take an intermediate temperature; that which had the higher temperature portion of its heat to that which had a lower rill likewise be intermixed and reduced to the common temperature. Now, in this case it may happen that the common temperature to which the entire mass is reduced, after intermixture, shall be either equal to or less than the greatest temperature compatible with the density of the vapour in the mass of air thus mixed. If it be equal to that temperature, the mass of air after intermixture will be saturated, though the strata before intermixture were both below saturation; and if less, condensation must take place until the density of the vapour suspended in the mixture be reduced to the greatest density compatible with the temperature.

2236. Air and vapour intermingle, though of different specific gravities.—It might be supposed that air and vapour being mixed together without combining chemically, would arrange themselves in strata, the lighter floating above the heavier as oil floats above water. This statical law, however, which prevails in liquids, is in the case of elastic fluids subject to important qualifications. The latter class of fluids have a tendency to intermingle and diffuse themselves through and among each other in opposition to their specific gravities. Thus if a stratum of hydrogen, the lightest of the gases, rest upon a stratum of carbonic acid, which is the heaviest, they will by slow degrees intermingle, a part of the hydrogen descending among the carbonic acid, and a part of the carbonic acid ascending among the hydrogen, and this will continue until the mixture becomes perfectly uniform, every part of it containing the two gases in the proportion of their entire quantities.

The same law prevails in the case of vapours mixed with gases; and thus may be explained the fact, that although the aqueous vapour suspended in the air, and having the same temperature, is always lighter bulk for bulk than the air, it does not ascend to the upper strata of the atmosphere, but is uniformly diffused through it.

2237. The pressure of air retards, but does not diminish evaporation.—It may be stated generally, that the effect of a column of air superposed upon the surface of water is only to retard, but not either to prevent or diminish, the evaporation. The same quantity of vapour will be developed as would be produced at the same temperature if no air were superposed on the water; but while in the latter case the entire quantity of vapour would be developed instantaneously, it is produced gradually, and completed only after a certain interval of time when the air is present. The quantity of vapour developed, and its density and pressure, are however exactly the same, whether the space through which it is diffused be a vacuum, or be filled by air, no matter what the density of the air may be.

The properties of the air, therefore, neither modify nor are modified

by those of the vapour which is diffused through it.

2288. When vapour intermices with air, it renders it specifically lighter.—Since, at the same temperature and pressure, the density of the vapour of water is less than that of air in the ratio of 5 to 8, it follows that when air becomes charged with vapour of its own temperature, the volume will be augmented, but the density diminished. If a certain volume of air weigh 8 grains, an equal volume of vapour will weigh 5 grains, the two volumes mixed together will weigh 13 grains, and, consequently, an equal volume of the mixture will weigh 6½ grains. In this case, therefore, the density of the air charged with vapour is less than the density of dry air of the same temperature in the ratio of 6½ to 8.

CHAP. III.

HYGROMETRY.

2239. Hygrometry. — This is the name given to that branch of meteorology which treats of the methods of measuring the elastic force and the quantity of aqueous vapour which is suspended in the atmosphere, and in which the influence of various natural bodies and physical agents upon this vapour is explained.

If the atmosphere were always charged with vapour to saturation, the pressure and density of the vapour contained in it would be immediately determined by its temperature, for there would then be the greatest pressure and density compatible with the temperature, and the pressure and density would be given by the tables (1494).

2240. The dew point. — But when the air, as generally happens, is not saturated, it becomes necessary to contrive means by which the temperature to which it must be reduced, in order to become saturated by the quantity of vapour actually suspended in it, can be determined.

Such temperature is called the DEW POINT, inasmuch as after reduction below that temperature, more or less condensation, and the consequent deposition of moisture or DEW, will take place.

2241. Method of determining the pressure and density of the answer suspended in the air.—When the actual temperature of the aid the dew point are known, the pressure and density of the

suspended in the air may be found.

respress the temperature of the air, the dew point, P the

ture T, p the pressure of the vapour which would saturate it at the temperature t, and, in fine, let p'express the pressure of the vapour actually suspended in the air.

This pressure \mathbf{r}' is greater than the pressure p, which the same vapour having the same density has at the temperature t, by that increase of pressure which is due to the increase of temperature from t to \mathbf{r} . If the increase of pressure due to one degree of augmented temperature be expressed by n, the increase due to $(\mathbf{r}-t)$ degrees will be expressed by $(\mathbf{r}-t)\times n$. Hence, we shall have

$$\mathbf{r}' = p \times \{1 + (\mathbf{r} - t) \times n\}$$

So that when p, the pressure of the saturating vapour at the dew point, is known, P', the actual pressure, can be found.

But any means by which the temperature t at the dew point can be determined, will necessarily also determine the pressure p, inasmuch as this pressure is that which corresponds to vapour having the greatest density compatible with the temperature t, and is therefore given by the tables (1494). This being found, \mathbf{r}' may be computed by the preceding formula.

To find the density of the vapour actually suspended in the air, or, what is the same, the weight of water in the state of vapour contained in a cubic foot of air, let this weight be expressed by w', and let w express the weight of vapour which would saturate a cubic foot of air at the temperature T.

Since the pressure is proportional to the density when the temperature is the same, we shall have

Therefore,

$$\mathbf{w'} = \mathbf{w} \times \frac{\mathbf{p'}}{\mathbf{p}} = \frac{\mathbf{w}}{\mathbf{p}} \times p \times \{1 + (\mathbf{T} - t) \times n\}$$

By this formula, therefore, the weight w' of vapour contained in a cubic foot of air can be found, provided the weight and pressure of the vapour which would saturate it at the same temperature, its dew point, and the pressure of the vapour which would saturate it at that point, are severally known.

2242. Table of pressures and densities of saturating vapours.—
The following table, in which are given the pressure and weight of
the saturating vapour in a cubic foot of air, at the several temperatures expressed in the first column, will supply all the data necessary
for such calculations, provided only that means be obtained for determining by experiment the dew point.

Table showing the Pressure and Weight of saturating Vapour contained in a Cubic Foot of Air at Temperatures varying from —4° Fahr. to + 104° Fahr.

Temperature.	Pressure: Inches, Mercury.	Weight of Vapour in a Cubic Foot of Air.	Temperature.	Pressure: Inches, Mercury.	Weight of Vepour in a Cubic Feet of Air.
• •		Grains.	•		Grains.
— 4 ·0	∙05	1 1	66.2	·6 4	7
5∙0	-08	1 1	68.0	∙68	7
14.0	·10	1 1	69.8	.72	8
28.0	.15	2 2 2	71.6	-76	8
82· 0	.20	2	78-4 -	-81	9
83.8	.22		75.2	-86	9
85.6	.28	8	77.0	∙91	10
87.4	.24	8	78.8	-96	10
89.2	-26	8 8 8 8 8	80.6	1.02	11
41.0	-28	8	82-4	1.08	12
42.8	-80	8	84.2	1.14	12
- 44·6	.82	4	86.0	1.21	18 -
46.4	·84	4 4	87.8	1.28	14
48.2	.86	4	89.6	1.35	14
50∙0	-88	4 5 5 5	91.4	1.48	15
51∙8	•40	5	98.2	1.51	16
53⋅6	·48	5	95.0	1.59	17
55· 4	·45	5	96.8	1.68	18
57.2	•48	5	98.6	1.77	18
59∙0	·51	5 6 6	100-4	1.87	19
60.8	•54	6	102.2	1.97	20
62.6	•58	6 7	104.0	2.09	21
64.4	·61	7	I	l	ļ

2243. Example of such a calculation. — As an example of the application of the preceding formulæ, let us suppose that the temperature of the air is 77°, and that the dew point is ascertaized to be 54½°.

By the preceding table then we obtain the following data:

$$T = 77^{\circ}$$
, $p = 0.91$, $t = 54\frac{1}{2}$, $p = 0.44$.

But it appears from what has been already explained (1495), that $n = 0.002037 = \frac{1}{190}$.

Hence we find

$$P' = 0.44 \times \{1 + 22.5 \times 0.002037\} = 0.46.$$

It follows, therefore, that the actual pressure of the vapour suspended in the air is 46 per cent. of the pressure of the vapour which would saturate it.

We have also

$$v = 0.96, w = 10$$
:

And therefore

2241. Method of ascertaining the dew point.—To determine the dew point, let a thin glass or decanter be filled with water, and, immersing a thermometer in it, let it be exposed in the open air. Let it be cold water be poured into it by small quantities and mixed with it, so as to reduce its temperature by slow degrees below that of the surrounding air. A temperature will at length be attained at which a cloudy deposition of moisture will be manifested on the external surface of the glass. The temperature at which this effect first begins to be manifested is the DEW POINT.

To explain this it must be considered that the shell of air in immediate contact with the glass is reduced to the temperature of the glass, and when that temperature has been reduced so low that the vapour suspended in the air saturates it, any further diminution of temperature is attended with condensation, which is in effect manifested by the dew which then immediately begins to collect upon the

arrice of the glass.

2245. Daniell's Hygrometer. - Hygrometers have been constructed

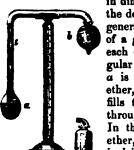


Fig. 670.

in different forms, on this principle, to indicate the dew point. That of Daniell has been most This instrument consists generally adopted. of a glass tube, having a thin bulb blown on each end of it, and being bent into the rectangular form represented in fig. 670. The bulb a is filled to two-thirds of its capacity with ether, which being boiled produces vapour which fills the tuke t and the bulb b, and escapes through a small opening in the bottom of b. In this manner the air is expelled from the ether, the tube, and the bulbs. The opening in b is then closed with the blowpipe, and the heat being removed from the bulb a, the vapour in the tube and bulb b is condensed, so

that the space within the instrument above the surface of the ether contains only the vapour of ether, which corresponds to the temperature of the fluid in the bulk a. A thermometer is previously inserted in the tube t, the bulb of which is plunged in the ether, and the bulb b is surrounded by a linen or muslin cloth, which, being saturated with ether by means of a small phial provided with a fine rectangular spout, evaporation takes place, by which the bulb b is cooled. The vapour of the ether which fills the bulb b is thus condensed in it, and more vapour flows in to fill its place from the tube t. The surface of the ether in a being thus continually released from the pressure of the vapour condensed, further evaporation and a consequent depression of the temperature of the fluid in the bulb a ensues, and this continues until the temperature of the bulb a is

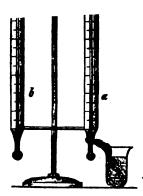


Fig. 671.

ration. Two t fig. 671,] exac are mounted on juxtaposition, enveloped in a stantly wetted 1 the atmosphere no evaporation be not saturated place from the the bulb, and a ture will be ind a certain relatio evaporation. fore, enveloped fall below the c

true temperature of the air, and the difference mometers thus becomes a measure of the rat the cloth, and thereby of the degree of dry greater the quantity of vapour with which t less will be the difference of the temperatures thermometers.

When the air is extremely dry, the different thermometers sometimes amounts to from 14° Professor August has constructed tables by

the vapour suspended in Al.



and being carried round a small wheel is kept extended by suspending to its extremity a small weight. Reing hygrometric, it absorbs moisture from the atmosphere, by which it is made to expand and increase its length. This causes the wheel round which it is coiled to turn through a corresponding space, which is shown by an index d fixed upon the centre of the wheel, which plays upon a graduated arch sh.

As the vapour suspended in the air increases or diminishes, the contraction of the hair varies in corresponding manner, and the index shows the changes, indicating extreme dryness at one extremity of the scale, and extreme humidity at the other.

Tables have been constructed by which the indications of this instrument give the pressure of the vapour suspended in the air.

Fig. 672.

[2217*. General consideration of hygrometers. — The quantity of watery vapour contained in the atmosphere, at any given moment, may be determined either by what is called the chemical method, or by means of instruments called hygrometers. The chemical method consists in absorbing, by means of substances which have a great avidity for water, the vapour contained in a certain volume of air, and in determining its weight by the balance. The air is drawn by means of an aspirator through tubes filled with coarse fragments of pumice-stone, moistened with sulphuric acid. Experiment has shown that tubes of this kind completely retain the humidity of the air. Hence, the increase of weight in the tubes represents the weight of the water which existed in a volume of air equal to the capacity of the aspirator. This method does not give the quantity of humidity which exists in the air at a determinate moment, but determines, with great precision, the mean quantity which the air contained during the experiment. But it is an experiment of the laboratory, requiring time and bulky apparatus for its performance; and, consequently, does not admit of adoption in meteorological observatories. It is, however, eminently adapted to the verification of the other methods; and for this purpose, was constantly made use of by Regnault in his hygrometrical researches, some of the results of which are given below.

Hygrometers, or instruments which serve to measure the clastic force of the watery vapour contained in the air, are of three kinds, being constructed on different principles. Some act by condensation, others by evaporation, and others again by absorption. The first are called condensing or dew point hygrometers—the second, wet-and-dry bulb hygrometers or psychrometers—and the third, absorption

hygrometers.

The state of this control of the state of th

to recent the distribution of its model application by the emergency of a Table Decreasing approximated 2245 is which, never manner to be absorbed to be a more street in its liable to the the write of estimated at The arribation of the other in the bulb s the many makes have at the surface of the begand where the empominute of the little and the confluences of hear, there is alwith a marrier and makes of temperature between the upper and to the layers in which s -- - r s with the the next temperature may differ time of the man man of which the first deposit of dew depends to the first deposit of dew depends to the first deposit of the the many the community and the present influences the bypromoted said of the art of Respectives, especially if the obkin nie it geleit wiere wet nem tenz wicht zie thermometer the reserve to the period of Several The evaporation of a great country of the makes maked on the back find a space extremely team to that it with the respect of hew upon the balb a is deter-In feet, and the second of rountegarity crused by this in the neighneutral stream mass comes of a release shall be change in the hygro-metric state of the act. I And hashly, the relinary commercial state for mass as more as newscatte its weight of water; and this where the agreement is great than by the vapour of ether into a space many takes to that it whose the deposit of dew is determined,

Forces of products country which is free from most of the frequent of products country which is free from most of the frequent of products country which is inserted a metallic bar b, having the first paper surface a grown containing mercury, into which dips a delicate thermometer is suspended from a support d: the thermometer teling mirrorle along the grown. The whole rests upon a wooden stand of the of the vertical sides of the bar b presents a surface of polished silver; sai the temperature of this bar, which is about zero near its insertion into the few gradually rises towards the other end. There will be a deposit of dew on this polished surface, terminating abruptly at a certain vertical line whose temperature will be that of the dew point. This temperature is easily asingly by placing the bulb of the thermometer opposite that line;

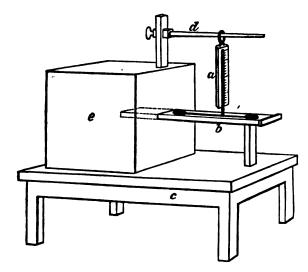


Fig. 673.

and hence this instrument allows of the dew point being read off at any moment by the observer.

But of all condensing hygrometers, that of Regnault, figs. 674 and 675, is the most perfect. It consists of a thimble, $a \ b \ c \ (fig.$ 674), made of silver, respection, and perfectly polished, $\frac{1}{8}$ inch in depth, and $\frac{1}{10}$ ths of an inch in diameter, which is fitted tightly upon a glass tube cd, open at both ends. The tube has a small lateral The upper opening of the tube is closed by a cork, which is traversed by the stem of a very sensible thermometer occupying its axis; the bulb of the thermometer is in the centre of the silver thimble. A very thin glass tube, fg, open at both ends, traverses the same cork, and descends to the bottom of the thimble. Ether is poured into the tube as high as mn, and the tubulure t is placed in communication by means of a leaden tube d, with an aspirator jar, six or eight pints in capacity, filled with water. aspirator jar is placed near the observer, while the hygrometer is kept as far from his person as is desirable. On allowing water to run from the aspirator jar, air enters by the tube gf, passing bubble by bubble through the ether, which it cools by carrying away vapour: the refrigeration is the more rapid the more freely the water is allowed to flow; and the whole mass of ether presents a sensibly uniform temperature, as it is briskly agitated by the passage of the bubbles of air. The temperature is sufficiently lowered in less than

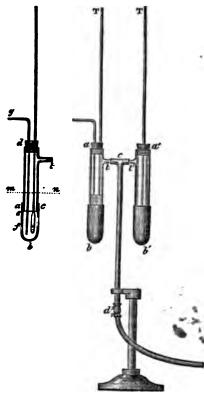


Fig. 674.

Fig. 675.

a minute to determine an abundant deposit of dew. The thermometer is then observed through a little telescope. Suppose that it is read off at 50°: this temperature is evidently somewhat lower than what corresponds exactly to the air's humidity. By alosing the stopcock of the aspirator, the passa air is stopped, the disappears in a fe conds, and the th meter again rises. pose that it marks 526 this degree is above the dew point. The stoneock of the aspirator is then opened very slightly, so as to determine the passage of a very small stream of air-bubbles through the ether. thermometer tinues, notwithstanding. to, rise, the stopcock is opened further, and the thermometer brought down to 51°.8: by shutting the stopcock slightly, it is easy to stop the falling range, and make the

thermometer remain stationary at 51°-8, as long as is desired. If no dew forms after the lapse of a few seconds, it is evident that 51°-8 is higher than the dew point. It is brought down to 51°-6, and maintained there by regulating the flow. The metallic surface being now observed to become dim after a few seconds, it is concluded that 51°-6 is too low, while 51°-8 is too high. A still greater approximation may be made, by now finding whether 51°-7 is above or below the point of condensation. These operations may be executed in a very short time, after a little practice; three or four minutes being found sufficient, by M. Regnault, to determine the dew point to within about $\frac{1}{10}$ th of a degree, Fahr. A more considerable fall of temperature may be obtained by means of this than the griginal

instrument of Daniell, with the consumption of a much less quantity of other; indeed, that liquid may be dispensed with entirely, and alcohol substituted for it. The thermometer T', to observe the temperature of the air during the experiment, is placed in a second similar glass tube and thimble a' b', also under the influence of the

It is evident from this description that Regnault's hygrometer

aspirator, but containing no ether.

obviates all of the objections to which that of Daniell is open. The thermometer indicates exactly the same temperature as the ether, and all the layers of this liquid present a uniform temperature, from the continual agitation produced by the passage of the bubbles of the metallic aide on which the dew is deposited has also the temperature as the ether, because it is very thin, and is in adiate contact with this liquid. The manipulation does not saire the observer to be close by; he may, on the contrary, be at distance of several yards, and observe the instrument with a telescope. No vapour is found near the point at which the hygrometric state is determined; and much lower temperatures may be obtained than with Daniell's hygrometer. Thus, during the greatest summer heat, Regnault succeeded in lowering the thermometer of the condenser several degrees below 32°, and covering the metallic side with a thick layer of hear frost.

2d. The psychrometer of August, which is more generally known in this country as the wet-and-dry bulb hygrometer, is perhaps the most extensively employed of all hygrometrical instruments. This has resulted, probably, from the fact, that it does not easily get out of order, and from its demanding no practical skill on the part of the observer.

The two following were the formulæ constructed by Professor August for the determination of the elastic force of the watery

vapour contained in the air.

I.
$$x = \frac{e - 0.558 (t - t) b}{512 - t}$$
,
II. $x = \frac{e - 0.558 (t - t) b}{572 - t}$;

x being the tension required of the vapour in the atmosphere in the Paris lines; e the tension in Paris lines which corresponds with the temperature of the moist thermometer; t the temperature of the dry, and t that of the moist thermometer, in degrees of Reaumur's scale; and lastly, b the altitude of the barometer in Paris lines. Formula I. serves for temperatures above 32°, and II. when the damp thermometer is covered with ice, i. c., for temperatures under 32°.

Regnault has shown (Annales de Chimie et de Physique, Tome

objects found there are not as strong radiators as the foliage and

flowers of vegetables.

2249. Hoar frost. — When the cold which follows the condensation of vapour falls below 32°, what would otherwise be DEW becomes HOAR FROST. For the same reason that dew is deposited when the temperature of the air is above the point of saturation, hoar frost may be manifested when the temperature of the air is many degrees above the point of congelation; for in this case, as in that of dew, the objects on which the hoar frost collects lose so much heat by their strong radiation, that while the atmosphere may be above 40° they will fall below 32°. In such cases, a dew is first deposited upon them which soon congeals, and forms the needles and crystals with which every observer is familiar.

The hoar frost is sparingly or not at all formed upon the naked earth, or on stones or wood, while it is profusely collected on leaves and flowers. The latter are strong, the former feeble radiators.

Glass is a good radiator. The panes of a window fall during the night to a temperature below 32°, although the air of the room be at a much higher temperature. Condensation and a profuse deposition of moisture takes place on their inner surfaces, which soon congeals and exhibits the crystallized coating so often witnessed.

The frosts of spring and autumn, which so frequently are attended with injury to the crops of the farmer and gardener, proceed generally not from the congelation of moisture deposited from the atmosphere, but from the congelation of their own proper moisture by the radiation of their temperature caused by the nocturnal radiation, which in other cases produces dew or hoar frost. The young buds of leaves and flowers in spring, and the grain and fruit in autumn, being reduced by radiation below 32°, while the atmosphere is many degrees above that temperature, the water which forms part of their composition is frozen, and blight ensues.

These principles, which serve to explain the cause of the evil, also suggest its remedy. It is only necessary to shelter the object from exposure to the unclouded sky, which may be done by matting,

gauze, and various other expedients.

2250. Fubrication of ice in hot climates.—In tropical climates the principle of nocturnal radiation has supplied the means of the artificial production of ice. This process, which is conducted on a considerable scale in Bengal, where some establishments for the purpose employ several hundred men, consists in placing water in shallow pans of unglazed pottery in a situation which is exposed to the clear sky and sheltered from currents of air. Evaporation is promoted by the porous quality of the pans which become soaked with water, and radiation takes place at the same time both from the water and the pans. Both these causes combine in lowering the

temperature of the water in the pans, which congeals when it falls below 32°.

2251. Fogs and clouds. — When the steam issuing from the surface of warm water ascends into air which is at a lower temperature, it is condensed, but the particles of water formed by such condensation are so minute, that they float in the air as would the minute particles of an extremely fine dust. These particles lose their transparency by reason of their minuteness, according to a general law of physical optics. The vapour of water is transparent and colourless. It is only when it loses the character and qualities of true vapour, that it acquires the cloudy and semi-opake appearance just mentioned.

Fogs are nothing more than such condensed vapour produced from the surface of seas, lakes, or rivers, when the water has a higher temperature than the stratum of air which rests upon it. These fogs are more thick and frequent when the air, besides having a lower temperature than the water, is already saturated with vapour, because in that case all the vapour developed must be immediately condensed, whereas, if the air be not saturated, it will absorb more or less of the vapour which rises from the water.

[Fogs are quite frequently observed in circumstances which seem, at first sight, very different from the foregoing. For example, at the time of a thaw, when the temperature of the air is sensibly higher than that of the water, very dense fogs still form on rivers, even when they are covered with ice: but appearances only are changed, the principle is the same. In fact, in this case, the warm air is saturated with humidity, and, when it comes to be mixed with the air which has been cooled by contact with the ice or other cold bodies, its vapour is condensed.]

Clouds are nothing but fogs suspended in the more elevated strata of the atmosphere. Clouds are most frequently produced by the intermixture of two strata of air, having different temperatures and differently charged with vapour, the mixture being supersaturated, and therefore being attended with partial condensation as already explained (2235).

It is generally admitted that the vapours which constitute clouds are vesicular vapours; that is to say, aggregations of little globules filled with moist air, altogether analogous to soap-bubbles. These globules are very easily distinguished by the naked eye in fogs which rise on warm water, and particularly on the surface of a black solution, as coffee. Their density is essentially greater than that of the air, on account of the liquid pellicle which forms their envelope; and it is somewhat difficult to explain how they can, notwithstanding this excess of density, remain suspended in the air. Gay-Lussac was of

opinion that the currents of warm air which rise incessantly from the earth during the day, have a great influence in determining the ascension and maintaining the suspension of clouds. Fresnel supposed that the solar heat, being absorbed by the clouds, forms out of them a species of air-balloons which rise to heights proportional to the excess of temperature. These two causes are without doubt very efficacious; but we are as yet in possession of too few data on the true constitution of clouds and on the properties of the vapours or different elements which compose them, to attempt a complete explanation of the phenomenon. We are still less able to present any thing but conjectures, more or less hazardous, on the causes which determine the form of clouds, their extent, their elevation, their colour, and all their various appearances, whose study is the object of the meteorologist.

2252. Rain. — When condensation of vapour takes place in the upper strata of the atmosphere, a fog or mist is first produced, after which the aqueous particles coalescing form themselves in virtue of the attraction of cohesion into spherules, and fall by their gravity to the earth, producing the phenomenon of rain.

2253. Rain gauge. — An instrument by which the quantity of rain which falls upon an area of given magnitude, at a given place, within a given time, is called a RAIN GAUGE or UDOMETER. [The terms PLUVIMETER and OMBROMETER are employed by some observers to denote the same instrument.]

These instruments, which vary in form, in magnitude, and in the provisions by which the quantity falling is measured and registered, consist, in general, of a cylindrical reservoir of known diameter, the bottom of which being funnel-shaped, terminates in a discharge-pipe, through which the contents pass into a close vessel. The quantity received from time to time by this vessel is measured and indicated by a great variety of expedients.

2254. Quantity of rain falling in various places.—The quantity of rain which falls in a given time at a given place, is expressed by stating the depth which it would have if it were received upon a plane and level surface, into which no part of it would penetrate.

At Paris, the average annual quantity of rain which falls, obtained from observations continued for thirty years at the Observatory, is 23.6 inches. There is, however, considerable variation in the quantities from which this average is deduced; the smallest quantity observed being 16.9 inches, and the greatest 27.9 inches.

The greatest annual fall of rain is that observed at Maranham, lat. 21° S., which is stated by Humboldt to amount to 277 inches. more than double the annual quantity hitherto observed elsewhere. The following are the annual quantities at the under-named places:-

	In.	•	In.
M. Domingo	120	Bordeaux (7 years)	33.5
Cayenne	116	Chalons (43 years)	23.5
Island Granada	112	Dijon (34 years)	27.6
Havana	91	Dieppe (8 years)	82.5
Calcutta	76 to 118	Metz (22 years)	26.0
Bombay	83 to 96	Nantes (7 years)	64.5
Martinique	87	Orange (80 years)	29.5
Sierra Leone	86	Jerwas (6 years)	50.0
Berlin	20.9	Rouen (8 years)	38.5
Brusels	19.0	St. Lo (3 years)	31.5
Florence	41.8	Toulouse (8 years)	25.0
Lyees	89.5	Basin of the Rhone (4 years)	35.0
Masstricht	86-1	Kendal	53.94
Marseilles	18-4	Dumfries	36.92
Padus	86-6	Manchester	36.14
Petersburg	18-2	Liverpool	34.12
Bone	81.2	Lancaster	39,71
Betterdam	22-4	Glasgow	21.33
Stockholm	18.7	London (Dalton)	20.69
Vienna	17-0	" (Howard)	24.90
Alais (35 years)	89.0	York	25.70
Algiers (10 years)	86-0	Edinburgh	25.00

Among the exceptional pluvial phenomena, the following may be mentioned:—

At Bombay, six inches of rain fell in a single day.

At Cayenne, ten inches fell in ten hours.

At Genoa, on the 25th of Oct. 1822, thirty inches of rain fell on the occurrence of a water spout. This is the greatest fall of rain on record.

2255. Snow. — The physical conditions which determine the production of snow are not ascertained. It is not known whether the sakes as they fall are immediately produced by the congelation of condensed vapour in the cloud whence they first proceed, or whether, being at first minute particles of frozen vapour, they coalesce with other frozen particles in falling through the successive strata of the air, and thus finally attain the magnitude which they have on reaching the ground.

The only exact observations which have been made on snow refer to the forms of the crystals composing it, which Captain Scoresby has observed with very great accuracy in his Polar Voyages, and of which he has given drawings. The flakes appear to consist of fine needles, grouped with singular symmetry. A few of the most

remarkable forms are represented in fig. 675.

[The red snow which is met with in polar regions and wherever the snows are permanent, owes its colour to a small fungus or mushroom, which has the property of vegetating in snow.]

2256. Hail.—The physical causes which produce this formidable

scourge of the agriculturist are uncertain. Hypotheses have been advanced to explain it which are more or less plausible, but which do not fulfil the conditions that would entitle them to the place of



Fig. 675.

physical causes. Volta proposed a theory, which has obtained some celebrity, and which is characterized by the ingenuity that marked every physical investigation of that great philosopher. of clouds, each charged with vapour, and with opposite electricities, are supposed to be carried by different atmospheric currents at different elevations to such a position, that one is vertically above the other, and separated from it by a stratum of the atmosphere of a certain thickness. Assuming that condensation and congelation are produced in the superior cloud, and that hailstones of small magnitude result directly from the congelation of particles of water, these fall in a shower upon the inferior cloud, where their electricity is first neutralized by an equal charge of the contrary fluid, and they are then charged with that fluid, when they are repelled upwards, and rise again to the superior, cloud, where like effects ensue, and they fall again to the inferior cloud, and so continue to rise and fall between the two clouds upon the same principle as the pith-balls move in the experiment described in (1794). The gradual increase of magnitude of the hailstones during this reverberation between the two clouds is thus explained by Volta: - When they fall from the superior upon the inferior cloud they penetrate it to a certain depth, and because of their low temperature, the vapour condenses and congeals upon their surface, thus increasing their volume. The same effect is produced when they rise again to the superior cloud, and is repeated each time that they pass to and fro from cloud to cloud, until the weight of the stones becomes so great that it resists the

electric attraction, and they then fall to the earth.

Volta also explained how two clouds might thus be charged with contrary electricities, by the effect of solar heat in producing evaporation, and by the assumption that vaporization develops positive and condensation negative electricity. This explanation is inadmissible, inasmuch as it is now established that evaporation and condensation are only attended with the development of electricity when they cause decomposition. However, as it is well ascertained that clouds are frequently charged with opposite electricities, this part of the hypothesis of Volta might be received without objection as a possibility. But even admitting this, the hypothesis cannot be regarded as more than an ingenious conjecture.

In the explanation of hail there are two difficulties, both of which have hitherto transcended all the efforts of physicists to

resolve them.

We require to know, 1st, how the cold which congeals the water, is produced; and 2d, how a hailstone which has acquired sufficient size to fall by its own weight, remains suspended in the air until it

acquires a circumference of 12 or 15 inches.

The theory of Volta just given answers only the second of these questions: it has been attempted to answer the first by saying that the cold is produced by wind. There are winds which are always accompanied by a greater or less depression of temperature: such are those which are propagated by rarefaction (2226). Observation has shown that they may produce, at the surface of the earth, a fall of thirty degrees; and there is no doubt that, in the higher regions of the atmosphere, they may cause a still greater cold. Meteorologists ought then to pay attention to this point, in order to ascertain whether the winds which bring hailstorms are or are not winds propagated by rarefaction. If the cold has not this origin, the whole difficulty remains, and other means must be sought for its solution. The theory which Volta proposed in answer to the second question is liable to some grave objections: and it is perhaps more correct to suppose that, the cold being produced by the wind, it is also the power of the wind which carries the hailstones horizontally or at least very obliquely in the atmosphere; that they thus traverse afteen or twenty leagues, and that they have no need of being suspended for a very long time, in the midst of very dense and cold clouds, to attain the enormous size which they sometimes have.

2257. The phenomena attending hailstorms.—In the absence of any satisfactory explanation of the phenomenon, it is important to secontain with precision and certainty the circumstances which attend

it, and the conditions under which it is produced.

It may then, in the first place, be considered as certain that the 111.

formation of hail is an effect of sudden electrical changes in clouds charged with vapour; for [hail ordinarily precedes thunderstorms, sometimes accompanying them, but hardly ever following them, especially if the storms are of any duration.]

Before the fall of hail, during an interval more or less, but sometimes of several minutes' duration, a rattling noise is generally heard in the air, which has been compared to that produced by shaking

violently bags of nuts.

Hail falls much more frequently by day than by night. Hail clouds have generally great extent and thickness, as is indicated by the obscuration they produce. They are observed also to have a peculiar colour, a grey having sometimes a reddish tint. Their form is also peculiar, their inferior surfaces having enormous protuberances, and their edges being indented and ragged.

These clouds are often at very low elevations. Observers on

mountains very frequently see a hail cloud below them.

It appears, from an examination of the structure of hailstones, that at their centre there is generally an opaque nucleus, resembling the spongy snow that forms sleet. Round this is formed a congealed mass, which is semi-transparent. Sometimes this mass consists of a succession of layers or strata. These layers are sometimes all transparent, but in different degrees. Sometimes they are alternately opaque and semi-transparent.

[Pouillet found that the temperature of hailstones varied from

315 to 25° Fahr.]

2258. Extraordinary examples of hailstones. — Extraordinary reports of the magnitude of hailstones, which have fallen during storms so memorable as to find a place in general history, have come down from periods of antiquity more or less remote. According to the Chronicles, a hailstorm occurred in the reign of Charlemagne, in which hailstones fell which measured fifteen feet in length by six feet in breadth, and eleven feet in thickness; and under the reign of Tippoo Saib, hailstones equal in magnitude to elephants are said to have fallen. Setting aside these and like recitals, as partaking rather of the character of fable than of history, we shall find sufficient to create astonishment in well authenticated observations on this subject.

In a hailstorm which took place in Flintshire on the 9th April,

1697, Halley saw hailstones which weighed five ounces.

On the 4th May, 1697, Robert Taylor saw fall hailstones measuring fourteen inches in circumference.

In the storm which ravaged Como on 20th August, 1787, Volta

saw hailstones which weighed nine ounces.

On 22d May, 1822, Dr. Noggerath saw fall at Bonn hailstones which weighed from twelve to thirteen ounces.

It appears, therefore, certain that in different countries hailstorms

have occurred in which stones weighing from half to three quarters

of a pound have fallen.

[2258*. Disastrous hailstorm in France and Holland, in 1788.

To give some idea of how far this terrible scourge may extend, and with what velocity it may be propagated, some details will here be reported of the famous storm which traversed France and Holland on the 18th of July, 1788. This storm was, without doubt, the most disastrous and frightful, as well as the best observed, on record.

The storm was propagated simultaneously in two bands, nearly parallel, and extending from the southwest to the northeast. The eastern band was the narrowest, having the average breadth of two leagues and a quarter: that of the western was four leagues. They were separated by a band, of about five leagues in average breadth, which received only an abundant rain. To the east of the eastern band, and to the west of the western band, there was also much rain, but over an extent not well determined. Each band had a total length of more than 200 leagues. All points in this immense extent were not struck at once; but it was found, on comparing the times, that the storm advanced at the rate of about 50 miles per hour from the Pyrenees, where it seemed to have originated, to the Baltic Sea, where all trace of it was lost. At each point, the hail fell only for about seven or eight minutes.

The number of parishes laid waste in France was 1039; the total

loss was found on official inquiry to be 24,690,000 francs.

This phenomenon presents the most prodigious example both of the forces which act in collecting watery vapour and maintaining it suspended in the air, and of those which produce, amid the heats of summer, a sudden depression of temperature in widely-extended atmospheric regions.]

CHAP. IV.

ATMOSPHERIC ELECTRICITY.

2259. The air generally charged with positive electricity. — The terrestrial globe which we inhabit is invested with an ocean of air the depth of which is about the 200th part of its diameter. It may therefore be conceived by imagining a coating of air, the tenth of an inch thick, investing a twenty-inch globe. This aerial ocean, relatively shallow as it is, at the bottom of which the tribes of organized nature have their dwelling, is nevertheless the theatre of stupendous electrical phenomena.

It may be stated as a general fact, that the atmosphere which thus covers the globe is charged with positive electricity, which, acting by induction on the superficial stratum of the globe on which it rests, decomposes the natural electricity, attracting the negative fluid to the surface and repelling the positive fluid to the inferior strats. The globe and its atmosphere may therefore be not inaptly compared to a Leyden phial, the outer coating of which being placed in connexion with the prime conductor of a machine, is charged with positive electricity, and the inner coating being in connexion with the ground, is charged by induction with negative electricity. The outer coating represents the atmosphere, and the inner the superficial stratum of the globe.

2260. This state subject to variations and exceptions.—This normal state of the general atmospheric ocean is subject to variations and exceptions; variations of intensity and exceptions in quality or name. The variations are periodical and accidental. The exceptions local; patches of the general atmosphere in which clouds float being occasionally charged with negative electricity.

2261. Diurnal variations of electrical intensity.—The intensity of the electricity with which the atmosphere is charged varies, in the course of twenty-four hours, alternately increasing and decreasing. It begins to decrease at a few minutes after sunrise, and continues to decrease until two or three o'clock in the afternoon, when it attains a minimum. It then increases and continues to increase until some minutes after sunset, when it attains a maximum. After that it again decreases, attaining a minimum at a certain time in the night, which varies in different places and different seasons, after which it again increases and attains a maximum at a few minutes after sunrise.

In general, in winter, the electricity of the air is more intense than in summer.

2262. Observations of Quetelet.—These were the general results of the extensive series of observations on atmospheric electricity made by Saussure. More recently they have been confirmed by the observations of M. Quetelet, which have been continued without interruption daily at the Observatory of Brussels for the last ten years. M. Quetelet found that the first maximum was manifested about 8 A. M., and the second about 9 P. M. The minimum in the day was at 3 P. M. He found also that the mean intensity was greatest in January and least in June.

Such are the normal changes which the electrical condition of the air undergoes when the atmosphere is clear and unclouded. When, however, the firmament is covered with clouds, the electricity is subject during the day to frequent and irregular changes not only in intensity but in name; the electricity being often negative, owing to

the pressure of clouds over the place of observation, charged some

with positive and some with negative electricity.

2203. Irregular and local variations and exceptions. — The intensity of the electricity of the air is also affected by the season of the year, and by the prevalent character and direction of the winds; it varies also with the elevation of the strata, being in general greater in the higher than in the lower regions of the atmosphere. The intensity is generally greater in winter, and especially in frosty weather, than in summer, and when the air is calm than when winds prevail.

Atmospheric deposits, such as rain, hail, snow, &c., are sometimes positive and sometimes negative, varying with the direction of the wind. North winds give positive, and south winds negative deposits.

2264. Methods of observing atmospheric electricity. — The electricity of the atmosphere is observed by erecting in it, to any desired elevation, pointed metallic conductors, from the lower extremities of which wires are carried to electroscopes of various forms, according to the intensity of the electricity to be observed. All the usual effects of artificial electricity may be reproduced by such means; sparks may be taken, light bodies attracted and repelled, electrical bells, such as those described in (1792), affected; and, in fine, all the usual effects of the fluid produced. So immediate is the increase of electrical tension in rising through the strata of the air, that a gold-leaf electroscope properly adapted to the purpose, and reduced to its natural state, when placed horizontally on the ground, will show a sensible divergence when raised to the level of the eyes.

2265. Methods of ascertaining the electrical condition of the higher strata.—To ascertain the electrical condition of strata too elevated to be reached by a fixed conductor, the extremity of a flexible wire, to which a metallic point is attached, is connected with a heavy ball, which is projected into the air by a gun or pistol, or to an arrow projected by a bow. The projectile, when it attains the limit of its flight, detaches the wire from the electroscope, which then indicates the electrical state of the air at the highest point

attained by the projectile.

The expedient of a kite, used with so much success by Franklin, Romas, and others, to draw electricity from the clouds, may also be adopted with advantage, more especially in cases where the atmospheric strata to be examined are at a considerable elevation.

2266. Remarkable experiments of Romas, 1757.—The vast quantities of electricity with which the clouds are sometimes charged were rendered manifest in a striking manner by the well-known experiments made by means of kites by Romas in 1757. The kite, carrying a metallic point, was elevated to the strata in which the electric cloud floated. A wire was connected with the cord, and carried from the pointed conductor borne by the kite to a part of the

cord at some distance from the lower extremity, where it was turned aside and brought into connexion with an electroscope, or other experimental means of testing the quantity and quality of the electricity with which it was charged. Romas drew from the extremity of this conducting wire not only strong electric sparks, but blades of fire nine or ten feet in length and an inch in thickness, the discharge of which was attended with a report as loud as that of a pistol. In less time than an hour, not less than thirty flashes of this magnitude and intensity were often drawn from the conductor, besides

many of six or seven feet and of less length.

2267. Electrical charge of clouds varies. — It has been shown by means of kites thus applied, that the clouds are charged some with positive and some with negative electricity, while some are observed to be in their natural state. These circumstances serve to explain some phenomena observed in the motions of the clouds which are manifested in stormy weather. Clouds which are similarly electrified repel, and those which are oppositely electrified attract each other. Hence arise motions among such clouds of the most opposite and complicated kind. While they are thus reciprocally attracted and repelled in virtue of the electricity with which they are charged, they are also transported in various directions by the currents which prevail in the atmospheric strata in which they float, these currents often having themselves different directions.

2268. Thunder and lightning. — Such appearances are the sure prognostics of a thunderstorm. Clouds charged with contrary electricities affect each other by induction, and mutually attract, whether they float in the same stratum or in strata at different elevations. When they come within striking distance, that is to say, such a distance that the force of the fluids with which they are charged surpasses the resistance of the intervening air, the contrary fluids rush to each other, and an electrical discharge takes place, upon the same principle as the same phenomenon on a smaller scale is produced when the charges of the internal and external contings of a Leyden jar, overcoming the resistance of the uncoated part, rush together

and a spontaneous discharge is made.

The sound and the flash, the thunder and the lightning, are only the reproduction on a more vast scale of the explosion and spark of

the jar.

The clouds, however, unlike the metallic coatings of the jar, are very imperfect conductors, and consequently, when discharged at one part of their vast extent, they preserve elsewhere their electricity in its original intensity. Thus, the first discharge, instead of establishing equilibrium, rather disturbs it; for the part of the cloud which is still charged is alone attracted by the part of the other cloud in which the fluid has not yet been neutralized. Hence arise various and complicated motions and variations of form of the clouds, and a suc-

ession of discharges between the same clouds must take place before the electrical equilibrium is established. This is necessarily attended by a corresponding succession of flashes of lightning and claps of thunder.

2269. Form and extent of the flush of lightning.—The form of the flush in the case of lightning, like that of the spark taken from an electrified conductor, is zigzng. The doublings or acute angles formed at the successive points when the flush changes its direction vary in number and proximity. The cause of this zigzag course, whether of the electric spark or of lightning, has not been explained

in any clear or satisfactory manner.

The length of the flashes of lightning also varies; in some cases they have been ascertained to extend to from two and a half to three miles. It is probable, if not certain, that the line of light exhibited by flashes of forked lightning are not in reality one continued line simultaneously luminous, but that on the contrary the light is developed successively as the electricity proceeds in its course; the appearance of a continuous line of light being an optical effect analogous to the continuous line of light exhibited when a lighted stick is moved rapidly in a circle, the same explanation being applicable to the case of lightning (1143).

2270. Cruses of the rolling of thunder.—As the sound of thunder is produced by the passage of the electric fluid through the air which it suddenly compresses, it is evolved progressively along the entire space along which the lightning moves. But since sound moves only at the rate of 1100 feet per second, while the transmission of light is so rapid that in this case it may be considered as practically instantaneous, the sound will not reach the ear for an interval greater or less after the perception of the light, just as the flash of a gun is seen before the report is heard (831).

By noting the interval, therefore, which elapses between the perception of the flash and that of the sound, the distance of the point where the discharge takes place can be computed approximately by

allowing 1100 feet for every second in the interval.

But since a separate sound is produced at every point through which the flash passes, and as these points are at distances from the observer which vary according to the position, length, direction, and form of the flash, it will follow necessarily that the sounds produced by the same flash, though practically simultaneous, because of the great velocity with which the electricity moves, arrive at the ear in comparatively slow succession. Thus, if the flash be transmitted in the exact direction in which the observer is placed, and its length be 11,000 feet, the distances of the points where the first and last sounds are produced will differ by ten times the space through which sound moves in one second. The first sound will, therefore, be heard

ten seconds before the last, and the intermediate sounds will be heard during the interval.

The varying loudness of the successive sounds heard in the rolling of thunder proceeds in part from the same causes as the varying intensity of the light of the flash. But it may, perhaps, be more satisfactorily explained by the combination of the successive discharges of the same cloud rapidly succeeding each other, and combining their effects with those arising from the varying distances of different parts of the same flash.

2271. Affected by the zigzag form of lightning.—It appears to us that the varying intensity of the rolling of thunder may also be very clearly and satisfactorily explained by the sigzag form of the flash, combined with the effect of the varying distance; and it seems extraordinary that an explanation so obvious has not been suggested. Let A, B, C, D, fig. 676., be a part of a sigzag flash seem by an

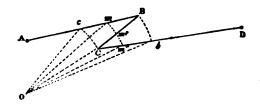


Fig. 676.

observer-at o. Taking o as a centre, suppose arcs o c and B b of circles to be drawn, with o c and o B as radii. It is clear that the points c and c, and B and b, being respectively equally distant from the observer, the sounds produced there will be heard simultaneously, and, supposing them equal, will produce the perception of a sound twice as loud as either heard alone would do. All the points on the zigzag c B C b are so placed that three of them are equi-Thus, if with o as centre, and o m as radius, distant from 0. a circular are be described, it will intersect the path of the lightning at the three points m, m', and m', and these three points being, therefore, at the same distance from o, the sounds produced at them will reach the observer at the same moment, and if they be equally intense will produce on the ear the same effect as a single sound three times as loud. The same will be true for all the points of the zigzag between c and b. Thus, in this case, supposing the intensity of the lightning to be uniform from A to D, there will be three degrees of loudness in the sound produced, the least between A and c and between b and D, the greatest between c and b along the zigzng, and the intermediate at the points c c and B b.

ident, that from the infinite variety of form and position on to the observer, of which the course of the lightning ble, the variations of intensity of the rolling of thunder be explained in this way have no limit.

Iffected by the varying distance of different parts of the ince the loudness of a sound diminishes as the square of ze of the observer is increased (844), it is clear that this other means of explaining the varying loudness of the

thunder.

Affected by echo and by interference.—As the rolling of much more varied and of longer continuance in moungions than in open plane countries, it is, no doubt, also y reverberation from every surface which it encounters ible of reflecting sound. A part therefore of the rolling such cases the effect of echo.

een also conjectured that the acoustic effects are modified

cts of interference (836).

Inductive action of clouds on the earth.—A cloud charged ricity, whatever be the quality of the fluid or the state of phere around it, exercises by induction an action on all on the earth's surface immediately under it. It has a o decompose their natural electricity, repelling the fluid in name, and attracting to the highest points the fluid of name. The effects thus actually produced upon objects is such induction will depend on the intensity and quality ctricity with which the cloud is charged, its distance, the lity of the materials of which the bodies affected consist, nitude, position, and, above all, their form.

being a much better conductor than earth in any state of in, thunder clouds act with greater energy on the sea, lakes, large collections of water. The flash has a tendency to sen the cloud and the water, just as the spark passes beconductor of an electric machine and the hand presented the water were covered with a thin sheet of glass, the would still pass, breaking through the glass; because, the glass be a non-conductor, it does not intercept the conttion of the cloud, any more than a thin glove of varnished e hand would intercept the spark from the conductor.

Formation of fulgurites explained.—This explains the fact ning sometimes penetrates strata of the solid ground under bterranean reservoirs of water are found. The water of rvoirs is affected by the inductive action of an electrified i in its turn reacts upon the cloud as one coating of a ar reacts upon the other. When this mutual action is sufstrong to overcome the resistance of the subjacent atmod the strata of soil under which the subterranean reservoir lies, a discharge takes place, and the lightning penetrates the strata, fusing the materials of which it is composed, and leaving a tubular hole with a hard vitrefied coating.

Tubes thus formed have been called fulgurites, or thunder tubes.

2276. Accidents of the surface which attract lightning.— The properties of points, edges, and other projecting parts, of conductors, which have been already stated (1776), will render easily intelligible the influence of mountains, peaked hills, projecting rocks, trees, lofty edifices, and other objects, natural and artificial, which project upwards from the general surface of the ground. Lightning never strikes the bottom of deep and close valleys. In Switzerland, on the slopes of the Alps and Pyrenees, and in other mountainous countries, multitudes of cultivated valleys are found, the inhabitant sof which know by secular tradition that they have nothing to fear from thunderstorms. If, however, the width of the valleys were so great as twenty or thirty times their depth, clouds would occasionally descend upon them in masses sufficiently considerable, and lightning would strike.

Solitary hills, or elevated buildings rising in the centre of an extensive plain, are peculiarly exposed to lightning, since there are no other projecting objects near them to divert its course.

Trees, especially if they stand singly apart from others, are likely to be struck. Being from their nature more or less impregnated with sap, which is a conductor of electricity, they attract the fluid, and are struck.

The effects of such objects are, however, sometimes modified by the agency of unseen causes below the surface. The condition of the soil, subsoil, and even the inferior strata, the depth of the roots and their dimensions, also exercise considerable influence on the phenomena, so that in the places where there is the greatest apparent safety there is often the greatest danger. It is, nevertheless, a good general maxim not to take a position in a thunderstorm either under a tree or close to an elevated building, but to keep as much as possible in the open plain.

2277. Lightning follows conductors by preference.—Its effects on buildings.— Lightning falling upon buildings chooses by preference the points which are the best conductors. It sometimes strikes and destroys objects which are non-conductors, but this happens generally when such bodies lie in its direct course towards conductors. Thus lightning has been found to penetrate a wall, attracted by a mass of metal, placed within it.

Metallic roofs, beams, braces, and other parts in buildings, are liable thus to attract lightning. The heated and rarefied air in chimneys acquires conductibility. Hence it happens often that lightning descends chimneys, and thus passes into rooms. It

ws bell-gires, metallic mouldings of wars and farmings and

, gilding. 278. Conductors or paratonneres lightening rice in the gram of buildings. — The purpose of parasants incoming inductors erected for the protection of buttonings is not in series. rather to attract lightning, and divert a man a manner or winill be innoxious.

A paratonnerre is a princed memilie rol. 12length of which varies with the intiding at which it is placed, but which is generally from the to forty feet. It is erected wateral were object it is intended to person. From the table an unbroken series of metallic inca minister. welded together end to end are maintain as the ground, where they are forced in mone soil. the escape of the I will insert upon the If water, or moist soil manor to sometime: found, it should be managed via a sugge metal of coesilerative superiors magnitude buried in a gir their wire genomen warmen or, better still will berief mai was .

The parts of a well-sometimes manufacture are represented in \$7 . The real water a of iron, is mand at its most than statement. decreases grainally in the street to the street. It is composed sometime, if these press size is joined together, and secured in him passed the versely through them. In the figure are more sented only the two extremities if the awar and those of the intermediate need to an engiving inconvenient magnitude it the diagram The superior piece, 7, is represented countries It is a rod of brass or stoper agout two feet in length, terminating in a postmess work sevil three inches long, attaches to the root of bloom solder, which is further secured in a trace forther which gives the projecting appearance in the the gram below the post.

Three of the meticale reposed me mor in cient for attaching the tartitaries at the raf in represented in Fy. 57. t. as 2. t and f. A. the rod is supported against a very east person which it is attached by stirreys; as (2 at 1917) upon a diagonal israes; and as f a a many. secured by bolts to a horizontal term dervice.



Fig. 677.

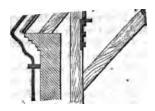


Fig. 678.

The conductor is continued downwards a fice, or in any other convenient course, to the of iron, round or square, or by a cable of it as is sometimes used for the lighter sort of its attached, at its upper extremity, to the base joint, which is hermetically closed, so which would produce a dangerous solution of

To comprehend the protective influence of be considered that the inductive action of a table the natural electricity of the rod more energy rounding objects, both on account of the attention that of the cloud suspection that of the cloud suspection is fluid in a jet towards the cloud, when neutralizes an equal quantity of the electric is charged, and, by the continuence.

2279. Effects of lightning on boiles which it works.—Therefore of lightning, like those of electricity extends by artificial mount for threefold: physiological, physical, and mentalized

When lightning kills, the parts where it has struct tears of severe burning; the bones are often indicated and ordered and been subjected to violent mechanical research on the system by induction only. Which is exact the mindirect shock, it does not immediately almost indirect shocks so severe as sometimes to leave affects with the contract.

The physical effects of lightning produced their established raise their temperature. This elevation is simulated a produced they are rendered incandescent, fused and their burned. The imperations pens occasionally with beli-wires, especially in expect and their tected positions, as in courts or gardene. The imperior matter it was produced in such cases set fire to any combatilitie matter it was they may chance to fall. Wood, straw, and such imperating bothes, are ignited generally by the lightning intwinting in the by the attraction of other boiles near them which are good ductors.

The mechanical effects of lightning, the physical cause of which has not been satisfactorily explained, are very extra randary. As a mous masses of metal are turn from their supports, which would stone are broken, and massive buildings are rule at this great

No theory or hypothesis which has communical general acts to the has yet been suggested for the explanation of this mercon, include appearances which attend the phenomenon are, however, electronic and its forms, directions, and positions, though ever varying always bear a remarkable relation to the magnetic meridians and positions, though ever varying always bear a remarkable relation to the magnetic meridians and positions. Whatever, therefore, be its physical cause, it is evident that the theatre of its action is the atmosphere: that the agent to which the development is due is electricity, influenced in some unascription manner by terrestrial magnetism. In the absence of any satisfactory theory for the explanation of the phenomenon, we shall comme ourselves here to a short description of it, derived from the most extensive and exact series of observations which have been made in those regions where the meteor has been seen with the most marked characters and in the greatest splendour.

2281. General character of the meteor. — The aurora borealis is a luminous phenomenon, which appears in the heavens, and is seen in high latitudes in both hemispheres. The term aurora borealis, or northern lights, has been applied to it because the opportunities of witnessing it are, from the geographical character of the globe, much more frequent in the northern than in the southern hemisphere. The term aurora polaris would be a more proper designation.

This phenomenon consists of luminous rays of various colours,

issuing from every direction, but converging to the same point, which appear after sunset, generally toward the north, occasionally toward the west, and sometimes, but rarely, toward the south. It frequently appears near the horizon, as a vague and diffuse light, something like the faint streaks which harbinger the rising sun and form the dawn. Hence the phenomenon has derived its name, the northern morning. Sometimes, however, it is presented under the form of a sombre cloud, from which luminous jets issue, which are often variously coloured,

and illuminate the entire atmosphere.

The more conspicuous auroras commence to be formed soon after the close of twilight. At first a dark mist or foggy cloud is perceived in the north, and a little more brightness towards the west than in the other parts of the heavens. The mist gradually takes the form of a circular segment, resting at each corner on the horizon. The visible part of the arc soon becomes surrounded with a pale light, which is followed by the formation of one or several luminous arcs. Then come jets and rays of light variously coloured, which issue from the dark part of the segment, the continuity of which is broken by bright emanations, indicating a movement of the mass, which seems agitated by internal shocks during the formation of these luminous radiations, that issue from it as flames do from a conflagration. When this species of fire has ceased, and the aurora has become extended, a crown is formed at the zenith, to which these rays converge. From this time the phenomenon diminishes in its intensity, exhibiting, nevertheless, from time to time, sometimes on one side of the heavens and sometimes on another, jets of light, a crown, and colours more or less vivid. Finally the motion ceases; the light approaches gradually to the horizon; the cloud quitting the other parts of the firmament settles in the north. The dark part of the segment becomes luminous, its brightness being greatest near the horizon, and becoming more feeble as the altitude augments, until it loses its light altogether.

The aurora is sometimes composed of two luminous segments, which are concentric, and separated from each other by one dark space, and from the earth by another. Sometimes, though rarely, there is only one dark segment, which is symmetrically pierced round its border by openings, through which light or fire is seen.

2282. Description of auroras seen in the polar regions by M. Lottin. — One of the most recent and exact descriptions of this meteor is the following, supplied by M. Lottin, an officer of the French navy, and a member of the Scientific Commission, sent some years ago to the North Seas. Between September, 1838, and April, 1839, this savant observed nearly 150 meteors of this class. They were most frequent from the 17th November to the 25th January, being the interval during which the sun remained constantly below the horizon. During this period there were sixty-four auroras visible,

besides many which a clouded sky concealed from the eye, but the presence of which was indicated by the disturbances they produced upon the magnetic needle.

The succession of appearances and changes presented by these

meteors are thus described by M. Lottin:

Between four and eight o'clock, P. M., a light fog, rising to the altitude of six degrees, became coloured on its upper edge, being fringed with the light of the meteor rising behind it. This border becoming gradually more regular took the form of an arc, of a pale yellow colour, the edges of which were diffuse, the extremities resting on the horizon. This bow swelled slowly upwards, its vertex being constantly on the magnetic meridian. Blackish streaks divided regularly the luminous arc, and resolved it into a system of rays; these rays were alternately extended and contracted; sometimes slowly, sometimes instantaneously; sometimes they would dart out, increasing and diminishing suddenly in splendour. The inferior parts, or the feet of the rays, presented always the most vivid light, and formed an arc more or less regular. The length of these rays was very various, but they all converged to that point of the heavens indicated by the direction of the southern pole of the dipping needle. Sometimes they were prolonged to the point where their directions intersected, and formed the summit of an enormous dome of light.

The bow then would continue to ascend toward the zenith: it would suffer an undulatory motion in its light — that is to say, from one extremity to the other the brightness of the rays would increase successively in intensity. This luminous current would appear several times in quick succession, and it would pass much more frequently from west to east than in the opposite direction. Sometimes, but rarely, a retrograde motion would take place immediately afterward; and as soon as this wave of light had run successively over all the rays of the aurora from west to east, it would return in the contrary direction to the point of its departure, producing such an effect that it was impossible to say whether the rays themselves were actually affected by a motion of translation in a direction nearly horizontal, or whether this more vivid light was transferred from ray to ray, the system of rays themselves suffering no change of position. The bow, thus presenting the appearance of an alternate motion in a direction nearly horizontal, had usually the appearance of the undulations or folds of a ribbon or flag agitated by the Sometimes one and sometimes both of its extremities would desert the horizon, and then its folds would become more numerous and marked, the bow would change its character, and assume the form of a long sheet of rays returning into itself, and consisting of several parts forming graceful curves. The brightness of the rays would vary suddenly, sometimes surpassing in splendour stars of the first magnitude; these rays would rapidly dart out, and curves would

be formed and developed like the folds of a serpent; then the rays would affect various colours: the base would be red, the middle green, and the remainder would preserve its clear yellow hue. Such was the arrangement which the colours always preserved; they were of admirable transparency, the base exhibiting blood-red, and the green of the middle being that of the pale emerald; the brightness would diminish, the colours disappear, and all be extinguished, sometimes suddenly, and sometimes by slow degrees. After this disappearance, fragments of the bow would be reproduced, would continue their upward movement, and approach the zenith; the rays, by the effect of perspective, would be gradually shortened; the thickness of the arc, which presented then the appearance of a large zone of parallel rays, would be estimated; then the vertex of the bow would reach the magnetic zenith, or the point to which the south pole of the dipping needle is directed. At that moment the rays would be seen in the direction of their feet. If they were coloured, they would appear as a large red band, through which the green tiuts of their superior parts could be distinguished; and if the wave of light above mentioned passed along them, their feet would form a long sinuous undulating zone; while, throughout all these changes, the rays would never suffer any oscillation in the direction of their axis, and would constantly preserve their mutual parallelisms.

While these appearances are manifested, new bows are formed, either commencing in the same diffuse manner, or with vivid and ready-formed rays: they succeed each other, passing through nearly the same phases, and arrange themselves at certain distances from As many as nine have been counted, forming as many bows, having their ends supported on the earth, and, in their arrangement, resembling the short curtains suspended one behind the other over the scene of a theatre, and intended to represent the aky. Sometimes the intervals between these bows diminish, and two or more of them close upon each other, forming one large zone, traversing the heavens, and disappearing toward the south, becoming rapidly feeble after passing the zenith. But sometimes, also, when this zone extends over the summit of the firmament from east to west, the mass of rays which have already passed beyond the magnetic zenith appear suddenly to come from the south, and to form with those from the north the real boreal corona, all the rays of which converge to the zenith. This appearance of a crown, therefore, is doubtless the mere effect of perspective; and an observer, placed at the same instant at a certain distance to the north or to the south, would perceive only an arc.

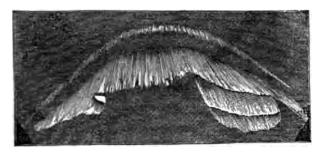
The total zone measuring less in the direction north and south than in the direction east and west, since it often leans upon the earth, the corona would be expected to have an elliptical form; but that does not always happen: it has been seen circular, the unequal rays not extending to a greater distance than from eight to twelve degrees from the zenith, while at other times they reach the horizon.

Let it, then, be imagined, that all these vivid rays of light issue forth with splendour, subject to continual and sudden variations in their length and brightness; that these beautiful red and green tints colour them at intervals; that waves of light undulate over them; that currents of light succeed each other; and, in fine, that the vast firmament presents one immense and magnificent dome of light, reposing on the snow-covered base supplied by the ground—which itself serves as a dazzling frame for a sea, calm and black as a pitchy lake—and some idea, though an imperfect one, may be obtained of the splendid spectacle which presents itself to him who witnesses the aurora from the bay of Alten.

The corona, when it is formed, only lasts for some minutes: it sometimes forms suddenly, without any previous bow. There are rarely more than two on the same night; and many of the auroras

are attended with no crown at all.

The corona becomes gradually faint, the whole phenomenon being to the south of the zenith, forming bows gradually paler, and generally disappearing before they reach the southern horizon. most commonly takes place in the first half of the night, after which the aurora appears to have lost its intensity: the pencils of rays, the bands and the fragments of bows, appear and disappear at intervals; then the rays become more and more diffused, and ultimately merge into the vague and feeble light which is spread over the heavens, grouped like little clouds, and designated by the name of auroral plates (plaques aurorales). Their milky light frequently undergoes striking changes in its brightness, like motions of dilatation and contraction, which are propagated reciprocally between the centre and the circumference, like those which are observed in marine animals The phenomena become gradually more faint, and called Medusse. generally disappear altogether on the appearance of twilight. times, however, the aurora continues after the commencement of day-



break, when the light is so strong that a printed book may be read. It then disappears, sometimes suddenly; but it often happens that, as the daylight augments, the aurora becomes gradually vague and undefined, takes a whitish colour, and is ultimately so mingled with the cirrho-stratus clouds that it is impossible to distinguish it from them.

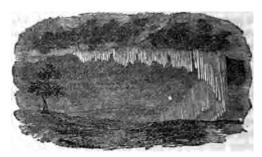


Fig. 680.



Fig. 681.

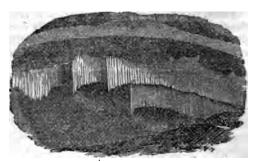
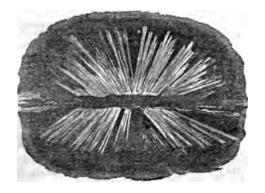


Fig. 682.

Some of the appearances here described are represented in figs. 679, 680, 681, 682., copied from the memoir of M. Lottin.

There is great difficulty in determining the exact height of the

realis above the earth, and accordingly the opinions given bject by different observers are widely discordant. Mairan the mean height to be 175 French leagues; Bergman says Euler several thousand miles. From the comparison of a f observations of an aurora that appeared in March, 1826, lifferent places in the north of England and south of Scot-Dalton, in a paper presented to the Royal Society, comheight to be about 100 miles. But a calculation of this hich it is of necessity supposed that the meteor is seen in ie same place by the different observers, is subject to very certainty. The observations of Dr. Richardson, Franklin, arry, and others, seem to prove that the place of the aurora hin the limits of the atmosphere, and scarcely above the f the clouds; in fact, as the diurnal rotation of the earth no change in its apparent position, it must necessarily parthat motion, and consequently be regarded as an atmophenomenon.



BOOK THE SECOND.

ASTRONOMY.

CHAPTER I.

METHODS OF INVESTIGATION AND MEANS OF OBSERVATION.

2283. The solar system. — The earth, which in the economy of the universe has become the babitation of the races of men, is a globular mass of matter, and one of an assemblage of bodies of like form and analogous magnitude, which revolve in paths nearly circular round a common centre, in which the sun, a globe having dimensions vastly greater than all the others, is established, maintaining physical order among them by his predominant attraction, and ministering to the well-being of the tribes which inhabit them by a fit and regulated supply of light and heat.

This group of bodies is the SOLAR SYSTEM.

2284. The stellar universe. — In the vast regions of space which surround this system other bodies similar to the sun are placed, countless in number, and most of them, according to all probability, superior in magnitude and splendour to that luminary. With these bodies, which seem to be scattered throughout the depths of immensity without any discoverable limit, we acquire some acquaintance by the mere powers of natural vision, aided by those of the understanding; but this knowledge has received, especially in modern times, prodigious extension from the augmented range given to the eye by the telescope, and by the great advances which have been made in mathematical science, which may be considered as conferring upon the mind the same sort of enlarged power as the telescope has conferred upon the eye.

2285. Subject of astronomy—origin of the name.—The investigation of the magnitudes, distances, motions, local arrangements, and, so far as it can be ascertained, the physical condition of these great bodies composing the UNIVERSE, constitutes the subject of that branch of science called ASTRONOMY, a term derived from the Greek words αστηρ (aster), a star (under which all the heavenly bodies were included), and νομος (nomos), A LAW—the science which expounds the LAWS which govern the motions of the STARS.

(92)

2286. It treats of inaccessible objects.—It is evident, therefore, that astronomy is distinguished from all other divisions of natural science by this peculiarity, that the bodies which are the subjects of observation and enquiry are all of them inaccessible. Even the earth itself, which the astronomer regards as a celestial object—an array,—is to him, in a certain sense, even more inaccessible than the others; for the very fact of his place of observation being confined strictly to its surface, an insignificant part of which alone can be observed by him at any one moment, renders it impossible for him to examine, by direct observation, the carth As A WHOLE—the only way in which he desires to consider it,—and obliges him to resort to a variety of indirect expedients to acquire that knowledge of its dimensions, form, and motions, which, with regard to other and more distant objects, results from direct and immediate observation.

2287. Hence arise peculiar methods of investigation and peculiar instruments of observation. — This circumstance of having to deal exclusively with inaccessible objects has obliged the astronomer to invent peculiar modes of reasoning and peculiar instruments of observation, adapted to the solution of such problems, and to the discovery of the necessary data. Much needless repetition will then be saved by explaining once for all, with as much brevity as is compatible with clearness, the most important classes of those problems which determine the circumstances of each particular celestial object, and by describing the principal instruments of observation by which the necessary data are obtained.

2288. Direction and bearing of visible objects.—The eye estimates only the direction or relative bearings of objects within the range of vision, but supplies no direct means of determining their distances from each other, or from the eye itself (1168, et seq.).

The absolute direction-of a visible object is that of a straight line

drawn from the eye to the object.

The relative direction or bearing of an object is determined by the angle formed by the absolute direction with some other fixed or known direction, such as that of a line drawn to the north, south,

east, or west.

2289. They supply the means of ascertaining the distances and positions of inaccessible objects. — By comparing the relative bearings of inaccessible objects, taken from two or more accessible points whose distance from each other is known, or can be ascertained by actual measurement, the distances of such inaccessible objects from the accessible objects, from the observer, and from each other, may be determined by computation. Such distances being once known, become the data by which the mutual distances of other inaccessible objects from the former, and from each other, may be in like manner computed; so that, by starting in this manner from two objects whose mutual distance can be actually measured, we may proceed,



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to distributions and a second enelogic with reference to the open than the direction for the property and a second angle with the Cooperation of the result on being all or the Royal to the later than the result. dere as the shirt of the art learned, with the effect as a centre soit to Concress a multi- soit if the direction of the origin from every spaces be at right angles to the line prints the statute the latter line may be considered as the size of the ar-In either case, the distance of the object bearing a high ratio to the distance between the stations, the angle formed by the two Precities of the object as seen from the stations, will be so small that the chord or sine may be considered as equal to the arm. and the solution of the problem will be simplified by the principles established in 2205.

Let s and s', py. 686, be the stations, and o the object; under the conditions supposed, the angle o will necessarily be small. Its magnitude may be ascertained by measuring the visual angles o s s' and o s' s; which may be done, since both stations a and s' are accessible, and each of them is visible from the other. By a well-known

blished in elementary geometry, the three angles of angle added together make 180°. If, therefore, the sum of observed angles at s and s' be subtracted from 180°, the will be the angle o. Now if this angle be expressed by

$$a = \frac{1}{57.3} \times r \times e^{\circ} = \frac{1}{3437.8} \times r \times e' = \frac{1}{206265} \times r \times e'.$$

2295. The arc, the chord, and the sine may be considered as equal when the angle is small. — If ACB, fig. 684, be the angle, AB the arc, and AC = CB the radius, a line AD drawn from one extremity of the arc perpendicular to the radius CB, which passes

through the other extremity of the arc, is called its sine; and the straight line AB joining the extremities of the arc is called its chord.

It will be evident by merely drawing the diagram with a gradually decreating angle, that the three lengths, the sine A., the chord AB, and the are AB, will approach to equality as the arc diminishes. Ever where the arc is so large as 30°, it does not exceed the length of the chord by more than three-tenths of a degree; and therefore for all angles less than this, the chord and are may be considered as equal where the most extreme precision is not required.

In tike manner, if the angle ACB be 15°, the sine A D will be less than the are by only two-tenths of a degree, that is, by the 75th part of the entire length of the arc. In all cases, therefore, where greater precision than this is not required, the sine AD, the chord, and the

are may be considered for such angles as interchangeable.

When the angles are so small as a degree or two, these quantities may for all practical purposes be considered to be equal.

2296. To ascertain the distance of an inaccessible object from two accessible stations. — This, which is a problem of the highest importance, being in fact the basis of all the knowledge we possess of the distances, dimensions, and motions of the great bodies of the universe, admits of easy solution.

Let s and s', fig. 685, be the two stations, and o the object of observation; and let the visual angles subtended by o and s' at s, and by o and s at s', be observed, and the distance s s' measured.

Take a line ss, consisting of as many inches as there are miles in ss', and draw two lines so and so from s and s, making with ss the same

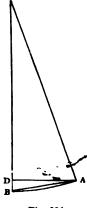


Fig. 684.

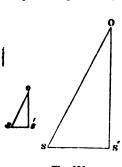


Fig. 685.

s o and s' o are ascertained by observation to make with that case the triangle sos' will be in all respects similar to le s o s', only drawn on a smaller scale, an inch in any of corresponding to a mile in one of the sides of the great If the sides so and s'o be therefore measured, they st of as many inches as there are miles in the correspondso and s' o of the great triangle. Now, since the small is always accessible to direct measurement, and as the of its scale to that of the great triangle is known, the e of the sides of the great triangle may be ascertained. at being identical in its actual details with the process by s problem is solved, the preceding reasoning is the same in and spirit. Trigonometrical tables supply much more means of determining the proportion of the sides of the but such tables are nothing more than the arithmetical ation of such diagrams as fig. 685.

Case in which the distance of the object is great relatively tance between the stations. — If in this case the stations be so selected with reference to the object that the directions of the object as seen from them shall form angles with the line joining the stations which shall be equal or nearly so, this latter line may be considered as the chord of the arc described, with the object as a centre and the distance as a radius; and if the direction of the object from either station be at right angles to the line joining the stations, this latter line may be considered as the sine of the arc. In either case, the distance of the object bearing a high ratio to the distance between the stations, the angle formed by the two directions of the object, as seen from the stations, will be so small that the chord or sine may be considered as equal to the arc, and the solution of the problem will be simplified by the principles established in (2295).

Let s and s', fig. 686, be the stations, and o the object; under the conditions supposed, the angle o will necessarily be small. Its magnitude may be ascertained by measuring the visual angles oss' and os's; which may be done, since both stations s and s' are accessible, and each of them is visible By a well-known principle estafrom the other. blished in elementary geometry, the three angles of angle added together make 180°. If, therefore, the sum

ro observed angles at s and s' be subtracted from 180°, the r will be the angle o. Now if this angle be expressed by nds, we shall have (2294)

86.

$$8 o = 8 s' \times \frac{206265''}{a''}$$

2298. Given the apparent distance between two distant objects, such distance being at right angles, or nearly so, to their visual directions, and their distance from the observers, to find the actual distance between them. — This problem is only a particular application of the general principle explained in (2294), a being the apparent distance of the objects, a the real distance between them, and r their distance from the observer.

This method may be applied without practical error, if the apparent distance between the objects be not greater than two or three degrees, and it may be used as a rough approximation in cases where the apparent distance is even so great as 30°. When the apparent distance amounts to so much as 60°, the actual distance computed in this way will not exceed the true distance by more than a 24th part of its whole amount; for the chord of 60° is equal to the radius, and therefore to an arc of 57°.3, being less than the arc by only 2°.7, or about a 24th part of its length.

2299. Given the apparent diameter of a spherical object and its distance from the observer, to find its real diameter.—This is also a particular application of the general problem (2294), a being the apparent diameter and r the distance, and in all cases which occur in astronomy the apparent diameters are so small that the results

of the computation may be considered as perfectly exact.

2300. Methods of ascertaining the direction of a visible and distant object.—It might appear an easy matter to observe the exact direction of any point placed within the range of vision, since that direction must be that of a straight line passing directly from the eye of the observer to the point to be observed. If the eye were supplied with the appendages necessary to record and measure the directions of visible objects, this would be true, and the organ of sight would be in fact a philosophical instrument. The eye is, however, adapted to other and different uses, and constructed to play a different part in the animal economy; and invention has been stimulated to supply expedients, by means of which the exact directions of visible distant points can be ascertained, observed, and compared one with another, so as to supply the various data necessary in the classes of problems which have just been noticed, and others which we shall have occasion hereafter to advert to.

2301. Use of sights. — The most simple expedient by which the visual direction of a distant point can be determined is by SIGHTS, which are small holes or narrow slits made in two thin opaque plates placed at right angles, or nearly so, to the line of vision, and so arranged, that when the eye is placed behind the posterior opening the object of observation shall be visible through the anterior

opening. Every one is rendered familiar with this expedient, by its application to fire-arms as a method of "taking aim."

This contrivance is, however, too rude and susceptible of error within too wide limits, to be available for astronomical purposes.

2302. Application of the telescope to indicate the visual direction of micrometric wires.—The telescope (1212) supplies means of determining the direction of the visual ray with all the necessary precision.

If T', fig. 687, represent the tube of a telescope, T the ex-

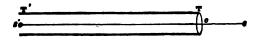


Fig. 687.

tremity in which the object-glass is fixed, and T' the end where the images of distant objects to which the tube is directed are formed, the visual direction of any object will be that of the line s' c drawn from the image of such object, formed in the field of view of the telescope, to the centre c of the object-glass; for if this line be continued it will pass through the object s.

But since the field of view of the telescope is a circular space of defiuite extent, within which many objects in different directions may at the same time be visible, some expedient is necessary, by which one or more fixed points in it may be permanently marked, or by which the entire field may be spaced out as a map is by the

lines of latitude and longitude.

This is accomplished by a system of fibres, or wires (38) so thin that even when magnified they will appear like hairs. These are extended in a frame fixed within the eye-piece of the telescope, so that they appear when seen through the eye-glass like fine lines drawn across the field of view. They are differently arranged, according to the sort of observation to which the instrument is to be applied.

2303. Line of collimation. — In some cases two wires intersect at right angles at the centre of the field of view, dividing it into quadrants, as represented in fig. 683. The wires are so adjusted that their point of intersection c coincides with the axis of the telescope tube; and when the instrument is so adjusted that the point of observation, a star for example, is seen precisely upon the intersection c of the wires, the line of direction, or visual ray of that star, will be the line it c, fig. 687, joining the intersection c, fig. 683, of the wires with the centre c, fig. 687, of the object-glass.

The line s'c, fig. 687, is technically called the line of collimation.

2304. Application of the telescope to a graduated instrument.—

The telescope thus prepared is attached to a graduated instrument

by which angular magnitudes can be observed and measured. Such instruments vary infinitely in form, magnitude, and mode of mounting and adjustment, according to the purposes to which they are applied, and to the degree of precision necessary in the observations to be made with them. To explain and illustrate the general principles on which they are constructed, we shall take the example of one, which consists of a complete circle graduated in the usual manner, being the most common form of instrument used in astronomy for the measurement of angular distances.

Such an apparatus is represented in fig. 688. The circle ABCD.

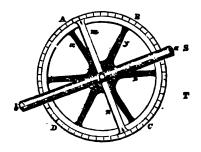


Fig. 688.

on which the divisions of the graduation are accurately engraved, is connected with its centre by a series of spokes x y z. At its centre is a circular hole, in which an axle is inserted so as to turn smoothly in it, and while it turns to be always concentric with the circle A B C D. To this axle the telescope ab is attached in such a manner that the imaginary line s'c, fig. 687, which joins the intersection of the wires, fig. 688, with the centre of the object-glass, shall be parallel to the plane of the circle, and in a plane passing through its centre and at right angles to it.

At right angles to the axis of the telescope are two arms, m n, which form one piece with the tube, so that when the tube is turned with the axis to which it is attached, the arms m n shall turn also, always preserving their direction at right angles to the tube. Marks or indices are engraved upon the extremities m and n of the arms which point to the divisions upon the LIMB (as the divided are is called).

A clamp is provided on the instrument, by which the telescope, being brought to any desired position, can be fixed immoveably in that position, while the observer examines the points upon the limb to which the indices m and n are directed.

Now let us suppose that the visual angle under the directions of two distant objects within the range of vision is required to be measured. The circle being brought into the plane of the objects, and fixed in it, the telescope is moved upon its axis until it is directed to one of the objects, so that its image shall coincide exactly with the intersection of the wires. The telescope is then clamped, and the observer examines the points of the divided limb, to which one of the indices, m for example, is directed. This process is called "reading off." The clamp being disengaged, the telescope is then in like manner directed to the other object, and being clamped as before, the position of the index is "read off." The difference between the numbers which indicate the position of the same index in both cases, will evidently be the visual angle under the directions of the two objects.

As a means of further accuracy, both the indices m and n may be "read off," and if the results differ, which they always will slightly, owing to various causes of error, a mean of the two may

be taken.

It is evident that the same results would be obtained if, instead of making the telescope move upon the circle, it were immoveably attached to it, and that the circle itself turned upon its centre, as a wheel does upon its axle, carrying the telescope with it. In this case the divided limb of the circle is made to move before a fixed index, and the angle under the directions of the objects will be measured by the length of the arc which passes before the index.

Such a combination is represented in section in fig. 689 where

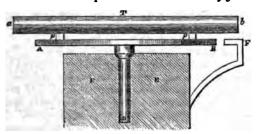


Fig. 689.

T is the telescope, p the pieces by which it is attached to the circle AB seen edgewise, the axis of which D works in a solid block of metal. The fixed index F is directed to the graduated limb which moves before it.

This is the most frequent method of mounting instruments used

in astronomy for angular measurement.

2305. Expedients for measuring the fraction of a division.—
It will happen in general that the index will be directed, not to any exact division, but to some point intermediate between two divisions of the limb. In that case expedients are provided by which

the fraction of a degree between the index, and the last division which it has passed, may be ascertained with an extraordinary degree of precision.

2306. By a Vernier. — This may be accomplished by means of a supplemental scale called a Vernier, already described (1354).

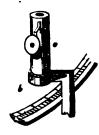


Fig. 690.

2807. By a compound microscope, and micrometric screw. — The same object may, however, be attained with far greater accuracy by means of a compound microscope mounted as represented in fig. 690, so that the observer looks at the index through it. A system of cross wires is placed in the field of view of the microscope, and the whole may be so adjusted by the action of a fine screw, that the index shall coincide precisely with the intersection of the wires. The screw is then turned until the intersection of the cross is brought to coincide with the

previous division of the limb; and the number of turns and fraction of a turn of the screw will give the fraction of a degree between the index and the previous division of the limb.

It is necessary, however, to ascertain previously the value of a complete revolution of the screw. This is easily done by turning the screw on which the intersection of the cross is moved from one division to the adjacent one. Dividing, then, one degree of the limb by the number of turns and fraction of a turn, the arc which corresponds to one complete turn will be found.

2308. Observation and measurement of minute angles. — When the points between which the angular distance required to be ascertained are so close together as to be seen at one and the same time within the field of view of the telescope, a method of measurement is applicable, which admits of even greater relative accuracy than do the methods of observing large angular distances. This arises from the fact that the distance between such points may be determined by various forms of micrometric instruments, in which fine wires, or lines of spider's web, are moved in a direction perpendicular to their length, so as to pass successively through the points whose distance is to be observed.

2309. The parallel wire micrometer. — One of the forms of micrometric apparatus used for this purpose is represented in transverse section in fig. 691. This, which is called the PARALLEL WIRE MICROMETER, consists of two sliding frames across which the parallel wires or threads c and D are stretched. These frames are both moved in a direction perpendicular to that of the wires by screws, constructed with very fine threads, and called from their use MICROMETER SCREWS. This frame is placed in the focus of the

object-glass of the telescope, so that the eye viewing the objects under observation sees also distinctly the parallel and moveable

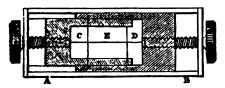


Fig. 691.

wires. These wires are moved by the screws until they pass through the points whose distance asunder is to be measured. This being accomplished, one of them is moved until it coincides with the other, and the number of turns and parts of a turn of the screw necessary to produce this motion gives the angular distance between

the points under observation.

In this, as in the case explained in (2307), it is necessary that the angle corresponding to one complete revolution of the screw be previously ascertained, and this is done by a process precisely similar to that explained in the former case. An object of known angular magnitude, as, for example, a footrule at the distance of a hundred yards, is observed, and the number of turns necessary to carry the wire from end to end of its image is ascertained. The angle such a rule subtends at that distance being divided by the number of turns and parts of a turn, the quotient is the angle corresponding to one complete revolution of the screw.

2310. Measurement of the apparent diameter of an object.—When an object is not too great to be included in the field of view of the telescope, its apparent diameter (1117) can be measured by such an apparatus. To accomplish this the screws are turned until the wires c and D, fig. 691, are made to touch opposite sides of the disk of the object. One of the screws is then turned until the wires coincide, and the number of turns and parts of a turn gives

the apparent magnitude.

CHAP. II.

THE GENERAL ROTUNDITY AND DIMENSIONS OF THE EARTH.

2311. The earth a station from which the universe is observed.

—The earth is, in various points of view, an interesting object of scientific investigation. The naturalist regards it as the habitation

of the numerous tribes of organized beings which are the special subject of his observation and inquiry, and examines curiously those properties and qualities of soil, climate, and atmosphere, by which it is fitted for their maintenance and propagation, and the conditions which govern their distribution over its surface. geologist and mineralogist regard it as the theatre of vast physical operations continued through periods of time extending infinitely beyond the records of human history, the results of which are seen in the state of its crust. The astronomer, rising above these details, regards it as a whole, examines its form, investigates its motions, measures its magnitude, and, above all, considers it as the station from which alone he can take a survey of that universe which forms the peculiar object of his study, and as the only modulus or standard by which the magnitudes of all the other bodies in the universe, and the distances which separate them from the earth and from each other, can be measured.

2312. Necessary to ascertain its form, dimensions, and motions.— But since the apparent magnitudes, motions, and relative arrangement of surrounding objects severally vary, not only with every change in the position of the station of the observer, but even with every change of position of the observer on that station, it is most necessary to ascertain with all attainable accuracy the dimensions of the earth, which is the station of the astronomical observer, its form, and the changes of position in relation to surrounding objects to which it is subject.

2313. Form globular. — The first impression produced by the aspect presented by the surface of the earth is that of a vast indefinite plane surface, broken only by the accidents of the ground on land, such as hills and mountains, and by the more mutable forms due to the agitation of the fluid mass on the sea. Even this departure from the appearance of an extensive plane surface ceases on the sea out of sight of land in a perfect calm, and on certain planes of vast extent on land, such as some of the prairies of the American continents.

This first impression is soon shown to be fallacious; and it is easily demonstrated that the immediate indications of the unaided sense of vision, such as they are, are loosely and incorrectly interpreted, and that, in fact, even that small part of the earth's surface which falls at once within the range of the eye in a fixed position does not appear to be a plane.

Supposing that any extensive part of the surface of the earth were really a plane, let several stakes or posts, of equal height, be erected along the same straight line, and at equal distances, say a mile apart. Let these stakes be represented by s s, s' s', s" s', cc., fig. 692, and let a stake of equal height o o be erected at the station of the observer. Now, if the surface were a plane, it is evi-

dent that the points s, s', s'', &c. must appear to an eye placed at o in the same visual line, and would each be visible through a tube

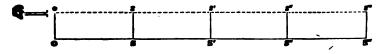


Fig. 692.

directed at o parallel to the surface o s. But such will not be found to be the case. When the tube is directed to s, all the succeeding points &, &, &c. will be below its direction. If it be directed to &, the point s will be above, and s' and all the succeeding points will be below its direction. In like manner, if it be directed to s', the preceding points s and s' will be above, and the succeeding points below its direction. In effect it will appear as though each succeeding stake were a little shorter than the preceding one. But as the stakes are all precisely equal, it must be inferred that the successive points of the surface 8, 8', 8", 8", &c. are relatively lower than the station o. Nor will the effects be explained by the supposition that the surface os s's", &c., is a descending but still a plane surface, because in that case the points s, s', s'', &c. must still be in the same visual line directed from o. It therefore follows that the surface in the direction o s' s" s", &c. is not plane but curved, as represented in fig. 693, where the visual lines are in obvious accordance with the actual appearances as above explained.

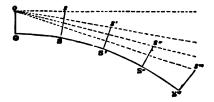


Fig. 693.

Now since these effects are found to prevail in every direction around the point of observation o, it follows that the curvature of the surface prevails all around that point; and since the extent of the depression of the points s, s', &c. at equal distances from o, are equal in every direction around o, it follows that the curvature is in every direction sensibly uniform around that point.

But by shifting the centre of observation o, and making similar

observations elsewhere, and on every part of the earth where such a process is practicable, not only are like effects observed, but the degree of depression corresponding to equal distances from the centres of observation is the same.

Hence we infer that the surface of the earth, as observed directly by the cye, is not a plane surface, but one everywhere curved, and that the curvature is everywhere uniform, at least that no departure from perfect uniformity in its general curvature exists sufficiently considerable to be discovered by this method.

But the only form of a solid body which has a surface of uniform ourvature is a sphere or globe, and it is therefore established that such is the form of the earth.

2314. This conclusion corroborated by circumnavigation. — If a vessel sail, as far as it is practicable to do so, constantly in the same direction, it will at length return to the port of its departure, having circumnavigated the earth; and during its course it appears to pass over an uniform surface. This is obviously what must take place so far as regards that part of the earth which is covered with water, supposing it to be a globe.

2315. Corroborated by lunar eclipses.—But the most striking and conclusive corroboration of the inference just made, and indeed a phenomenon which alone would demonstrate the form of the earth, is that which is exhibited in lunar eclipses. These appearances, which are so frequently witnessed, are caused by the earth coming between the sun and the moon, so as to cast its shadow upon the latter. Now the form of that shadow is always precisely that which one globe would project upon another. The phenomenon thus at once establishes not only the globular form of the earth, but that of the moon also.

2316. Various effects indicating the earth's rotundity.—The rotundity of the earth being once admitted, a multitude of its consequences and effects present themselves, which supply corroborative evidence of that important proposition.

When a ship sails from the observer, the first part which should cease to be visible, if the earth was a plane, would be the rod of the top-mast, having the smallest dimensions, and the last the hull and sails, being the greatest in magnitude; — but, in fact, the very reverse takes place. The hull first disappears, then the sails, and in fine the top-mast alone is visible by a telescope, appearing like a pole planted in the water. This becomes gradually shorter, appearing to sink in the water as the vessel recedes from the eye.

These appearances are the obvious consequences of the gradual interposition of the convexity of the part of the earth's surface over which the vessel has passed, and will be readily comprehended by the fig. 691.

If the observer take a more elevated position, the same succession of phenomena will be presented, only greater distances will be



Fig. 694.

necessary to produce the same degree of apparent sinking of the vessel.

Land is visible from the top-mast in approaching the shore, when it cannot be seen from the deck.

The top of the peak of Teneriffe can be seen from a distance when the base of the mountain is invisible.

The sun shines on the summits of the Alps long after sunset in the valleys.

An aeronaut ascending after sunset has witnessed the sun to reappear with all the effects of sunrise. On descending, he witnessed a second sunset.

2317. Dimensions of the earth. — Method of measuring a degree. — Having thus ascertained that the form of the carth is a globe, it now remains to discover its magnitude, or what is the same, its diameter.

For this purpose it will be necessary first to ascertain the actual length of a degree upon its surface, that is, the distance between two points on the surface, so placed that the lines drawn from them to the centre shall make with each other an angle of one degree.

Let p and p', fig. 695, represent two places upon the carth's surface, distant from each other from 60 to 100 miles, and let c be the centre of the earth. Now, let us suppose that two observers at the places p and p' observe two stars s and s', which at the same time are vertically over the two places, and to which, therefore, plumblines suspended at the two places would be directed. The direction of these plumb-lines, if continued downwards, would intersect at c, the centre of the earth.

The visual angle under the directions of these stars s and s' at p' is s p' s', and at c is s o s'. But, owing to the insignificant proportion which the distances p p' and p c bear to the distances of the stars (as will be made evident hereafter), the visual angle of the stars, whether seen from p or c, will be the same. If, then, this visual

-- we centre c an angle of 1°, we

a:3600::D:d=D

since the number of seconds in a (2292).

2318. Length of a degree. — In been ascertained that the length o earth's surface is a little less than 7 miles, and may be expressed in feet bers) by 365,000.

It will therefore be easy to ren length of a degree is as many thousa

are days in the year.

2319. Length of a second of the a second is the 3600th part of a de also that the length of a second is a very nearly, a measure also easily ren

2820. Change of direction of the passing over a given direction. --] just been explained it will be under a plumb-line always points to the cer (when its direction is undisturbed by tion), its change of direction, in passi place to any other, may be always for I" for every hand



Fig. 695.

If the distance a be one degree, this will become -

$$r = \frac{365000}{3600} \times 206265 = 20,912,979,$$

or very nearly 21 million feet, which is equal to 3960 statute miles. So that the diameter of the earth would be 7920 miles, or in round numbers (for we are not here pretending to extreme arithmetical

precision) 8000 miles.

The process of observation above explained is not in its details exactly that by which the magnitude of the earth is ascertained, but it is in spirit and principle the method of observation and calculation. It would not be easy to find, for example, any two sufficiently observable stars which at one and the same moment would be vertically over the two places p and p', but any two stars nearly over them would equally answer the purpose by observing the extent of their departure from the vertical direction. Neither is it necessary that the two observations should exactly coincide as to time; but these details do not affect the principle of the method, and will be more clearly intelligible as the student advances.

2322. Superficial inequalities of the earth relatively insignificant. - It is by comparison alone that we can acquire any clear or definite notions of distances and magnitudes which do not come under the immediate cognizance of the senses. If we desire to acquire a notion of a vast distance over which we cannot pass, we compare it with one in which we have immediate and actual acquaintance, such as a foot, a yard, or a mile. And since the area or superficial extent of surfaces and the volume or bulk of solids are respectively determined by the length of their linear dimensions, the same expedient suffices to acquire notions of them. Astronomy, having to deal with magnitudes exceeding in enormous proportions those of all objects, even the most stupendous, which are so approachable as to afford means of direct sensible observation, we are incessantly obliged to have recourse to such comparisons in order to give some degree of clearness to our ideas, since without them our knowledge would become a mere assemblage of words, numbers, and geometrical diagrams.

Let us, then, consider the dimensions and form of the earth, as

they have been ascertained in the preceding paragraphs.

When it is stated that the earth is a globe, the first objection which will be raised by the uninformed student is that the continents, islands, and tracts of land with which it is covered are marked by considerable inequalities of level; that mountains rise into ridges and peaks of vast height; that the seas and oceans, though level at their surface in a certain general sense, are agitated by great waves, and alternately swelled and depressed by tides, and that the solid bottom of them is known to be subject to inequalities

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analogous in character, and not less in depth than those which prevail on the land. Since, then, it is the characteristic property of a globe that all points on its surface are equally distant from its centre, how, it may be demanded, can a mass of matter, so unequal in its surface as the earth is, be a globe?

It may be conceded at once, in reply to this objection, that the earth is not, in the strict geometric sense of the term, a globe. But let us consider the extent of its departure from the globular form, so far as relates to the superficial inequalities just adverted to.

The most lofty mountain peaks do not exceed five miles in height. Few, indeed, approach that limit. Most of the considerable mountainous districts are limited to less than half that height. No considerable tract of land has a general elevation even of one mile. The deepest parts of the sea have not been sounded; but it is certain that their depth does not exceed the heights of the most lofty mountains, and the general depth is incomparably less. The superficial inequalities of the aqueous surface produced by waves and tides are comparatively insignificant.

Now, let us consider how these several superficial inequalities would be represented, observing a due proportion of scale, even

on the most stupendous model.

Construct a globe 20 feet in diameter, as a model of the earth. Since 20 feet represents 8000 miles, 1-400th part of a foot, or 8-100th parts of an inch, represents a mile. The height, therefore, of the most lofty mountain peak, and the greatest depth of the ocean, would be represented by a protuberance or a hole having no greater elevation or depth than 15-100ths, or about the seventh part of an inch. The general elevation of a continent would be fairly represented by a leaf of paper pasted upon the surface, having the thickness of less than the fiftieth of an inch; and a depression of little greater amount would express the depth of the general bed of the sea.

It will therefore be apparent, that the departure of such a model from the true form of a globe would be in all, save a strictly geometrical sense, absolutely insignificant.

2323. Relative dimensions of the atmosphere. — The surface of the earth is covered by an ocean of air, which floats upon it as the waters of the seas rest upon their solid bed. The density of this fluid is greatest in the stratum which is in immediate contact with the surface of the land and water of the earth, and it diminishes in a very rapid ratio in ascending, so that one half of the entire atmosphere is included in the strata whose height is within 3½ miles of the surface. At an altitude of 80 miles, or the hundredth part of the earth's diameter, the rarefaction must be so extreme, that neither animal life nor combustion could be maintained.

The atmosphere, being then limited to such a height, would be

represented on the model above described by a stratum two inches and a half thick.

2224. If the earth moved, how could its motion be perceived?—Having thus ascertained, in a rough way, the form and dimensions of the earth, let us consider the question of its rest or mobility.

Nothing is more repugnant to the first impressions received from the aspect of the surface of the earth, and all upon it, than the idea that it is in motion. But if this universal impression be traced to its origin, and rightly interpreted, it will not be found erroneous, and will form no exception to the general maxim which induces all persons, not even excepting philosophers, to regard without disrespect

notions which have obtained universal popular acceptation.

What is the stability and repose ascribed by the popular judgment to the earth? Repose certainly absolute, so far as regards all objects of vulgar or popular contemplation. It is maintained, and maintained truly, that every thing upon the earth, so far as the agency of external causes is concerned, is at relative rest. Hills, mountains, and valleys, oceans, seas, and rivers, as well as all artificial structures, are in relative repose; and if our observation did not extend to objects exterior to the globe, the popular maxim would be indisputable. But the astronomer contemplates objects which either escape the attention of, or are imperfectly known to, mankind in general; and the phenomena which attend these render it manifest, that while the earth, in relation to all objects upon it and forming part of it, is at rest, it is in motion with relation to all the other bodies of the universe.

The motion of objects external to the observer is perceived by the sense of sight only, and is manifested by the relative displacement it produces among the objects affected by it, with relation to objects around them which are not in motion, and with relation to each Motions in which the person of the observer participates may affect the senses both of feeling and sight. The feeling is affected by the agitation to which the body of the observer is exposed. Thus, in a carriage which starts or stops, or suddenly increases or slackens its speed, the matter composing the person of the observer has a tendency to retain the motion which it had previous to the change, and is accordingly affected with a certain force, as if it were pushed or drawn from rest in one direction or the other. But once in a state of uniform motion, the sense of feeling is only affected by the agitation proceeding from the inequalities of the road. If these inequalities are totally removed, as they are in a boat drawn at a uniform rate on a canal, the sense of feeling no longer affords any evidence whatever of the motion.

A remarkable example of the absence of all consciousness of motion, so far as mere feeling is concerned, is presented to all who have ascended in a balloon. As the aerial vehicle floats with the

stratum of the air in which it is suspended, the feeling of the acronaut is that of the most absolute repose. The balloon seems as fixed and immoveable as the solid globe itself, and nothing could produce in the voyager, blindfolded, any consciousness whatever of motion. When however his eyes, unbandaged, are turned downwards, he sees the vast diorama below moving under him. Fields and woods, villages and towns, pass in succession, and the phenomena are such as to impress on the eye, and through the eye upon the mind, the conviction that the balloon is stationary, and the earth moving under it. A certain effort of the understanding, slight, it is true, but still an effort, is required to arrive at the inference that the impression than produced on the sense of vision is an illusion, that the motion with which the landscape seems to be affected is one which in reality affects the balloon in which the spectator is suspended, and that this motion is equal in speed, and contrary in direction, to that which appears to affect the subjacent country.

Now it will be evident, that if the globe of the earth, and all upon it, were floating in space, and moving in any direction at any uniform rate, no consciousness of such motion could affect any seasitive being upon it. All objects partaking in common in such motion, no more derangement among them would ensue than among the persons and objects transported in the car of the balloon, where the aeronaut, no matter what be the speed of the motion, can fill a glass to the brim as easily as if he were upon the solid ground. Supposing, then, that the earth were affected by any motion in which all objects upon it, including the waters of the ocean, the atmosphere, and clouds, would all participate, would the existence of such a motion be perceived by a spectator placed upon the earth who would himself partake of it? It is clear that he must remain for ever unconscious of it, unless he could find within the range of his vision some objects which, not partaking of the motion, would appear to have a motion contrary to that which the observer has in

But such objects are only to be looked for in the regions of space beyond the limits of the atmosphere. We find them in fine in the sun, the moon, the stars, and all the objects which the firmament presents. Whatever motion the earth may have, will impart to all these distant objects the appearance of a motion in the contrary direction.

common with the earth.

But how, it may be asked, is the apparent motion produced in distant objects by a real motion of the station in which the observer is placed, to be distinguished from the real motion of the distant objects themselves, which would give them the same apparent motion? Since the phenomena are absolutely identified, whether the apparent motion observed is produced by a real motion in the observer, or a real motion in the object observed, it is necessary to

seek for evidence; either that the object cheered make lare the real motion which would produce the there meets to that the statute of the observer has it. But before engaging in this treasure in it necessary, first, to obtain a clear and definite knowledge of what the apparent motion in question is; secondly, which is the real with a of the earth which could produce it: and wheth, what with the the real motion, or motions of the objects where when which produce the same phenomena.

2325. Parallax. - Since the apparent time if a limit time. depends on the direction of the visual line imparimental me memorial to such object, and since while the object remain remaining the direction of this visual line is charged with every thange of the things of the observer, such change of position produces accommend to a -

placement in the apparent position of the object.

This apparent displacement of any in the west and a tissue and to the change of position of the observer, is which required

It follows that a distant object seen by two bearings at informer places on the earth is seen in different directions, so that the some rent place in the firmament will be different. It would there are follow, that the aspect of the heavens would vary with mary things of position of the observer on the earth, just as the searche teach of objects on land which are stationary, that government there the deck of a vessel which sails or warms a long the man. The so happens, as will appear hereafter, that even the greatest to five to of position which can exist between itemseen to the same and or the is so small compared even with the neurest took se to the same. the apparent displacement, or PARALLAM, this interior is the small; while for the most numerous of these or a second transfer it is absolutely inappreciable by the most related mosts of some of tion and measurement.

Small as it is, however, so for as relates to the nearest we as of the universe, it is capable of deficise measurement and the amount of each of them supplies one if the name of which their themselve are calculated.

2826. Apparent and the place of the come - learn rallox. — When an original a way a second a would cause a sensible displace to the work and the viewed from different pure of the complement of the complement in registering its apparent point as at a fixed station if on which it is not only in the case of the The direction in which an in the man to be a series were to centre of the earth is called the TAUR Photowhich it is seen from any pass of observe that the earliest called its APPARENT PLACE and the apparent comparation of would be produced by the transfer of the observer from the course 16.

to the surface or vice verse, or, what is the same, the difference between the true and apparent places, is called the DIURNAL PARALLAX.

In fig. 696, let o represent the centre of the earth, P a place of observation on its surface, o an object seen in the zenith of P, o'

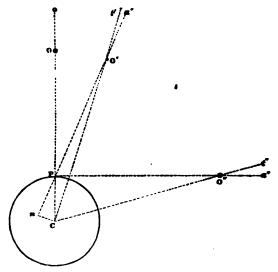


Fig. 696.

the same object seen at the zenith distance o P o', and o" the same object seen in the horizon.

It is evident that o will appear in the same direction, whether it be viewed from P or c. Hence it follows that in the zenith there is no diurnal parallax, and that there the apparent place of an object is its true place.

But if the object be at O', then the apparent direction is PO', while the true direction is CO', and the apparent place of the object will be a', while its true place will be a'; and the diurnal parallax corresponding to the zenith distance OPO' will be a', or the angle a' o' a'', which is equal to PO' C.

As the object is more remote from the zenith the parallax is angmented, because the semidiameter CP of the earth, which passes through the place of observation, is more and more nearly at right angles to the directions CO' and PO'.

2327. Horizontal parallax. — When the object is in the horizon, as at o", the diurnal parallax becomes greatest, and is called the

HORISONTAL PARALLAX. It is the angle PO" o which the semidiameter of the earth subtends at the object.

If z express the zenith distance, or the angle P C O', a line C n drawn from C at right angles to P O' s will be expressed by $z \times r \times \sin z$, r being the semidiameter C P of the earth. If D express the distance of the object O', and $\tilde{\omega}$ the parallactic angle P O' C, which is always very small, we shall have, by the principle explained in (2294):

$$\tilde{z}'' = 206265'' \times \sin z \times \frac{r}{p},$$

the parallax being expressed in seconds.

If the object be in the horizon as at o", we shall have $z=90^{\circ}$, and therefore

$$\tilde{\omega}'' = 206265'' \times \frac{r}{p}.$$

2328. Given the horizontal parallax and the earth's semidiameter, to compute the distance of the object.—It is evident that this important problem can be solved by the preceding formulæ; for we have (2297)

 $\mathbf{D} = \frac{206265}{200} \times \mathbf{r}.$

CHAP. III.

APPARENT FORM AND MOTION OF THE FIRMAMENT.

2329. Aspect of the firmament. — If we examine the heavens with attention on clear starlight nights, we shall soon be struck with the fact, that the brilliant objects scattered over them in such incalculable numbers maintain constantly the same relative position and arrangement. Every eye is familiar with certain groups of stars called constellations. These are never observed to change their relative position. A diagram representing them now would equally represent them at any future time; and if a general map be made, showing the relative arrangement of these bodies on any night, the same map will represent them with equal exactness and fidelity on any other night. There are a few, — some thirty or forty or so, — among many thousands, which are exceptions to this, with which, however, for the present we need not concern ourselves.

2330. The celestial hemisphere. — The impression produced upon the sight by these objects is that they are at a vast distance, but all

at the same distance. They seem as though they were attached in fixed and unalterable positions upon the surface of a vast hemisphere, of which the place of the observer is the centre. Setting aside the accidental inequalities of the ground, the observer seems to stand in the centre of a vast circular plane, which is the base of this celestial hemisphere.

2331. Horizon and zenith. — This plane, extended indefinitely around the observer, meets the celestial hemisphere in a circle which is called the Horizon, from the Greek word ὁριζεω (horizein), to terminate or bound, being the boundary or limit of the visible heavens.

The centre point of the visible hemisphere—that point which is perpendicularly above the observer, and to which a plumb-line suppended at rest would be directed—is called the Zenith.

2332. Apparent rotation of the firmament. — A few hours' attentive contemplation of the firmament at night will enable any common observer to perceive, that although the stars are, relatively to each other, fixed, the hemisphere, as a whole, is in motion. Looking at the zenith, constellation after constellation will appear to pass across it, having risen in an oblique direction from the horizon at one side, and, after passing the zenith, descending on the other side to the horizon, in a direction similarly oblique. Still more careful and longer continued observation, and a comparison, so far as can be made by the eye, of the different directions successively assumed by the same object, creates a suspicion, which every additional observation strengthens, that the celestial vault has a motion of slow and uniform rotation round a certain diameter as an axis, carrying with it all the objects visible upon it, without in the least deranging their relative positions or disturbing their arrangement.

Such an impression, if well founded, would involve, as a necessary consequence, that a certain point in the heavens, placed at the extremity of the axis of its rotation, would be fixed, and that all other points would appear to be carried around it in circles; each such point preserving therefore, constantly, the same distance from the point thus fixed.

2333. The pole star. — To verify this inference, we must look for a star which is not affected by the apparent rotation of the heavens, which affects more or less every other star.

Such a star is accordingly found, which is always seen in the same direction, — so far at least as the eye, unaided by more accurate means of observation, can determine.

The place of this star is called the POLE, and the star is called the POLE STAR.

2384. Rotation proved by instrumental observation. — Mere visual observation, however, can at most only supply grounds for probable conjecture, either as to the rotation of the sphere, or the position of its pole, if such rotation take place. To verify this conjecture, to determine with certainty whether the motion of the sphere be one of rotation, and if so, to ascertain with precision the direction of the axis round which this rotation takes place, its velocity, and, in fine, whether it be uniform or variable, — are problems of the highest importance, but which are altogether beyond the powers of mere visual observation, unaided by instruments of precision.

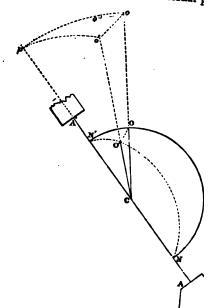
2335. Exact direction of the axis and position of the pole. -Suppose a telescope of low magnifying power, supplied with micrometric wires (2302), to be directed to the pole star, so that the star may be seen exactly upon the intersection of the middle wires. If this star were precisely at the extremity of the axis of the hemisphere, or at the pole, it would remain permanently at the intersection of the wires, notwithstanding the rotation of the firmament. Such is not, however, found to be the case. The star will appear to move; but, if the magnifying power of the telescope be low enough, it will not leave the field of view. It will appear to move in a small circle, the diameter of which is about three degrees. The telescope may be so adjusted that the star will move in a circle round the intersection of the middle wires as a centre; and in that case the point marked by the intersection of the middle wires is the true position of the Pole, round which the pole star is carried in a circle, at the distance of about 11°, by the rotation of the sphere.

2336. Equatorial instrument. — The exact direction of the axis of the celestial sphere being thus ascertained, it is possible to construct an apparatus which shall be capable of revolving upon a fixed axis, the direction of which shall coincide with that of the sphere; so that if a telescope were fixed in the direction of this axis, its line of collimation (2303) would exactly point to the celestial pole.

Upon this axis, thus directed and fixed, suppose a telescope to be so mounted that it may be placed with its line of collimation at any desired angle with the axis, and let a properly graduated are be provided, by which the magnitude of this angle may be measured with

all practical precision.

Thus, let A A', fig. 697, represent the direction of the axis on which the instrument is made to revolve. The line A A', if continued to the firmament, would pass through the pole p. Let c o represent the line of collimation of a telescope, so attached to the axis at c that it may be placed at any desired angle with it; which may be accomplished by placing a joint at o on which the telescope can turn. Let NON' be a graduated arc, to which the telescope is attached at 0, and which turns with the telescope round the axis



effected is represented in fig. 698, as given by the Astronomer Royal, in his lectures delivered at the Ipswich Museum.

The instrument is supported upon pivots, so that its axis A'B' shall coincide exactly with the direction of the celestial axis. The

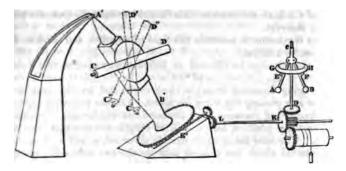


Fig. 698.

telescope C D turns upon a joint at the centre, so that different directions, such as C' D', C' D'', may be given to it. The motion upon its axis is imparted to it by wheel-work E L K, impelled by clockwork, as already mentioned.

2337. Rotation of firmament proved by equatorial. — Now, to establish, by means of this instrument, the fact that the firmament really has a motion of apparent rotation with a velocity rigorously uniform round the axis, let the telescope be first directed to any star, o, fig. 697, for example, so that it shall be seen upon the intersection of the middle wires. The line of collimation will then be directed to the star, and the angle OCN' or the arc ON' will express the ap-

parent distance of such star from the pole p.

Let the instrument be then turned upon its axis from east to west (that is, in the same direction as the rotation of the firmament), through any proposed angle, say 90°, and let it be fixed in that position. The firmament will follow it, and after a certain interval the same star will be seen upon the intersection of the wires; and in the same manner, whatever be the change of position of the instrument upon its axis, provided the direction of the telescope upon the arc o n', fig. 697, be not changed, the star will always arrive, after an interval more or less, according to the angle through which this instrument has been turned, upon the intersection of the wires.

It follows, therefore, from this, that the particular star here observed is carried in a circle round the heavens, always at the same distance, op, from the celestial pole.

The same observations being made with a like result upon every

star to which the telescope is directed, it follows that the motion of the firmament is such that all objects upon it describe circles at right angles to its axis, each object always remaining at the same distance from the pole.

This is precisely the effect which would be produced by the rotation of the heavens round an axis directed to the pole from the place

of the observer.

But it remains to ascertain the time of rotation, and whether the rotation be uniform.

If the telescope be directed as before to any star, so that it shall be seen at the intersection of the wires, let the instrument be then fixed, being detached from the clock-work, and let the exact time of the star passing the wires be noted. On the following night, at the approach of the same hour, the same star will be seen approaching to the same position, and it will at length arrive again upon the wires. The time being again exactly observed, it will be found that the interval which has elapsed between the two successive passages of the star over the wires is

23h. 56m. 4.09s.

Such is, therefore, the time in which the celestial sphere makes one complete revolution, and this time will be always found to be the same, whatever be the star to which the telescope is directed.

To prove that not only every complete revolution is performed in the same time, but that the rotation during the same revolution is uniform, let the instrument, after being directed to any star, be turned in the direction of the motion of the sphere through any proposed angle, 90° for example. It will be found that the interval which will elapse between the passage of the star over the wires in the two positions will, in this case, be the fourth part of 23^{h.} 56^{m.} 4.09^{s.}; and, in general, whatever be the angle through which the instrument may be turned, the interval between the passages of the same star over the wires in the two positions will bear the same proportion to 23^{h.} 56^{m.} 4.09^{s.}, as the angle bears to 360°.

It follows, therefore, that the apparent rotation of the heavens is

rigorously uniform.

It will be observed that the time of one complete revolution is 8^m. 55.91^s less than twenty-four hours, or a common day. The cause of this difference will be explained hereafter.

2338. Sidereal time. — The time of one complete revolution of the firmament is called a SIDEREAL DAY. This interval is divided, like a common day, into 24 hours, each hour into 60 minutes, and each minute into 60 seconds.

Since in 24 sidereal hours the sphere turns through 360°, and since its motion is rigorously uniform, it turns 15° in a sidereal hour, and through 1° in four sidereal minutes.

339. The same apparent motion observed by day. — It may be cted that although this description of the movement of the ens accords with the appearances during the night, there is no ence of the continuance of the same rotation during the day, e in a cloudless firmament no object is visible except the sun, the being alone cannot manifest the same community of motion exhibited by the multitudinous objects which, being crowded bickly on the firmament at night, move together without any age in their apparent relative position. To this objection it be answered that the moon is occasionally seen in the dayas well as the sun; and, moreover, that before sunset and rise the planets Jupiter and Venus are occasionally seen under purable atmospheric circumstances. Besides, with telescopes afficient power properly directed, all the brighter stars can be inctly seen when not situated very near the position of the sun. v, in all these cases, the objects thus seen appear to be carried ad by the same motion of the firmament, which is so much e conspicuously manifested in the absence of the sun and at

340. Certain fixed points and circles necessary to express the ition of objects on the heavens.—It will greatly contribute to facility and clearness with which the celestial phenomena and r causes shall be understood, if the student will impress upon memory the names and positions of certain fixed points, lines, circles of the celestial sphere, by reference to which the posiof objects upon it are expressed. Without incumbering him a more complex nomenclature than is indispensably necessary this purpose, we shall therefore explain some of the principal hese landmarks of the heavens.

341. Vertical circles, zenith, and nadir. — If from the place he observer a straight line be imagined to be drawn perpendar to the plane of the horizon, and to be continued indefinitely upwards and downwards, it will meet the visible hemisphere wertex, the Zenith, and the invisible hemisphere, which is er the plane of the horizon, at a corresponding point called the DIR.

f a plane be supposed to pass through the place of the obrer and the zenith, it will meet the celestial surface in a series points, forming a circle at right angles to the horizon. Such a le is called a VERTICAL CIRCLE, or, shortly, a VERTICAL.

f this plane be supposed to be turned round the line passing rards to the zenith, it will assume successively every direction and the observer, and will meet the heavens in every possible tical circle.

The vertical circles, therefore, all intersecting at the zenith as a

common point, divide the horizon as the divisions of the hours and minutes divide the dial-plate of a clock.

2342. The celestial meridian and prime vertical. — That vertical which passes though the celestial pole is called the MERIDIAN.

The meridian is, therefore, the only circle of the heavens which passes at once through the two principal fixed points, the pole and the zenith.

It divides the visible hemisphere into two regions on the right and left of the observer; as he looks to the north, that which is on his right being called the EASTERN, and that which is on his left the WESTERN.

Another vertical at right angles to the meridian is called the PRIME VERTICAL. This is comparatively little used for reference.

2343. Cardinal points. — The meridian and prime vertical divide the horizon at four points, equally distant, and therefore separated by arcs of 90°. These points are called the CARDINAL POINTS. Those formed by the intersection of the meridian with the horizon are called the NORTH and SOUTH points, that which is nearest to the visible pole in the northern hemisphere being the north. Those formed by the intersection of the prime vertical with the horizon are called the EAST and WEST, that to the right of an observer looking towards the north being the east.

The cardinal points correspond with those marked on the card of a mariner's compass, allowance being made for the variation of

the needle.

2344. The azimuth. — The direction of an object, whether terrestrial or celestial, in reference to the cardinal points, or to the plane of the meridian, is called its AZIMUTH. Thus it is said to have so many degrees of azimuth east or west, according as the vertical circle, whose plane passes through it, forms that angle east or west of the plane of the meridian.

2345. Zenith distance and altitude.—It is always possible to conceive a vertical circle which shall pass through any proposed object on the heavens. The arc of such a circle between the senith

and the object is called its ZENITH DISTANCE.

The remainder of the quadrant of the vertical between the object

and the horizon is called its ALTITUDE.

It is evident, therefore, that the altitude of the zenith is 90°, and the zenith distance of every point on the horizon is also 90°.

The arc of the meridian between the zenith and the pole is the zenith distance of the pole, and the arc of the meridian between the

pole and the horizon is the altitude of the pole.

2346. Celestial equator.—If a plane be imagined to pass through the place of the observer at right angles to the axis of the sphere, and to be continued to the heavens, it will meet the surface of the celestial vault in a circle which shall be 90° from the pole, and

which will divide the sphere into two hemispheres, at the vertex of one of which is the visible or north pole, and at the vertex of the other the invisible or south pole.

This circle is called the CELESTIAL EQUATOR.

The several fixed points and circles described above will be more clearly conceived by the aid of the diagram, fig. 699, where o is the

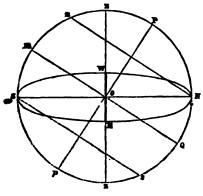


Fig. 699.

place of the observer, z the zenith, P the pole, S Z P N the visible, and S p z N the invisible half of the meridian; S E N W is the horizon seen by projection as an oval, being, however, really a circle; N and S are the north and south, and E and W the east and west cardinal points. The points of the several circles which are below the horizon are distinguished by dotted lines. The celestial equator is represented at Æ Q, and the prime vertical at z W E z, both being looked at edgewise.

A plane N n, drawn through the north cardinal point [and parallel to the celestial equator], cuts off a portion of the sphere, having the visible pole P at its centre, all of which is above the horizon; and a corresponding plane, S s, through the south cardinal point, cuts off a part, leaving the invisible pole at its centre, all of which is below

the horizon.

2347. Apparent motion of the celestial sphere. — Now, if the estire sphere be imagined to revolve on the line POp through the poles as a fixed axis, making one complete revolution, and in such a direction that it will pass over an observer at 0, looking towards N from his right to his left, carrying with it all the objects on the firmament, without disturbing their relative position and arrangement, we shall form an exact notion of the apparent motion of the heavens. All objects rise upon the eastern half, SEN, of the borizon, and set

upon the western half, swn. The objects which are nearer to the visible pole P than the circle nn never set; and those which are nearer to the invisible pole p than the circle ss never rise. Those which are between the equator EQ and the circle nn are longer above the horizon than below it; and those which are between the equator EQ and the circle ss are longer below the horizon than above it. Objects, in fine, which are upon the equator are equal times above and below the horizon.

When an object rises, it gradually increases its altitude until it reaches the meridian. It then begins to descend, and continues to

descend until it sets.

CHAP. IV.

DIURNAL ROTATION OF THE EARTH.

2348. Apparent diurnal rotation of the heavens—its possible causes.—The apparent diurnal rotation of the celestial sphere being such as has been explained, it remains to determine what is the real motion which produces it. Now it is demonstrable that it may be caused indifferently, either by a real motion of the sphere round the observer, corresponding in direction and velocity with the apparent motion, or by a real motion of the earth in the contrary direction, but with the same angular velocity upon that diameter of the globe which coincides with the direction of the axis of the celestial sphere, and that no other conceivable motion would produce that apparent rotation of the heavens which we witness. Between these two we are to decide which really exists.

2349. Supposition of the real motion of the universe inadmissible.—The fixity and absolute repose of the globe of the earth being assumed by the ancients as a physical maxim which did not even admit of being questioned, they perceived the inevitable character of the alternative which the apparent diurnal rotation of the heavens imposed upon them, and accordingly embraced the hypothesis, which now appears so monstrous, and which is implied in the

term UNIVERSE,* which they have bequeathed to us.

It is true that, owing to the imperfect knowledge which prevailed as to the real magnitudes and distances of the bodies to which this common motion was so unhesitatingly ascribed, the improbability of the supposition would not have seemed so gross as it does to the more enlightened enquirers of our age. Nevertheless, in any view

^{*} UNUS, one, and VERSUM, turning, or rotation, - turning with one common motion of rotation.

of it, and even with the most imperfect knowledge, the hypothesis which required the admission that the myriads of bodies which sppear upon the firmament should have, besides the proper motions of several of them, such as the moon and planets, of which the ancients were not unaware, motions of revolution with velocities so prodigious and so marvellously related, that all should, in the short interval of twenty-four hours, whirl round the axis of the earth with the unerring harmony and regularity necessary to explain the apparent diurnal rotation of the firmament, ought to have raised serious difficulties and doubts.

But with the knowledge which has been obtained by the labours of modern astronomers respecting the enormous magnitudes of the principal bodies of the physical universe, magnitudes compared with which that of the globe of the earth dwindles to a mere point, and their distances, under the expression of which the very power of number itself almost fails, and recourse is had to colossal units in order to enable it to express even the smallest of them, the hypothesis of the immobility of the earth, and the diurnal rotation of the countless orbs, of magnitudes so inconceivable filling the immensity of space once every twenty-four hours round this grain of matter composing our globe, becomes so preposterous that it is rejected, not as an improbability, but as an absurdity too gross to be even for a moment seriously entertained or discussed.

2350. Simplicity and intrinsic probability of the rotation of the earth. — But if any ground for hesitation in the rejection of this hypothesis existed, all doubt would be removed by the simplicity and intrinsic probability of the only other physical cause which can produce the phenomena. The rotation of the globe of the earth upon an axis passing through its poles, with an uniform motion from west to east once in twenty-four hours, is a supposition against which not a single reason can be adduced based on improbability. Such a motion explains perfectly the apparent diurnal rotation of the celestial sphere. Being uniform and free from irregularities, checks, or jolta, it would not be perceivable by any local derangement of bodies on the surface of the earth, all of which would participate in it. Observers upon the surface of our globe would be no more conscious of it, than are the voyagers shut up in the cabin of a canal-boat, or transported above the clouds in the car of a balloon.

2351. Direct proofs of the earth's rotation. — Irresistible, nevertheless, as this logical alternative is, the universality and antiquity of the belief in the immobility of the earth, and the vast physical importance of the principle in question, have prompted enquirers to search for direct proofs of the actual motion of the earth upon its axis. Two phenomena have accordingly been produced as immediate and conclusive proof of this motion.

11 *

2852. Proof by the descent of a body from a great height.—It has been already (184) shown that a body descending from a great height does not fall in the true vertical line, which it would if the earth were at rest, but eastward of it, which it must, if the earth have a motion of rotation from west to east.

2353. M. Leon Foucault's mode of demonstration.—An ingenious expedient, by which the diurnal rotation of the earth is rendered visible, has been conceived and reduced to experiment by M. Leon This contrivance is based upon the principle, that the direction of the plane of vibration of a pendulum is not affected by any motion of translation which may be given to its point of su-Thus, if a pendulum suspended in a room and put into vibration in a plane parallel to one of the walls be carried round a circular table, the plane of its vibration will continually be parallel to the same wall, and will therefore vary constantly in the angle it forms with the radius of the table which is directed to it.

Now, if a pendulum, suspended any where so near the pole of the earth that the circle round the pole may be considered a plane, be put in vibration in a plane passing through the pole, this plane, continuing parallel to its original direction as it is carried round the pole by the earth's rotation, will make a varying angle with the line drawn to the pole from the position it occupies. After being carried through a quarter of a revolution it will make an angle of 90° with the line to the pole, and so on. In fine, the direction of the pole will appear to be carried round the plane of vibration of the pendulum.

The same effects will be produced at greater distances from the pole, but the rate of variation of the angle under the plane of vibration and the plane of the meridian will be different, owing to the effects of the curvature of the meridian.

This phenomenon, therefore, being a direct effect of the rotation of the earth, supplies a proof of the existence of that motion, attainable without reference to objects beyond the limits of the

globe.

2354. Analogy supplies evidence of the earth's rotation. - The obvious analogy of the planets to the earth, which will appear more fully hereafter, would supply strong evidence in favour of the earth's rotation, even if positive demonstration were wanting. planets are globes like the earth, receiving light and heat from the same luminary, and, like the earth, revolving round it. the planets which we have been enabled to observe have motions of rotation on axes, in times not very different from that of the earth.

2355. Figure of the earth supplies another proof. - Besides these, it will be shown hereafter that another proof of the rotation of the earth is supplied by a peculiar departure from the strictly

globular form.

23.6. How this rotation of the earth explains the diurnal phonomona.—We are then to conclude that the earth, being a globe, has a motion of uniform rotation round a certain diameter. The universe around it is relatively stationary, and the bodies which compase it being at distances which mere vision cannot appreciate, appear as if they were situate on the surface of a vast celestial sphere in the centre of which the earth revolves. This rotation of the earth gives to the sphere the appearance of revolving in the contrary direction, as the progressive motion of a boat on a river gives to the banks an appearance of retrogressive motion; and since the apparent motion of the heavens is from east to west, the real rotation of the earth which produces that appearance must be from west to east.

How this motion of rotation explains the phenomena of the rising and setting of celestial objects is easily understood. An observer placed at any point upon the surface of the earth is carried round the axis in a circle in twenty-four hours, so that every side of the celestial sphere is in succession exposed to his view. As he is serried upon the side opposite to that in which the sun is placed, he sees the starry heavens visible in the absence of the splendour of that luminary. As he is turned gradually towards the side where the sun is placed, its light begins to appear in the firmament, the dawn of morning is manifested, and the globe continuing to turn, he is brought into view of the luminary itself, and all the phenomena of dawn, morning, and sunrise are exhibited. While he is directed towards the side of the firmament in which the sun is placed, the other bodies of inferior lustre are lost in the splendour of that luminary, and all the phenomena of day are exhibited. When by the continued rotation of the globe the observer begins to be turned away from the direction of the sun, that luminary declines, and at length disappears, producing all the phenomena of evening and sunset.

Such, in general, are the effects which would attend the motion of a spectator placed upon the earth's surface, and carried round with it by its motion of rotation. He is the spectator of a gorgeous diorama exhibited on a vast scale, the earth which forms his station being the revolving stage by which he is carried round, so as to view in succession the spectacle which surrounds him.

These appearances vary with the position assumed by the observer on this revolving stage, or, in other words, upon his situation on the earth, as will presently appear.

2357. The earth's axis.—That diameter upon which it is necessary to suppose the earth to revolve in order to explain the pheno-

mena, is that which passes through the terrestrial poles.

2358. The terrestrial equator, poles, and meridians.—If the globe of the earth be imagined to be cut by a plane passing through its centre at right angles to its axis, such a plane will meet the sur-

face in a circle, which will divide it into two hemispheres, at the summits of which the poles are situate. This circle is called the TERRESTRIAL EQUATOR.

That hemisphere which includes the continent of Europe is called the NORTHERN HEMISPHERE, and the pole which it includes is called the NORTHERN TERRESTRIAL POLE; the other hemisphere being the SOUTHERN HEMISPHERE, and including the SOUTHERN TERRESTRIAL POLE.

If the surface of the earth be imagined to be intersected by planes passing through its axis, they will meet the surface in circles which, passing through the poles, will be at right angles to the counter. These circles are called TERRESTRIAL MERIDIANS, and will be seen

delineated on any ordinary terrestrial globe.
2359. Latitude and longitude.—The position of places upon the surface of the earth are expressed and indicated by stating their distance north or south of the equator, measured upon a meridian passing through them, and by the distance of such meridian east or west of some fixed meridian arbitrarily selected, such as the meri-dian passed through the observatory at Greenwich. The former distance, expressed in degrees, minutes, and seconds, is called the LATITUDE, and the latter, similarly expressed, the Longitude of

the place.

2860. Fixed meridians - those of Greenwich and Paris. - As no natural phenomenon is found by which a fixed meridian from which longitude is measured can be determined, astronomers and geographers have not agreed in the arbitrary selection of one. The meridians of the Greenwich and Paris observatories have been taken, the former by English and the latter by French authorities. To reduce the longitudes expressed by either as the starting-point. to the other, it is only necessary to add or substract the angle under the meridians of the two observatories, which has been ascertained to be 2° 20' 22", the meridian of Paris being east of that of Greenwich.

2361. How the diurnal phenomena vary with the latitude. -Let s Æ N Q, fig. 700, represent the earth suspended in space, surrounded at an immeasurable distance by the stellar universe. The magnitude of the earth being absolutely insignificant compared with the distances of the stars, the aspect of these will be the same whether they are viewed from any point on its surface, or from its The observer may therefore, whatever be his position on the earth, be considered as looking from the centre of the celestial sphere.

Let us suppose, in the first place, the observer to be at o, a point on its surface between the equator Æ and the north pole N, the latitude of which will therefore be o z, and will be measured by the angle oc z. If a line be imagined to be drawn from the centre o through the place of the observer, and continued upwards to the francest, it will arrive at the point z, which is the senith of the deserver. If the terrestrial axis s n be imagined to be continued to the francest, it will arrive at the north celestial pole n and the stab colorial pole s. If the plane of the terrestrial equator z q has a pole of the celestial sphere at the celestial equator z q.

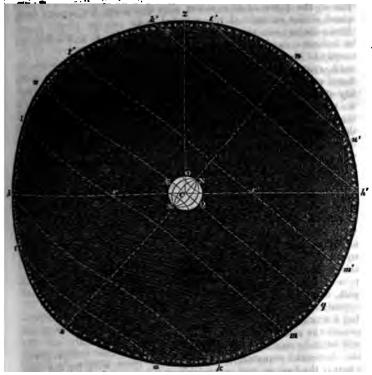


Fig. 700.

The cheavest placed at o will see the entire hemisphere hzh' of which his menith s is the summit; and the other hemisphere hzh' will be invisible to him, being in fact concealed from his view by the earth on which he stands.

Is a evident that the are of the heavens an between his zenith and the mosth delectial pole consists of the same number of degrees in the are on of the terrestrial meridian between his place of ob-

servation 0 and the north terrestrial pole N. The zenith distance therefore of the visible pole at any place is always equal to the actual distance expressed in degrees of that place from the terrestrial pole, and as this distance is the COMPLEMENT* OF THE LATITUDE, it follows that the zenith distance of the visible pole is the complement of the latitude, and that the altitude of the visible pole

is equal to the latitude of the place.

2362. Method of finding the latitude of the place. - The latitude of the place of observation may therefore be always determined if the altitude of the celestial pole can be observed. there were any star situate precisely at the pole, it would therefore be sufficient to observe its altitude. There is, however, no star exactly at the pole, although, as has been already observed, the POLE STAR is very near it. The altitude of the pole is found, therefore, not by one, but by two observations. The pole star, or any other star situate near the pole, is carried round it in a circle by the apparent diurnal motion of the sphere, and it necessarily crosses the meridian twice in each revolution, once above, and once below the pole. Its altitude in the latter position is the least, and in the former the greatest it ever has; and the pole itself is just midway between these two extreme positions of this circumpolar star. To find the actual altitude of the pole, it is only necessary therefore to take the mean, that is, half the sum of these two extreme altitudes. By making the same observations with several circumpolar stars, and taking a mean of the whole, still greater accuracy may be attained.

2363. Position of celestial equator and poles varies with the latitude.—Since the altitude of the celestial pole is everywhere equal to the latitude of the place, and since the position of the celestial equator and its parallels, in which all celestial objects appear to be moved by the diurnal rotation, varies with that of the pole, it is evident that the celestial sphere must present a different appearance to the observer at every different latitude. In proceeding towards the terrestrial pole, the celestial pole will gradually approach the zenith, until we arrive at the terrestrial pole, when it will actually coincide with that point; and in proceeding towards the terrestrial equator, the celestial pole will gradually descend towards the horizon, and on arriving at the Line it will be actually on the horizon.

2364. Parallel sphere seen at the poles. — At the poles, therefore, the celestial pole being in the zenith, the celestial equator will coincide with the horizon, and by the diurnal motion all objects will move in circles parallel to the horizon. Every object will

^{*} The complement of an angle or arc is that number of degrees by which it differs from 90°. Thus 30° degrees is the complement of 60°.

therefore preserve during twenty-four hours the same slittude and the same zenith distance. No object will either rise or set, at least so far as the diurnal motion is concerned.

This aspect of the firmament is called a PARALLEL SPHERE, the

motion being parallel to the horizon.

2365. Right sphere seen at the equator. — At the terrestrial equator, the poles being upon the horizon, the axis of the celestial sphere will coincide with a line drawn upon the plane of the horizon connecting the north and south points. The celestial equator and its parallels will be at right angles to the plane of the horizon; and since the plane of the horizon passes through the centre of all the parallels, it will divide them all into equal somicircles.

It follows, therefore, that all objects on the heavens will be equal times above and below the horizon, and that they will rise and set

in planes perpendicular to the horizon.

This aspect of the firmament is called a RIGHT SPHERE, the diurnal

motion being at right angles to the horizon.

2366. Oblique sphere seen at intermediate latitudes.—At latitudes between the equator and the pole, the celestial pole holds a place between the horizon and the zenith determined by the latitude. The celestial equator x = q, fig. 700, and its parallels, are inclined to the plane of the horizon at angles equal to the distance of the pole from the zenith, and therefore equal to the complement of the latitude. The centres of all parallels to the celestial equator x = q which are between it and the visible pole are above the plane of the horizon, between c and n, and the centres of all parallels at the other side of the equator below it. The parallels, such as l' m' and l m, will therefore be all divided unequally by the plane of the horizon, the visible part l' r' being greater than the invisible part l' r' for the former, and the invisible part l' r' for the latter.

It follows, therefore, that all objects between the celestial equator $x \neq q$ and the visible pole n will be longer above than below the horizon, and all objects on the other side of the equator will be longer

below the horizon than above it.

A parallel k'k' to the celestial equator, whose distance from the visible pole is equal to the latitude, will be entirely above the horizon, just touching it at the point under the visible pole; and a corresponding parallel hk, at an equal distance from the invisible pole, will be entirely below the horizon, just touching it at the point above the invisible pole.

All parallels nearer to the visible pole than h' k' will be entirely above the horizon, and all parallels nearer to the invisible pole than

hk will be entirely below it.

Hence it is that, in European latitudes, stars within a certain limited distance of the north or visible celestial pole never set, and stars

at a corresponding distance from the south or invisible celestial pole never rise.

The observer can only see these by going to places of observation having lower latitudes.

This aspect of the firmament is called an OBLIQUE SPHERE, the diurnal motion being oblique to the horizon.

2367. Objects in celestial equator equal times above and below horizon. — Whether the sphere be right or oblique, the centre of the celestial equator being on the plane of the horizon, one half of that circle will be below, and the other half above the horizon. Every object upon it will therefore be equal times above and below the horizon, rising and setting exactly at the east and west points.

In the parallel sphere, the celestial equator coinciding with the horizon, an object upon it will be carried round the horizon by the diurnal rotation, without either rising or setting.*

2368. Method of determining the longitude of places.—This perfect uniformity of the earth's rotation, inferred from the observed uniformity of the apparent rotation of the firmament, is the basis of all methods of determining the longitude. The longitude of a place will be determined if the angle under the meridian of the place, and that of any other place whose longitude is known, can be found. But since, by the uniform rotation of the globe, the meridians of all places upon it are brought in regular succession under every part of the firmament, the moments at which the two meridians pass under the same star, or, what is the same, the moments at which the same star is seen to pass over the two meridians, being observed, the interval will bear the same ratio to the entire time of the earth's rotation as the difference of the longitudes of the two places bears to 360°.

To make this more clear, let us take the case of two places P and P', fig. 701, upon the equator. If c be the centre of the earth, the angle P C P' will be the difference between the longitudes. Now, let the time be observed at each place at which any particular stars is seen upon the meridian. If the motion of the earth be in the direction of the arrow, the meridian of P will come to the star before the meridian of P'. This necessarily supposes P to be east of P', since the earth revolves from west to east. Let the true interval of time between the passage of s over the two meridians be t, let T be the time of one complete revolution of the globe on its axis, and

^{*}The teacher will find it advantageous to exercise the student in the subject of the preceding paragraphs, aided by an armillary sphere, or, if that be not accessible, by a celestial globe, which will serve nearly as well. Many questions will suggest themselves, arising out of and deducible from what has been explained above, with respect to the various altitudes of the sphere in different latitudes.



Fig. 701.

let L be the difference of the longitudes, or the angle PCP'; we shall then have

t: T:: L: 360°,

$$L = \frac{t}{\pi} \times 360^{\circ}$$
.

But in the practical solution of this problem a difficulty is presented which has conferred historical celebrity upon the question, and caused it to be referred to as the type of all difficult enquiries. It is supposed, in what has just been explained, that means are provided at the two places P and P' by which the absolute moments of the transit of the star over the respective meridians may be ascertained, so as to give the exact interval between them. If these moments be observed by any form of chronometer, it would

then be necessary that the two chronometers should be in exact accordance, or, what is the same, that their exact difference may be known. If a chronometer, set correctly by another which is stationary at one place P, be transported to the other place 1', this object will be attained, subject, however, to the error which may be incidental to the rate of the chronometer thus transported. If the distances between the places be not considerable, the chronometers may thus be brought into very exact accordance; but when the distance is great, and that a long interval must elapse during the transport of the chronometer, this expedient is subject to errors too considerable to be tolerated in the solution of a problem of such capital importance.

It will be apparent that the real object to be attained is, to find some phenomenon sufficiently instantaneous in its manifestation to mark, with all the necessary precision, a certain moment of time. Such a phenomenon would be, for example, the sudden extinction of a conspicuous light seen at once at both places. The moment of such a phenomenon being observed by means of two chronometers at the places, the difference of the times indicated by them would be known, and they would then serve for the determination of the difference of the longitudes by the method explained above. Several phenomena, both terrestrial and celestial, have accordingly been used Among the former may be mentioned the sudden for this purpose. extinction of the oxyhydrogen or electric light, the explosion of a rocket, &c.; among the latter, the extinction of a star by the disc of the moon passing over it, and the eclipse of the satellites of certain planets, phenomena which will be more fully noticed hereafter.

2369. Lunar method of finding the longitude. - The change of position of the moon with relation to the sun and stars being very rapid, affords another phenomenon which has been found of great utility in the determination of the longitude, especially for the purposes of mariners. Tables are calculated in which the moon's spparent distances from the sun, and many of the most conspicuous fixed stars, are given for short intervals of time, and the exact times at Greenwich when the moon has these distances are given. If then the mariner, observing with proper instruments the position of the moon with relation to these objects, compares his observed distances with the tables which are supplied to him in the Nautical Almanack, he will find the time at Greenwich corresponding to the moment of his observation; and being always, by the ordinary methods, able to determine by observation the local time at the place of his observation, the difference gives him the time required for a star to pass from the meridian of Greenwich to the meridian of the place of his observation, or vice versa; and this time gives the longitude, as already explained.

This last is known as the LUNAR METHOD OF DETERMINING THE

LONGITUDE.

In practice, many details are necessary, and various calculations

must be made, which cannot be explained here.

2370. Method by electric telegraph. — When two places are connected by a line of electric telegraph, their difference of longitude can be easily and exactly determined, inasmuch as instantaneous signals can be transmitted, by which the local clocks can be compared and regulated, and, if it be so desired, kept in exact accordance.

2371. Parallels of latitude. — A series of points on the earth which are at equal distances from the equator, or which have the same latitude, form a circle parallel to the equator, called a PARALLEL OF LATITUDE.

Thus all places which have the same latitude are on the same par-

All places which are on the same meridian have the same longitude.

CHAP. V.

SPHEROIDAL FORM, MASS, AND DENSITY OF THE EARTH.

2372. Progress of physical investigation approximative.—It is the condition of man, and probably of all other finite intelligences, to arrive at the possession of knowledge by the slow and laborious

process of a sort of system of trial and error. The first conclusions to which, in physical inquiries, observation conducts us, are never better than very rough approximations to the truth. These being submitted to subsequent comparison with the originals, undergo a first series of corrections, the more prominent and conspicuous departures from conformity being removed. A second approximation, but still only an approximation, is thus obtained; and another and still more severe comparison with the phenomena under investigation is made, and another order of corrections is effected, and a closer approximation obtained. Nor does this progressive approach to perfect exactitude appear to have any limit. The best results of our intellectual labours are still only close resemblances to truth, the absolute perfection of which is probably reserved for a higher intellectual state.

The labours of the physical inquirer resemble those of the sculptor, whose first efforts produce from the block of marble a rude and uncouth resemblance of the human form, which only approaches the grace and beauty of nature by comparing it incessantly and indefatigably with the original; detaching from it first the grosser and rougher protuberances, and subsequently reducing its parts by the nicer and more delicate touches of the chisel to near

conformity with the model.

It would, however, be a great mistake to depreciate on this account the results of our first efforts in the acquisition of a knowledge of the laws of nature. If the first conclusions at which we arrive are erroncous, they are not therefore the less necessary to the ultimate attainment of more exact knowledge. They prove, on the contrary, not only to be powerful agents in the discovery of those corrections to which they are themselves to be submitted, but to be quite indispensable to our progress in the work of investigation and discovery.

These observations will be illustrated by the process of instruction and discovery in every department of physical science, but in none so frequently and so forcibly as in that which now occupies us.

2373. Figure of the earth an example of this.—The first conclusions at which we have arrived respecting the form of the earth is that it is a globe; and with respect to its motion is, that it is in uniform rotation round one of its diameters, making one complete revolution in twenty-four hours sidereal time, or 23h. 56m. 4.09s. common or civil time.

2374. Globular figure incompatible with rotation.—The first question, then, which presents itself is, whether this form and rotation are compatible? It is not difficult to show, by the most simple principles of physics, that they are not; that with such a form such a rotation could not be maintained, and that with such a rotation such a form could not permanently continue. And if this can be

certainly established, it will be necessary to retrace our steps, to submit our former conclusions to more rigorous comparison with the objects and phenomena from which they were derived, and ascertain which of them is inexact, and what is the modification and correction to which it must be submitted in order to be brought into harmony with the other.

2375. Rotation cannot be modified—supposed form may.—The conclusion that the earth revolves on its axis with a motion corresponding to the apparent rotation of the firmament, is one which admits of no modification, and must from its nature be either absolutely admitted or absolutely rejected. The globular form imputed to the earth, however, has been inferred from observations of a general nature, unattended by any conditions of exact measurement, and which would be equally compatible with innumerable forms, departing to a very considerable and measurable extent from

that of an exact geometrical sphere

or globe.

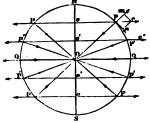


Fig. 702.

2376. How rotation would affect the superficial gravity on a globe.—
Let NQS, fig. 702, represent a section of a globe supposed to have a motion of rotation round the diameter NS as an axis. Every point on its surface, such as P or P', will revolve in a circle, the centre of which o or o' will be upon the axis, and the radius o P or o' P' will gradually decrease in approaching the poles N and S, where no motion takes place, and will gra-

dually increase in approaching the equator QOQ, where the circle of rotation will be the equator itself.

A body placed at any part of the surface, such as P, being thus carried round in a circle, will be affected by a centrifugal force, the intensity of which will be expressed by (314)

$$c = 1.226 \times R \times N^2 \times W$$

where R = Po, the radius of the circle, N the fraction of a revolution made in one second, and W the weight of the body, and the direction of which is Pc.

This centrifugal force being expressed by Pc is equivalent (170) to two forces expressed in intensity and direction by Pm and Pm. The component Pm is directly opposed to the weight W of the body, which acts in the line PO directed to the centre, and has the effect of diminishing it. The component Pm being directed towards the equator Q, has a tendency to cause the body to move towards the equator; and the body, if free, would necessarily so move.

Now it will be evident, by the mere inspection of the diagram, that the nearer the point P is to the equator Q, the more directly will the centrifugal force P c be opposed to the weight, and consequently the greater will be that component of it, P m, which will

have the effect of diminishing the weight.

But this diminution of the weight is further augmented by the increase of the actual intensity of the centrifugal force itself in approaching the equator. By the above formula, it appears that the intensity of the centrifugal force must increase in proportion as the radius R or Po increases. Now it is apparent that Po increases gradually in going from P to Q, since P' O' is greater, and Q o greater, still than Po; and that, on the other hand, it decreases in going from P to N or S, where it becomes nothing.

Thus the effect of the centrifugal force in diminishing weight being nothing at the pole N or S, gradually increases in approaching the equator; first, because its absolute intensity gradually increases; and secondly, because it is more and more directly opposed to gravity until we arrive at the equator itself, where its intensity is greatest,

and where it is directly opposed to gravity.

The effects, therefore, produced by the rotation of a globe, such as the earth has been assumed to be, are —1°. The decrease of the weights of bodies upon its surface, in going from the pole to the equator; and 2°. A tendency of all such bodies as are free to move from higher latitudes in either hemisphere towards the equator.

2377. Amount of the diminution of weight produced at the equator by centrifugal force. This quantity may be easily com-

puted by means of the formula

$$c = 1.226 \times R \times N^2 \times W$$
.

Taking the radius of the equator in round numbers (which are sufficient for this purpose) at 4000 miles, and reducing it to feet, and reducing the time of rotation 23th 56m 4.09 to seconds, we shall have

$$R = 21,120,000, \qquad N = \frac{1}{86.164}$$
:

substituting these numbers we have

$$c = 1,226 \times 21,120,000 \times \frac{1}{(86,164)^2} \times w;$$

and executing the arithmetical operations here indicated, we find

$$c = \frac{1}{287} \times w.$$

The centrifugal force would therefore be the 287th part of the weight, and as it is directly opposed to gravity, the weight would sustain this entire loss.

2378. Loss of weight at other latitudes. — The centrifugal force at any latitude P would be less than at Q in the ratio of Q to oP. But the part of this P m which is directly opposed to the weight is less than the whole P c, in the ratio of P c to P m, or, what is the same, of P o or O Q to P o. If then c' express the whole centrifugal force at P, and C' that part of it which is directly opposed to gravity, we shall have

$$\sigma' = \frac{1}{287} \times \frac{Po}{OQ}, \qquad \sigma'' = \sigma' \times \frac{Po}{OQ} = \frac{1}{287} \times \left(\frac{Po}{OQ}\right).$$

The number which expresses $\frac{PO}{OQ}$ is that which is called in Tr gonometry the cosine of the arc PQ, that is, the cosine of the lat tude. Therefore we have

$$c'' = \frac{1}{287} \times \cos^2 \text{ lat.}$$

The loss of weight, therefore, which would be sustained by reast of the centrifugal force at any proposed latitude, would be a fration of the whole weight, found by dividing the square of the cosi of latitude by 287.

2379. Effect of centrifugal force on the geographical condition of the surface of the globe.— In what precedes, we have only considered the effect of that one, Pm, of the two components of the centrifugal force which is opposed to the weight. It remains examine the effect of the other, Pn, which is directed towards the equator.

If the surface of the globe were composed altogether of sol matter, of such coherence as to resist separation by the agency of this force, no other effect would take place except a tendent towards the equator, which would be neutralized by cohesion. But if the surface or any parts of it were fluid, whether liquid or gaseous, such parts, in virtue of their mobility, would yield to the impulse of the element Pn of the centrifugal force, and would not towards the equator. The waters of the surface would the flow from the higher latitudes in either hemisphere, and accumulating round the equator, the surface of the globe would be resolve into two great polar continents, separated by a vast equator ocean.

2380. Such effects not existing, the earth cannot be an exa globe.—But such is not the actual geographical condition of the surface of the globe. On the contrary, although about two-thir of it are covered with water, no tendency of that fluid to accum late more about the equator than elsewhere is manifested. Lan and water, if not indifferently distributed over the surface, are or tainly not apportioned so as to indicate any tendency such as the

above described. If, therefore, the rotation of the earth be admitted, it follows that its figure must be such as to counteract the tendency of fluid matter to flow towards any one part of the surface atter than any other. In short, its figure must be such that gravity itself shall counteract that element Pn of the centrifugal force which tends to move a body from the higher latitudes of either hemisphere towards the equator.

2381. The figure must therefore be some sort of oblate spheroid.

Now this condition would be fulfilled, if the earth, instead of being an exact sphere, were an oblate spheroid, having a certain definite ellipticity, — that is, a figure which would be produced by an ellipse revolving round its shorter axis. Such a figure would resemble an orange or a turnip. It would be more convex at the equator than at the poles. A globe composed of elastic materials would be reduced to such a figure by pressing its poles together, so as to flatten more or less the surface of these points, and produce a pro-

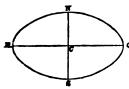


Fig. 703.

tuberance around the equator. The meridians of such a globe would be ellipses, having its axis as their lesser axis, and the diameters of the equator as their greater axes.

The form of the meridian would be such as is represented in fig. 703, Ns being the axis of rotation, and Æ Q the

equatorial diameter.

2382. Its ellipticity must depend on gravity and centrifugal force. — The protuberance around the equator may be more or less, according to the ellipticity of the spheroid; but since the distribution of land and water is indifferent on the surface, having no prevalence about the equator rather than about the poles, or vice versá, it is evident that the degree of protuberance must be that which counteracts, and no more than counteracts, the tendency of the fluids, in virtue of the centrifugal force, to flow towards the equator. This protuberance may be considered as equivalent in its effects to an acclivity of regulated inclination, rising from each pole towards the equator. To arrive at the equator, the fluid must ascend this acclivity, to which ascent gravity opposes itself, with a force depending on its steepness, which increases with the magnitude of the protuberance, or, what is the same, with the ellipticity of the sphe-If the ellipticity be less than is necessary to counteract the effect of the centrifugal force, the fluid will still flow to the equator, and the earth would consist, as before, of a great equatorial ocean separating two vast polar continents. If the ellipticity were greater than is necessary to counteract the effect of the centrifugal force, then gravity would prevail over the centrifugal force, and the waters would flow down the acclivities of the excessive protuberance towards the poles, and the earth would consist of a vast equatorial

continent separating two polar oceans.

Since the geographical condition of the surface of the earth is not consistent with either of these consequences, it is evident that its figure must be an oblate spheroid, having an ellipticity exactly corresponding to the variation of gravity upon its surface, due to the combined effect of the attraction exerted by its constituent parts upon bodies placed on its surface, and the centrifugal force arising from its diurnal rotation.

It remains, therefore, to determine what this particular degree of ellipticity is, or, what is the same, to determine by what fraction of its whole length the equatorial diameter A Q exceeds the polar axis NS.

2383. Ellipticity may be calculated and measured, and the results compared.—The degree of ellipticity of the terrestrial spheroid may be found by theory, or ascertained by observation and measurement, or by both these methods, in which case the accordance or discrepancy of the results will either prove the validity of the reasoning on which the theoretical calculation is founded, or indicate the conditions or data in such reasoning which must be modified.

Both these methods have accordingly been adopted, and their re-

sults are found to be in complete harmony.

2384. Ellipticity calculated. — The several quantities which are involved in this problem are:—

The time of rotation = R.

2. The fraction of its whole length by which the equatorial ex-

ceeds the polar diameter = ϵ .

3. The fraction of its whole weight by which the weight of a body at the pole exceeds the weight of the same body at the equator = w.

4. The mean density of the earth.

5. The law according to which the density of the strata varies in proceeding from the surface to the centre.

All these quantities have such a mutual dependence, that when

some of them are given or known, the others may be found.

In whatever way the solution of the problem may be approached, it is evident that the form of the spheroid must be the same as it would be if the entire mass of the earth were fluid. If this were not so, the parts actually fluid would not be found, as they are always, in local equilibrium. The state of relative density of the strata proceeding from the surface to the centre is, however, not so Newton investigated the question by ascertaining the form which the earth would assume if it consisted of fluid matter of uniform density from the surface to the centre; and the result of his analysis was that, in that case, assuming the time of rotation to be what it is, the equatorial diameter must exceed the polar by the 230th part of its whole length, and gravity at the pole must exceed gravity at the equator by the same fraction of its entire force.

As physical science progressed, and mathematical analysis was brought to a greater state of perfection, the same problem was investigated by Clairault and several other mathematicians, under more rigorous conditions. The uniform density of the constituents of the earth—a highly improbable supposition—was put aside, and it was assumed that the successive strata from the centre to the surface increased in density according to some undetermined conditions. It was assumed that the mutual attraction of all the constituent parts upon any one part, and the effect of the centrifugal force arising from the rotation, are in equilibrium; so that every particle composing the spheroid, from its centre to its surface, is in repose, and would remain so were it free to move.

By a complicated and very abstruse, but perfectly clear and certain mathematical analysis, it has been proved that the quantities above mentioned have the following relation. Let r express a certain number, the amount of which will vary with R. We shall then have

$$e + w = r$$
.

Now it has been shown that when $n = 23^{h} \cdot 56^{m} \cdot 4 \cdot 09^{s}$, the number r will be r_{12} , so that in effect

$$e+w=\frac{1}{115}$$

This result was shown to be true, whatever may be the law according to which the density of the strata varies.

It further results from these theoretical researches that the mean density of the entire terrestrial spheroid is about twice the mean density of its superficial crust.

It follows from this that the density of its central parts must

greatly exceed twice the density of its crust.

It remains, therefore, to see how far these results of theory are in accordance with those of actual observation and measurement.

2385. Ellipticity of terrestrial spheroid by observation and measurement.—If a terrestrial meridian were an exact circle, as it would necessarily be if the earth were an exact globe, every part of it would have the same curvature. But if it were an ellipse, of which the polar diameter is the lesser axis, it would have a varying curvature, the convexity being greatest at the equator, and least at the poles. If, then, it can be ascertained by observation, that the curvature of a meridian is not uniform, but that on the contrary it increases in going towards the Line, and diminishes in going towards the poles, we shall obtain a proof that its form is that of an oblate spheroid.

To comprehend the method of ascertaining this, it must be considered that the curvature of circles diminishes as their diameters

are augmented. It is evident that a circle of one foot in diameter has a less degree of curvature, and is less convex than a circle one inch in diameter. But an arc of a circle of a given angular magnitude, such for example as 1°, has a length proportional to the diameter. Thus, an arc of 1° of a circle a foot in diameter, is twelve times the length of an arc of 1° of a circle an inch in diameter. The curvature, therefore, increases as the length of an arc of 1° diminishes.

If, therefore, a degree of the meridian be observed, and measured, by the process already explained (2317), at different latitudes, and it is found that its length is not uniformly the same as it would be if the meridian were a circle, but that it is less in approaching the equator, and greater in approaching the pole, it will follow that the convexity or curvature increases towards the equator, and diminishes towards the poles; and that consequently the meridian has the form, not of a circle, but of an ellipse, the lesser axis of which is the polar diameter.

Such observations have accordingly been made, and the lengths of a degree in various latitudes, from the Line to 66° N. and to 35° S., have been measured, and found to vary from 363,000 feet on the Line to 367,000 feet at lat. 66°.

From a comparison of such measurements, it has been ascertained that the equatorial diameter of the spheroid exceeds the polar by $\frac{1}{100}$ of its length. Thus (2384)

$$\epsilon = \frac{1}{300}$$

2386. Variation of gravity by observation. — The manner in which the variation of the intensity of superficial gravity at different latitudes is ascertained by means of the pendulum, has been already explained (552). From a comparison of these observations it has been inferred that the effective weight of a body at the pole exceeds its weight at the equator by about the The part of the whole weight.

2387. Accordance of these results with theory. — By comparing these results with those obtained by Newton, on the supposition of the uniform density of the earth, a discrepancy will be found sufficient to prove the falsehood of that supposition. The value of e found by Newton is $\frac{1}{2}\frac{1}{3}$, its actual value being $\frac{1}{3}\frac{1}{0}$, and that of w $\frac{1}{3}\frac{1}{3}$, its actual value being $\frac{1}{3}\frac{1}{6}$.

On the other hand, the accordance of these results of observation and measurement with the more rigorous conclusions of later researches is complete and striking.

• Different values are assigned to this — Sir John Herschel prefers 1 the Astronomer Royal 1 to the Nave taken a mean between these estimates.

n the relation between e and w, explained in (2884),

$$e+w=\frac{1}{115},$$

stitute for w the value Thy, obtained by observation, we find

$$e = \frac{1}{115} - \frac{1}{187} = \frac{1}{300},$$

is the value of e obtained by computation founded on mea-

8. Diminution of weight due to ellipticity. — It has been y shown (2377) that the loss of weight at the equator due to atrifugal force is the 287th of the entire weight. From what sen stated (2386), it appears that the actual loss of weight at untor is greater than this, being the 187th part of the entire to the difference in these is

$$\frac{1}{187} - \frac{1}{287} = \frac{1}{537}.$$

wears, therefore, that while the 287th part of the weight is ed by the centrifugal force, the actual attraction exerted by rth upon a body at the equator is less than at the pole by the part of the whole weight. This difference is due to the last form of the meridian, by which the distance of the body he centre of the earth is augmented.

9. Actual linear dimensions of the terrestrial spheroid. — It enough to know the proportions of the earth. It is required ermine the actual dimensions of the spheroid. The following e lengths of the polar and equatorial diameters, according to mputations of the most eminent and recent authorities:—

	Bessel.	Airy.
r dismeter	Miles, 7899-114 7925-604 26-471 1 299-407	Miles. 7899-170 7925-648 26-478 1 209-830

lose coincidence of these results supplies a striking example of recision to which such calculations have been brought.

departure of the terrestrial spheroid from the form of an globe is so inconsiderable that, if an exact model of it turned were placed before us, we could not, either by sight or distinguish it from a perfect billiard ball. A figure of a me-

According to Herschel, the 590th part.

ridian accurately drawn on paper could only be distinguished from a circle by the most precise measurement. If the major axis of such an ellipse were equal in length to the page now under the eye of the reader, the lesser axis would fall short of the same length less than the fortieth of an inch.

2390. Dimensions of the spheroidal equatorial excess.—If a sphere N q s q be imagined to be inscribed within the terrestrial sphe-

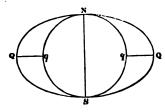


Fig. 704.

roid having the polar axis N 8, fg. 704, for its diameter, a spheroidal shell will be included between its surface and that of the spheroid composed of the protuberant matter, having a thickness Q q of 13 miles at the equator, and becoming gradually thinner in proceeding to the poles, where its thickness vanishes. This shell, which constitutes the equatorial excess of the spheroid, and which, as will hereafter ap-

pear, has a density of not more than half the mean density of the earth, the bulk of which, moreover, would be imperceptible upon a mere inspection of the spheroid, is nevertheless attended with most important effects, and by its gravitation is the origin of most striking phenomena, not only in relation to the moon, but also to the far more distant mass of the sun.

2391. Density and mass of the earth by observation.—The magnitude of the earth, being known with great precision, the determination of its mass and that of its mean density become one and the same problem, since the comparison of its mass with its magnitude will give its mean density, and the comparison of its mean density with its magnitude will give its mass.

The methods of ascertaining the mass or actual quantity of matter contained in the earth, are all based upon a comparison of the gravitating force or attraction which the earth exerts upon an object with the attraction which some other body, whose mass is exactly known, exerts on the same object. It is assumed, as a postulate or axiom in physics, that two masses of matter which at equal distances exert equal attractions on the same body, must be equal. But as it is not always possible to bring the attracting and attracted bodies to equal distances, their attractions at unequal distances may be served, and the attractions which they would exert at equal distances may thence be inferred by the general law of gravitation, by which the attraction exerted by the same body increases as the aquare of the distance from it is diminished.

Thus, if E be the mass of the earth, A the attraction it exerts at

the distance D from its centre of gravity, and A' the attraction it exerts at any other distance D', we have—

 $A:A'::D'^2:D^2$;

and therefore

$$A' = A \times \frac{D^2}{D'^2}.$$

If a be the attraction which any mass m of known quantity exerts at the distance D' upon the same body upon which the earth exerts the attraction A', we shall have—

E:m::A':a;

and therefore

$$\mathbf{E} = m \times \frac{\mathbf{A}'}{a} = m \times \frac{\mathbf{A}}{a} \times \frac{\mathbf{D}^2}{\mathbf{D}'^2}.$$

If, therefore, the mass m, the ratio of the attractions A and a, and the ratio of the distances D and D', be respectively known, the mass \mathbf{z} of the earth can be computed.

2392. Dr. Maskelyne's solution by the attraction of Schehallien.

—This celebrated problem consisted in determining the ratio of the mean density of a mountain called Schehallien, in Perthshire, to that of the earth, by ascertaining the amount of the deviation of a plumb-line from the direction of the true vertical produced by the local attraction of the mountain.

To render this method practicable, it is necessary that the mountain selected be a solitary one, standing on an extensive plain, since otherwise the deviation of the plumb-line would be affected by neighbouring eminences to an extent which it might not be possible to estimate with the necessary precision. No eminence sufficiently considerable exists near enough to Schehallien to produce such disturbance.

The mountain ranging east and west, two stations were selected on its northern and southern acclivities, so as to be in the same meridian, or very nearly so. A plumb-line, attached to an instrument called a zenith sector, adapted to measure with extreme accuracy small zenith distances, was brought to each of these stations, and the distance of the same star, seen upon the meridian from the directions of the plumb-line, were observed at both places.

The difference between those distances gave the angle under the two directions of the plumb-line. This will be more clearly understood by reference to fig. 705, where P and P' represent the points of suspension of the two plumb-lines. If the mountain were removed, they would hang in the direction P c and P' c of the earth's centre, and their directions would be inclined at the angle P C P'. But the attraction exerted by the interjacent mass produces on each side a alight deflection towards the mountain, so that the two directions would be inclined as the two directions towards the mountain, so that the two directions was produced to the standard of the two directions to the standard of the sta

111.

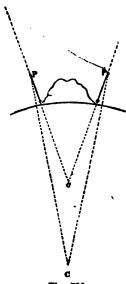


Fig. 705.

Now by means of the zenith sector the dists the points z and z' from any star such as s, can precision so extreme as not to be subject to a small fraction of a second. The difference of the To determine the magnitude of the angle PCP', therefore, the cet distance between the stations P and P' is ascertained by king a survey of the mountain, which, as will presently appear, also necessary, in order to determine its exact volume. For ry hundred feet in the distance between P and P' there will be in the angle PCP' (2319). Finding, therefore, the direct disc between P and P' in feet, and dividing it by 100, we shall e the angle PCP' in seconds.

n the case of the experiment of Dr. Maskelyne, which was made 774, the angle PCP was found to be 41", and the angle PCP

The sum of the two deflections was therefore 12".

he survey of the mountain supplied the data necessary to detere its actual volume in cubic miles, or fraction of a cubic mile. elaborate examination of its stratification, by means of sections, ngs, and the other usual methods, supplied the data necessary etermine the weights of its component parts, and thence the ht of its entire volume; and the comparison of this weight with olume gave its mean density.

If the mean density of the earth were equal to that of the mounthe entire weight of the earth would be greater than that of mountain, in exactly the same proportion as the entire volume he earth exceeds that of the mountain; and these volumes being rn, the weight E of the earth on that supposition was computed, by the formula given in (2391), or others based upon the same

ciples, the ratio $\frac{A}{a}$ of the attraction of the earth to that of the

ntain was computed, and thence the sum of the deflections which mountain would produce was found, which instead of 12" was t 24". It followed, therefore, that the density of the earth must omble, or, more exactly, eighteen-tenths of that of the mounin order to reduce the deflections to half their computed amount. he mean density of the mountain having been ascertained to be to 21 times that of water, it followed, therefore, that the mean atty of the earth is about five times that of water.

393. Cavendish's solution. — At a later period Cavendish made experiment which bears his name, in which the attraction exerted be earth upon a body on its surface was compared with the attion exerted by a large metallic ball on the same body; and this siment was repeated still more recently by Dr. Reich, and by late Mr. Francis Baily, as the active member of a committee of Royal Astronomical Society of London. All these several exmenters proceeded by methods which differed only in some of r practical details, and in the conditions and précautions adopted btain more accurate results.

n the apparatus used by Mr. Baily, the latest of them, the at-

were two balls of lead, each a foot in diameter. The bodies upon which their attraction was manifested were small balls, about we inches in diameter. The former were supported on the ends of an oblong horizontal stage, capable of being turned round a vertical axis supporting the stage at a point midway between them. Let fig. 706 represent a plan of the apparatus. The large metallic balls Band

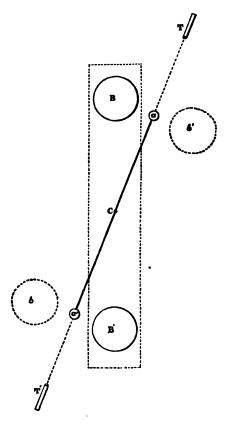


Fig. 706.

B' are supported upon a rectangular stage represented by the detail lines, and so mounted as to be capable of being turned round is centre c in its own plane. Two small balls a, a', about two inches in diameter, are attached to the ends of a rod, so that the distance

between their centres shall be nearly equal to BB'. This rod is supported at C by two fine wires at a very small distance asunder, so that the balls will be in repose when the rod a a' is directed in the plane of the wires, and can only be turned from that plane by the action of a small and definite force, the intensity of which can always be ascertained by the angle of deficction of the rod a a'. The exact direction of the rod a a' is observed, without approaching the apparatus, by means of two small telescopes a and a', and the extent of its departure from its position of equilibrium may be measured with great precision by micrometers.

In the performance of the experiment a multitude of precautions were taken to remove or obviate various causes of disturbance, such as currents of air, which might arise from unequal changes of tem-

perature which need not be described here.

The large balls being first placed at a distance from the small ones, the direction of the rod in its position of equilibrium was observed with the telescopes TT. The stage supporting the large balls was then turned until they were brought near the small ones, as represented at BB. It was then observed that the small balls were attracted by the large ones, and the amount of the deflection of the rod a a' was observed.

The frame supporting the large balls was then turned until B was brought to b, and B' to b', so as to attract the small balls on the other side, and the deflection of a a' was again observed. In each case the amount of the deflection being exactly ascertained, the intensity of the deflecting force, and its ratio to the weight of the

balls, became known.

The properties of the pendulum supplied a very simple and exact means of comparing the attraction of the balls B and B' with the attraction of the earth. The balls a a' were made to vibrate through a small arc on each side of the position which the attraction gave them, and the rate of their vibration was observed and compared with the rate of vibration of a common pendulum. The relative intensity of the two attractions was computed from a comparison of these rates by the principles established in (542). The precision of which this process of observation is susceptible may be inferred from the fact that the whole attraction of the balls BB' upon a a' did not amount to the 20-millionth part of the weight of the balls a', and that the possible error of the result did not exceed 2 per cent of its whole amount.

The attraction which the balls BB' would exert on a a', on the supposition that the mean density of the earth is equal to that of the metallic balls BB', was then computed on the principles explained in (2381), and found to be less than the actual attraction charved, and it was inferred that the density of the earth was less than that of the balls BB' in the same ratio.

In fine, it resulted that the mean density of the earth is 5-67

times the density of water.

The accordance of this result with those of the Schehallien experiment, and the calculations upon the figure of the terrestrial spheroid, supply a striking proof of the truth of the theory of gravitation on which all these three independent investigations are based, and of the validity of the reasoning upon which they have been conducted.

2894. Volume and weight of the earth. — Having ascertained the linear dimensions and the mean density of the earth, it is a question of mere arithmetical labour to compute its volume and its weight. Taking the dimensions of the globe as already stated, its volume contains

259,800 millions of cubic miles. 382,425,600,000 billions of cubic feet.

The average weight of each cubic foot of the earth being 5.67 times the weight of a cubic foot of water, is 354.375 lbs., or 0.1587 of a ton. It follows, therefore, that the total weight of the earth is 6,069,094,272 billions of tons.

CHAP. VI.

THE OBSERVATORY.

2895. Knowledge of the instruments of observation necessary.—Having explained the dimensions, rotation, weight, and density of the earth, and described generally the aspect of the firmament and fixed lines and points upon it, by which the relative position and motions of celestial objects are defined, it will be necessary, before proceeding to a further exposition of the astronomical phenomena, to explain the principal instruments with which an observatory is furnished, and to show the manner in which they are applied, so as to obtain those accurate data which supply the basis of those calculations from which has resulted our knowledge of the great laws of the universe. We shall therefore here explain the form and use of such of the instruments of an observatory as are indispensably necessary for the observations by which such data are supplied.

2396. The astronomical clock. — Since the immediate objects of all astronomical observation are motions and magnitudes, and since motions are measured by the comparison of space and time, one of the most important instruments of observation is the time-piece or chronometer, which is constructed in various forms, according to the circumstances under which it is used and the degree of accuracy

necessary to be obtained. In a stationary observatory, a pendulum cieck is the form adopted.

The rate of the astronomical clock is so regulated that, if any of the stars be observed which are upon the celestial meridian at the moment at which the hands point to 0th 0th, they will again point to 0th 0th 0th when the same stars are next seen on the meridian. The interval, which is called a sidereal day, is divided into twenty-four equal parts, called SIDEREAL HOURS. The hour-hand moves over one principal division of its dial in this interval. In like manner the MINUTE and SECOND-HANDS move on divided circles, each moving over the successive divisions in the intervals of a minute and a second respectively.

The pendulum is the original and only real measure of time in this instrument. The hands, the dials on which they play, and the mechanism which regulates and proportions their movements, are only expedients for registering the number of vibrations which the pendulum has made in the interval which clapses between any two phenomena. Apart from this convenience, a mere pendulum unconnected with wheel-work or any other mechanism, the vibrations of which would be counted and recorded by an observer stationed

near it, would equally serve as a measure of time.

And this, in fact, is the method actually used in all exact astronomical observations. The eye of the observer is occupied in watching the progress of the object moving over the wires (2302) in the field of view of the telescope. His ear is occupied in noting, and his mind in counting the successive beats of the pendulum, which in all astronomical clocks is so constructed as to produce a sufficiently loud and distinct sound, marking the close of each successive second. The practised observer is enabled with considerable precision in this way to subdivide a second, and determine the moment of the occurrence of a phenomenon within a small fraction of that interval. A star, for example, is seen to the left of the wire

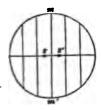


Fig. 707.

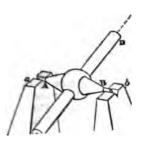
m m' at s, fig. 707, at one beat of the pendulum, and to the right of it at s' with the next. The observer estimates with great precision the proportion in which the wire divides the distance between the points s and s', and can therefore determine the fraction of a second after being at s, at which it was upon the wire m m'.

Although the art of constructing chronometers has attained a surprising degree of perfection, it is not perfect, and the RATE of even

the best of such instruments is not absolutely uniform. It is therefore necessary from time to time to check the indications of the clock by observing its rate. If the clock were absolutely perfect,

24th part of a second. If, however this error may be allowed for, and n remote possibility of a change of rate tained.

2397. The transit instrument.—A nomical observations are made at the observed are upon the celestial merical class of such observations the sole pudetermine with precision the time when meridian by the apparent diurnal motical control of the cont



er, supplied with a clock, to ascertain the exact time of the NEIT, is called a TRANSIT INSTRUMENT.

such an instrument consists of a telescope so mounted that the of collimation will be successively directed to every point of celestial meridian when the telescope is moved upon its axis rough 180°.

This is accomplished by attaching the telescope to an axis at right igles to its line of collimation, and placing the extremities of such zis on two horizontal supports, which are exactly at the same level. and in a line directed east and west. The line of collimation when horizontal will therefore be directed north and south; and if the telescope be turned on its axis through 180°, its line of collimation will move in the plane of the meridian, and will be successively directed to all points on the celestial meridian from the north to the

pole, thence to the zenith, and thence to the south.

The instrument thus mounted is represented in fig. 708. stone piers are erected on a solid foundation standing east and west. In the top of each of them is inserted a metallic support in the form of a y to receive the cylindrical extremities of the transverse arms AB of the instrument. The tube of the telescope CD consists of two equal parts inserted in a central globe, forming part of the transversal axis A B. Thus mounted, the telescope can be made to revolve like a wheel upon the axis A B, and while it thus revolves its line of collimation would be directed successively to all the prints of a vertical circle, the plane of which is at right angles to the axis A B. If the axis be exactly directed east and west, this vertical must be the meridian.

2398. Its adjustments.—This, however, supposes three conditions to be fulfilled with absolute precision:

The axis AB must be level.

2°. The line of collimation must be perpendicular to it

3°. It must be directed due east and west.

In the original construction and mounting of the instrument the three conditions are kept in view, and are nearly, but cannot exactly, fulfilled in the first instance. In all astronomical inst ments the conditions which they are required to fulfil are only proximated to in the making and mounting; but a class of exp ents called ADJUSTMENTS are in all cases provided, by which a of the requisite conditions, only nearly attained at first, are full with infinitely greater precision.

In all such adjustments two provisions are necessary: fi method of detecting and measuring the deviation from the fulfilment of the requisite condition; and secondly, an expedi-

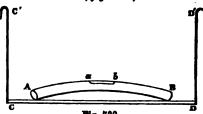
which such deviation can be corrected.

2399. To make the axis level. - If the axis AB be no

level, its deviation from this direction may be ascertained by sus-

pending upon it a SPIRIT LEVEL.

This consists of a glass tube nearly filled with alcohol or ether, liquids selected for the purpose, in consequence of the absence of all viscidity, their perfect mobility, and because they are not hable to congelation. The tube AB, fig. 709, is formed slightly coaves,



and when it is placed horizontally with its convexity upwards, the bubble a b produced by its deficient fulness will take the highest position, and therefore rest at the centre of its length. Marks are engraved on or attached to the tube at a and b indicating the centre of its length. The tube is attached to a straight bar CD, or so mounted as to be capable of being suspended from two points o' D', and is so adjusted that when the lower surface of the bar c D, or the line joining the two points of suspension c' D', is exactly level, the bubble will rest exactly in the centre of the tube between the marks a and b.

To ascertain whether a surface, or the line joining two proposed points, be level, the instrument is applied upon the one, or suspended from the other. If the bubble rest between the marks a and b, they are level; if not, that direction towards which it deviates is the more elevated, and it must be lowered, or the other raised. The operation must be repeated until the bubble is found to rest between the central marks a and b, whichever way the level be placed.

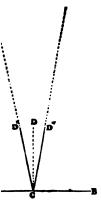
A level is provided for the transit instrument with two loops of suspension corresponding with the cylindrical extremities of the axis AB, fig. 708, so that its points of suspension may rest on these cylinders. If it be found that, when the level is properly suspended thus upon the axis, the bubble rests nearer to one extremity than the other, it will be necessary to raise that end from which it more remote, or to lower that to which it is nearer.

To accomplish this, one of the supports in which the extremity A of the axis rests is constructed so as to be moved through a small space vertically by a finely constructed screw. This support is therefore raised or lowered by such means, until the bubble of the level rests between the central marks a and b, whichever way the level be suspended.

To make the line of collimation perpendicular to the axis. st be remembered, that the line of collimation is a line on the centre of the object-glass to the intersection of the res in the field of view of the telescope. The centre of reglass is fixed relatively to the telescope, but the wires are ed that the position of their intersection can be moved a certain small space by means of a micrometer screw. If the line of collimation, therefore, being moveable, while is fixed, its direction may be changed at pleasure within termined by the construction of the eye-glass and its mi-

ertain whether the line of collimation is or is not at right the line joining the points of support A and B, fig. 708, stant point be observed upon which the intersection of the s. Let the instrument be then reversed upon its supports, if the axis which rested on a being transferred to b, and h rested on b to a, and let the same object be observed. I coincide with the intersection of the wires, the line of m is in the proper direction; but if not, its distance from section of the wires will be twice the deviation of the line ation from the perpendicular, and the wires must be moved ljusting screw, until the intersection is moved towards the rough half of its apparent distance from it.

der this more clear, let A B, fig. 710, represent the direction



Mr. 710.

of the axis, CD that of a line exactly at right angles to it, or the direction which is to be given to the line of collimation, and let c D' represent the erroneous direction which that line actually has. Let 8 be a distant object to which it is observed to be directed, this object being seen upon the intersection of the wires. If the instrument be reversed, the line CD' will have the direction C D", deviating as much from CD to the right as it before deviated to the left. object s will now be seen at a distance to the left of the intersection of the wires which measures the angle D'OD", which is twice the angle DCD', or the deviation of the line of collimation from the perpendicular DC.

To render the direction of the supports due east and west.—
n some cases accomplished by a MERIDIAN MARK, which is
t object, such as a white vertical line painted on a black

ground; erected at a sufficient distance from the instrument in the exact meridian of the observatory. If, on directing the telescope to it, it is seen on the one side or the other of the middle wire (which ought to coincide with the meridian), the direction of the axis AB, fig. 710, will deviate to the same extent from the true east and west, since it has been already, by the previous adjustments, readered perpendicular to the line of collimation. The entire instrument must therefore be shifted round, until the meridian mark coincides with the middle wire. This is accomplished by a provision made in the support on which the extremity of the axis B, fig. 708, rest, by which it has a certain play in the horizontal direction urged by a fine screw. In this way the axis AB is brought into the true direction east and west, and therefore the line of collimation into the true meridian.

It will-be observed that, in explaining the second adjustment, it has been assumed that the deviations are not so great as to throw the object s out of the field of view after the instrument is reversed. This condition in practice is always fulfilled, the extent of deviation left to be corrected by the adjustments being always very small.

2402. Micrometer wires — method of observing transit. — In the focus of the eye-piece of the transit instrument, the system of micrometer wires (2302), already mentioned, is placed. This consists commonly of 5 or 7 equidistant wires, placed vertically at equal distances, and intersected at their middle points by a horizontal wire, as represented in fig. 707. When the instrument has been adjusted, the middle wire m m' will be in the plane of the meridian, and when an object is seen upon it, such object will be on the celestial meridian, and the wire itself may be regarded as a small are of the meridian rendered visible.

The fixed stars, as will be explained more fully hereafter, appear in the telescope, no matter how high its magnifying power be, as mere lucid points, having no sensible magnitude. By the diurnal motion of the firmament, the star passes successively over all the wires, a short interval being interposed between its passages. The observer, just before the star approaching the meridian enters the field of view, notes and writes down the hours and minutes indicated by the clock, and he proceeds to count the seconds by his ear. He observes, in the manner already explained, to a fraction of a second, the instant at which the star crosses each of the wires; and taking a mean of all these times, he obtains, with a great degree of precision, the instant at which the star passed the middle wire, which is the time of the transit.

By this expedient the result has the advantage of as many independent observations as there are parallel wires. The errors of observation being distributed, are proportionally diminished.

When the sun, moon, or a planet, or, in general, any object which

has a sensible disk, is observed, the time of the transit is the instant at which the centre of the disk is upon the middle wire. This is obtained by observing the instants which the western and eastern edges of the disk touch each of the wires. The middle of these intervals are the moments at which the centre of the disk is upon the wires respectively. Taking a mean of the contact of the western edges, the contact of the western edge with the middle wire will be obtained; and, in like manner, a mean of the contacts of the eastern edge will give the contact of that edge with the middle wire, and a mean of these two will give the moment of the transit of the centre of the disk, or a mean of all the contacts of both edges will give the same result.

By day the wires are visible, as fine black lines intersecting and spacing out the field of view. At night they are rendered visible by a lamp, by which the field of view is faintly illuminated.

2403. Apparent motion of objects in field of view. — Since the telescope reverses the objects observed, the motion in the field will appear to be from west to east, while that of the firmament is from east to west. An object will therefore enter the field of view on the west side, and, having crossed it, will leave it on the east side.

Since the sphere revolves at the rate of 15° per hour, 15 per minute, or 15" per second of time, an object will be seen to pass across the field of view with a motion absolutely uniform, the space passed over between two successive beats of the pendulum being invariably 15".

Thus, if the moon or sun be in or near the equator, the disk will be observed to pass across the field with a visible motion, the interval between the moments of contact of the western and eastern edges with the middle wire being 2^m·8^s, when the apparent diameter is 32'. Thus, the disk appears to move over a space equal to half its own diameter in 1^m·4^s·

2404. Circles of declination, or hour circles.— Circles of the celestial sphere which pass through the poles are at right angles to the celestial equator, and are on the heavens exactly what meridians are upon the terrestrial globe. They divide the celestial equator into arcs which measure the angles which such circles form with each other. Thus, two such circles which are at right angles include an arc of 90° of the celestial equator, and two which form with each other an angle of 1° include between them an arc of 1° of the celestial equator. These CIECLES OF DECLINATION, or HOUR CIECLES as they are called, are carried round by the diurnal motion of the heavens, and are brought in succession to coincide with the celestial meridian, the intervals between the moments of their coincidence with the meridian being always proportional to the angle they form with each other, or, what is the same, to the arc of the celestial equator included between them. Thus, if two circles of

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declination form with each other an angle of 30°, the interval between the moments of their coincidence with the meridian will be two sidereal hours.

The relative position of the circles of declination with respect to cach other and to the meridian, and the successive positions assumed by any one such circle during a complete revolution of the sphere, will be perceived and understood without difficulty by the aid of a celestial globe, without which it is scarcely possible to obtain any clear, or definite notion of the apparent motions of celestial objects.

2405. Right ascension. — The arc of the celestial equator between any circle of declination and a certain point on the equator called the FIRST POINT OF ARIES (which will be defined hereafter), is called the RIGHT ASCENSION of all objects through which the circle of declination passes. This arc is always understood to be measured from the point where the circle of declination meets the celestial equator westward, that is, in the direction of the apparent diurnal motion of the heavens, and it may extend, therefore, over any part whatever of the equator from 0° to 860°.

Right ascension is expressed sometimes according to angular magnitude, in degrees, minutes, and seconds; but since, according to what has been explained, these magnitudes are proportional to the time they take to pass over the meridian, right ascension is also often expressed immediately by this time. Thus, if the right ascension of an object is 15° 15", it will be expressed also by

1h. 1m. 1s.

In general, right ascension expressed in degrees, minutes, and seconds may be reduced to time by dividing it by 15; and if it be expressed in time, it may be reduced to angular language by multi-

plying it by 15.

The difference of right ascensions of any two objects may be ascertained by the transit instrument and clock, by observing the interval which elapses between their transits over the meridian. This interval, whether expressed in time or reduced to degrees, is their difference of right ascension.

Hence, if the right ascension of any one object be known, the

right ascension of all others can be found.

2406. Sidereal clock indicates right ascension. — If the hands of the sidereal clock be set to 0^h· 0^m· 0^h· when the first point of Aries is on the meridian, they will at all times (supposing the rate of the clock to be correct) indicate the right ascension of such objects as are on the meridian. For the motion of the hands in that case corresponds exactly with the apparent motion of the meridian on the celestial equator produced by the diurnal motion of the heavens. While 15° of the equator pass the meridian the hands move through 1^h·, and other motions are made in the same proportion.

2407. The mural circle. — The transit instrument and sidereal clock supply means of determining with extreme precision the instant at which an object passes the meridian; but the instrument is not provided with any accurate means of indicating the point at which the object is seen on the meridian. A circle is sometimes, it is true, attached to the transit, by which the position of this point may be roughly observed; but to ascertain it with a precision proportionate to that which the transit instrument determines the right ascensions, requires an instrument constructed and mounted for this express object in a manner, and under conditions, altogether different from those by which the transit instrument is regulated. The form of instrument adopted in the most efficiently furnished observatories for this purpose is the MURAL CIRCLE.

This instrument is a graduated circle, similar in form and principle to the instrument described in (2304). It is centred upon an axis established in the face of a stone pier or wall (hence the name), erected in the plane of the meridian. The axis, like that of a transit instrument, is truly horizontal, and directed due east and west. Being by the conditions on which it is first constructed and mounted, very nearly in this position, it is rendered exactly so by two adjustments, one of which moves the axis vertically, and the other horizontally, by means of screws, through spaces which, though small, are still large enough to enable the observer to correct

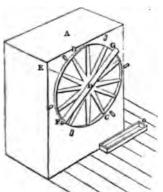


Fig. 711.

the slight errors of position incidental to the workmanship and mounting.

The instrument, as mounted and adjusted, is represented in perspective in fig. 711, where A is the stone wall to which the instrument is attached, D the central axis on which it turns; and FG the telescope, which does not move upon the circle, but is immoveably attached to it, so that the entire instrument, including the telescope, turns in the plane of the meridian upon the axis D.

A front view of the circle in the plane of the instrument is given in fig. 712.

The graduation is usually made on the edge, and not on the face limb. The hoop of metal thus engraved forms, therefore, what may be called the tire of the wheel.

Troughs o, containing mercury, are placed on the floor in convenient positions in the plane of the instrument, in the surface of

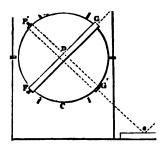


Fig. 712.

which are seen, by reflection, the objects ridian. The observer is thus enabled to a well of the images of the objects reflected objects themselves, the advantage of which

Convenient ladders, chairs, and couch justed by racks and other mechanical arrainclinations, enable the observer, with the to apply his eye to the telescope, no matte

In the more important national observare eight feet in diameter, and consequentl ference. Each degree upon the circumfer above eight-tenths of an inch, admits or division.

The divisions on the graduated edge of bered as usual from 0° to 260° tion which it is

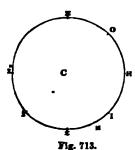
heir images reflected in the mercury, being observed, the angular tance, or the arc of the meridian between them, will be found by extaining the arc of the graduated limb of the instrument, which saes before any fixed point or index, when the telescope is turned on the direction of the one object to the direction of the other.

2409. Compound microscopes—their number and use.—This are is observed by a compound microscope (2307), attached to the wall or pier, and directed towards the graduated limb. The manner in which the fraction of a division of the limb is observed by this expedient has been already explained. But to give greater precision to the observation, as well as to efface the errors which might arise, either from defective centreing, or from the small derangement of figure that might arise from the flexure produced by the weight of the instrument, several compound microscopes—generally six—are provided at nearly equal distances around the limb, so that the observer is enabled to note the position of six indices. The six arcs of the limb which pass under them being observed, are equivalent to six independent observations, the mean of which being taken, the errors incidental to them are reduced in proportion to their number.

2410. Circle primarily a differential instrument. — The observations, however, thus taken are, strictly speaking, only differential. The arc of the meridian between the two objects is determined, and this arc is the difference of their meridianal distances from the zenith or from the horizon; but unless the positions which the six indexes have, when the line of collimation is directed to the zenith or horizon, be known, no positive result arises from the observations; nor can the absolute distance of any object, either from the

horizon or the zenith, be ascertained.

2411. Method of ascertaining the horizontal point.—The "reading," as it is technically called, at each of the microscopes, in ar proposed position of the instrument, is the distance of that microscope from the zero point of the limb. Now it is easy to show the half the sum of the two readings at any microscope, when the to



scope is successively directed to an ject and its image in the mercury, be the reading at the same micros when the line of collimation is horizon

Let a circle be imagined to be d upon the stone pier around the inment, and let M, fig. 713, represer position of any of the microscopes. co be the position of the telescope directed to the object, and let z position of the zero of the limit of the telescope directed to the position of the telescope directed to the object, and let z position of the zero of the limit of the telescope directed to the position of the telescope directed to the tele

directed to the image of the same object in the mercury. If zz' = 0, z' will then be the place of the zero, because the zero will be moved with the instrument through the same space as that through which the telescope is moved. Since the direction CI is as much below the horizon as CO is above it, the direction of the horizon must be that of the point H which bisects the arc OI. The telescope, when horizontal, will have therefore the direction CH, and when it has this position the zero will evidently be at z', the point which bisects the arc zz''.

The "readings" of the microscope M, when the telescope is directed to o and I, are Mz and Mz". The "reading" of the same microscope when the telescope is horizontal would be Mz'. Now it is evident, from what has been stated above, that

$$Mz' - Nz = Mz'' - Mz';$$

and, therefore,

$$Mz' = \frac{1}{2} (Mz \times Mz'');$$

that is, the reading for the horizontal direction of the telescope would be half the sum of the readings for an object and its image.

2412. Method of observing altitudes and zenith distances.—The readings of all the microscopes, when the telescope is directed to the horizon, being thus determined, are preserved as necessary data in all observations on the altitudes or zenith distances of objects. To determine the altitude of an object o, let the telescope be directed to it, so that it shall be seen at the intersection of the wires; and let the readings of the six microscopes be o_1 , o_2 , o_4 , o_5 , and o_6 and let their six horizontal readings be H_1 , H_2 , H_3 , H_4 , H_4 , and H_7 . We shall have six values for the altitudes:

$$A_1 = H_1 - o_1,$$

$$A_2 = H_2 - o_3,$$

$$A_3 = H_3 - o_3,$$

$$A_4 = H_4 - o_4,$$

$$A_5 = H_5 - o_5,$$

$$A_6 = H_6 - o_6,$$

These will be nearly, but not precisely, equal, because they will differ by the small errors of observation, centreing, and form. A mean of the six being taken by adding them and dividing their sum by 6, these differences will be equalized, and the errors nearly effect, so that we shall have the nearest approximation to the true altitude—

$$A = \frac{1}{6} \{ A_1 + A_2 + A_3 + A_4 + A_5 + A_6 \}.$$

The altitude of an object being known, its zenith distance may be found by subtracting the altitude from 90°: thus, if z express the zenith distance, we shall have

$$z = 90^{\circ} - A$$

2413. Method of determining the position of the pole and equator.

—The mural circle may be regarded as the celestial meridian reduced in scale, and brought immediately under the hands of the observer, so that all distances upon it may be submitted to exact examination and measurement. Besides the zenith and horizon, the positions of which, in relation to the microscopes, have just been exertained, there are two other points of equal importance, the

pole and the equator, which should also be established.

The stars which are so near the celestial pole that they never set, are carried by the diurnal motion of the heavens round the pole in small circles, crossing the visible meridian twice, once above and once below the pole. Of all these circumpolar stars, the most important and the most useful to the observer is the pole star, both because of its close proximity to the pole, from which its distance is only 1½°, and because its magnitude is sufficiently great to be visible with the telescope in the day. This star, then, crosses the meridian above the pole and below it, at intervals of twelve hours sidereal time, and the true position of the pole is exactly midway between the two points where the star thus crosses the meridian.

If, therefore, the readings of the six microscopes be taken when the pole star makes its transit above and below the pole, their readings for the pole itself will be half the sum of the former for each

miscroscope.

The readings for the pole being determined, those which correspond to the point where the celestial equator crosses the meridian may be found by subtracting the former from 90°.

When the positions of the microscopes in relation to the pole and equator are determined, the latitude of the observatory will be known, since it is equal to the altitude of the celestial pole (2362).

2414. All circles of declination represented by the circle. — Since the circles of declination, which are imagined to surround the heavens, are brought by the diurnal motion in succession to coincide with the celestial ineridian (2404), since that meridian is itself represented by the mural circle, that circle may be considered as presenting successively a model of every circle of declination; and the position of any object upon the circle of declination is represented on the mural circle by the position of the telescope when directed to the point of the meridian at which the object crosses it.

If the object have a fixed position on the firmament, it is evident that it will always pass the meridian at the same point; and if the telescope be directed to that point and maintained there, the object will be seen at the intersection of the wires regularly after intervals

of twenty-four hours sidereal time.

2415. Declination and polar distance of an object. — The distance of an object from the celestial equator, measured upon the circle of declination which passes through it, is called its DECLINA-

TION, and is NORTH or SOUTH, according to the side of the equator

at which the object is placed.

The declination of an object is ascertained with the mural circle in the same manner and by the same observation as that which gives its altitude. The readings of the microscopes for the object being compared with their readings for the pole (2413), give the polar distance of the object; and the difference between the polar distances and 90° gives the declination.

Thus the polar distance and declination of an object are to the equator exactly what its altitude and zenith distance are to the horizon. But since the equator maintains always the same position during the diurnal motion of the heavens, the declination and polar distance of an object are not affected by that motion, and remain the same, while the altitude and zenith distances are constantly changing.

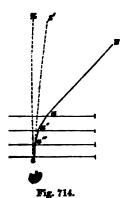
2416. Position of an object defined by its declination and right ascension. — The position of an object on the firmament is determined by its declination and right ascension. Its declination expresses its distance north or south of the celestial equator, and its right ascension expresses the distance of the circle of declination upon which it is placed from a certain defined point upon the celestial equator.

It is evident, therefore, that declination and right ascension define the position of celestial objects in exactly the same manner as latitude and longitude define the position of places on the earth. A place upon the globe may be regarded as being projected on the heavens into the point which forms its zenith; and hence it appears that the latitude of the place is identical with the declination of its zenith.

CHAP. VII.

ATMOSPHERIC REFRACTION.

2417. Apparent position of celestial objects offected by refraction—It has been shown that the ocean of air which surrounds, rests upon, and extends to a certain limited height above the surface of the solid and liquid matter composing the globe, decreases gradually in density in rising from the surface (719); that when a ray of light passes from a rarer to a denser transparent medium, it is deflected towards the perpendicular to their common surface; and that the amount of such deflection increases with the difference of densities and the angle of incidence (978 et seq.). These properties, which air has in common with all transparent media, produce important effects on the apparent positions of celestial objects.



Let s a, fig. 714, be a ray of light coming from any distant object s, and falling on the surface of a series of layers of transparent matter, increasing in density downwards. The ray s a, passing into the first layer, will be deflected in the direction a a' towards the perpendicular; passing thence into the next, it will be again deflected in the direction a' a'', more towards the perpendicular; and, in fine, passing through the lowest layer, it will be still more deflected, and will enter the eye at e, in the direction a'' e: and since every object is seen in the direction from which the visual ray enters the eye,

bject s will be seen in the direction es, instead of its true ion as. The effect, therefore, is to make the object appear mearer to the zenithal direction than it really is.

In this is what actually occurs with respect to all celestial obseen, as such objects always must be, through the atmosphere. risual ray s D, fig. 715, passing through a succession of stratar, gradually and continually increasing in density, its path will curve bending from D towards A, and convex towards the

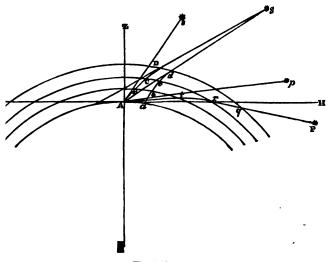


Fig. 715.

senithal line A Z. The direction in which the object will be seen, being that in which the visual ray enters the eye, will be the tangent A s to the curve at A. The object will therefore be seen in the direction A s instead of D S.

It has been shown that the deflection produced by refraction is increased with the increase of the angle of incidence. Now, in the present case, the angle of incidence is the angle under the true direction of the object and the zenithal line, or, what is the same, the zenith distance of the object. The extent, therefore, to which any celestial object is disturbed from its true place by the refraction of the atmosphere, increases with its zenith distance. The refraction is, therefore, nothing in the zenith, and greatest in the horizon.

2418. Law of atmospheric refraction. — The extent to which a celestial object is displaced by refraction, therefore, depends upon and increases with its distance from the zenith; and it can be shown to be a consequence of the general principles of optics, that when other things are the same, the actual quantity of this displacement (except at very low altitudes) varies in the proportion of the tangent of the zenith distance.

Thus, if A z, fig. 716, be the zenithal direction, and A o, A o',

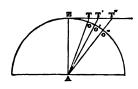


Fig. 716.

e the zenithal direction, and A O, A O', A O', &c., be the directions of celestial objects, their zenith distances being Z A O, Z A O', Z A O'', &c., the quantities of refraction by which they will be severally affected, or, what is the same, the differences between their true and apparent directions, will be in the ratio of the tangents Z T, Z T', Z T'', &c., of the zenith distances.

$$\sin z = m \times \sin (z - r) = m \times \sin z \cos r - m \times \cos z \sin r$$
.

But since r is a very small angle, if it be expressed in seconds, we shall have

cos.
$$r = 1$$
, sin. $r = \frac{r}{206265}$

and, consequently,

$$\sin z = m \times \sin z - m \times \cos z \times \frac{\tau}{206265}$$

and, therefore,

$$r = 206265'' \times \frac{m-1}{m} \times \frac{\sin z}{\cos z} = 206265'' \times \frac{m-1}{m} \times \tan z$$
.

^{*} This law may be demonstrated as follows:—The angle of incidence of the visual ray is equal to the zenith distance z of the object. If r express the refraction, the angle of refraction will be z—r. Let the index of refraction (980) be m. By the general law of refraction we have, therefore,

law prevails with considerable exactitude, except at very tudes, where the refractions depart from it, and become un-

. Quantity of refraction. — When the latitude of the oby is known, the actual quantity of refraction at a given
may be ascertained by observing the altitudes of a circumar, when it passes the meridian above and below the pole.
m of these altitudes would be exactly equal to twice the
(2362) if the refraction did not exist, but since by its
the star is seen at greater than its true altitudes, the sum of
itudes will be greater than twice the latitude by the sum of
refractions. This sum will therefore be known, and being
between the two altitudes in the ratio of the tangents of
ith distances, the quantity of refraction due to each altitude
known.

pole star answers best for this observation, especially in these gher latitudes, where it passes the meridian within the limits more regular influence of refraction; and the difference of tudes being only 3°, no considerable error can arise in aping the total refraction between the two altitudes.

D. Tables of refraction. — To determine with great exactible average quantity of refraction due to different altitudes, e various physical conditions under which the actual refractions are connected with phenomena subject ertain and imperfectly known laws. Thus, the quantity of ion at a given altitude depends, not only on the density, but a the temperature of the successive strata of air through the visual ray has passed. Although, as a general fact, it is not that the temperature of the air falls as we rise in the shere (2185), yet the exact law according to which it dei is not fully ascertained. But even though it were, the ion is also influenced by other agencies, among which the netric condition of the air holds an important place.

m these causes, some uncertainty necessarily attends astroal observations, and some embarrassment arises in cases where
antities to be detected by the observations are extremely
be. Nevertheless, it must be remembered, that since the total
it of refraction is never considerable, and in most cases it is
sely minute, and since, small as it is, it can be very nearly
ited and allowed for, and in some cases wholly effaced, no
s obstacle is offered by it to the general progress of astro-

observation and partly from theory, by which the observer tonce obtain the average quantity of refraction at each alti-

horizon is 33', which being a little more diameters of the sun and moon, it follows moment of rising and setting, are visible lower edge of their disks just touching it below it, the upper edge of the disk just

The moments of rising of all objects and those of setting retarded, by refraction appear to rise before they have really rise have really set; and the same is true of a

2423. General effect of the barometer the barometer rises with the increased wair, its rise is attended by an augment decrease, of refraction. It may be assume any proposed altitude is increased or diminitis mean quantity for every 10th of an inche exceeds or falls short of the height of 30 in

exceeds or falls short of the height of 30 in 2424. Effect of thermometer.— As the causes a decrease of density, the effect of by the elevation of the thermometer, the being the same. It may be assumed, tha proposed altitude is diminished or increase its mean amount for each degree by which F exceeds or falls hort of the mean temperat

2425. Twilight caused by the reflection. The sun continues to illuminate the all

at length, and by slow degrees, all reflection ceases, and night

The same series of phenomena are developed in an opposite order before sunrise in the morning, commencing with the first feeble light of dawn, and ending with the full blaze of day when the disk of the sam becomes visible.

The general effect of the air, clouds, and vapours in diffusing light, and rendering more effectual the general illumination produced by the sun, has been already explained in (923, 924).

2426. Oval form of disks of sun and moon explained. — One of the most curious effects of atmospheric refraction is the oval form of the disks of the sun and moon, when near the horizon. This arises from the unequal refraction of the upper and lower limbs. The latter being nearer the horizon is more affected by refraction, and therefore raised in a greater degree than the upper limb, the effect of which is to bring the two limbs apparently closer together, by the difference between the two refractions. The form of the disk is therefore affected as if it were pressed between two forces, we acting above, and the other below, tending to compress its vertical diameter, and to give it the form of an ellipse, the lesser axis of which is vertical, and the greater horizontal.*

CHAP. VIII.

ANNUAL MOTION OF THE EARTH.

2427. Apparent motion of the sun in the heavens.—Independently of the motion which the sun has in common with the entire firmament, and in virtue of which it rises, ascends to the meridian, and sets, it is observed to change its position from day to day with relation to the other celestial objects among which it is placed. In this respect, therefore, it differs essentially from the stars, which maintain their relative positions for months, years, and ages, unaltered.

If the exact position of the sun be observed from day to day and from month to month, through the year, with reference to the stars, it will be found that it has an apparent motion among them in a great circle of the celestial sphere, the plane of which forms an angle of 23° 28' with the plane of the celestial equator.

2428. Ascertained by the transit instrument and mural circle.— This apparent motion of the sun was ascertained with considerable

[•] For an explanation of the great apparent magnitude of the solar and lunar disks in rising and setting, sec (1170).

15

.... as waich the sun's centre be observed with the mural circle (2408) from day to day. Let its distance from t declination, be observed (2415) daily at r be nothing on the 21st of March and 21s days the polar distance of the sun's cen The sun's centre is, then, on these days After the 21st March the sun's centre wil and its declination will continually increa 28' on the 21st June. It will then begin will continue to decrease until 21st Septem the sun will again be in the equator. Af meridian south of the equator, and will c declination. This will increase until it beca December; after which it will decrease unti returns to the equator on the 21st March.

By ascertaining the position of the centre day to day, by means of its right ascension and tracing its course upon the surface of a is proved to be a great circle of the heavens at an angle of 23° 28'.

2429. The ecliptic. — This great circle in disk of the sun thus appears to move, compl in a year, is called the ECLIPTIC, because, for explained hereafter, solar and lunar eclipses except when the moon is in or year.

electial equator is called the VERNAL, and that at which it passes from the north to the south is called the AUTUMNAL, equinoctial point. The TIMES at which the centre of the sun is found at these points are called, respectively, the VERNAL and AUTUMNAL EQUI-

The vernal equinox, therefore, takes place on the 21st March,

and the autumnal on the 21st September.

2432. The seasons.—That semicircle of the ecliptic through which the sun moves from the vernal to the autumnal equinox is sent of the celestial equator; and during that interval the sun will therefore (2351) be longer above than below the horizon, and will must be meridian above the equator in places having north latitude. The days, therefore, during that half-year, will be longer than the sights.

That semicircle through which the centre of the sun moves from the autumnal to the vernal equinox being south of the celestial equator, the sun, for like reasons, will during that half-year be longer below than above the horizon, and the days will be shorter than the nights, the sun rising to a point of the meridian below tho

equator.

The three months which succeed the vernal equinox are called SPRING, and those which precede it WINTER; the three months which precede the autumnal equinox are called SUMMER, and those which succeed it WINTER.

2433. The solstices. — Those points of the ecliptic which are midway between the equinoctial points are the most distant from the celestial equator. The arcs of the ecliptic between these points and the equinoctial points are therefore 90°. These are called the SOLSTITIAL POINTS, and the times at which the centre of the solar disk passes through them are called the SOLSTICES.

The summer solstice, therefore, takes place on the 21st June, and

the winter solstice on the 21st December.

This distance of the summer solstitial point north, and of the winter solstitial point south of the celestial equator is 23° 28'.

The more distant the centre of the sun is from the celestial equator, the more unequal will be the days and nights (2356), and consequently the longest day will be the day of the summer, and

the shortest the day of the winter, solstice.

It will be evident that the seasons must be reversed in southern latitudes, since there the visible celestial pole will be the south pole. The summer solstice and the vernal equinox of the northern, are the winter solstice and autumnal equinox of the southern hemisphere. Nevertheless, as the most densely inhabited and civilized parts of the globe are in the northern hemisphere, the names in reference to the local phenomena are usually preserved.

2434. THE ZODIAC. — It will be shown hereafter that the ap-

ASTRONOMY.

motions of the planets are included within a space al sphere extending a few degrees north and south c. The zone of the heavens included within these ! the ZODIAC.

5. The signs of the zodiac. — The circle of the zodi into twelve equal parts, called signs, each of which tres 30°. They are named from principal constellas of stars, which are placed in or near them. But the vernal equinoxial point, they are as follows:—

Sign.	The second second second
es (the ram)	7. Libra (the balance) 8. Scorpio (the scorpion) 9. Sagittarius (the archer 10. Capricornus (the goat) 11. Aquarius (the waterma 12. Pisces (the fishes)
us the position of the veri OF ARIES, and that of the The summer solstitial ER, and the winter at the FI	e autumnal the FIRST P

36. The tropics. — The points of the ecliptic at w

exclusion of the earth round the sun at rest. Either of these exacts would explain, in an equally satisfactory manner, all the circumstances attending the apparent annual motion of the sun around the firmament. There is nothing in the appearance of the sun itself which could give a greater probability to either of these hypotheses than to the other. If, therefore, we are to choose between them, we must seek the grounds of choice in some other circumstances.

It was not until the revival of letters that the annual motion of the earth was admitted. Its apparent stability and repose were until then universally maintained. An opinion so long and so deply rooted must have had some natural and intelligible grounds. These grounds, undoubtedly, are to be found only in the general impression, that if the globe moved, and especially if its motion had so enormous a velocity as must be imputed to it, on the supposition that it moves annually round the sun, we must in some way or ther be sensible of such movement.

All the reasons, however, why we are unconscious of the real rotation of the earth upon its axis (2350) are equally applicable to show why we must be unconscious of the progressive motion of the earth in its annual course round the sun. The motion of the globe brough space being perfectly smooth and uniform, we can have no passible means of knowing it, except those which we possess in the se of a boat moving smoothly along a river: that is, by looking shroad at some external objects which do not participate in the motion imputed to the earth. Now, when we look abroad at such sbjects, we find that they appear to move exactly as stationary objects would appear to move, seen from a moveable station. It is plain, then, if it be true that the earth really has the annual motion round the sun which is contended for, that we cannot expect to be conscious of this motion from anything which can be observed on our own bodies or those which surround us on the surface of the earth: we must look for it elsewhere.

But it will be contended that the apparent motion of the sun, even upon the argument just stated, may equally be explained by the motion of the earth round the sun, or the motion of the sun round the earth; and that, therefore, this appearance can still prove nothing positively on this question. We have, however, other proofs, of a very decisive character.

Newton showed that it was a general law of nature, and part, in fact, of the principle of gravitation, that any two globes placed at a distance from each other, if they are in the first instance quiescent and free, must move with an accelerated motion to their common centre of gravity, where they will meet and coalesce; but if they be projected in a direction not passing through this centre of gravity, they will both of them revolve in orbits around that point periodically.

remarkable evidence of this motion has been in a vast body of apparently complicated phenimmediate effects of such a motion, which coif the earth were at rest and the sun in motion would be inexplicable on any other supposition of the earth round the sun.

It has been ascertained, as has been already is propagated through space with a certain gres of about 192,000 miles per second. That light proved by the body of optical phenomena which without imputing to it such a motion, and which plicable if such a motion be admitted. Incanother demonstration that light moves with this by an astronomical phenomenon which will be quent part of this volume.

2440. Aberration of light. — Assuming, the light, and that the earth is in motion in an orbit a velocity of about 19 miles per second, which it move at all, as will hereafter appear, an effect upon the apparent places of all celestial objects of these two motions, which we shall now explain

It has been stated that the apparent direction is the direction from which the visual ray entithis direction will depend on the actual directions which receives it be quiescent; but if the egame effect is produced upon the organ of sensides the motion which is proper to it had an

nt to a motion from the direction of the north-east. The rom which the light comes would, therefore, be apparently

displaced, and would be seen at a point beyond that which it really occupies in the direction in which the eye of the observer is moved. This displacement is called accordingly the ABERRATION OF LIGHT.

This may be made still more evident by the following mode of illustration. Let o, fig. 717, be the object from which light comes in the direction o o e". Let e be the place of the eye of the observer when the light is at o, and let the eye be supposed to move from e to e" in the same time that the light moves from o to e". Let a straight tube be imagined to be directed from the eye at e to the light at o, so that the light shall be in the centre of its opening, while the tube moves with the eye from 0 e to o" e", maintaining constantly the same direction, and remaining parallel to itself: the light in moving from \bar{o} to e'', will pass along its axis, and will arrive at e" when the eye arrives at that point. Now it is evident that in this case the direction in which the object would be visible, would be the direction of the axis of the tube, so that, instead of appearing in the direction oo, which is its

otion, it would appear in the direction o o' advanced from direction of the motion ee" with which the observer is

notion of light being at the rate of 192,000 miles per ind that of the earth (if it move at all) at the rate of 19 second (both these velocities will be established hereafter), s, that the proportion of oe' to ee' must be 192,000 to 1,000, to 1.

INGLE OF ABERRATION 0.00' will vary with the obliquity irection ee'' of the observer's motion to that of the visual

In all cases the ratio of oe'' to ee'' will be 10,100 to 1. lirection of the earth's motion be at right angles to the oe'' of the object 0, we shall have (2294) the aberration.

$$a = \frac{206,265}{10,100} = 20^{\prime\prime} \cdot 42.$$

mponent at right angles to oe", which is done by multiplythe trigonometrical sine of the obliquity oe" e of the di-

rection of the object to that of the earth's motion. If this obliquity be expressed by 0, we shall have for the aberrations in general

$$a = 20'' \cdot 42 \times \sin 0$$
.

According to this, the aberration would be greatest when the direction of the earth's motion is at right angles to that of the object, and would decrease as the angle o decreases, being nothing when the object is seen in the direction in which the earth is moving, or

in exactly the contrary direction.

The phenomena may also be imagined by considering that the earth, in revolving round the sun, constantly changes the direction of its motion; that direction making a complete revolution with the earth, it follows that the effect produced upon the apparent place of a distant object would be the same as if that object really revolved once in a year round its true place, in a circle whose plane would be parallel to that of the earth's orbit, and whose radius would subtend at the earth an angle of 20".42, and the object would be always seen in such a circle 90° in advance of the earth's place in its orbit.

These circles would be reduced by projection to ellipses of infinitely various' excentricities, according to the position of the object with relation to the plane of the earth's orbit. At a point perpendicularly above that plane, the object would appear to move annually in an exact circle. At points nearer to the ecliptic, its apparent path would be an ellipse, the excentricity of which would increase as the distance from the ecliptic would diminish, according

to definite conditions.

Now, all these apparent motions are actually observed to affect all the bodies visible on the heavens, and to affect them in precisely the degree and direction which would be produced by the annual motion of the earth round the sun.

As the supposed motion of the earth round the sun completely and satisfactorily explains this complicated body of phenomena called aberration, while the motion of the sun round the earth would altogether fail to explain them, they afford another striking

evidence of the annual motion of the earth.

2441. Aryument from analogy. — In fine, another argument in favour of the earth's annual motion round the sun is taken from its analogy to the planets, to all of which, like the earth, the san is a source of light and heat, and all of which revolve round the sun as a centre, having days, nights, and seasons in all respects similar to those which prevail upon the earth. It seems, therefore, contrary to all probability, that the earth alone, being one of the planets, and by no means the greatest in magnitude or physical importance, should be a centre round which not only the sun, but all the other planets, should revolve.

442. Annual parallax.—If the earth be admitted to move anily round the sun, as a stationary centre in a circle whose neter must have the vast magnitude of 200 millions of miles, observers placed upon the earth, seeing distant objects from its of view so extremely distant one from the other as are oppoextremities of the same diameter of such a circle, must necesy, as might be supposed, see these objects in very different tions.

o comprehend the effect which might be expected to be proal apon the apparent place of a distant object by such a motion,

let E E' E", fig. 718, represent the earth's annual course round the sun as seen in perspective, and let o be any distant object visible from the earth. The extremity E of the line EO, which is the visual direction of the object, being carried with the earth round the circle EE'E"E", wil' annually describe a cone of which the base is the path of the earth, and the vertex is the place of the object o. While the earth moves round the circle EE", the line of visual direction would therefore have a corresponding motion, and the apparent place of the object would be successively changed with the change of direction of this line. If the object be imagined to be projected by the eye upon the firmament, it would trace upon it a path o o' o" o", which would be circular or elliptical, according to the direction of the object. When the earth is at E, the object would be seen at o; and when the earth is at E", it would be seen at o". The extent of this apparent displacement of the object would be measured by the angle E O L", which the dismeter E E" of the earth's path or orbit would subtend at the object o.

It has been stated that, in general, the apparent displacement of a distant visible object produced by any change in the station from which it is viewed is called PARALLAX. That which is produced by the change of position due to the diurnal motion of the earth being called DIURNAL PARAL-

Fig. 718. of the earth being called DIURNAL PARAL-, the corresponding displacement due to the annual motion of sarth is called the ANNUAL PARALLAX.

The greatest amount, therefore, of the annual parallax for my proposed object is the angle which the semidiameter of the earth's orbit subtends at such object, as the greatest amount of the diurnal parallax is the angle which the semidiameter of the earth itself subtends at the object.

Now, as the most satisfactory evidence of the annual motion of the earth would be the discovery of this displacement, and seccessive changes of apparent position of all objects on the firmances consequent on such motion, the absence of any such phenomenon must be admitted to constitute, prima facie, a formidable argument

against the earth's motion.

2443. Its effects upon the bodies of the solar system apparent.—
The effects of annual parallax are observable, and indeed are of considerable amount, in the case of all the bodies composing the solar system. The apparent annual motion of the sun is altogether due to parallax. The apparent motions of the planets and other bodies composing the solar system are the effects of parallax, combined with the real motions of these various bodies.

2444. But erroneously explained by the ancients — Ptolemais system. — Until the annual motion of the earth was admitted, these effects of annual parallax on the apparent motions of the solar system were ascribed to a very complicated system of real motions of these bodies, of which the earth was assumed to be the stationary centre, the sun revolving around it, while at the same time the planets severally revolved round the sun as a moveable centre. This hypothesis, proposed originally by Apollonius of Pergs, a Grecian astronomer, some centuries before the birth of Christ, received the name of the PTOLEMAIC SYSTEM, having been developed and explained by PTOLEMY, an Egyptian astronomer who flourished in the second century, and whose work, entitled "Syntax," obtained great celebrity, and for many centuries continued to be received as the standard of astronomical science.

Although Pythagoras had thrown out the idea that the annual motion of the sun was merely apparent, and that it arose from a real motion of the earth, the natural repugnancy of the human mind to admit a supposition so contrary to received notions prevented this happy anticipation of future and remote discovery from receiving the attention it merited; and Aristotle, less sagacious than Pythagoras, lent the great weight of his authority to the contrary hypothesis, which was accordingly adopted universally by the learned world, and continued to prevail, until it was overturned in the middle of the sixteenth century, by the celebrated Copernicus, who revived the Pythagorean hypothesis of the stability of the sun and the

motion of the earth.

2445. Copernican system. — The hypothesis proposed by him in a work entitled "De Revolutionibus Orbium Coelestium," pal-

lished in 1543, at the moment of his death, is that since known as the COPERNICAN SYSTEM, and, being now established upon evidence sufficiently demonstrative to divest it of its hypothetical character, is admitted as the exposition of the actual movements by which that part of the universe called the solar system is affected.

2446. Effects of annual parallax of the stars. — The greatest difficulty against which the Copernican system has had to struggle, even among the most enlightened of its opponents, has been the absence of all apparent effects of parallax among the fixed stars, those objects which are scattered in such countless numbers over every part of the firmament. From what has been explained, it will be perceived that, supposing these bodies to be, as they evidently must be, placed at vast distances outside the limits of the solar system and in every imaginable direction around it, the effects annual parallax would be to give to each of them an apparent annual motion in a circle or ellipse, according to their direction in relation to the position of the earth in its orbit, the ellipse varying in its eccentricity with this position, and the diameter of the circle or major axis of the ellipse being determined by the angle which the diameter EE' (fig. 718) of the earth's orbit subtends at the star, being less the greater the distance of the star, and vice versá. The apparent position of the star in this circle or ellipse would be evidently always in the plane passing through the star and the line joining the sun and earth.

2447. Close resemblance of these to aberration. — Now, it will be apparent, that such phenomena bear a very close resemblance to those of aberration already described (2440). In both the stars appear to move annually in small circles when situate 90° from the ecliptic; in both they appear to move in small ellipses between that position and the ecliptic; in both the eccentricities of the ellipses increase in approaching the ecliptic; and in both the ellipses flatten into their transverse axis when the object is actually in the ecliptic.

2448. Yet aberration cannot arise from parallax. — Notwithstanding this close correspondence, the phenomena of aberration are atterly incompatible with the effects of annual parallax. The apparent displacement produced by aberration is always in the direction of the earth's motion, that is to say, in the direction of the tangent to the earth's orbit at the point where the earth happens to be placed. The apparent displacement due to parallax would, on the contrary, be in the direction of the line joining the earth and sun. The apparent axis of the ellipse or diameter of the circle of aberration is exactly the same, that is 20"-42, for all the stars; while the apparent axis of the ellipse or diameter of the circle due to annual parallax would be different for stars at different distances, and would vary, in fact, in the inverse ratio of the distance of the star, and could not therefore be the same for all stars whatever, except on the

paramax can only be ascribed to the placed at distances from the solar s orbit of the earth shrinks into a potion of an observer round this orbit, with all our familiar standards of magarent displacement of a fixed star thround a grain of mustard seed would direction of the moon or sun.

We shall return to the subject of the in a subsequent chapter.

2450. The diurnal and annual phemotions of the earth. — Considering, the earth, as well as its diurnal rotations how how these two motions will expendifested in the succession of seasons.

While the earth revolves annually ro of rotation at the same time upon a c which is inclined from the perpendicula 23° 28'. During the annual motion keeps continually parallel to the same d pletes its revolution upon it in twent minutes. In consequence of the combitation of the earth upon its axis with it sun, we are supplied with the alternathe succession of seasons.

When the globe of the earth is in su pole leans toward the sun, the greater p sphere is enlightened, and the subsection is

mal orbit, circumstances are reversed: then the days are longer has the nights in the southern hemisphere, and the nights are

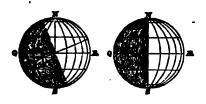


Fig. 719.

Fig. 720.

ger than the days in the northern hemisphere. At the intermeis points of the earth's annual path, when the axis assumes a ition perpendicular to the direction of the sun, fig. 720, then circle of light and darkness passes through the poles; all paralin every part of the earth are equally divided, and there is conmently equal day and night all over the globe.

In the annexed perspective diagram, fig. 721, these four positions the earth are exhibited in such a manner as to be clearly intellable.

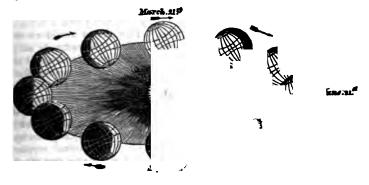


Fig. 721.

On the day of the 21st of June, the north pole is turned in the ection of the sun; on the 21st of December, the south pole is ned in that direction. On the days of the equinoxes, the axis the earth is at right angles to the direction of the sun, and it is sal day and night everywhere on the earth.

The annual variation of the position of the sun with reference to requator, or the changes of its declination, are explained by these tions. The summer solstice—the time when the sun's distance III.

from the equator is the greatest — takes place when the north pole leans towards the sun; and the winter solstice — or the time when the sun's distance south of the equator is greatest — takes place when the south pole leans toward the sun.

In virtue of these motions, it follows that the sun is twice a year vertical at all places between the tropics; and at the tropics themselves it is vertical once a year. In all higher latitudes the point at which the sun passes the meridian daily alternately approaches to and recedes from the zenith. From the 21st of December until the 21st of June, the point continually approaches the zenith. It comes nearest to the zenith on the 21st of June; and from that day until the 21st of December, it continually recedes from the senith. and attains its lowest position on the latter day. The difference, therefore, between the meridional altitudes of the sun on the days of the summer and winter solstices at all places will be twice twenty-three degrees and twenty-eight minutes, or forty-six degrees and fifty-six minutes. In all places beyond the tropics in the northern hemisphere, therefore, the sun rises at noon on the 21st of June, forty-six degrees and fifty-six minutes higher than it rises on the 21st of December. These are the limits of meridional altitude which determine the influence of the sun in different places.

2451. Mean solar or civil time. — It has been explained that the rotation of the earth upon its axis is rigorously uniform, and is the only absolutely uniform motion among the many and complicated motions observable on the heavens. This quality would render it a highly convenient measure of time, and it is accordingly adopted for that purpose in all observatories. The hands of a sidereal clock move in perfect accordance with the apparent motion of the firmament.

But for civil purposes, uniformity of motion is not the only condition which must be fulfilled by a measure of time. It is equally indispensable that the intervals into which it divides duration should be marked by conspicuous and universally observable phenomens. Now it happens that the intervals into which the diurnal revolution of the heavens divides duration, are marked by phenomena which astronomers alone can witness and ascertain, but of which mankind in general are, and must remain, altogether unconscious.

2452. Civil day — noon and midnight. — For the purposes of common life, mankind by general consent has therefore adopted the interval between the successive returns of the centre of the sun's disk to the meridian, as the unit or standard measure of time. This interval, called a CIVIL DAY, is divided into 24 equal parts called Hours, which are again subdivided into minutes and seconds as already explained in relation to sidereal time. The hours of the civil day, however, are not counted from 0 to 24, as in sidereal time, but are divided into two equal parts of 12 hours, one commencing

he centre of the sun is on the meridian, the moment of which d NOON or NID-DAY; and the other 12 hours later, when the of the sun must pass the meridian below the horizon, the t of which is MIDNIGHT.

civil purpose, this latter moment has been adopted as the neement of one day, and the end of the other.

- 3. Difference between mean solar and sidereal time. A ay is evidently longer than a sidereal day. If the sun did inge its position on the firmament, its centre would return to ridian after the same interval that elapses between the suctransits of a fixed star. But since the sun, as has been ed. moves at the rate of about 1° per day from west to id since this motion takes place upon the ecliptic, which is I to the equator at an angle of 23° 28', the centre of the sun es its right ascension from day to day, and this increase varies ng to its position on the ecliptic. When the circle of declion which the centre of the sun is placed at noon on one day to the meridian the next day, the centre of the sun will have and will be found upon another circle of declination to the it; and it will not consequently come to the meridian until a nutes later, when this other circle of declination, by the dinotion of the heavens, shall come to coincide with the meridian. ce the solar day is longer than the sidereal day.
- 1. Difference between apparent noon and mean noon.— But rom the cause just stated and another which will be presently red, the daily increase of the sun's right ascension is variable, ference between a sidereal day and the interval between the ive transits of the sun is likewise variable, and thus it would that the solar days would be more or less unequal in length.
- 5. Mean solar time Equation of time. Hence has arisen edient adopted for civil purposes to efface this inequality. An ary sun is conceived to accompany the true sun, making the te revolution of the heavens with a rigorously uniform increase it ascension from hour to hour, while the increase of the right ion of the true sun thus varies. The time measured by the of this imaginary sun is called MEAN SOLAR TIME, and the neasured by the motion of the true sun is called APPARENT TIME.

difference between the apparent and mean solar time is called EQUATION OF TIME."

variation of the increase of the sun's right ascension being ad within narrow limits, the true and imaginary suns can never asunder, and consequently the difference between mean and ent time is never considerable.

L

The time indicated by a sun-dial is apparent time, that indicated by an exactly regulated clock or watch is mean time.

The correction to be applied to apparent time, to reduce it to mean time, is often engraved on sun-dials, where it is stated how

much "the sun is too fast or too slow."

2456. Distance of the sun. — Although the problem to determine with the greatest practical precision the distance of the sun from the earth is attended with great difficulties, many phenomena of easy observation supply the means of ascertaining that this distance must bear a very great proportion to the earth's diameter, or must be such that, by comparison with it, a line 8000 miles in length is almost a point. If, for example, the apparent distance of the centre of the sun from any fixed star be observed simultaneously from two places upon the earth, no matter how far they are apart, no difference will be discovered between them, unless means of observation susceptible of extraordinary precision be resorted to. The expedients by which the apparent displacement of the sun's centre by a change of position of the observer from one extremity of a diameter of the earth to the other, or, what is the same, the apparent magnitude of the diameter of the earth as it would be seen from the sun, has been ascertained, will be explained hereafter. Meanwhile, however, it may be stated that this visual angle amounts to no more than 17"2, or about the hundredth part of the apparent diameter of the sun as seen from the earth.

Supplied with this datum, and the actual magnitude of the diameter of the earth, we can calculate the distance of the sun by the rule explained in 2298. If r express the distance of the sun, and a the diameter of the earth, we shall have

$$r = \frac{2,062,050}{172} \times a = 11,992 \times a.$$

It appears, therefore, that the distance of the sun is equal to 11,992 diameters of the earth, and since the diameter of the earth measures about 7900 miles (2389), the distance of the sun must be

$$11,992 \times 7900 = 94,736,800$$
 miles.

or very nearly NINETY-FIVE MILLIONS OF MILES.

Since the mean distance of the earth from the sun has been adopted as the unit or standard, with reference to which astronomical distances generally are expressed, it is of the highest importance to ascertain its value with the greatest precision which our means of observation and measurement admit. By elaborate calculations, based upon the observations made, in 1769, on the transit of Venus, it has accordingly been shown by Professor Encke, that when the earth is at its mean distance from the sun, the semidiameter of the terrestrial equator subtends at the sun an angle of 8".5776. This is therefore the mean equatorial horizontal parallax of the sun; and

if respress the semidiameter of the equator, and D the mean distance of the earth from the sun, we shall therefore have

$$\mathbf{p} = \frac{206265}{8 \cdot 5776} \times r = 24047 \times r,$$

and since the semidiameter of the equator measures 8962.8 miles (2389), it follows that

D = 95,293,452.

Since all the numerical results of observation and measurement are liable to some amount of error, it is important, when precision is required, to know the limit of this error, in order to appreciate the extent to which such results are to be relied upon. In all cases this is possible, a major and minor limit of the computed or observed quantity being assignable, which cannot be exceeded. In the present case the value of D cannot vary from the truth by more than its three-hundredth part; that is to say, the actual mean distance of the earth from the sun, or the semiaxis major of the orbit, cannot be greater than

95,293,452 + 117,645 = 95,411,097 miles,

or less than

$$95,293,452 - 117,645 = 95,175,807$$
 miles.

2457. Linear value of 1" at the sun's distance. — By what has been explained in 2298, it appears that the linear value of 1" at the sun's distance is

$$\frac{95,000,000}{206,265}$$
 = 466 miles.

2458. Daily and hourly apparent motion of the sun, and real motion of the earth.—Since the sun moves over 360° of the heavens in 365½ days, its daily apparent motion must be 59'·14, or 3548", which being about twice the sun's apparent diameter, it is easy to remember that the disk of the sun appears to move in the firmament daily over a space nearly equal to twice its own apparent diameter. Its hourly apparent motion is

 $\frac{3548''}{24} = 147'' \cdot 8.$

Since 1" at the sun's distance is equal to 466 miles, and since the real orbitual motion is equal to that which the sun would have if it moved round the earth in a year, it follows that the daily orbitual motion of the earth is

 $3548 \times 466 = 1,653,368$ miles,

and its motions per hour, minute, and second, are

68,890 miles per hour, 1,148 miles per minute, 19·1 miles per second.







Fig. 723.

and the position of the wires; he will find that, afte the wires will no longer touch the sun, but will per within it, as represented in fig. 723. And after a time, he will find, on the other hand, that they fall it, as in fig. 724.

Now, as the wires throughout such a series of maintained always in the same position, it follows the sun must appear smaller at one time, and large that, in fact, the apparent magnitude of the sun m It is true that this variation is confined within very still it is distinctly perceptible. What, then, it may be its cause? Is it possible to imagine that the st goes a change in its size? This idea would, une stances, be absurd; but when we have ascertained, that the change of apparent magnitude of the sun periodical—that for one half of the year it continumtil it attains a minimum, and then for the ner increases until it attains a maximum—such a sur of a real periodical change in the globe of the sun becincredible.

If, then, an actual change in the magnitude of the sible, there is but one other conceivable cause for the

of December; that from December to July, it regularly decreases; and from July to December, it regularly increases.

Since the distance of the earth from the sun must increase in the mme ratio as the apparent diameter of the sun decreases, and vice xxxx (1118), the variation of the distance of the earth from the sun a every position which it assumes in its orbit can be exactly ascerained. A plan of the form of the orbit may therefore be laid lown, having the point occupied by the centre of the sun marked in & Such a plan proves on geometric examination to be an ellipse, he place of the sun being one of the foci.

2460. Method of describing an ellipse—its foci, axis, and eccenricity. — If the ends of a thread be attached to two points less listant from each other than its entire length, and a pencil be looped n the thread, and moved round the points, so as to keep the thread ight, it will trace an ellipse, of which the two points are the FOCI.

The line drawn joining the foci, continued in both directions to be ellipse, is called its TRANSVERSE, or MAJOR AXIS.

Another line, passing through the middle point of this at right magles to it, is called its MINOR AXIS.

The middle point of the major axis is called the CENTRE of the slipes:

The fractional or decimal number which expresses the distance of the focus from the centre, the semiaxis major being taken as the mit, is called the ecceutricity of the ellipse.

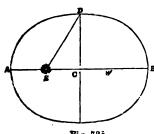


Fig. 725.

In fig. 725, c is the centre, s and s' the foci, AB the transverse axis.

The less the ratio of s s' to A B, or, what is the same, the less the eccentricity is, the more nearly the form of the ellipse approaches to that of a circle, and when the foci actually coalesce, the ellipse becomes an exact circle.

2461. Eccentricity of the earth's orbit. — The eccentricity of the

elliptic orbit of the earth is so small, that if an ellipse, representing truly that orbit, were drawn upon paper, it would be distinguishable from a circle only by submitting it to exact measurement. The eccentricity of the orbit has been ascertained to be only 0.01679. The semiaxis major, or mean distance, being 1.0000, the greatest and least distances of the earth from the sun will be—

B s =
$$1.0000 + 0.01679 = 1.01679$$

A s = $1.0000 - 0.01679 = 0.98321$.

Contrary to what might be expected, therefore, distant from the sun in summer than in winter.

2463. Variations of temperature through the cession of spring, summer, autumn, and winter, so of temperature of the seasons—so far as these on the position of the sun—will now require to be

The influence of the sun in heating a portion of face, will depend partly on its altitude above the greater that altitude is, the more perpendicularly that and the greater will be their calorific effect.

To explain this, let us suppose ABCD, fig. 72

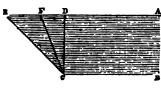


Fig. 726.

beam of the sol represent a portion surface, upon we would fall perpeter the control of the surfaces CD as surfaces CE being of the surfaces CE be

than CD, the rays will necessarily fall more dense and as the heating power must be in proportion t the rays, it follows that CD will be heated more tha same proportion as CE is greater than CD. But if pare two surfaces on neither of which the sun's he direction in which its rays will strike the surface at the more effective will be their heating power. So far, he heating power depends on the altitude of the sun, it reased with every increase of its meridian altitude.

t is that the heat of summer increases as we approach the The lower the latitude is, the greater will be the height he sun will rise. The meridian altitude of the sun at the olstice being everywhere outside the tropics forty-six d fifty-six minutes more than at the winter solstice, the

ect will be proportionately greater.

is not the only cause which produces the greatly superior immer as compared with winter, especially in the higher The heating effect of the sun depends not alone on its midday; it also depends on the length of time which it he horizon and below it. While the sun is above the is continually imparting heat to the air and to the surface th; and while it is below the horizon, the heat is coneing dissipated. The longer, therefore, - other things mme. — the sun is above the horizon, and the shorter time it, the greater will be the amount of heat imparted to the v twenty-four hours. Let us suppose that between sununset, the sun, by its calorific effect, imparts a certain heat to the atmosphere and the surface of the earth, and sunset to sunrise a certain amount of this heat is lost: of the action of the sun will be found by deducting the 1 the former.

then, it appears that the influence of the sun upon the pends as much upon the length of the days and nights as littude; but it so happens that one of these circumstances upon the other. The greater the sun's meridional altitude ger will be the days, and the shorter the nights; and the the longer will be the nights, and the shorter the days. circumstances always conspire in producing the increased re of summer, and the diminished temperature of winter. Why the longest day is not also the hottest.— The dogard difficulty is sometimes felt when the operation of these

considered, in understanding how it happens that, noting what has been stated, the 21st of June—when the the highest, when the days are longest and the nights—is not the hottest day, but that, on the contrary, the as they are called, which comprise the hottest weather of occur in August; and in the same manner, the 21st of —when the height to which the sun rises is least, the test, and the nights longest—is not usually the coldest day, on the other hand, the most inclement weather occurs at a ad.

crease. On the 21st of June, when the night is shortest, and the sun rises high reaches its maximum; but the temperature not therefore cease to increase. After the 2 tinues to be still a daily augmentation of heat tinues to impart more heat during the day the night. The temperature of the weather will increase when, by the diminished length of the night, and the diminished merical sun, the heat imparted during the day is just lost during the night. There will be, then, not temperature, and the heat of the weather will temperature, and the heat of the weather will second the sun temperature, and the heat of the weather will be then, not temperature, and the heat of the weather will be the sun the sun temperature, and the heat of the weather will be the sun temperature.

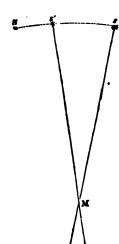
But it might occur to a superficial observer, would lead to the conclusion that the weather increase in its temperature, until the length become equal to the length of the nights; and case, if the loss of heat per hour during the night gain of heat per hour during the day. But su the loss is more rapid than the gain, and the the hottest day usually comes within the month long before the day of the autumual equinox.

maximum.

The same reasoning will explain why the construction of December, when and the night longest, and when the sun attains on a latitude. The decrease of the temperate depends upon the loss of heat during the cain during

that the position of the sun within the elliptic orbit of the such that the earth is nearest to the sun about the 1st of and most distant from it about the 1st of July. power of the sun's rays increases as the distance from the minishes, in even a higher proportion than the change of , it might be expected that the effect of the sun in heating on the 1st of January would be considerably greater than st of July. If this were admitted, it would follow that the notion of the earth in its elliptic orbit would have a tendiminish the cold of the winter in the northern hemisphere. gate the heat of summer, so as to a certain extent to equalize ons; and, on the contrary, in the southern hemisphere, e 1st of January is in the middle of summer, and the 1st in the middle of winter, its effects would be to aggravate the winter and the best in summer. The investigations, howich have been made in the physics of heat, have shown principle is governed by laws which counteract such effects. poperation of all other physical agencies, the sun's caloer requires a definite time to produce a given effect, and the sived by the earth at any part of its orbit will depend conon its distance from the sun and the length of time it takes se that portion of its orbit. In fact, it has been ascertained heating power depends as much on the rate at which the nges its longitude as upon the earth's distance from it. happens that, in consequence of the laws of the planetary discovered by Kepler, and explained by Newton, when the most remote from the sun, its velocity is least, and consethe hourly changes of longitude of the sun will be proporless. Thus it appears that what the heating power loses mented distance, it gains by diminished velocity; and again, e earth is nearest to the sun, what it gains by diminished , it loses by increased speed. There is thus a complete comn produced in the heating effect of the sun, by the dimielocity of the earth which accompanies its increased distance. period of the year, during which the heat of the weather is most intense, was called the CANICULAR DAYS, or DOG These days were generally reckoned as forty, commencing se 3d of July, and received their name from the fact, that in times the bright star Sirius, in the constellation of Canis or the Great Dog, at that time rose a little before the sun, was to the sinister influence of this star that were ascribed effects of the inclement heat, and especially the prevalence ness among the canine race. Owing to a cause which will ained hereafter (the precession of the equinoxes), this star er rises with the sun during the hot season.

various influences, affecting not only the physical globe, but also the phenomena of the organized wor as much an object of popular superstition as of scier These circumstances doubtless are in some degratriking appearance in the firmament, to the var form to which it is subject, and above all to its earth, and the close alliance existing between it and



2466. Its distance. — The moon is computed, by the u in 2328, by first ascertainin parallax.

parallax.

Let E and E', fig. 727, lends of a diameter of the e be the place of the moon's be any conspicuous star seen in the heavens, in the plane E, E', and M. The apparent star from the moon's centre server at E, and it is 8 s' to at The difference of these distance of the heavens which mess M s', or, what is the same, the under which the diameter E would be seen from the moon.

Now the arcs 8 s and 8 have been measured, and the

ence ss' has been ascertained = 6852", subject to a al

$$\text{M E} = \frac{206265}{3426} \times r = 60.2 \times r.$$

It follows, therefore, that the moon's distance is about thirty times the earth's diameter; and since the value of the latter is 7900 miles, the moon's distance is

$$7900 \times 30 = 237,000$$
 miles,

er, as appears by more exact computation, 237,630 miles.

2467. Linear value of 1" on it. — Having thus ascertained the mean's distance, we are enabled, by the method explained in 2319, to ascertain the actual length measured transversely to the line of rision on the moon which corresponds to the visual angle of 1". This length is

$$\frac{237630}{206265} = 1.15 \text{ mile.}$$

By this formula any space upon the moon, measured by its visual angle, can be reduced to its actual linear value, provided its direction be at right angles to the visual ray, which it will be if it be at the centre of the lunar disk. If it be between the centre and the edges, it will be foreshortened by the obliquity of the moon's surface to the line of vision, and, consequently, the linear value thus computed will be the real linear value diminished by projection, which, however, can be easily allowed for, so that the true linear value can be obtained for every part of the lunar disk.

2463. Its apparent and real diameter. — The apparent diameter of the moon is subject to a slight variation, owing to a corresponding variation due to the small ellipticity of its orbit. Its mean value is found to be 31' 7" or 1867".

By what has just been established (2392), therefore, its real diameter must be

 $1867 \times 1.15 = 2147$ miles.

More exact methods give 2153 miles.

Since the superficial magnitude of spheres is as the squares, and their volume or solid bulk as the cubes, of their diameters, it follows that the superficial extent of the moon is about the fourteenth part of the surface, and its volume about the forty-ninth part of the bulk, of our globe.

2469. Apparent and real motion. — The moon, like the sun, appears to move upon the celestial sphere in a direction contrary to that of the diurnal motion. Its apparent path is a great circle of the sphere, inclined to the ecliptic at an angle of about 5° 8′ 48″. It completes its revolution of the heavens in 27^d· 7^h· 44^m.

This apparent motion is explained by a real motion of the moon round the earth at the mean distance above mentioned, and in the time in which the apparent revolution is completed.

17

of the moon per hour in her orbit, is

 $6.9 \times 32.9 = 227 \text{ mi}$

Her orbitual motion is therefore at the rate 2471. Orbit elliptical. — Although, in it racter, the path of the moon round the eart the planets and satellites, circular, yet whe observation, we find that it is strictly an ell of the earth occupying one of its foci. by immediate observation upon the appare It will be easily comprehended that moon. apparent magnitude, as seen from the carth, from corresponding changes in the moon's disif at one time the disk of the moon appears la time, as it cannot be supposed that the actu itself could be changed, we can only ascribe apparent magnitude to the diminution of its di by observation that such apparent changes are its monthly course around the earth. The 1 small though perceptible variation of apparent it diminishes until it reaches a minimum, an creases until it reaches a maximum.

When the apparent magnitude is least, it i tance, and when greatest, at its least distance which these distances lie are directly opposite. positions the apparent size of the moon und gradual change, incre ; continually from maximum, and continually from the state of the moon under the state of th

arth, is called its perioe; and the point where its apparent cast, and where, therefore, its distance from the earth is is called its apoyee. These two points are called the moon's

positions of these points in the heavens be observed accua length of time, it will be found that they are subject to
change; that is to say, the place where the moon appears
will every month shift its position; and a corresponding
ill take place in the point where it appears largest. The
it of these points in the heavens is found to be in the same
as the general movement of the planets; that is, from west
r progressive. This phenomenon is called the PROGRESTHE MOON'S APSIDES.

te of this progression of the moon's apsides is 40° 68' in a recommon year, being equivalent to 6' 41" per day. They atly make a complete revolution in 8.85 years.

Moon's nucles — ascending and descending node—their rem. — If the position of the moon's centre in the heavens ed from day to day, it will be found that its apparent path it circle, making an angle of about 5° with the ecliptic. I consequently crosses the ecliptic at two points in opposite of the heavens. These points are called the moon's nodes. Initially are ascertained by observing from time to time the of the moon's centre from the ecliptic, which is the moon's by watching its gradual diminution, and finding the point

it becomes nothing; the moon's centre is then in the and its position is the node. The node at which the moon om the south to the north of the collection is called the asnode, and that at which it passes from the north to the called the descending node.

points, like the apsides, are subject to a small change of but in a retrograde direction. They make a complete revothe ecliptic in a direction contrary to the motion of the
8-6 years, being at the rate of 3' 10"-6 per day.

Rotation on its axis. — While the moon moves round the us in its monthly course, we find, by observations of its ce, made even without the aid of telescopes, that the same ere is always turned towards us. We recognise this fact ving that the same marks are always seen in the same posimit. Now in order that a globe which revolves in a circle a centre abould turn continually the same hemisphere hat centre, it is necessary that it should make one revoluntist axis in the time it takes so to revolve. For let us that the globe, in any one position, has the centre round; revolves north of it, the hemisphere turned toward the turned toward the north. After it makes a quarter of a

revolution, the centre is to the east of it, and the hemisphere we was previously turned to the north must now be turned to the After it has made another quarter of a revolution the centre, we south of it, and it must be now turned to the south. In the manner, after another quarter of a revolution, it must be turned the west. As the same hemisphere is successively turned to all points of the compass in one revolution, it is evident that the itself must make a single revolution on its axis in that time.

It appears, then, that the rotation of the moon upon its axis, equal to that of its revolution in its orbit, is $27^{\circ}.7^{\circ}.44^{\circ}$ or 44° . The intervals of light and darkness to the inhabitants o moon, if there were any, would then be altogether different those provided in the planets; there would be about $327^{\circ}.52^{\circ}$ of continued dark the analogy, then, which, as will hereafter appear, prevails a the planets with regard to days and nights, and which forms a argument in favour of the conclusion that they are inhabited like the earth, does not hold good in the case of the moon.

2475. Inclination of axis of rotation.— Although as a proposition it be true that the same hemisphere of the moon ways turned toward the earth, yet there are small variations edge, called librations, which it is necessary to notice. The at the moon is not exactly perpendicular to its orbit, but is inclination northern and southern poles of the moon lean alternately in a sedgree to and from the earth.

2476. Libration in latitude.—When the north pole leans to the earth, we see a little more of that region, and a little less it leans the contrary way. This variation in the northern southern regions of the moon visible to us, is called the LIBRA

IN LATITUDE.

2477. Libration in longitude. — In order that in a strict the same hemisphere should be continually turned toward the e the time of rotation upon its axis must not only be equal to the time rotation in its orbit, which in fact, it is, but its angular velocities axis in every part of its course, must be exactly equal to it gular velocity in its orbit. Now it happens that while its an velocity on its axis is rightened yuniform throughout the montiangular velocity in its orbit is subject to a slight variation; the sequence of this is that a little more of its eastern or western is seen at one time than at another. This is called the LIBRA IN LONGITUDE.

2478. Diurnal libration. — By the diurnal motion of the e we are carried with it round its axis; the stations from whice view the moon in the morning and evening, or rather when it and when it sets, are then different according to the latitude of

earth in which we are placed. By thus thewing it four 1.7.1, places, we see it under slightly different aspects. This is about a cause of a variation, which we see in its eastern and vestern engages this is called the DIURNAL LIBRATION.

2479. Phases of the moon.—While the mode retrives round earth, its illuminated hemisphere is always presented to the sun therefore takes various positions in reference to the earth. In 728, the effects of this are exhibited. Let z a represent the man-

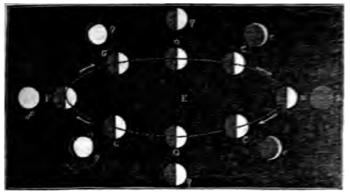


Fig. 724

tion of the sun, and E the earth; when the moon is at N. between the sun and the earth, its illuminated hemisphere being more atward the sun, its dark hemisphere will be presented toward to earth; it will therefore be invisible. In this coeffice the more mid to be in CONJUNCTION.

When it moves to the position of the subgistered herder having still presented to the sun, a small perform of it only is to me, to the earth, and it appears as a thin crescent, as represented as

When the moon takes the position of Q, at right angles of sun, it is said to be in QUADRATURE: the half of the engine of hemisphere only is then pre-antel to the earth, and the model pears halved, as represented at Q.

When it arrives at the position 6, the greater part of the colling lightened portion is turned to the earth, and it is greater, appearing

as represented at q.

When the moon comes in opposition to the sum as were to the enlightened hemisphere is turned full toward the earth, at it moon will appear full, as at it unless it be obscured by the earth, at it shadow, which rarely happens. In the same manner it is about that of it is again gibbous; at of it is halved, and at if it is a creation.

..... quarter. I Be

the fourth octant; G the second octant; G' the the fourth octant. At the first and fourth and at the second and third octants it is gibbe

2480. Synodic period or common month.of the moon in the heavens is much more 1 sun; for while the sun makes a complete cir 365.25 days, and therefore moves over it at a moon moves at the rate of 13° 10' 35" (247) sun and moon appear to move in the same d ment, both proceeding from west to east, the 1 junction, depart from the sun toward the east 12° 9' per day. If then, the moon be in conju on any given day, it will be 12°9' east of it at the following day; 24° 18' east of it after two d then, the sun set with the moon on any evening, ment of sunset on the following evening, be 1: at sunset will appear as a thin crescent, at a cor on the succeeding day it will be 24° 18' east of be at a still greater altitude at sunset, and will be After seven days, the moon will be removed no sun; it will be at or near the meridian at sunse in the heavens for about six hours after sunset, : the west as the half-moon. Each successive ever distance from the sun, and also increasing its visible in the meridian at a later hour, and wi longer apparent in the firmament during the n be gibbous. After about fifteen days, it will be? the sun, and will be full and ...

the period of the moon. But from what has been explained, it will be evident that while the moon makes its apparent revolution of the heavens in about 27.3 days, the sun advances through somewhat more than 27° of the heavens, in the same direction. Before the moon can reassume the same phase, it must have the same position relative to the sun, and must, therefore, overtake it. But since it moves at the rate of about 1° in two hours, it will take more than two days to move over 27°. Hence the synodic period, or lanar month, or the interval between two successive conjunctions, is about two days longer than the sidereal period of our satellite.

The exact length of the synodic period is 29d 12h 14m 2 87, or

29-53059 mean solar days.

2481. Mass and density. — The methods by which the mass or weight of the moon has been ascertained will be explained herester; meanwhile it may be stated here that the result of the most recent solutions of this problem, by various methods and on different data, proves that the mass or quantity of matter composing the globe of the moon, is a little more than the 90th part of the mass of the earth; or, more exactly, if the mass of the earth consist of a million of equal parts, the mass of the moon will be equal to 11,399 of these parts.

Since the volume or bulk of the moon is about the 50th part of that of the earth, while its mass or weight is little more than the 90th part of that of the earth, it follows that its mean density must be little more than half the density of the earth, and therefore

(2393) about 2.83 times that of water.

2482. No air upon the moon. — In order to determine whether or not the globe of the moon is surrounded with any gaseous envelope like the atmosphere of the earth, it is necessary first to consider what appearances such an appendage would present, seen at the moon's distance, and whether any such appearances are discoverable.

According to ordinary and popular notions, it is difficult to separate the idea of an atmosphere from the existence of clouds; yet to produce clouds something more is necessary than air. The presence of water is indispensable; and if it be assumed that no water exist, then certainly the absence of clouds is no proof of the absence of an atmosphere. Be this as it may, however, it is certain that there are no clouds upon the moon; for if there were, we should immediately discover them, by the variable lights and shadows they would produce. If there is, then, an atmosphere upon the moon, it is one entirely unaccompanied by clouds.

One of the effects produced by a distant view of an atmosphere surrounding a globe, one hemisphere of which is illuminated by the san, is, that the boundary, or line of separation between the hemisphere enlightened by the sun and the dark hemisphere, is not

of the semicircle is also that boundary. In nei however, do we ever discover the slightest ind appearance as that which has just been described fading away of the light into the dar trary, the boundary, though serrated and irregreefectly well defined and sudden.

All these circumstances conspire to prove t exist upon the moon an atmosphere capable of any sensible degree.

2483. Absence of air indicated by absence of it may be contended that an atmosphere may still attenuated to produce a sensible twilight. Ast have resorted to another test of a much more de kind, the nature of which will be understood by a principle of optics.

Let mm', fig. 729, represent the disk of the

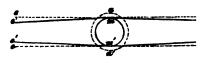


Fig. 729.

represent the atmosphere which surrounds it. Le

edge of the moon, would be visible at the earth, for the ray s'm, a passing through the atmosphere, would be bent at an angle the direction m's', and in like manner the ray s'm' would be bent the angle m's'—so that the stars s's' would be visible at e's', twithstanding the interposition of the edges of the moon.

This reasoning leads to the conclusion that as the moon moves er the face of the firmament, stars will be continually visible at edge which are really behind it if it have an atmosphere, and the tent to which this effect will take place will be in proportion to

density of the atmosphere.

The magnitude and motion of the moon and the relative positions the stars are so accurately known that nothing is more easy, cera, and precise, than the observations which may be made with view of ascertaining whether any stars are ever seen which are mibly behind the edge of the moon. Such observations have meade, and no such effect has ever been detected. This species observation is susceptible of such extreme accuracy, that it is rain that if an atmosphere existed upon the moon a thousand see less dense than our own, its presence must be detected.

Bessel has calculated that if the difference between the apparent ameter of the moon, and the arc of the firmament moved over by e moon's centre during the occultation of a star, centrically oclaed, were admitted to amount to so much as 2", and allowing for a possible effect of mountains, by which the edge of the disk is trated, taking these at the extreme height of 24,000 feet, the maity of the lunar atmosphere, whose refraction would produce the an effect, would not exceed the 968th part of the density of earth's atmosphere, supposing the two fluids to be similarly continued. Nor would this conclusion be materially modified by any apposition of an atmosphere composed of gases different from the positivents of the earth's atmosphere.

The earth's atmosphere supports a column of 30 inches of merary: an atmosphere 1000 times less dense would support a column f three-tenths of an inch only. We may therefore consider it as a established fact, that no atmosphere exists on the moon having a ensity even as great as that which remains under the receiver of he most perfect air-pump, after that instrument has withdrawn from

the air to the utmost extent of its power.

If further proofs of the nonexistence of a lunar atmosphere were equired, Sir J. Herschel indicates several which are found in the henomena of eclipses. In a solar eclipse the existence of an atmosphere having any sensible refraction, would enable us to trace to him of the moon beyond the cusps externally to the sun's disk, y a narrow but brilliant line of light extending to some distance long its edge. No such phenomenon has, however, been seen.

If there were any appreciable quantity of vapour suspended over

the moon's surface, very faint stars ought to disappear behind it before the moment of their occultation by the interposition of the moon's edge. Such, however, is not the case. When occulted st the enlightened edge of the lunar disk, the light of the moon over powers them and renders them invisible, and even at the dark edge the glare in the sky, caused by the proximity of the enlightened part of the disk, renders the occultation of extremely minute stars incapable of observation. But these obstacles are removed in the case of total solar eclipses; on which occasions stars, so faint as to be only seen by the aid of a telescope, come up close to the limb with out any sensible diminution of their brightness, and undergo an extinction as instantaneous as the largest and brightest by the inter-

position of the moon's limb.

2484. Moonlight not sensibly calorific. - It has long been . object of inquiry whether the light of the moon has any heat; but the most delicate experiments and observations have failed to detect this property in it. The light of the moon was collected into the focus of a concave mirror of such magnitude as would have been sufficient, if exposed to the sun's light, to evaporate gold or platnum. The bulb of a differential thermometer, sensitive enough show a change of temperature amounting to the 500th part of a degree, was placed in its focus, so as to receive upon it the concestrated rays. Yet no sensible effect was produced. We must, therefore, conclude that the light of the moon does not possess the cale rific property in any sensible degree. But if the rays of the moon be not warm, the vulgar impression that they are cold is equally erroncous. We have seen that they produce no effect either way the thermometer.

2485. No liquids on the moon. — The same physical tests which show the nonexistence of an atmosphere of air upon the moon are equally conclusive against an atmosphere of vapour. It might, therefore, be inferred that no liquids can exist on the moon's surface, since they would be subject to evaporation. Sir John Herschel, however, ingeniously suggests that the nonexistence of vapour not conclusive against evaporation. One hemisphere of the more being exposed continuously for 328 hours to the glare of sunshine of an intensity greater than a tropical noon, because of the absence of an atmosphere and clouds to mitigate it, while the other is for an equal interval exposed to a cold far more rigorous than that which prevails on the summits of the loftiest mountains or in the polar region, the consequence would be the immediate evaporation of liquids which might happen to exist on the one hemisphere, and the instantaneous condensation and congelation of the vapour on the The vapour would, in short, be no sooner formed on the enlightened hemisphere than it would rush to the vacuum over dark hemisphere, where it would be instantly condensed and com-

gealed, an effect which Herschel aptly illustrates by the familiar experiment of the CRYOPHORUS. The consequence, as he observes, of this state of things, would be absolute aridity below the vertical sun, constant accretion of hoar frost in the opposite region, and perhaps a narrow zone of running water at the borders of the enlightened hemisphere. He conjectures that this rapid alternation of evaporation and condensation may to some extent preserve an equilibrium of temperature, and mitigate the severity of both the diurnal and nocturnal conditions of the surface. He admits, nevertheless, that such a supposition could only be compatible with the tests of the absence of a transparent atmosphere even of vapour within extremely narrow limits; and it remains to be seen whether the general physical condition of the lunar surface, as disclosed by the telescope, be not more compatible with the supposition of the total absence of all liquid whatever.

It appears to have escaped the attention of those who assume the possibility of the existence of water in the liquid state on the moon, that, in the absence of an atmosphere, the temperature must necessarily be, not only far below the point of congelation of water, but even that of most other known liquids. Even within the tropics, and under the line with a vertical sun, the height of the snow line does not exceed 16,000 feet (2187), and nevertheless at that elevation, and still higher, there prevails an atmosphere capable of supporting a considerable column of mercury. At somewhat greater elevations, but still in an atmosphere of very sensible density, mercury is congealed. Analogy, therefore, justifies the inference that the total, or nearly total, absence of air upon the moon is altogether incompatible with the existence of water, or probably any other body in the liquid state, and necessarily infers a temperature altogether incompatible with the existence of organised beings in any respect analogous to those which inhabit the earth.

But another conclusive evidence of the nonexistence of liquids on the moon is found in the form of its surface, which exhibits none of those well-understood appearances which result from the longcontinued action of water. The mountain formations with which the entire visible surface is covered are, as will presently appear, universally so abrupt, precipitous, and unchangeable, as to be utterly

incompatible with the presence of liquids.

2486. Absence of air deprives solar light and heat of their utility. — The absence of air also prevents the diffusion of the solar light. It has been already shown (923) that the general diffusion of the sun's light upon the earth is mainly due to the reflection and refraction of the atmosphere, and to the light reflected by the clouds; and that without such means of diffusion the solar light would only illuminate those places into which its rays would directly penetrate. Every place not in full sunshine, or exposed to

2487. As seen from the moon, appearance of firmament. - If the moon were inhabited, obseit would witness celestial phenomena of a sin differing in many respects from those presented 1 of our globe. The heavens would be perpetually less. The stars and planets would shine with ex dour during the long night of 328 hours. The axis being only 5°, there would be no sensible c The year would consist of one unbroken monotony inhabitants of one hemisphere would never see the inhabitants of the other would have it constantly in by day and by night, and always in the same po who inhabit the central part of the hemisphere pre earth would appear stationary in the zenith, and w it, never rising nor setting, nor in any degree char in relation to the zenith or horizon. To those w intermediate between the central part of that hemi places which are at the edge of the moon's disk, appear at a fixed and invariable distance from the at a fixed and invariable azimuth; the distance from everywhere equal to the distance of the observer f point of the hemisphere presented to the earth. any of the places which are at the edge of the luna would appear perpetually in a fixed direction on the

The earth shone upon by the sun would appear a to us; but with a disk having an apparent diamethat of the moon in the ratio of 79 to 21 and an

we to the moon, and vice versá: when the moon is a e carth is gibbous, and vice versá.

res of light and shade would not, as on the moon, be int and invariable. So far as they would arise from the ing in the terrestrial atmosphere, they would be variable. so, their arrangement would have a certain relation to the ing to the effect of the prevailing atmospheric currents the line.* This cause would produce streaks of light the general direction of which would be at right angles h's axis, and the appearance of which would be in all nilar to the BELTS which, as will appear hereafter, are pon some of the planets, and which are ascribed to a all cause.

the openings of the clouds the permanent geographical the surface of the earth would be apparent, and would khibit a variety of tints according to the prevailing chathe soil, as is observed to be the case with the planet at an immensely greater distance. The rotation of the its axis would be distinctly observed and its time ascerhe continents and seas would be seen to disappear in sucone side and to reappear at the other, and to pass across? the earth as carried round by the diurnal rotation.

Why the full disk of the moon is faintly visible at new loon after conjunction, when the moon appears as a thin out is so removed from the sun as to be seen at a suffiude after sunset, the entire lunar disk appears faintly d within the horns of the crescent. This phenomenon ed by the effect of the earth shining upon the moon and ig it by reflected light as the moon illuminates the earth, degree of intensity greater in the ratio of about 14 to 1. to what has just been explained, the earth appears to the ly full at the time when the moon appears to the earth as cent, and it therefore receives then the strongest possible on. As the lunar crescent increases in breadth, the phase th as seen from the moon becomes less and less full, and ity of the illumination is proportionately diminished. find, that as the lunar crescent passes gradually to the ie complement of the lunar disk becomes gradually more ible, and soon disappears altogether.

Physical condition of the moon's surface.—If we examine carefully, even without the aid of a telescope, we shall con it distinct and definite lineaments of light and shadow. ures never change; there they remain, always in the same pon the visible orb of the moon. Thus the features that

^{*} See Chapter on the tides and trade winds.

been attempted to be explained by the hypothesis sphere of the satellite, which is turned toward the clongated and protuberant, and it is the excess of it makes it tend to direct itself always toward the prima to the universal principle of attraction. Be this effect is, that our selenographical knowledge is need to that hemisphere which is turned toward us.

But what is the condition and character of the moon? What are the lineaments of light and shade upon it? There is no object outside the earth with v scope has afforded us such minute and satisfactory infe

If, when the moon is a crescent, we examine with even of moderate power, the concave boundary, which of the surface where the enlightened hemisphere ends hemisphere begins, we shall find that this boundary is and regular curve, which it undoubtedly would be i were smooth and regular, or nearly so. If, for exami surface resembled in its general characteristics that supposing that the entire surface is land, having the ge teristics of the continents of the earth, the inner box lunar crescent would still be a regular curve broken c only at particular points. Where great mountain rang of the Alps, the Andes, or the Himalaya, might chan these lofty peaks would project vastly elongated shade adjacent plain; for it will be remembered that, being the moment in question, at the boundary of the enl darkened hemispheres, the shadows would be those o morning: which am -

md, on the contrary, rugged and serrated, and brilliantly i points are seen in the dark parts at some distance from irk shadows of considerable length appear to break into ated surface. The inequalities thus apparent indicate tracteristics of the surface. The bright points seen within misphere, are the peaks of lofty mountains tinged with the They are in the condition with which all travellers



Fig. 730.

in Alpine countries are familiar; after the sun has set, and darkness has set in over the valleys at the foot of the chain, the sun still continues to illuminate the peaks above.

The sketch of the lunar crescent in fig. 730, will illustrate these

observations.

The visible hemisphere of our satellite has, within the last quarter of a century, been subjected to the most rigorous examination which unwearied industry, aided by the vast improvement which has been effected in the instruments of telescopic observation, rendered possisible; and it is no exaggeration now to state that we possess a chart of that hemisphere which in

of detail far exceeds any similar representation of the

the relenographical observers, the Prussian astronomers, r and Mädler, stand pre-eminent. Their descriptive work her Monde contains the most complete collection of observable physical condition of our satellite, and the chart, meaninches in diameter, exhibits the most complete represen-

the lunar surface extant. Besides this great work, a phie chart was produced by Mr. Russell, from observations h a seven-foot reflector, a similar delineation by Lohrmann, ne, a very complete model in relief of the visible hemisphere me Witte, an Hanoverian lady.

ivey to the student any precise or complete idea of the mass nation collected by the researches and labours of these emiervers, would be altogether incompatible with the necessary? a work like that which we have undertaken. We shall confine ourselves to a selection from some of the most represents of those works, aided by the telescopic chart of the stern quadrant of the moon's disk, given in Plate I., which

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epercon or the chart of the S. E. quadrant, Plate I., will and the other three quadrants of the disk do not difference character.*

- (b) Causes of the lints of white and gray on the moon's tints of white and gray which mark the lineaments obs of the full moon arise partly from the different reflec matter composing different parts of the lunar surface. different angles at which the rays of the solar light are If the surface of the lunar hemisphere were uniformly these angles of incidence would be determined by the po with relation to the centre of the illuminated hemisp case, the tints would be more regular and would vary in: to the centre of the disk; but, owing to the great inequ the vast and complicated mountainous masses which ; part of the surface, and the great depths of the cavities are surrounded by the circular mountain ranges, the ang the solar rays are subject to extreme and irregular variati those lineaments and forms tinted with various shades with which every eye is familiar.
- (c) Shadows risible only in the phases—they supply meas depths.—When the moon is full, no shadows upon it can be that position, the visual ray coinciding with the luminous directly interposed between the observer and its shadous progress, however, the shadows gradually come into visual ray is inclined at a gradually increasing angle to t

^{*} It must be observed that the chart represents the m seen on the south meridian in an astronomical telescope, ment produces an inverted image, the south pole apper and the north pole at the lowest point of the disk, and the on the right and the western on the left of the observer, tions are the reverse of those which the same points he without a telescope, or with one which does not invertible measured east and war. A first consumer that the consumer of the

in the quarters, this angle having increased to 90°, and the boundary of the enlightened hemisphere being then in the centre of the hemisphere resented to the observer, the position is most favourable for the observation of the shadows by which chiefly, not only the forms and dispositions of the mountainous masses and the intervening and enclosed valleys and ravines are ascertained, but their heights and depths are measured. This latter problem is solved by the well-understood principles of geometrical projection, when the directions of the visual and solar rays, the position of the object, and of the surface on which the shadows are projected, are severally given.

(d) Uniform patches, called oceans, seas, &c., proved to be irregular land surface. - Uniform patches of greater or less extent, each having an uniform gray tint more or less dark, having been supposed, by early observers, to be large collections of water, were designated by the names, Ockanus, MARE, PALUS, LACUS, SINUS, &c. These names are still retained, but the increased power of the telescope has proved that such regions are diversified, like the rest of the lunar surface, by inequalities and undulations, of permanent forms, and are therefore not, as was imagined, water or other liquid. They differ from other regions only in the magnitude of the mountain passes which prevail upon them. About two-thirds of the visible hemisphere of the moon consists of this character of surface. Examples of these are presented by the Mare Nubium, Oceanus Procellarum, Mare Humorum, &c., on the chart.

(e) Whiter spots, mountains. - The more intensely white parts are mountains of various magnitude and form, whose height, relatively to the moon's magnitude, greatly exceeds that of the most stupendous terrestrial eminences; and there are many, characterised by an abruptness and steepness which sometimes assume the position of a vast vertical wall, altogether without example upon the earth. These are generally disposed in broad masses, lying in close contiguity, and intersected with vast and deep valleys, gullies, and abysses, none of which, however, have any of the characters which betray the agency of water.

(f) Classes of circular mountain ranges. — Circular ranges of mountains which, were it not for their vast magnitude, might be inferred from their form to have been volcanic craters, are by far the most prevalent arrangement. These have been denominated, according to their magnitudes, Bul-

WARK PLAINS, RING MOUNTAINS, CRATERS, and Holes.

(3) Bulwark plains. - These are circular areas, varying from 40 to 120 miles in diameter, enclosed by a ring of mountain ridges, mostly contiguous, but in some cases intersected at one or more points by vast ravines. The enclosed area is generally a plain on which mountains of less height are often scattered. The surrounding circular ridge also throws out spurs, both externally and internally, but the latter are generally shorter than the former. In some cases, however, internal spurs, which are diametrirally opposed, unite in the middle so as to cut in two the enclosed plain. In some rare cases the enclosed plain is uninterrupted by mountains, and it is almost invariably depressed below the general level of the surrounding A few instances are presented of the enclosed plain being convex.

The mountainous circle enclosing these vast areas is seldom a single ridge. It consists more generally of several concentric ridges, one of which, however, always dominates over the rest and exhibits an unequal summit, broken by stupendous peaks, which here and there shoot up from it to vast Occasionally it is also interrupted by smaller mountains of the beights. circular form.

Examples of bulwark plains are presented in the cases of Clavius, Wal-18 *

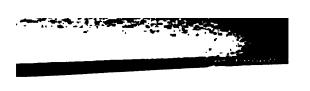
than the bulwark plains, varying from 10 to 50 miles in diare generally more regular and more exactly circular in the are sometimes found upon the ridge which encloses a bulinterrupting the continuity of their boundary, and sometim within the enclosed area. Sometimes they stand in the miles they concave, often includes a central mountain, presenting the character of a volcanic cruter, but on a scale of magnitude in terrestrial volcances. The surface enclosed is always region surrounding the enclosing ridge, and the central mouto such a height that, if it were levelled, it would fill the di

(i) Tycho, a ring mountain. — The most remarkable examis Tycho (see chart, lat. 42°, long. 12°). This object is without a telescope on the lunar disk when full; but, owir tude of other features which become apparent around it is can then be only distinguished by a perfect knowledge of i with a good telescope. The enclosed area, which is very is 47 miles in diameter, and the inside of the enclosing steepness of a wall. Its height above the level of the en 16,000 feet, and above that of the external region, 12,000 as central mount, height 4,700 feet, besides a few lesser henclosure.

(k) Craters and holes. — These are the smallest formations class. Craters enclose a visible area, containing generally a or peak, exhibiting in a striking manner the volcanic chainclude no visible area, but may possibly be craters on a see be distinguished by the telescope.

Formations of this class are innumerable on every part surface of the moon, but are no where more prevalent than around Tycho, which may be seen on a very enlarged seals which represents that ring mountain, and the adjacent region, sixteen degrees of latitude, and from sixteen to twenty degree

(1) Other mountain formations. — Besides the preceding, most remarkable the most absence



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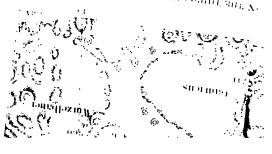


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 $w_{t,m_{X},n_{Y},n_{Y},m_{H(Y)},m_{H(Y)},n_{X}}$



centres round which this extraordinary radiation is manihenomena, less conspicuously developed, however, are leyer, Ruler, Proclus, Aristillus, Timocharis, and some

a. as displayed when the moon is full around Tycho, are ste III. on the same scale as Plate II. streaks commence at a distance of about 20 miles out-ridge of Tycho. From that limit they diverge and overparth part of the visible hemisphere. On the S. they ge of the disk; on the E. to Hainzel and Capuanus; on are Nubium; on the N. to Alphonse; on the N.W. to the id to the W., so as to cover nearly the entire south-western

visible when the sun's rays fall upon the region of Tycho greater than 25°, and the more perpendicularly the rays nore fully developed the phenomena will be. They are, en in their splendour, as represented in Plate III., when

As the moon moves from opposition to the last quarter, fore gradually disappear, and the shadows of the mounre at the same time gradually brought into view, so that moon undergoes a complete transformation. This change exhibited by holding the Plate III. before a window to f the observer is turned. He will then see the phenomena nted on the full moon. Let him then turn slowly upon face is presented to the window, holding the paper beid the light. The Plate II. will then be seen by means of of the paper, and it will gradually become more and more at as he turns more directly towards the light.*

nountain formations generally disappear under the splenliating streaks, some few, as will be perceived on Plate

be visible through them.

imerous selenographic observers have proposed any satison of these phenomena, which are exhibited nearly in the ound the other ring mountains above named. Schröter be mountains, an hypothesis overturned by the observawith more powerful instruments. Herschel, the elder, ea of streams of lava: Cassini imagined they might be ers even suggested the possibility of their being roads! that these ring mountains may have been among the first nations; and, consequently, the points to which all the the formation of our satellite would have been attracted. s produced effects, such as vitrification or oxydation, which ective powers of the surface. We must, however, dismiss 1, however ingenious and attractive, referring those who the subject to the original work.

' Tycho .- This region is crowded with hundreds of peaks, rs (see Plate II.); not the least vestige of a plain can covered. Towards the E. and S.E. craters predominate, thains parallel to the ring are more numerous. On the S.

us expedient is suggested by Müdler. It must be rememthat, while Plate II. represents the region as it appears in 1 inverts. Plate III. represents it as if it were reflected in t would be seen with a telescope having a prismatic eye-

the mountains are thickly scattered in confused masses. At a distance of 15 to 25 miles, craters and small ring mountains are seen, few being circular, but all approaching to that form. All are surrounded by steep ramparts.

(o) Wilhelm I. — This is a considerable ring mountain S.E. of Tycho. The altitude of its eastern parapet is 10,000 feet, that of its western being only 6,000. Its crest is studded with peaks; and craters of various magnitudes, heights, and depths, surrounding it in great numbers, and giving

a varied appearance to the adjacent region.

(p) Longomontanus.— A large circular range, having a diameter of 80 miles, enclosing a plain of great depth. The eastern and western ridger rise to the height of 12,000 to 13,000 feet above the level of the enclosed plain. Its shadow sometimes falls upon and conceals the numerous craters and promontories which lie near it. The whole surrounding region is savage and rugged in the highest degree, and must, according to Mader, have resulted from a long succession of convulsions. The principal, and apparently original, crater has given way in course of time to a series of new and less violent eruptions. All these smaller formations are visible on the full moon, but not the principal range, which then disappears, though its place may still be ascertained by its known position in relation to Tycho.

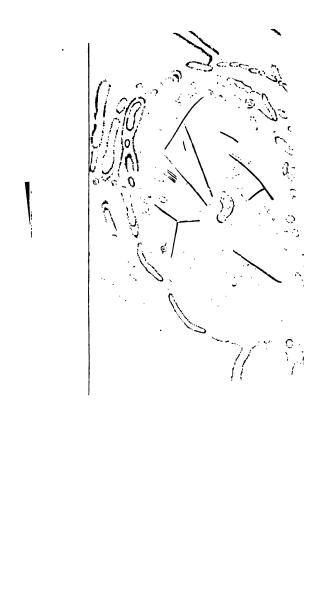
(q) Maginus.—This range N.W. of Tycho (see Plate I.) has the appearance of a vast and wild ruin. The wide plain enclosed by it lies in deep shade even when the sun has risen to the meridian. Its general height is 13,000 feet. A broad elevated base connects the numberless peaks, terraces, and groups of hills constituting this range, and small craters are numerous among these wild and confused masses. The central peak A is a low but well-defined hill, close to which is a crater-like depression, and

other less considerable hills.

(r) Analogy to terrestrial volcanoes more apparent than real - enlarged view of Gassendi.—The volcanic character observed in the selenographic formstions loses much of its analogy to like formations on the earth's surface when higher magnifying powers enable us to examine the details of what appear to be craters, and to compare their dimensions with even the most extensive terrestrial craters. Numerous examples may be produced to illustrate this. We have seen that Tycho, which, viewed under a moderate magnifying power, appears to possess in so eminent a degree the volcanic character, is, in fact, a circular chain enclosing an area upwards of fifty Gassendi, another system of like form, and of still miles in diameter. more stupendous dimensions, is delineated in fig. 1, Plate IV., as seen with high magnifying powers. This remarkable object consists of two enormous circular chains of mountains; the lesser, which lies to the north. measuring 164 miles in diameter, and the greater, lying to the south, enclosing an area 60 miles in diameter. The area enclosed by the former is therefore 214, and by the latter 2,827 square miles. The height of the lesser chain is about 10,000 feet, while that of the greater varies from 3.300 to 5,000 feet. The vast area thus enclosed by the greater chain includes at or near its centre, a principal central mountain, having eight peaks and a height of 2,000 feet, while scattered over the surrounding enclosure upwards of a hundred mountains of less considerable elevation have been counted.

It is easy to see how little analogy to a terrestrial volcanic crater is presented by these characters.

The preceding selections, combined with the charts, Plates I, IL,



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and the second second second

III, and IV, will serve to show the general physical character of the lunar surface, and the elaborate accuracy with which it has been submitted to telescopic examination. In the work of Beer and Madler, a table of the heights of above 1000 mountains is given, several of which attain to an elevation of 28,000 feet, equal to that of the highest summits of terrestrial mountains, while the diameter of the moon is little more than one fourth that of the earth.

2491. Observations of Herschel.—Sir John Herschel says, that among the lunar mountains may be observed in its highest perfection the true volcanic character, as seen in the crater of Vesuvius and elsewhere; but with the remarkable peculiarity that the bottoms of may of the craters are very deeply depressed below the general sarface of the moon, the internal depth being in many cases two or three times the external height. In some cases, he thinks, decisive marks of volcanic stratification, arising from a succession of deposits of ejected faatter, and evident indications of currents of lava straming outwards in all directions, may be clearly traced with powerful telescopes.

2492. Observations of the Earl of Rosse. — By means of the great reflecting telescope of Lord Rosse, the flat bottom of the enter called Albateguius is distinctly seen to be strewed with blocks, set visible with less powerful instruments; while the exterior of mother (Aristillus) is intersected with deep gullies radiating from

is centre.

2493. Supposed influence of the moon on the weather.—Among the many influences which the moon is supposed, by the world in general, to exercise upon our globe, one of those, which has been not universally believed, in all ages and in all countries, is that which it is presumed to exert upon the changes of the weather. Although the particular details of this influence are sometimes pretended to be described, the only general principle, or rule, which nevails with the world in general is, that a change of weather may be looked for at the epochs of new and full moon: that is to say, if the weather be previously fair it will become foul, and if foul will become fair. Similar changes are also, sometimes, though not so confidently, looked for at the epochs of the quarters.

A question of this kind may be regarded either as a question of

science, or a question of fact.

If it be regarded as a question of science, we are called upon to explain how and by what property of matter, or what law of nature or attraction, the moon, at a distance of a quarter of a million of miles, combining its effects with the sun, at four hundred times that distance, can produce those alleged changes. To this it may be readily answered that no known law or principle has hitherto explained any such phenomena. The moon and sun must, doubtless, affect the ocean of air which surrounds the globe, as they affect the

observe the phenomena of the changes of put them in juxtaposition with the conten lunar phases. If there be any discoverab becomes a question of physics to assign its

Such a course of observation has been tories with all the rigour and exactitude quiry, and has been continued over periods to efface all conceivable effects of accidental

We can imagine, placed in two parallel co the series of epochs of the new and full me and the corresponding conditions of the weat fifty or one hundred years back, so that we a amine, as a mere matter of fact, the conditione thousand or twelve hundred full and nev

From such a mode of observation and inquiculsively that the popular notions concerning lunar phases on the weather have no foundat correspondence with observed facts. That the tation, exerts an attraction on our atmosphere but the effects which that attraction would program not in accordance with observed phenoic these effects are either too small in amount to actual state of meteorological instruments, or by other more powerful causes, from which been eliminated. It appears, however, by see time, that a slight correspondence

exally entertained even in countries remote from each other, as at which presumes an influence of the moon over the changes of a weather, will do well to remember that against that opinion we see not here opposed mere theory. Nay, we have abandoned for a occasion the support that science might afford, and the light it ight ahed on the negative of this question, and have dealt with it a mere question of fact. It matters little, so far as this question concerned, in what manner the moon and sun may produce an fact on the weather, nor even whether they be active causes in orducing such effect at all. The point, and the only point of immance, is, whether, regarded as a mere matter of fact, any corspondence between the changes of the moon and those of the eather exists? And a short examination of the recorded facts roves that IT DOES NOT.

2494. Other supposed lunar influences.—But meteorological pheomena are not the only effects imputed to our satellite; that body, ke comets, is made responsible for a vast variety of interferences rith organised nature. The circulation of the juices of vegetables, he qualities of grain, the fate of the vintage, are all laid to its account; and timber must be felled, the harvest cut down and gathered a, and the juice of the grape expressed, at times and under circumstances regulated by the aspects of the moon, if excellence be upped for in these products of the soil.

According to popular belief, our satellite also presides over human maladies; and the phenomena of the sick chamber are governed by he lunar phases; nay, the very marrow of our bones, and the weight our bodies, suffer increase or diminution by its influence. Nor a its imputed power confined to physical or organic effects; it noto-

iously governs mental derangement.

If these opinions respecting lunar influences were limited to parisular countries, they would be less entitled to serious consideration; at it is a curious fact that many of them prevail and have prevailed in quarters of the earth so distant and unconnected, that it is lifficult to imagine the same error to have proceeded from the same parce.

Our limits, and the objects to which this volume is directed, ender it impossible here to notice more than a few of the principal physical and physiological influences imputed to the moon; nor even with respect to these can we do more than indicate the kind of exmination to which they have been submitted, and the conclusions which have been deduced from it.

2495. The red moon.—Gardeners give the name of Red Moon that moon which is full between the middle of April and the close of May. According to them the light of the moon at that season exercises an injurious influence upon the young shoots of plants. They say that when the sky is clear the leaves and buds

rne sky be clouded, their temperature is ma above stated.

The moon, therefore, has no connection whand it is certain that plants would suffer un stances whether the moon is above or below it is quite true that if the moon be above the hor suffer unless it be visible; because a clear at much to the production of the injury to the bility of the moon; and, on the other hand, the veil the moon and intercept her light give bac warmth which prevents the injury here adverte opinion is therefore right as to the cffect, but we and its error will be at once discovered by show night, when the moon is new, and, therefore, no may nevertheless suffer.

2496. Supposed influence on timber. — An a centertained that timber should be felled only due the moon; for if it be cut down during its increase of a good and durable quality. This impression countries. It is acted upon in England, and is a legislation in France. The forest laws of the diet the cutting of timber during the increase same opinion prevails in Brazil. Signor France ment agriculturist in the province of Espirito Sarresult of his experience, that the wood which was full of the moon was immediately attacked by wrotted. In the extensive forests of Germany intertained and acted was

The increase or decrease of the moon has no appreciable influence on the phenomena of vegetation; and the experiments and observations of several French agriculturists, and especially of M. Duhamel du Monceau (already alluded to) have clearly established this.

2498. Supposed lunar influence on wine-making.—It is a maxim of wine-growers, that wine which has been made in two moons is

never of a good quality, and cannot be clear.

To this we need only answer, that the moon's rays do not affect the temperature of the air to the extent of one thousandth part of a degree of the thermometer, and that the difference of temperatures of any two neighbouring places in which the process of making the wine of the same soil and vintage might be conducted, may be a thousand times greater at any given moment of time, and yet no one ever imagines that such a circumstance can affect the quality of the wine.

2499. Supposed lunar influence on the complexion. — It is a prevalent popular notion in some parts of Europe, that the moon's light is attended with the effect of darkening the complexion.

That light has an affect upon the colour of material substances is a fact well known in physics and in the arts. The process of bleaching by exposure to the sun is an obvious example of this class of facts. Vegetables and flowers which grow in a situation excluded from the light of the sun are different in colour from those which have been exposed to its influence. The most striking instance, however, of the effect of certain rays of solar light in blackening a light-coloured substance, is afforded by chloride of silver, which is a white substance, but which immediately becomes black when acted upon by the rays near the red extremity of the spectrum. substance, however, highly susceptible as it is of having its colour affected by light, is, nevertheless, found not to be changed in any sensible degree when exposed to the light of the moon, even when that light is condensed by the most powerful burning lenses. would seem, therefore, that as far as any analogy can be derived from the qualities of this substance, the popular impression of the influence of the moon's rays in blackening the skin receives no support.

2500. Supposed lunar influence on putrefaction. — Pliny and Plutarch have transmitted it as a maxim, that the light of the moon facilitates the putrefaction of animal substances, and covers them with moisture. The same opinion prevails in the West Indies, and in South America. An impression is prevalent, also, that certain kinds of fruit exposed to moonlight lose their flavour and become soft and flabby; and that if a wounded mule be exposed to the light of the moon during the night, the wound will be irritated, and

frequently become incurable.

ASTRONOMY.

effects, if real, may be explained upon the same pr by which we have already explained the effects imp noon. Animal substances exposed to a clear sky a to receive a deposition of dew, which humidity ha accelerate putrefaction. But this effect will be 1 y be clear, whether the moon be above the horizon n, therefore, in this case, is a witness and not ar nust acquit her of the misdeeds imputed to her. sed lunar influence on shell-fish. - It is a very an at oysters and other shell-fish become larger during an during the decline of the moon. This maxim the poet Lucilius, by Aulus Gellius, and others: of the academy del Cimento appear to have tacitly nce they endeavour to give an explanation of it. has been carefully examined by Rohault, who I ell-fish taken at all periods of the lunar month, an exhibit no difference of quality.

Supposed lunar influence on the marrow of ani on is prevalent among the butchers that the marrones of animals varies in quantity according to the poor in which they are slaughtered. This ones

new. In France it is a maxim generally adopted, that the hetter and more successfully reared when they break the the full of the moon. The experiments and observations irou de Buzareingues have given countenance to this opinut such observations require to be multiplied before the an be considered as established. M. Girou inclines to the that during the dark nights about new moon the hens sit so bed that they either kill their young or check their develby too much heat; while in moonlight nights, being more this effect is not produced.

Supposed lunar influence on mental derangement and man maladies. — The influence on the phenomena of human imputed to the moon is very ancient. Hippocrates had so faith in the influence of celestial objects upon animated that he expressly recommends no physician to be trusted gnorant of astronomy. Galen, following Hippocrates, mainhe same opinion, especially of the influence of the moon n diseases the lunar periods were said to correspond with the a of the sufferings of the patients. The critical days or s they were afterward called), were the seventh, fourteenth, enty-first of the disease, corresponding to the intervals bene moon's principal phases. While the doctrine of alchymrailed, the human body was considered as a microcosm; the presenting the sun, the brain the moon. The planets had proper influence: Jupiter presided over the lungs, Mars : liver, Saturn over the spleen, Venus over the kidneys, and y over the organs of generation. Of these grotesque noiere is now no relic, except the term lunacy, which still tes unsoundness of mind. But even this term may in some be said to be banished from the terminology of medicine, ias taken refuge in that receptacle of all antiquated absurdiphraseology — the law. Lunatic, we believe, is still the r the subject who is incapable of managing his own affairs. ough the ancient faith in the connection between the phases moon and the phenomena of insanity appears in a great to be abandoned, yet it is not altogether without its votaries; e we been able to ascertain that any series of observations ed on scientific principles has ever been made on the phenoof insanity, with a view to disprove this connection. We ven met with intelligent and well-educated physicians who intain that the paroxysms of insane patients are more violent be moon is full than at other times.

i. Examples produced by Faber and Ramazzini. — Ma-Faber gives an instance of a maniac who, at the very mof an eclipse of the moon, became furious, seized upon a and fell upon every one around him. Ramazzini relates ıs evident I س رـــ س

have been recorded.

At no very distant period from that time, in related that patients in considerable numbers we physicians, shut up in chambers well closed, warr with a view to escape the injurious influence of which happened at that time; and such was the persons of all classes, that the numbers who flowere so great that the ecclesiastics found it impost that rite. An amusing ancedote is related of a variety, who, with a view to case the minds of his the necessary time to get through his business, them that the eclipse was postponed for a fortnight

2507. Examples of Vallishieri and Bacon.—remarkable examples recorded, of the supposed moon on the human body, are those of Vallishieri lishieri declares that, being at Padua, recovering illness, he suffered, on the 12th of May, 1706, d of the sun, unusual weakness and shivering. Lun happened without making Bacon faint; and he di senses till the moon recovered her light.

That these two striking examples should be adm the existence of lunar influence, it would be no Arago, to establish the fact, that feebleness and character are never connected with high qualities o

2508. Supposed influence on culaneous affectionsidered that cutaneous maladies had a manifest the lunar phases. He says that he himself obsci 1760, a patient afflicted with a scale head in the says that he had a manifest that he had a m

etween the lunar phases and the distemper of the itch; but the reumstances were the reverse of those in the former case; the alady attaining its maximum at the full of the moon, and its inimum at the new moon.

Without disputing the accuracy of these statements, or throwing y suspicion on the good faith of the physician who has made em, we may observe that such facts prove nothing except the relatious coincidence. If the relation of cause and effect had risted between the lunar phases and the phenomena of these dismpers, the same cause would have continued to produce the same fact in like circumstances; and we should not be left to depend rethe proof of lunar influence on the statements of isolated cases, curring under the observation of a physician who was himself a slience.

2509. Remarkable case adduced by Hoffman. — Maurice Hoffman relates a case which came under his own practice, of a young oman, the daughter of an epileptic patient. The abdomen of this irl became inflated every month as the moon increased, and regurly resumed its natural form with the decline of the moon.

Now, if this statement of Hoffman were accompanied by all the conservy details, and if, also, we were assured that this strange first continued to be produced for any considerable length of time, he relation of cause and effect between the phases of the moon at the malady of the girl could not legitimately be denied; but receiving the statement in so vague a form, and not being assured at the effect continued to be produced beyond a few months, the gitimate conclusion at which we must arrive is, that this is another nample of fortuitous coincidence, and may be classed with the fullment of dreams, prodigies, &c., &c.

2510. Cases of nervous diseases. - As may naturally be exected, nervous diseases are those which have presented the most requent indications of a relation with the lunar phases. The celerated Mead was a strong believer, not only in the lunar influence, ut in the influence of all the heavenly bodies on all the human. le cite the case of a child who always went into convulsions at the noment of full moon. Pyson, another believer, cites another case f a paralytic patient whose disease was brought on by the new Menuret records the case of an epileptic patient whose fits eturned with the full moon. The transactions of learned societies bound with examples of giddiness, malignant fever, somnambusm, &c., having in their paroxysms more or less corresponded with he lunar phases. Gall states, as a matter having fallen under his wn observation, that patients suffering under weakness of intellect ad two periods in the month of peculiar excitement; and, in a fork published in London so recently as 1829, we are assured that hese epochs are between the new and full moon.

directed his attention to this question, excepcelebrated for his discovery of the planets states that, in the course of a long medical able to discover the slightest trace of any ophenomena of disease and the phases of the

d traffic me . delle

2512. Influence not to be hastily rejected. philosophy, M. Arago, nevertheless, recommen against this influence. The nervous system, t stances an instrument infinitely more delicate apparatus of modern physics. Who does not tory nerves inform us of the presence of odo the traces of which the most refined physical detect? The mechanism of the eye is hig lunar light which, even condensed with all the burning lenses, fails to affect by its heat the n mometers, or by its chemical influence, the ch a small portion of this light introduced throug sufficient to produce an instantiateous contra nevertheless, the integuments of this ment light, appear to be completely fact when the pupil remains unmoved, whether we scrape it needle, moisten it with liquid acids, or impart sparks. The retina itself, which sympathises insensible to the influence of the most active Phenomena so mysterious should teach us w should reason on analogies drawn f---animate ---1

CHAP. X.

THE TIDES AND TRADE WINDS.

2513. Correspondence between the recurrence of the tides, and the diurnal appearance of the moon. — The phenomena of the tides of the ocean are too remarkable not to have attracted notice at an early period in the progress of knowledge. The intervals between the epochs of high and low water everywhere corresponding with the intervals between the passage of the moon over the meridian above and below the harmon, suggested naturally the physical connection between these two effects, and indicated the probability of the cause of the tides being spund in the motion of the moon.

2514. Erestions notions of the lunar influence. - There are few subjects in physical science about which more erroneous notions repair among those who are but a little informed. A common in, that the attraction of the moon draws the waters of the toward that side of the gibbs on which it happens to be placed, it that consequently they are nearly up on that side, so that the man and seek acquire there a greater depth than elsewhere; and that high water will thus take place under, or nearly under, the moon. But this does not correspond with the fact. High water is not prodeced merely under the moon but is equally produced upon those most removed from the moon. Suppose a meridian of the eirth so selected, that if it were continued beyond the earth, its than yould past through the moon; we find that, subject to certain modifications, a great sidal wave, or what is called high water, will be formed on both sides of this meridian; that is to say, on the side next the moon, and on the side remote from the moon. As the moon moves, these two great tidal waves follow her. They are of course separated from each other by half the circumference of the As the globe revolves with its diurnal motion upon its axis, every part of its surface passes successively under these tidal waves; and at all such parts, as they pass under them, there is the phenomenon of high water. Hence it is that in all places there are two tides daily, having an interval of about twelve hours between them. Now, if the common notion of the cause of the tides were well founded, there would be only one tide daily-viz., that which would take place when the moon is at or near the meridian.

2515. The moon's attraction alone will not explain the tides.—
That the moon's attraction upon the earth simply considered would not explain the tides is easily shown. Let us suppose that the

position as if they were not attracted at all.

2516. Tides caused by the difference of the ferent parts of the earth. — When we observe composed of various particles of matter, that ment of these particles is disturbed, some be directions more than others, the inference is, parts of such a mass must be placed under the forces; those which tend more than others in being driven with a proportionally greater force with the earth, placed under the attraction of the is, in fact, what must happen under the operation of the distance increases.

Let A, B, C, D, E, F, G, H, fig. 781, representerth, and, to simplify the explanation, let us first

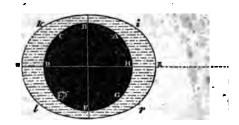


Fig. 731.

which it exercises at A and G, and still greater than that which it produces at B and F; and the attraction which it exercises at D is least of all. Now this attraction equally affects matter in every state and condition. It affects the particles of fluid as well as solid matter; but there is this difference, that where it acts upon solid matter, the component parts of which are at different distances from it, and therefore subject to different attractions, it will not disturb the relative arrangement, since such disturbances or disarrangements are prevented by the cohesion which characterises a solid body; but this is not the case with fluids, the particles of which are mobile.

The attraction which the moon exercises upon the shell of water, which is collected immediately under it near the point z, is greater than that which it exercises upon the solid mass of the globe; consequently there will be a greater tendency of this attraction to draw the fluid which rests upon the surface at H toward the moon, than to draw the solid mass of the earth which is more distant.

As the fluid, by its nature, is free to obey this excess of attraction, it will necessarily heap itself up in a pile or wave, over H, forming a convex protuberance, as represented between r and i. Thus high water will take place at H, immediately under the moon. The water which thus collects at H will necessarily flow from the regions B and F, where therefore there will be a diminished quantity in the same proportion.

But let us now consider what happens to that part of the earth D. Here the waters, being more remote from the moon than the solid mass of the earth under them, will be less attracted, and consequently will have a less tendency to gravitate toward the moon. The solid mass of the earth, DH, will, as it were, recede from the waters at n, in virtue of the excess of attraction, leaving these waters behind it, which will thus be heaped up at n, so as to form a convex protuberance between I and k, similar exactly to that which we have already described between r and i. As the difference between the attraction of the moon on the waters at z and the solid earth under the waters is nearly the same as the difference between its attraction on the latter and upon the waters at n, it follows that the height of the fluid protuberances at z and n are equal. In other words, the heights of the tides on opposite sides of the earth, the one being under the moon and the other most remote from it, are equal.

It appears, therefore, that the cause of the tides, so far as the action of the moon is concerned, is not, as is vulgarly supposed, the mere attraction of the moon; since, if that attraction were equal on all the component parts of the earth, there would assuredly be no tides. We are to look for the cause, not in the attraction of the moon, but in the inequality of its attraction on different parts of the earth. The greater this inequality is, the greater will be the

bestow on these observations a little reflection have stated in reference to the effects produced the moon upon the earth, will also be applicable the sun. This is undoubtedly true; but in the effects are modified in some very important resp 400 times a greater distance than the moon, and of its attraction on the earth would, on that s times less than that of the moon; but the mass that of the moon in a much greater ratio than th It therefore possesses a much greater attracting its mass compared with the moon, than it loses tance. It exercises, therefore, upon the earth mously greater than the moon exercises. Now, it of its attraction were, as is commonly supposed tides, the sun ought to produce a vastly greater t The reverse is, however, the case, and the cause Let it be remembered that the tides are due sole of the attraction on different sides of the earth, a inequality is, the greater will be the tides, and equality is, the less will be the tides.

In the case of the sun, the total distance is 1: the earth, and consequently the difference between the one side and the other of the earth will be part of the whole distance, while in the case of i distance being only 30 diameters of the earth, the tauces from one side and the other is the 30th distance. The inequality of the attraction, upor not on its whole amount the production.

same side of the earth, or on the opposite sides of the earth er words, when it is new or full moon - their effects in protides are combined, and the spring tide is produced, the of which is equal to the solar and lunar tides taken together. the other hand, when the sun and moon are separated from ther by a distance of one fourth of the heavens, that is, when oon is in the quarters, the effect of the solar tide has a tento diminish that of the lunar tide.

tides produced by the combination of the lunar and solar tide at the time of new and full moon are called SPRING TIDES; some produced by the lunar wave diminished by the effect of

lar wave at the quarters are called NEAP TIDES.

9. Why the tides are not produced directly under the moon. physical effects followed immediately, without any appreciable al of time, the operation of their causes, then the tidal wave sed by the moon would be on the meridian of the earth directly and opposite to that luminary; and the same would be true of lar tides. But the waters of the globe have, in common with ner matter, the property of inertia, and it takes a certain inof time to impress upon them a certain change of position. it follows that the tidal wave produced by the moon is not d immediately under that body, but follows it at a certain dis-

In consequence of this, the tide raised by the moon does not place for two or three hours after the moon passes the meridian; the action of the sun is still more feeble, there is a still r interval between the transit of the sun and occurrence of the

20. Priming and lagging of the tides.—But besides these ate effect of either of these bodies, but to the combined effect th, that the effects are due; and at every period of the month, me of actual high water is either accelerated or retarded by the

In the first and third quarters of the moon, the solar tide is rard of the lunar one; and, consequently, the actual high water, h is the result of the combination of the two waves, will be to restward of the place it would have if the moon acted alone, the time of high water will therefore be accelerated. In the d and fourth quarters the general effect of the sun is, for a ar reason, to produce a retardation in the time of high water. effect, produced by the sun and moon combined, is what is nonly called the priming and lagging of the tides. The highest g tides occur when the moon passes the meridian about an hour the sun; for then the maximum effect of the two bodies ides.

21. Researches of Whewell and Lubbock. - The subject of ides has of late years received much attention from several scipoints connected with these questions.

2522. Vulyar and corrected establishment. of high water at any port in the afternoon of moon, is what is usually called the establishme fessor Whewell calls this the vulgar establishment corrected establishment the mean of all the inte transit of half a month. This corrected est quently the luni-tidal interval corresponding the moon passes the meridian at noon or midni

the moon passes the meridian at noon or midni 2523. Diurnal inequality. — The two tides i one another, or the tides of the day and night. and time of high water at any particular place, the sun and moon from the equator. As the ve always tends to place itself vertically under the duces it, it is evident that of two consecutive tide when the moon is nearest the zenith or nadir the other; and, consequently, when the moon's same denomination as the latitude of the place. responds to the upper transit will be greater th and vice versa, the difference being greatest whe are in opposition, and in opposite tropics. NAL INEQUALITY, because its cycle is one day; at different places, and its laws, which appear local circumstances, are very imperfectly known

2524. Local effects of the land upon the tid described the principal phenomena that would earth a sphere, and covered entirely with a fluid But the actual phenomena of the tides are int

ly covered with water, the summit of the tide wave, being governed by the moon, would everywhere follow the moon's at the same interval of time, and consequently travel round :h in a little more than twenty-four hours. But the circumof the earth at the equator being about 25,000 miles, the of propagation would therefore be about 1,000 miles per The actual velocity is, perhaps, nowhere equal to this, and is fferent at different places. In latitude 60° south, where no interruption from land (excepting the narrow promontory gonia), the tide wave will complete a revolution in a lunar d consequently travel at the rate of 670 miles an hour. On ing Mr. Whewell's map of cotidal lines, it will be seen that at tide wave from the Southern Ocean travels from the Cape d Hope to the Azores in about twelve hours, and from the to the southermost part of Ireland in about three hours more. Atlantic, the hourly velocity in some cases appears to be 10° , or near 700 miles, which is almost equal to the velocity of through the air. From the south point of Ireland to the point of Scotland, the time is eight hours, and the velocity 160 miles an hour along the shore. On the eastern coast of , and in shallow water, the velocity is less. From Buchan-Sunderland it is about 60 miles an hour; from Scarborough mer, 35 miles; from the North Foreland to London, 30 from London to Richmond, 13 miles an hour in that part of er. (Whewell, Phil. Trans. 1833 and 1836.) It is scarcely by to remind the reader that the above velocities refer to the ission of the undulation, and are entirely different from the of the current to which the tide gives rise in shallow water. Range of the tides. - The difference of level between nd low water is affected by various causes, but chiefly by the aration of the land, and is very different at different places. p inbends of the shore, open in the direction of the tide wave radually contracting like a funnel, the convergence of water a very great increase of the range. Hence the very high in the Bristol Channel, the Bay of St. Malo, and the Bay of r. where the tide is said to rise sometimes to the height of one ed feet. Promontories, under certain circumstances, exert an ite influence, and diminish the magnitude of the tide. red ranges are also very anomalous. At certain places on the east coast of Ireland, the range is not more than three feet. at a little distance on each side it becomes twelve or thirteen and it is remarkable that these low tides occur directly opposite bristol Channel, where (at Chepstow) the difference between and low water amounts to sixty feet. In the middle of the c it amounts to only two or three feet. At London Docks, verage range is about 22 feet; at Liverpool, 15.5 feet; at 20

__ _ LUBUUR LOCKS, a fall of one-tenth (to a rise in the Thames of about seven-tenths low barometer, therefore, the tide may be exp vice versa. The tide is also liable to be disti John Lubbock states that, in the violent hur 1839, there was no tide at Gainsborough, which up the Trent—a circumstance unknown before five miles up the Ouse from the Humber, the and never flowed until the river was dry in sc Ostend, toward which the wind was blowing, observed. During strong north-westerly gales water earlier in the Thames than otherwise, a much water, while the ebb tide runs out late, at upon the gales abating and weather moderating, rise much higher, while they also run longer marked, and with more velocity of current: nor long or so low.

2528. The trade winds. — The great atmosp denominated, from the advantages which navi from them, as well as other currents arising from them, as well as other currents arising from the produced by the unequal exposure of the which coats the terrestrial globe, to the action expansion and contraction that air, in common bodies, suffers from increase and diminution of tendency which lighter fluids have to rise through the rotation of the earth upon its axis.

The regions in which the TRADES prevail are belts extending through a certain limited numb and south of the limited numb ial equator, is vertical daily to different points around the troregions, the rotation of the earth bringing these points succesunder his disk. The sun, at noon, for places within the s, is never so much as 231° from the zenith. The intertropical from these causes becomes much more intensely heated upon face than the parts of either hemisphere at higher latitudes. heat, reflected and radiated upon the incumbent atmosphere, it to expand and become specifically lighter, and it ascends ske and heated air do in a chimney. The space it deserts is by colder and therefore heavier air, which rushes in from the r parts of either hemisphere; while the air thus displaced, by its buoyancy above its due level, and unsustained by any l pressure, flows down towards either pole, and, being cooled course and rendered heavier, it descends to the surface of the at those upper latitudes from which the air had been sucked rards the line by its previous ascent.

constant circulation and an interchange of atmosphere between itertropical and extratropical regions of the earth would thus place, the air ascending from the intertropical surface and flowing towards the extratropical regions, where it descends to

irface to be again sucked towards the line.

t in this view of the effects, the rotation of the earth on its s not considered. In that rotation the atmosphere participates. air which rises from the intertropical surface carries with it elocity of that surface, which is at the rate of about 1,000 miles our from west to east. This velocity it retains to a considerable t after it has passed to the higher latitudes and descended to prface, which moving with much less velocity from west to mere is an effective current produced in that direction equivathe excess of the eastward motion of the air over the eastward n of the surface of the earth. Hence arises the prevalent rard winds, especially at sea, where causes of local disturbance not frequent, which are so familiar, and one of the effects of h has been, that, while the average length of the trip of good g vessels from New York to Liverpool has been only twenty. that of the trip from Liverpool to New York has been thirtylavs.

r the friction of the earth and other causes, the air, however, the surface, at length acquires a common velocity with it, and it is, as above described, sucked towards the line to fill the num produced by the air drawn upwards by the solar heat, it is with it the motion from west to east which it had, in common the surface, at the higher latitudes. But the surface at the has a much greater velocity than this from west to east. The ce, therefore, and all objects upon it, are carried against the rith the relative velocity of the surface and the air, that is to

ASTRONOMY.

the effect of the difference of their velocities. Since the nd the objects upon it, are carried eastward at a much ste than the air which has just descended from the higher they will strike against the air with a force proportional to ence of their velocities, and this force will have a direction to that of the motion of the surface, that is to say, from est.

must be considered that this eastward force, due to the fithe earth's surface, is combined with the force with which moves from the extratropical regions towards the line, the northern hemisphere, the force eastward is combined motion of the air from north to south, and the resultant forces is that north-east current which actually prevails; I like reasons, south of the line, the motion of the air from north, being combined with the force eastward, produces eastern current which prevails south of the line.

any considerable mass of air, as Sir J. Herschel observes, idenly transferred from beyond the tropics to the equator, rence of the rotary velocities proper to the two situations as ogreat, as to produce, not merely a wind, but a tempest ost destructive violence; and the same observation would

CHAP. XI

THE SUN.

2529. Apparent and real magnitude. — Owing to the ellipticity of the earth's orbit, the distance of the sun is subject to a periodical variation, which causes, as has been already explained, a corresponding variation in its apparent magnitude. Its greatest apparent diameter, when in perihelion, is 32' 35".6, or 1955".6, and its least apparent magnitude, when in aphelion, is 31' 30", or 1890". Its mean apparent diameter is therefore 1923".

It has been already (2457) shown that the linear value of 1" at the sun's distance is 466 miles. It follows, therefore, that the actual length of the diameter of the globe of the sun is

 $1923 \times 466 = 896.118$ miles.

The real magnitude of the sun may also be easily inferred in round numbers from that of the moon. The apparent diameter of the moon being equal in round numbers to that of the sun, and the diameter of the sun being 400 times greater than that of the moon, it follows that the real diameter of the sun must be 400 times greater than that of the moon. It must, therefore, be

 $2153 \times 400 = 861,200$ miles.

By methods of calculation susceptible of closer approximation than them, it has been found that the magnitude is 882,000 miles, or

1117 times the diameter of the earth.

2530. Magnitude of the sun illustrated. — Magnitudes such as that of the sun so far transcend all standards with which the mind is familiar, that some stretch of imagination, and some effort of the understanding, are necessary to form a conception, however imperfect, of them. The expedient which best serves to obtain some adequate idea of them is, to compare them with some standard, stupendous by comparison with all ordinary magnitudes, yet minute when compared with them.

The earth itself is a globe 8000 miles in diameter. If the sun be represented by a globe nine feet four inches in diameter, the earth would be represented by a globe an inch in diameter. If the orbit of the moon, which measures 474,000 miles in diameter, were filled by a sun, such a sun might be placed within the actual sun, leaving between their surfaces a distance of 200,000 miles. Such a sun, seen from the earth, would have an apparent diameter little

more than balf the diameter of the actual sun.

'redth part the globe of the sun: in other w in is five hundred times greater than the agg rest of the bodies of the system.

2532. Its mass and density. — By methor observation, which will be explained hereafter, of matter composing the globe of the sun, to composing the earth, has been ascertained to b

By comparing this proportion of the qua matter in the sun and earth with their relative vident that the mean density of the matter must be about four times less than the mean decomposing the earth; for although the volume that of the earth in the ratio of 1,400,000 to 1 exceeds that of the earth in the lesser ratio of latter ratio being four times less than the form therefore, the sun is four times lighter than the

Since the mean density of the earth is 5.67 (2393), it follows that the mean density of the about one half, greater than that of water.

From the comparative lightness of the matter schel infers the probability that an intense heat rior, by which its elasticity is reinforced, and a resisting the almost inconceivable pressure due t tation, without collapsing into smaller dimension

2533. Form and rotation—axis of rotation minds unaccustomed to the rigour of scientific repear sufficiently evident, without further '

ove, then, that a body is globular, something more is necessary an the mere fact that it always appears circular.

When a telescope is directed to the sun, we discover upon it cerin marks or spots, of which we shall speak more fully presently. e observe that these marks, while they preserve the same relative sition with respect to each other, move regularly from one side of e sun to the other. They disappear, and continue to be invisible ra certain time, come into view again on the other side, and so see more pass over the sun's disk. This is an effect which would idently be produced by marks on the surface of a globe, the glob elf revolving on an axis, and carrying these marks upon it. Thus is is the case, is abundantly proved by the fact that the periods of tation for all these marks are found to be exactly the same, viz., out twenty-five days and a quarter, or more exactly 25d. 7h. 48m. sch is, then, the time of rotation of the sun upon its axis, and at it is a globe remains no longer doubtful, since a globe is the ly body which, while it revolves with a motion of rotation, would ways present the circular appearance to the eye. The axis on hich the sun revolves is very nearly perpendicular to the plane of e earth's orbit, and the motion of rotation is in the same direction the motion of the planets round the sun, that is to say, from west gast.

2534. Spots. — One of the earliest fruits of the invention of the except was the discovery of the spots upon the sun; and the eximation of these has gradually led to some knowledge of the yaical constitution of the centre of attraction and the common patrin of light and heat of our system.

when we submit a solar-spot to telescopic examination, we district its appearance to be that of an intensely black irregularly sped patch, edged with a penumbral fringe. When watched for considerable time, it is found to undergo a gradual change in its rm and magnitude; at first increasing gradually in size, until it tains some definite limit of magnitude, when it ceases to increase, it soon begins, on the contrary, to diminish; and its diminution as on gradually, until at length, the bright sides closing in upon a dark patch, it dwindles first to a mere point, and finally disapars altogether. The period which elapses between the formation the spot, its gradual enlargement, subsequent diminution, and tal disappearance, is very various. Some spots appear and disappear very rapidly, while others have lasted for weeks and even for onths.

The magnitude of the spots, and the velocities with which the atter composing their edges and fringes moves, as they increase ad decrease, are on a scale proportionate to the dimensions of the bof the sun itself. When it is considered that a space upon the

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the apparent breadth of which was 90", was close in about 40 days. Now, the actual line a spot must have been

 $466 \times 90 = 41,940$ mile

and consequently, the average daily motion of its edges must have been 1050 miles, a velc miles an hour.

2535. Cruse of the spots — physical state Two, and only two, suppositions have been prospots. One supposes them to be scorize, or d bustible matter, floating on the general surfact other supposes them to be excavations in the lacoats the sun, the dark part of the spot being non-luminous nucleus of the sun. In this is assumed that the sun is a solid non-luminous geometring of a certain thickness of luminous matter.

That the spots are excavations, and not mere surface, is proved by the following observations which is at the centre of the sun's disk, having such as that of a circle, and watch its changes oby the rotation of the sun, it is carried toward first, that the circle becomes an oval. This, ho be expected, even if the spot were a circular p circle seen obliquely is foreshortened into an that as the spot moves toward the side of the supatch gradually disappears, the penumbral fring the spot becomes invisible while the

surface of the inner shelving side also taking the direction of ne of vision or very nearly, diminishes in apparent breadth, cases to be visible, while the surface of the shelving side next ige of the sun becoming nearly perpendicular to the line of appears of its full breadth.

short, all the variations of appearance which the spots undergo, cy are carried round by the rotation of the sun, changing distances and positions with regard to the sun's centre, are ly such as would be produced by an excavation, and not at all

as a dark patch on the solar surface would undergo.

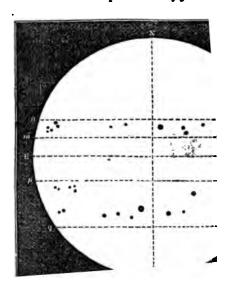
86. Sun invested by two atmospheres, one luminous and the non-luminous. — It may be considered, then, as proved, that pots on the sun are excavations; and that the apparent blackis produced by the fact, that the part constituting the dark in of the spot is either a surface totally destitute of light, or imparison so much less luminous than the general surface of un as to appear black. This fact, combined with the appearoff the penumbral edges of the spots, has led to the suppositude by Sir W. Herschel, which appears scarcely to admit subt, that the solid, opaque nucleus, or globe of the sun, is sted with at least two atmospheres; that which is next the sun g, like our own, non-luminous, and the superior one being that in which light and heat are evolved; at all events, whether strats be in the gaseous state or not, the existence of two, one placed above the other, the superior one being luminous, as to be exempt from doubt.

37. Spots may not be black. — We are not warranted in astat that the black portion of the spots are surfaces really is d of light, for the most intense artificial lights which can be used, such, for example, as that of a piece of quick-lime exd to the action of the compound blow-pipe, when seen projected he sun's disk, appear as dark as the spots themselves; an effect the must be ascribed to the infinitely superior splendour of the slight. All that can be legitimately inferred respecting the s, then, is, not that they are destitute of light, but that they incomparably less brilliant than the general surface of the sun. 538. Spots variable. — The prevalence of spots on the sun's is both variable and irregular. Sometimes the disk will be pletely divested of them, and will continue so for weeks or iths; sometimes they will be spread over certain parts of it in usion. Sometimes the spots will be small, but numerous;

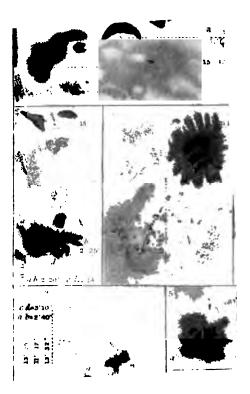
The duration of each spot is also subject to great and irregular intion. A spot has appeared and vanished in less than twenty-

etimes individual spots will appear of vast extent; sometimes will be manifested in groups, the penumbræ or fringes being in

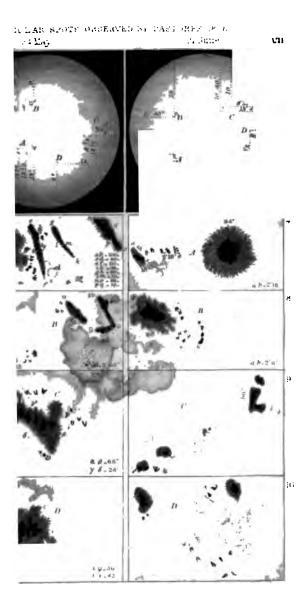
separated from it by a space several degraquator itself, and this space which thus sones, are absolutely divested of such phenc. Thus, for example, in the latter part of 1 of 1837, when a large number of spots 1 position was such as is represented in fig. 73:













subject, are M. Capocci, of Naples, Dr. Pastorff, of Frankfort (on the Oder), and Sir John Herschel.

M. Capocci made a series of observations on the spots which were developed on the sun's disk in 1826, when he recognised most of the characters above described. He observed that, during the increase of the spot from its first appearance as a dark point, the edges were sharply defined, without any indication of the gradually fading away of the fringes into the dark central spot, or into each other; a character which was again observed by Sir J. Herschel, in He found, however, that the same character was not maintained when the sides began to contract and the spots to diminish: during that process the edges were less strongly defined, being apparently covered by a sort of luminous atmosphere, which often extended so completely across the dark nucleus as to throw a thin thread of light across it, after which the spot soon filled up and disappeared. Capocci concurs with Sir W. Herschel in regarding the internal fringes surrounding the dark nucleus as the section of the inferior stratum of the atmosphere which forms the coating of the sun; he nevertheless thinks that there are indications of solid well as gaseous luminous matter.

Capocci also observed veins of more intensely luminous matter

Capocci also observed veins of more intensely luminous matter on the fringes converging towards the nucleus of the spot, which he compares to the structure of the iris surrounding the pupil of the

The drawings of the spots elicated by M. Capocci, given in Plate V., will illustrate these observations. It is to be regretted, however, that he has not given any measures, either in his memoirs or upon his drawings, by which the position or magnitude of the spots can be determined.

2541. Observations and drawings of Dr. Pastorff, in 1826. — Dr. Pastorff commenced his course of solar observations as early as 1819. He observed the spots which appeared in 1826, of which he published a series of drawings, from which we have selected those given in Plate VI., from observations made in September and October, contemporaneously with those of M. Capocci. Pastorff gives the position of all, and the dimensions of the principal spots. The numbers on the horizontal and vertical lines express the apparent distances of the spots severally from the limb of the sun in each direction. The actual dimensions may be estimated by observing that 1" measured at right angles to the visual ray represents 466 miles.

2542. Observations and drawings of Pastorff, in 1828.—In May and June, 1828, a profusion of spots were developed, which were observed and delineated by Pastorff with the most elaborate accuracy.

In Plate VII., fig. 1 represents the positions of the spots as

they appeared on the disk of the sun on the 24th of May, at 10 A.M., and figs. 2, 3, 4, and 5, represent their forms and magnitu The letters A, B, C, D, in fig. 1, give the positions of the spots marked by the same letters in figs. 2, 8, 4, and 5.

The dimensions of the principal spot of the group A were supendous; measured in a plane at right angles to the visual line, the length was $466 \times 100 = 46,600$ miles, and the breadth 466×60

= 27.960 miles.

The apparent breadth of the black bottom of the spot was 40", which corresponds to an actual breadth of $466 \times 40 = 18640$ miles. So that the globe of the earth might pass through such hole, leaving a distance of upwards of 5000 miles between its surface and the edges of the chasm.

The superficial dimensions of the several groups of spots observed on the sun on the 24th of May, at 10 A. M., including the shelving

sides, were calculated to be as follows:-

	Square Geog. Miles.
Group A, principal spot	928,000,000
Ditto, smaller spots	736,000,000
Group B	296,000,000
Group C	232,000,000
Group D	804,000,000
<u>.</u>	
Group D	309,000,000

2,496,000,000

Thus it appears that the principal spot of the group A covered a space equal to little less than we times the entire surface of the earth; and the total area compiled by all the spots collectively amounted to more than twelve times that surface.

On the days succeeding the 24th of they, all the spots were all the s

served to change their form and magnitude from day to day. The great spot of the group A, which even when so close to the limb of the sun as 5', or a sixth of the apparent diameter, still measured 80" by 40", was especially rapid in its variation. Its shelving sides as well as its dark bottom, were constantly varied, and luminous clouds were seen floating over the latter.

After the disappearance of this large spot, and several of the lesser ones of the other groups, a new spot of considerable magnitude made its appearance on the 13th of June, at the eastern edge of the disk, which gradually increased in magnitude for eight days. On the 21st of June, at half-past 9 in the morning, the disk of the sun exhibited the spots whose position is represented in fig. 6, Plat VII, and whose forms and magnitudes are indicated in figs. 7, 8,% and 10.

The chief spot of the group A was nearly circular, and measured 64" in apparent diameter, the diameter of its dark base being about 80", which, without allowing for projection, represent actual length of $466 \times 64 = 29,824$ miles, and $466 \times 80 = 13,980$ miles, where mer being above 31 times, and the latter nearly 12 times the th's diameter. The process of formation of this spot, surrounded luminous clouds, was clearly seen. The shelving sides were rersed by luminous ravines or rills, converging towards the centre the black nucleus, and exhibiting the appearance which Capocci spared to the structure of the iris.

In the same day (the 21st), another large spot, B, fig. 8, appeared, ich measured 60" by 40".

Pastorff rejects the supposition that these spots were the mere recarances of those which had been observed on the 24th of May, they differed essentially in their form, and still more in their

purage.

III.

2543. Observations of Sir J. Herschel in 1827. — Sir J. Herel, at the Cape of Good Hope, in 1837, observed the spots which that time appeared upon the sun, and has given various drawings them in his Cape Observations. These diagrams do not differ in respect in their general character from those of Capocci and Sir J. Herschel recognised on this occasion the striated radiated appearance in the fringes already noticed by Capocci and He thinks that this structure is intimately connected with s physical agency by which the spots are produced.

2544. Boundary of fringes distinctly defined. — It is observed Esir J. Herschel, that one of the most universal and striking efacters of the solar spots is, that the penumbral fringe and black ot are distinctly defined, and do not melt gradually one into the The spots are intensely black, and the penumbral fringe of perfectly uniform degree of shade. In some cases there are two nances of fringe, one lighter than the other; but in that case no thermixture or gradual fiding away of one into the other is apparant. "The idea conveyed," observes Sir J. Herschel, "is more est of the successive withdrawal of veils,—the partial removal of chaite films,—than the melting away of a mist or the mutual diluion of gaseous media." This absence of all graduation, this harply marked suddenness of transition, is, as Sir J. Herschel also otices, entirely opposed to the idea of the easy miscibility of the sminous, non-luminous, and semi-luminous constituents of the solar nvelope.

2545. Solar facules and lucules. - Independently of the dark spots just described, the luminous part of the solar disk is not uniformly bright. It presents a mottled appearance, which may be compared to that which would be presented by the undulated and agitated surface of an ocean of liquid fire, or to a stratum of luminous clouds of varying depth and having an unequal surface, or the appearance produced by the slow subsidence of some flocculent chemical precipitates in a transparent fluid, when looked at perpendicularly from above. In the space immediately around the edges

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luminous matter which coats the globe of

solid, liquid, or gaseous.

That it is not solid is admitted to be prextraordinary mobility, as indicated by the edges of the spots in closing; and it is copable of moving at the rate of 44 miles per to be liquid, an elastic fluid alone admitting 2547. Test of this proposed by Arayo.

suggested a physical test, by which it appear luminous matter must be gaseous; in short invested with an ocean of flame, since flame aëriform fluid in a state of incaudescence (1 posed is based upon the properties of polarise

It has been proved that the light emitted body in the liquid or solid state, issuing in to the surface, even when the body emitting polished, presents evident marks of polarisation when viewed through a polariscopic telescope ages in complementary colours (1290). But, signs of polarisation are discoverable, howeved direction in which the rays are emitted, if the flame.

2548. Its result.—The light proceeding fro has been accordingly submitted to this test. from its borders evidently issue in a direction to the surface, and therefore, under the cond to polarisation, if the luminous matter were the borders of the luminous matter were

obliquity; and, consequently, that the luminous

where gaseous.

un probably invested with a double gaseous coating.

comena which have been here described, and others a compel us to omit, are considered as giving a high cal probability to the hypothesis of Sir W. Herschel in which the aun is considered to be a solid, opaque, clobe, invested by two concentric strata of gaseous at, or that which rests immediately on the surface, nous, and the other, which floats upon the former, a gas or flame. The relation and arrangement of strata may be illustrated by our own atmosphere, a it a stratum of clouds. If such clouds were flame, four atmosphere would represent the two strata on

this hypothesis are explained by occasional openings is stratum by which parts of the opaque and nonce of the solid globe are disclosed. These partial be compared to the openings in the clouds of our

the firmament is rendered partially visible.

It diameter of the sun is not, therefore, the diameter be, but that of the globe bounded by the surface of luminous atmosphere; and this circumstance may it upon the small computed mean density of the sunterise these atmospheric strata, and especially the sudensity of the solid globe will necessarily be much ble than the mean density of the volume in which atter is included.

rd gaseous atmosphere probable. — Many circumindications of the existence of a gaseous atmosphere above the luminous matter which forms the visible It is observed that the brightness of the solar diminished towards its borders. This effect would it were surrounded by an imperfectly transparent atreas if no such gaseous medium surrounded it, the an effect might be expected, since then the thickness s coating measured in the direction of the visual ray eased very rapidly in proceeding from the centre This gradual diminution of brightness in prothe borders of the solar disk has been noticed by ers; but it was most clearly manifested in the series made by Sir J. Herschel in 1837, so conclusively, ave no doubt whatever of its reality on the mind of By projecting the image of the sun's disk by means of a good achromatic telescope, this diThe immediate cause of the spots being ruptures of continuity in the ocean of lut the visible surface of the solar globe, it is physical agency can be imagined to produce on a scale so vast as that which the change spots indicate.

The regions of the spots being two zon equator, manifests a connection between the sun's rotation. The like regions on the eat the trade-winds and anti-trades, and of hurrispouts, and other violent atmospheric disturb the same regions are marked by belts, appear by analogy to the same physical causes as the trades and other atmospheric perturbations prand ultra-tropical zones. Analogy, therefore whether any physical agencies can exist up those which produce these phenomena on the

So far as relates to the earth it is certain, a the planets probable, that the immediate p phenomena is the inequality of the exposure to solar radiation, and the consequent inec produced in different atmospheric zones, either flected calorific rays of the sun, combined wit (2528). But since the sun is itself the com supplying to all, and receiving from none, prevail upon it. It remains, therefore, to con of the physical principles which are in operat irrespective of any other heads.

miform temperature must be everywhere maintained. But if, from my local cause, the radiation be more obstructed in some regions han in others, heat will accumulate in the former, and the local emperature will be more elevated there than where the radiation is some free.

But the only obstruction to free radiation from the sun must arise rom the atmosphere with which to an height so enormous it is surrounded. If, however, this atmosphere have everywhere the same eight and the same density, it will present the same obstruction to adiation; and the effective radiation which takes place through it, hough more feeble than that which would be produced in its abstrace, is still uniform.

But since the sun has a motion of rotation on its axis in 54 72 48 , its atmosphere, like that of the earth, must participate a that motion and the effects of centrifugal force upon matter so sobile: the equatorial zone being carried round with a velocity reater than 300 miles per second, while the polar zones are moved at a rate indefinitely slower, all the effects to which the spheroidal form of the earth is due will affect this fluid with an energy proportionate to its tenuity and mobility, the consequence of which the that it will assume the form of an oblate spheroid, whose axis will be that of the sun's rotation. It will flow from the poles to the equator, and its height over the zones contiguous to the interest will be greater than over those contiguous to the poles, in a degree proportionate to the ellipticity of the atmospheric spheroid.

Now, if this reasoning be admitted, it will follow that the obstruction to radiation produced by the solar atmosphere is greatest over the equator, and gradually decreases in proceeding towards either pole. The accumulation of heat, and consequent elevation of temperature, is, therefore, greatest at the equator, and gradually decreases towards the poles, exactly as happens on the earth from

other and different physical causes.

The effects of this inequality of temperature, combined with the rotation, upon the solar atmosphere, will of course be similar in their general character, and different only in degree from the phenomena produced by the like cause on the earth. Inferior currents will, as upon the earth, prevail towards the equator, and superior counter-currents towards the poles (2528). The spots of the sun would, therefore, be assimilated to those tropical regions of the carth in which, for the moment, hurricanes and tornadoes prevail, the upper stratum which has come from the equator being temporarily carried downwards, displacing by its force the strata of luminous matter beneath it (which may be conceived as forming an habitually tranquil limit between the opposite upper and under currents), the upper of course to a greater extent than the lower, and thus wholly

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y denuding the opaque surface of the sun below.
cannot be unaccompanied by vorticose motions, whi
lves, die away by degrees, and dissipate, with thi
at their lower portions come to rest more speedi
r, by reason of the greater distance below, as well
s from the point of action, which lies in a higher
eir centre (as seen in our waterspouts, which are
tornadoes) appears to retreat upwards.

Herschel maintains that all this agrees perfectly wid during the obliteration of the solar spots, which in by the collapse of their sides, the penumbra claspot and disappearing afterwards.

d have rendered this ingenious hypothesis still mot Sir J. Herschel had assigned a reason why the licent non-luminous atmosphere, both of which are sous fluids, do not affect, in consequence of the spheroidal form which he ascribes to the superiore.

Calorific power of solar rays. — It has been alread not the intensity of heat on the sun's surface must great as that of the vivid ignition of the fuel in the

CHAP. XII.

THE SOLAR SYSTEM.

. Perception of the motion and position of surrounding depends upon the station of the observer. - The facility, and certainty with which the motions, distances, magniand relative position and arrangement of any surrounding can be ascertained, depends, in a great degree, upon the of the observer. The form and relative disposition of the gs, streets, squares, and limits of a great city, are perceived, mple, with more clearness and certainty if the station of the er be selected at the summit of a lofty building, than if it any station level with the general plane of the city itself. dvantage attending an elevated place of observation is much pted if the objects observed are affected by various and com-**A** motions inter se. A general, who directs the evolutions of e, seeks an elevated position from which he can obtain, as far me practicable to do so, a bird's-eye view of the field; and it one time proposed to employ captive balloons by which obs could be raised to a sufficient elevation above the plane of ilitary manœuvres.

these difficulties, which arise from the station of the observer in the general plane of the motions observed, are, however, ely aggravated when the station has itself motions of which enter is unconscious; in such case the effects of these motions tically transferred to surrounding objects, giving them apparent as in directions contrary to that of the observer, and apparent ties, which vary with their distance from the observer, inag as that distance diminishes, and diminishing as that distance accs.

such effects are imputed by the unconscious observer to so real motions in the objects observed; and, being mixed up the motions by which such objects themselves are actually aftended in inextricable confusion of changes of position, apparent and results, which involves the observer in obscurity and difficulty, purpose be to ascertain the actual motions and relative dispared arrangement of the objects around him.

56. Peculiar difficulties presented by the solar system. — All difficulties are presented in their most aggravated form to the ver, who, being placed upon the earth, desires to ascertain the ma and positions of the bodies composing the solar system.

which they produce among the objects of h

The difficulties arising out of these circages the progress of astronomical science. versally entertained of the absolute immobionly a vast error itself, but the cause of numisled inquirers by compelling them to a which are stationary, and to ascribe to bodicaltogether different from those with which

2557. Two methods of exposition. — The which a knowledge of the motions and ar system may be imparted. We may first expland changes as actually seen from the earth, combined with our knowledge of the motions itself, the real motions of the other bodies of the on the contrary, first explain the real motions they are now known, and then show how the motion of the earth, produce the apparent motion of the earth, produce the apparent motions.

The former method would perhaps be more it would proceed from observed facts as data to deduced from them; while the other method fit that which we desire to ascertain, and then patible with all the observed phenomena. Not tary purposes, such as those to which this volater method is preferable; we shall, therefor and relative arrangement of the bodies of the we proceed, how their motions cause the pheserved in the heavens.

2558. General areas

the same manner and according to the same dynamical laws as

govern their own motion round the sun.

2559. Planets primary and secondary. — This assemblage of globes which thus revolve round the sun as a common centre, of which the earth itself is one, are called PLANETS; and the secondary globes, which revolve round several of them, are called SECONDARY PLANETS, SATELLITES, or MOONS, one of them being our moon, which revolves round the earth as the earth itself revolves round the sun.

2560. Primary carry with them the secondary round the sun.—
The primary planets which are thus attended by satellites, carry the satellites with them in their orbital course; the common orbital motion, thus shared by the primary planet with its secondaries, not preventing the harmonious motion of the secondaries round the pri-

mary as a common centre.

2561. Planetary motions to be first regarded as circular, uniform, and in a common plane. — It will be conducive to the more easy and clear comprehension of the phenomena to consider, in the first instance, the planets as moving round the sun as their common centre in exactly the same plane, in exactly circular orbits, and with notions exactly uniform. None of these suppositions correspond precisely with their actual motions; but they represent them so very pearly, that nothing short of very precise means of observation and measurement is capable of detecting their departure from them. The motions of the system thus understood will form a first and very close approximation to the truth. The modifications to which the ecaelusions thus established must be submitted, so as to allow for the departure of the several planets from the plane of the ecliptic, of their orbits from exact circles, and of their motions from perfect uniformity, will be easily introduced and comprehended. But even these will supply only a second approximation. Further investigation will show series after series of corrections more and more minute in their quantities, and requiring longer and longer periods of time to manifest the effects to which they are directed.

2562. This method follows the order of discovery. — As to the rest, in following this order, proceeding from first suppositions, which are only rough approximations to the truth, to others in more exact accordance with it, we, in fact, only follow the order of discovery itself, by which the laws of nature were thus gradually, slowly, and laboriously evolved from masses of obscure and inexact

hypotheses.

2563. Inferior and superior planets. — The concentric orbits of the planets then are included one within another, augmenting successively in their distances from the centre, so as in general to leave a great space between orbit and orbit. The third planet, proceeding from the sun outwards, is the earth. Two orbits, those of the

ASTRONOMY.

called Mercury and Venus, are therefore included h's orbit, which itself is included within the orbits of lanets.

e planets which are included within the orbit of the dinferior planets, and all the others are called st

Periods.—The PERIODIC TIME of a planet is the a two successive returns to the same point of its orbine time it takes to make a complete revolution rout is found by observation, as might be naturally e e periodic time increases with the orbit, being much more distant planets; but, as will appear hereafter, of the periodic time is not in the same proportion of the orbit.

Synodic motion. — The motion of a planet coin relation to that of the earth, without reference to it

in its orbit, is called its SYNODIC MOTION.

of a planet as they appear to an observer on the e seocentric*; and as they would appear if the obserred to the sun, are called HELIOCENTRIC*.

it will be necessary to reduce 360° also to seconds. We shall efore have (2292)

$$a'' = \frac{1296000}{P}, P = \frac{1296000}{a''}.$$

569. Daily synodic motion. — The daily synodic motion is the e by which the planet departs from or approaches to the earth s course round the sun. Thus if A express in degrees the angle sed by two lines drawn from the sun, one to the planet and the r to the earth, the daily synodic motion will be the daily inet. Now, since the earth and planet both move in the same etion round the sun with different angular motions, the increase ecrease of a will be the difference of their motions. Thus, if planet move through 3° while the earth moves through 1° per , it is evident that the daily increase or decrease of A will be 2° ; if, while the earth moves through 1°, the planet move through the daily increase or decrease of A will be ½°.

I we express, therefore, the daily synodic motion of a planet by a daily heliocentric motion by a, and that of the earth by s, we Il have, for an inferior planet, whose angular motion exceeds t of the earth,

for a superior planet, whose angular motion is slower,

2570. Relation between the synodic motion and the period. see the daily heliocentric motions are found by dividing 360° by periods, we shall have for an inferior planet

$$\sigma^{\circ} = \frac{360^{\circ}}{P} - \frac{360^{\circ}}{E}, \quad \sigma'' = \frac{1296000}{P} - \frac{1296000}{E};$$

I for a superior planet
$$\sigma^{\circ} = \frac{360^{\circ}}{E} - \frac{360^{\circ}}{P}, \quad \sigma'' = \frac{1296000}{E} - \frac{1296000}{P}.$$
2571 Elegation — The geocentric position of a plane

2571. Elongation. — The geocentric position of a planet in reion to the sun, or the angle formed by lines drawn from the earth the sun and planet, is called the ELONGATION of the planet, and EAST OF WEST, according as the planet is at the one side or the er of the sun.

2572. Conjunction. - When the elongation of a planet is noing, it is said to be in conjunction, being then in the same direcn as the sun when seen from the earth.

2573. Opposition. — When the elongation of a planet is 180°, is said to be in opposition, being then in the quarter of the avens directly opposite to the sun.

ASTRONOMY.

vident that a planet which is in conjunction passes to or very near noon, and is therefore above the he day, and below it during the night. to other hand, a planet which is in opposition part or very near midnight, and therefore is all during the night, and below it during the day.

Quadrature. - A planet is said to be in quadrati

ation is 90°.

s position it passes the meridian at about six o'clo, when it has western quadrature, and six o'cloc when it has eastern quadrature. It is, therefor zon on the eastern side of the firmament during the night in the former case, and on the western side part of the night in the latter case. It is a morn ne case, and an evening star in the other.

Synodic period. — The interval which elapses lar elongations of a planet is called the synodic lanet. Thus, the interval between two successive two successive eastern or western quadratures

period.

Inferior and superior conjunction. - A superio

vident, therefore, that in the interval between two successive inzrior conjunctions the planet describes round the sun 360°, together

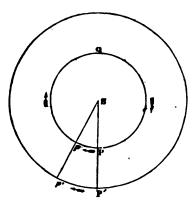


Fig. 783.

with the angle p s p, which the earth has described in the same expectal. If this angle, described by the earth in the synodic exict, be called Δ , the angle described by the planet in the same atterval will be $360^{\circ} + \Lambda$.

If P represent the place of the earth, and P that of a superior planet in opposition, the earth leaving P, and having a more rapid agular motion round s, will get before the planet as the minuteand gets before the hour-hand, and when it returns to P the planet will have advanced in its orbit, so that before another opposition can take place the earth must overtake it. If this happen when the planet is at p', the earth in the synodic period will have made an entire revolution, and have in addition described the angle $p \in P$, or a, which the planet has described. Thus, while A expresses the angle describes in the synodic period, $260^{\circ} + A$ expresses the angle described by the earth in the same time.

If a, as before, express the daily synodic motion of the planet, we shall have

$$\sigma^{\circ} = \frac{360^{\circ}}{\pi}$$
 $\sigma'' = \frac{1296000}{\pi}$

and consequently

$$T = \frac{360^{\circ}}{\sigma^{\circ}} = \frac{1296000}{\sigma''}.$$

Thus, when the daily synodic motion is given, the synodic time can be computed, and vice versa.

ш.

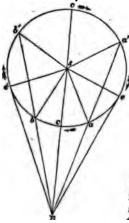
for an inferior planet, and

$$\frac{360^{\circ}}{\mathbf{T}} = \frac{360^{\circ}}{\mathbf{E}} - \frac{360^{\circ}}{\mathbf{P}}$$

and therefore

$$\frac{1}{r} = \frac{1}{r} - \frac{1}{r}$$

for a superior planet, showing in each case the 2578. The apparent motion of an inferior



the apparent from inferior planet, let place of the earth, and coce the orbi direction of the pla shown by the an which it assumes so cated at c', a', e, a, c, the earth moves rot same direction as th rent motion of the the left to the righ looking from E at s; tion is always from planet will be west of is any where in the s and east of it when is

atly the elongation and the angle esE, or e'sE, at the gether, make up 90°.

therefore, that the greatest elongation of an inferior me less than 90°.

h were stationary, the real orbital motion of the planet an apparent motion alternately east and west of the g to a certain limited distance, resembling the oscilla-dulum. While the planet moves from d to e it will art from the sun eastward, and when it moves from e appear to return to the sun; the elongation in the constantly increasing till it attain its maximum eastthe latter constantly decreasing till it become nothing. served, however, that the orbital arc c'e being greater time of attaining the greatest eastern elongation after unction is greater than the time of returning to the

greatest elongation to inferior conjunction.

rior conjunction, while the planet passes from c to d, constantly increases from nothing at c to its maxie; and when the planet moves from e to e, it again il it becomes nothing at superior conjunction. Since cs, ce' and e'c', are respectively equal to ce and c'e, it the interval from inferior conjunction to the greatest st, is equal to the interval from the greatest elongation ior conjunction. In like manner, the interval from anction to the greatest elongation east, is equal to the the greatest elongation west to superior conjunction. ation of the planet alternately east and west is thereirough the same angle - that is, the angle e E e', inigents drawn to the planet's orbit from the earth; but motion from the greatest elongation west to the greatest

st is slower than the apparent motion from the greatest

st to the greatest elongation west, in the ratio of the orbitual arcs e c'e' to e c e'.

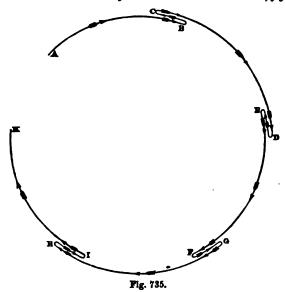
t being included within the orbit of the earth, the orof the earth will give it an apparent motion in the ie same direction as the apparent motion of the sun; apparent motion of a visible object increases as its sases, and vice versa, and since the planet being at a distance from the centre of the earth's orbit, the disearth from it is subject to variation, the apparent ted to the planet by the earth's orbital motion will be proportionate variation, being greatest when the planet conjunction, and least when in superior conjunction. ent motion of the planet, as it is projected upon the 7 the visual ray, arises from the combined effect of its action and that of the earth. Now it is evident from

earth is to give the planet an apparent n to east, both causes combine to impart to while passing from its western to its eas superior conjunction. On the other hand, motion of the planet being an apparent mot passing from its eastern to its western elo conjunction, while, on the contrary, the eart an apparent motion from west to east, the of the planet, resulting from the difference of the planet, resulting from the difference of the planet, and the planet will be opposite effects are equal.

In leaving the greatest eastern elongation t motion predominates, and the apparent motitinues to be, as before, eastward. As, in appl junction, the direction of the planet's motion more transverse to the visual line, and the di decreases, the effect of the planet's motion in length, equal to the effect of the earth's me then becomes stationary. This takes place a After this, the effect of the planet's n the apparent motion becomes westward, and continues through inferior conjunction, until 1 certain elongation west, equal to that at which stationary. Here the effects becoming again again stationary, after which, the effect of the dominating, the apparent motion hearso to the greatest

nces, and consequent relative orbital velocities, of the earth and

580. Apparent motion as projected on the ecliptic. — From that been here explained, the apparent motion of the planet on firmament will be easily understood. Let ABEFK, fig. 785,



resent the ecliptic in which the planet is at present supposed to re. While passing from its western to its eastern elongation it cars to move in the same direction as the sun, from A towards As it approaches B, its apparent motion eastward becomes grally slower until it stops altogether at B, and becomes, for a short treal, stationary; it then moves westward, returning upon its ree to c, where it again becomes stationary; after which it again reseastward, and continues to move in that direction till it arrives a certain point D, where it again becomes stationary; and then, runing upon its course, it again moves westward to E, where it in becomes stationary; after which it again changes its direction I moves eastward to F, where, after being stationary, it turns tward, and so on.

The middle points of the arcs BC, DE, FG, &c., of retrogression those at which the planet is in inferior conjunction; and the ldle points of the arcs CD, EF, GH, &c., of progression are those which the planet is in superior conjunction.



Fig. 736.

P that of the planet, and E E' E" E" the orbi within that of the planet, the direction of t and planet being indicated by the arrows.

When the earth is at E", the sun s and p visual line, and the planet is consequently

When the earth is at E''', the sun s and p visual line, and the planet is consequently the earth moves to e', the elongation of the is se' P. This elongation increasing as the obecomes 90° at E', when the visual direction tangent to the carth's orbit

the planet is a tangent to the earth's orbit. The planet is then in its eastern quadrature.

As the earth moves from E" to E", the elongation, being still east, constantly decreases until it becomes nothing at a", where the

planet is in conjunction. 2583. Direct and retrograde motion .- If the planet were immoveable, the effect of the earth's motion would be to give it an oscillatory motion alternately eastward and westward through the angle E' PE', which the carth's orbit subtends at the planet. While the earth moves from E" through E" to E', the planet would appear to move castward through the angle E' P E', and while the earth moves from E' through E to E", it would appear to move westward through the same angle.

Thus the effect of the earth's motion alone is to make the planet appear to move from east to west and from west to east alternately through a certain are of the ecliptic, the length of which will depend on the relation between the distances of the earth and planet from the sun, the are being in fact measured by the angle which the earth's orbit subtends at the planet, and, consequently, this angle of apparent oscillation will decrease in the same ratio as the distance of the planet increases.

The times in which the two oscillations castward and westward would be made are not equal; the time from the western to the eastern quadrature being less than the time from the eastern to the western quadrature in the ratio of the orbital are me me to the arc E'E" E'.

It is evident that the more distant the planet P is the less unequal these area, and, consequently, the less unequal the intervals between

quadrature and quadrature will be.

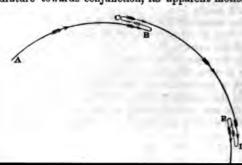
But, meanwhile, the earth being included within the orbit of the met, the effect of the planet's orbital motion will be to give it an erent motion in the ecliptic always in the same direction in which sun would move when in the same place, and therefore always ward or direct.

s apparent motion, though always direct, is not uniform, since ses in the same ratio as the distance of the earth from the decreases, and vice versa. This apparent motion thus due to lemet's own orbital motion is, therefore, greater from western gestern quadrature than from cestern to western quadrature.

rom eastern to western quadrature, through conjunction, the must motion of the planet is direct, because both its own orbital and that of the earth combine to render it so. From western greature, as the planet approaches opposition, the effect of the l'a motion is to render the planet retrograde, while the effect of an motion is to render it direct. On leaving quadrature the but predominates, and the apparent motion is direct; but at

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elongation, before arriving at opposition, the effect notion increasing becomes equal to that of the planing it, renders the planet stationary; after which, the rth's motion predominating, the planet becomes retrauses so until it acquires an equal elongation east, comes stationary, and is afterwards direct, and continuation Apparent motion projected on the ecliptic.—Let A, for the place of a superior planet when moving for quadrature towards conjunction, its apparent motion



planet projected on the ecliptic is, in all respects, similar to that of an inferior planet; the difference being, that in the latter the middle point of the arc of retrogression corresponds to inferior conjunction, while in the former it corresponds to opposition.

It will be apparent from what has been explained, that the angle which the earth gains upon the planet in the interval between its western and eastern quadratures is the angle which the earth's orbit subtends at the planet, or twice the annual parallax (2442) of the

planet.

2585. Conditions under which a planet is visible in the absence of the sun. — It is evident that to be visible in the absence of the sun a celestial object must be so far elongated from that luminary as to be above the horizon before the commencement of the morning twilight or after the end of the evening twilight. One or two of the planets have, nevertheless, an apparent magnitude so considerable, and a lustre so intense, that they are sometimes seen with the naked eye, even before sunset or after sunrise, and may, in some cases, be seen with a telescope when the sun has a considerable altitude. In general, however, to be visible without a telescope, a planet must have an elongation greater than 30° to 35°.

2586. Evening and morning star. — Since the inferior planets can never attain so great an elongation as 90°, they must always pass the meridian at an interval considerably less than six hours before or after the sun. If they have eastern elongation they pass the meridian in the afternoon, and are visible above the horizon after sunset, and are then called EVENING STARS. If they have western elongation they pass the meridian in the forenoon, and are visible above the eastern horizon before sunrise, and are then called MORN-

ING STARS.

*2587. Appearance of superior planets at various elongations.—
A superior planet, having every degree of elongation east and west of the sun from 0° to 180°, passes the meridian during its synodic period at all hours of the day and night. Between conjunction and quadrature, its elongation east or west of the sun being less than 90°, it passes the meridian earlier than six o'clock in the afternoon in the former case, and later than six o'clock in the forenoon in the latter case; being, like an inferior planet, an evening star in the former and a morning star in the latter case.

At eastern quadrature it passes the meridian at six in the evening, and at western quadrature at six in the morning; appearing still as an evening star in the former and as a morning star in the latter case.

Between the eastern quadrature and opposition, the elongation being more than 90° east of the sun, the planet must pass the meridian between six o'clock in the evening and midnight, and is therefore visible from sunset until some hours before sunrise. Between western quadrature and opposition, the elongation being more than

of the sun, the planet must pass the meridian at so midnight and six o'clock in the morning, and it is om some hours after sunset until sunrise. position the planet passes the meridian at midnigh visible from sunset to sunrise.

To find the periodic time of the planet.—T olutions of this problem, which give results having of approximation to the exact value of the quantity 1°. By means of the synodic period.—If the be ascertained by observation, we shall have for an 2577),

$$\frac{1}{\mathbf{T}} = \frac{1}{\mathbf{P}} - \frac{1}{\mathbf{E}},$$

equently

$$\frac{1}{P} = \frac{1}{E} + \frac{1}{T};$$

superior planet

$$\frac{1}{\mathrm{T}} = \frac{1}{\mathrm{E}} - \frac{1}{\mathrm{P}};$$

cfore

same sidereal place.—The periodic time of a planet being approximately found by either of the preceding methods, it may be rendered

more exact by the following.

When a planet is in superior conjunction or in opposition, its place in the firmament is the same, whether viewed from the earth or from the sun. Now, if two oppositions or conjunctions separated by a long interval of time be found, at which the apparent place of **he planet in the firmament** is the same, it may be inferred that a semplete number of revolutions must have taken place in the inter-Now the periodic time being found approximately by either the methods already explained, it will be easy to find by it how many revolutions of the planet must have taken place between the two distant oppositions. If the periodic time were known with precision, it would divide the interval in question without a remainder; but being only approximate, it divides it with a remainder. Now the nearest multiple of the approximate period to the interval between the two oppositions will be that multiple of the true period which is exactly equal to the interval. The division of the interval by the number thus determined will give the more exact value of the period.

2592. 4°. By the daily angular motion.—The daily angular geocentric motion may be observed, and the heliocentric motion thence computed. If the mean heliocentric daily motion a" can be obtained by means of a sufficient number of observations, the period will be given by the formula (2568),

$$\mathbf{P} = \frac{1296000}{\mathbf{a}''}.$$

2593. To find the distances of the planets from the sun. — One of the most obvious methods of solving this problem is by observing the elongation of the planet, and computing, as always may be done, the angle at the sun. Two angles of the triangle formed by the earth, sun, and planet, will thus be known, and a triangle may be drawn of which the sides will be in the same proportion as those of the triangle in question. The ratio of the earth's distance from the sun to the planet's distance from the sun will thus become known (2296); and as the earth's distance has been already ascertained, the planet's distance may be immediately computed.

Other methods of determining the distances will be explained

hereafter.

2594. Phases of a planet.—While a planet revolves, that hemisphere which is presented to the sun is illuminated, and the other dark. But since the same hemisphere is not presented generally to the earth, it follows that the visible hemisphere of the planet will consist of a part of the dark and a part of the enlightened hemisphere, and, consequently, the planet will exhibit PHASES, the varie-

and limits of which will depend upon the relative direct lines drawn from the earth and sun to the planet. It is t the section of the planet at right angles to a line draw sun to its centre is the base of its enlightened hemisphe

the section at right angles to a lin from the earth to its centre, is the its visible hemisphere. The less t included between these lines is, the will be the portion of the visible her which is enlightened.

Let v. fig. 738, be the centre

which is enlightened.

Let p, fig. 738, be the centre planet, p s the direction of a line of the sun, and p that of one draw earth; ll' will then be the base of lightened, and vv' the base of the hemisphere of the planet. The l will be the centre of the former, at the latter. The visible hemisph



Fig. 738.

n be enlightened over the space v' m' m l, the part v l being is dark part will be measured by the arc v l, which is east to m m', and therefore measured by the angle formed as $p \in p$ and $p \in p$ drawn from the planet in the directions of

an 90°, and the planet appears gibbous, as the moon does when tween opposition and quadratures.

When the angle sp = is greater than 90°, as in fig. 739, the sadth v'l of the enlightened part of the visible hemisphere is less an 90°, and the planet appears as a crescent, like the moon be-

conjunction and quadrature.

When the angle sp = 0, which happens when the earth is tween the sun and planet, as in fg. 740, the centre m' of the lightened hemisphere is presented to the earth, and the planet pears with a full phase, as the moon does in opposition. This rays happens when the planet is in opposition.

When the angle sp E becomes = 180° , as in fig. 741, the centre of the dark hemisphere is presented to the earth, and therefore entire hemisphere turned in that direction is dark. This takes see when the planet is between the earth and sun, which can only

ppen when an inferior planet is in inferior conjunction.

2595. Phases of an inferior planet.—It will be evident from specting the diagram, fig. 734, representing the relative positions [an inferior planet with respect to the sun and earth, that the angle smed by lines drawn from the planet to the sun and earth passes brough all magnitudes from 0° to 180°, and consequently such a lanet exhibits every variety of phase. Passing from c towards c', he angle s b E gradually decreases from 180° to 90°, and therefore he phase, at first a thin crescent, increases in breadth until it is alved like the moon in quadrature. From c' to c' the angle s b' E gradually decreases from 90° to 0°, and the planet beginning by being gibbous, the breadth of the enlightened part gradually increases until it becomes full at c'. From c' to c, and thence to c.



Fig. 742.

ш.

these phases are reproduced for like reasons in the opposite order.

2596. Phases of a superior planet.

— It will be evident on inspecting fig. 742, that in all positions whatever of a superior planet, the lines drawn from it to the earth are inclined at an angle less than 90°; and this angle is so much the smaller the greater the orbit of the planet is comparatively with that of the earth. The angle sa E being nothing at o increases until the planet is in quadrature at q', where it is greatest; and then the breadth of the enlightened part is least, and is equal to

ened part is least, and is equal to the difference between the angle $s \not = a$ and 180°. From q' to c the angle $s \not = a$ decreases, and becomes nothing at c. The planet is

_____ to the attraction

must move in a straight line. If, therefore in any curvilinear path, it may be inferred some force or forces exterior to it, which ce the straight course which, in virtue of its in left to itself (220). This force must, more operation, since, if its action were suspended during such suspension would move in the aline, which would be a tangent to the curve action of the force was suspended.

Now, since the orbits of the planets, inclu curved, it follows that they are all under the some force or forces, and it becomes an imp termine what is the direction of these forces, or several, and, in fine, whether they are of in if variable, what is the law and conditions of the

2598. What is the centre to which this attra We are aided in this inquiry by a principle of t and the greatest simplicity, established by Newt of which forms the subject of the first two probrated work, entitled "PRINCIPIA."

2599. General principle of the centre of strated. — If from any point taken as fixed, a si to a body which moves in a curvilinear path, si radius vector of the moving body with relatio centre of motion. As the body moves along the radius vector sweeps over a certain superfless, according to the velocity and direction of length of the radius vector



pears that whenever a body moves in a curvilinear orbit, under the attraction of a force directed to a fixed centre, such a body will describe round such centre equal areas in equal times; and it is proved also conversely, that if a point can be found within the curvilinear orbit of a revolving body, round which such body describes equal areas in equal times, such body is in that case subject to the action of a single force, always directed towards that moint as a centre. It follows, in short, that "the centre of equable areas is the centre of force, and that the centre of force is the centre of equable areas."

As this is a principle of high generality and capital importance, and admits of demonstration by the most elementary principles of mechanics and geometry, it may be proper to explain it have

If a body B move independently of the action of any force upon it, its motion must be in a straight line, and must be uniform. It must, therefore, move over equal spaces per second. Let its velocity be such, that in the first second it would move from B to B'. In the next

if no force acted upon it, it would move through the equal 'b' in the same direction. But if at B' it receive from a receted to c, an impulse which in a second would carry it 'to c', it will then be affected by two motions, one repreby B'b', and the other by B'c', and it will move in the dia'B" of the parallelogram, and at the end of the second second at B".

, in the first second, the radius vector described the area and in the next second it described the area B'OB". It is show that these areas are equal. For since BB' = B'b', the CB' and B'Cb' are equal; and since b'B' is parallel to B'O, as B'Cb' and B'CB' are equal by the well-known property igles. Therefore the areas BOB' and B'CB", described by its vector in the first and second seconds, are equal.

ne body received no impulse from the central force at B", it move over B" b'' = B'B'' in the third second, but receiving ne central force another impulse sufficient to carry it from B" tagain moves over the diagonal B" B" of the next parallelound at the end of the third second is found at B". It is in the same manner that the area of the triangle B" CB''' is

;. 743.

smaller sides. In fine, if the intervals of the be infinitely small, the sides of the polygon small in magnitude and great in number. The be continuous, instead of being intermitting, a body would be a curve, instead of being a po however, described by the radius vector round c, would still be proportional to the time.

The converse of the principle is easily infa altogether similar. If C, fig. 743, be the centr will be the centre of attraction; for let B'b' be to the triangular area B'Cb' will then be equal to the common properties of triangles, and since to round C in successive seconds are equal, we have BCB', and therefore = B'Cb'. Hence we infer the and therefore that the line b'B'' is parallel to B'C. fore expressed by the diagonal B'B'' of the parallel ent to the forces expressed by the sides. The fore, besides the projectile force BB' or B'b', is u force directed to C.

2600. Linear, angular, and areal velocity. and analysis of the planetary motions, there are which there is frequent occasion to express in ref of time, and to which the common name of "v quently applied.

1°. The linear velocity of a planet is the actual it moves in its orbit in the unit of time. We should be pressent this velocity.

may be considered as the arc of a circle, of which c is the centre and B" c the radius, we shall have (2292),

$$\mathbf{B}'' \, c' = \frac{r \times a}{206265},$$

where the distance B" o of the planet from the sun, or the radius vector, is expressed by r. Hence we have

$$A = \frac{1}{2} B' C \times B'' C' = \frac{\frac{1}{2} r^3 \times \alpha}{206265}.$$

Hence the areal velocity is always proportional to the product of the angular velocity and the square of the radius vector or distance.

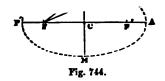
To ascertain, therefore, whether any point within the orbit of a planet be the "centre of equal areas," and therefore the centre of attraction, it is only necessary to compare the angular velocity round such point with the square of the distance; and if their product be always the same, or, in other words, if the angular velocity increase in the same ratio as the square of the distance or radius vector decreases, and vice versa, then the point in question must be the centre of equal areas, and therefore the centre of attraction.

2602. Case of the motion of the earth. — In the case of the earth, the variation of its distance from the sun is inversely as the variation of the sun's apparent diameter, which may be accurately observed, as may also be the sun's apparent motion in the firmament. Now, it is found that the apparent motion of the sun increases exactly in the same ratio as the square of its apparent diameter, and therefore inversely as the square of its distance; from which it follows that its centre is the centre of equal areas for the earth's motion, and therefore the centre of attraction.

2603. Case of the planets. — In the same manner, by calculating from observation the angular motions of the planets, and their distances from the sun, it may be shown that their angular motions are inversely as the squares of their distances, and consequently that the centre of the sun is the centre of the attraction which moves them.

2604. Orbits of the planets ellipses. — By comparing the variation of the distance of any planet from the sun with the change of direction of its radius vector, it may be ascertained that its orbit is an ellipse; the centre of the sun being at one of the foci, in the same manner as has been already explained in the case of the earth.

2605. Perihelion, aphelion, mean distance. — That point of the elliptic orbit at which a planet is nearest to the sun is called PERIBELION, and that point at which it is most remote is called APHE-



drawn throu minating in longest, while angles to it, c is the short which is equa axis, and ther

of the greatest and least distances of the el the MEAN DISTANCE.

A planet is, therefore, at its mean distance is at the extremities of the minor axis of its

There is another point F on the major as from the centre, equal to F c, which has also t ties of the focus. It is sometimes distinguing Focus of the planet's orbit.

Ellipses may be more or less ECCENTRIC, the less oval. The less eccentric they are, the less from a circle. The degree in which they have pends on the ratio which the distance FC of centre bears to PC, the semi-axis major. Two magnitudes in which this ratio is the same, he are equally eccentric. The less the ratio of C: nearly does the ellipse resemble a circle. The called the ECCENTRICITY.

The eccentricity of a planet's orbit will, then ber which expresses the distance of the sun freellipse, the semi-axis major of the orbit being to 2607. Apsides, anomaly. — The points of APHELION, are called by the

a variable angular motion, the anomaly of this imaginary planet is called the MEAN ANOMALY of the planet.

2608. Place of perihelion. — The PLACE OF PERIHELION is expressed by indicating the particular fixed star at or near which the planet at P is seen from F, or, what is the same, the distance of that point from some fixed and known point in the heavens. The point selected for this purpose is the vernal equinoxial point, or the first point of Aries (2435). The distance of perihelion from this point, as seen from the sun, is called the LONGITUDE OF PERIHELION, and is an important condition affecting the position of the planet's orbit in space.

2609. Excentricities of orbits small. — The planets' orbits, like that of the earth, though elliptical, are very slightly so. The ecsentricities are so minute, that if the form of the orbit were delineated on paper, it could not be distinguished from a circle except by very exactly measuring its breadth in different directions.

2610. Law of attraction deduced from elliptic orbit. — As the squable description of areas round the centre of the sun proves that point to be the centre of attraction, the elliptic form of the orbit and the position of the sun in the focus indicate the LAW according to which this attraction varies as the distance of the planet from the san varies. Newton has demonstrated, in his PRINCIPIA, that such a motion necessarily involves the condition that the intensity of the attractive force, at different points of the orbit, varies inversely as the aquare of the distance, increasing as the square of the distance decreases, and vice versá.

2611. The orbit might be a parabola or hyperbola. — Newton also proved that the converse is not necessarily true, and that a body may move in an orbit which is not elliptical round a centre of force which varies according to this law. But he showed that the crit, if not an ellipse, must be one or other of two curves, a PARABOLA or HYPERBOLA, having a close geometric relation to the ellipse, and that in all cases the centre of force would be the focus of the curve.

These three sorts of curves, the ellipse, the parabola, and hyperbola, are those which would be produced by cutting a cone in different directions by a plane, and they are hence called the CONIC SECTIONS.

2612. Conditions which determine the species of the orbit. — The conditions under which the orbit of a planet might be a parabola or hyperbola, depend on the relation which the velocity of the motion of the planet, at any given point of the orbit, bears to the intensity of the attractive force at that point. It is demonstrable that, if the velocity with which a planet moves at any given point of its orbit were suddenly augmented in a certain proportion, its orbit

pass near the sun once, following a curved depart never to return.

2613. Law of gravitation general. - The orbit of a planet indicates the law which gov the sun's attraction from point to point of suc this orbit it proves nothing. It remains, the the planetary motions round the sun, and from satellites round their primaries, that the same which the intensity decreases as the square of t

centre of attraction increases, and vice versa, is

The attraction exerted upon any body may be ral, as that of the earth on bodies near its surf. the spaces through which the attracted body wo given time. It has been shown, that the attract exerts at its surface, is such as to draw a body 193 inches in a second. Now if the space thro would, by its attraction at any proposed distanc one second could be found, the attraction of the s could be exactly compared with and measured by the earth, just as the length of any line or dist by applying to it and comparing it with a standar



2614. Method of calculating the central fo and curvature. - Now th which any central attraction body in a given time can be the body in question move nearly circular orbit round all the planets and

towards the centre E, through the space mn, in the unit of time. By means of this space, therefore, the force which the central attraction exerts at m can be brought into direct comparison with the force which terrestrial gravity exerts at the surface of the earth.

It follows, therefore, that if f express the space through which such a body would be drawn in the unit of time, falling freely towards the centre of attraction, we shall have f = m n. But by the elementary principles of geometry,

$$mn \times 2 E m = m m'^2$$
.

Therefore,

$$f = \frac{\mathbf{v}^2}{2r};$$

that is, the space through which a body would be drawn towards the centre of attraction, if deprived of its orbital motion, in the unit of time, is found by dividing the square of the linear orbital velocity by twice its distance from the centre of attraction.

Since
$$\mathbf{v} = \frac{\mathbf{r} \times \mathbf{a}}{206265}$$
, (2601), we shall also have

$$f = \frac{r \times a^2}{2 \times 206265}.$$

The attractive force, or, what is the same, the space through which the revolving body would be drawn towards the centre in the wit of time, can, therefore, be always computed by these formulæ, when its distance from the centre of attraction and its linear or angler velocity are known.

Since (2568)

$$a = \frac{1296000}{P}$$

this, being substituted for a in the preceding formula, will give

$$f = 412541 \times \frac{r}{r^2};$$

by which the attractive force may always be calculated when the distance and period of the revolving body are known.

2615. Law of gravitation shown in the case of the moon. — The attraction exerted by the earth, at its surface, may be compared with the attraction it exerts on the moon, by these formulæ.

In the case of the moon, v = 0.6356 miles, and r = 239,000 miles; and by calculation from these data, we find

$$f = 0.0000008459$$
 miles. $= 0.0536$ inch.

The attraction exerted by the earth at the moon's distance would,

centre is 60 times the earth's radius. It ap this case the attraction of the earth decrease distance from the attracting centre increases; the same law of gravitation prevails as in planet.

2616. Sun's attraction on planets compation fulfilled. — In the same manner, exactly, the sun exerts at different distances may be tions and distances of the planets. The distathe circumference of its orbit, and this, comptime, will give the arc through which it moves a minute. This, represented by mm', fig. 74 space m n through which the planet would fall the same time may be calculated; and this bein planets, it will be found that these spaces are of the squares of their distances.

Thus, for example, let the earth and Jupiter manner. If D express the distance from the period in days, A the arc of the orbit in mil planet in an hour, and H the space mn in miles planet would fall towards the sun in an hour if were destroyed, we shall then have

	D	P	A
EarthJupiter	95,000,000	365-26	68,0
	494,000,000	4382-02	20.5

their satellites, is concerned. But this law does not alone affect the central attracting bodies. It belongs equally to the revolving bodies themselves. Each planet attracts the sun, and each satellite attracts its primary as well as being attracted by it; and this reciprocal attraction depends on the mass of the revolving as well as on the mass of the central body and their mutual distance.

The planets, moreover, as well as the satellites, attract each other, and thus modify, to some small extent, the effects of the predominant central attraction.

2618. Its analogy to the general law of radiating influences.—
It will be observed that this law is similar to that which governs light, heat, sound, and other physical principles which are propagated by radiation; and it might thus be inferred that gravitation is an agency of which the seat is the sun, or other gravitating body, and that it emanates from it as other physical principles obeying the same law are supposed to do.

2619. Not, however, to be identified with them. — No such hynotheris as this, however, is either assumed or required in astronomy. The law of gravitation is taken as a general fact established by observation, without reference to any modus operandi of the force. The planets may be drawn towards the sun by an agency whose seat is established in the sun, or they may be driven towards it by an agency whose seat is outside and around the system, or they may be pressed towards it by an agency which appertains to the space in which they move. Nothing is assumed in astronomy which would be incompatible with any one of these modes of action. The hw of gravitation assumes nothing more than that the planets are subject to the agency of a force which is every where directed to the sun, and whose intensity increases as the square of the distance from the sun decreases, and vice versa; and this, as has been shown, is proved as a matter of fact independent of all theory or hypothesis.

2620. The harmonic law.—A remarkable numerical relation thus denominated prevails between the periodic times of the planets and their mean distances, or major axes of their orbits. If the squares of the numbers expressing their periods be compared with the cubes of those which express their mean distances, they will be found to be very nearly in the same ratio. They would be exactly so if the masses or weights of the planets were absolutely insignificant compared with that of the sun. But although these masses, as will appear, are comparatively very small, they are sufficiently considerable to affect, in a slight degree, this remarkable and important law.

Omitting for the present, then, this cause of deviation, the harmonic law may be thus expressed. If P, P', P'', &c., be a series of

from the law as may be due to the cause 2621. Fulfilled by the planets. — Meth tance of a planet from the sun when its 1. To show the near approach to numerical remarkable law is fulfilled by the motions the solar system, we have exhibited in the tive approximate numerical values of the periods, and have shown that the quotient cubes of the distances by the squares of equal:—

	Distance.	Period. P.	Cube of Distance.
Mercury Venus Rarth	0-387 0-723 1-00 1-52	0-241 0-615 1-00 1-88	57961 377933 1000000 3525668
Planetoids Jupiter Seturn Uranus Neptune	2-50 5-20 9-24 19-18 30-00	4·00 11·86 29·50 84·00 164·60	15625000 140608000 865250664 7055792682 2700000000

In general, the distance of a planet from puted by means of this law, when the distanc periodic times of the earth and planet are known

For this purpose find the number which time P of the planet, that of the

number whose cube is the square of the number expressing the period, or, what is the same, to extract the cube root of the square of the period.

2622. Harmonic law deduced from the law of gravitation. -It is not difficult to show that this remarkable law is a necessary

 Somequence of the law of gravitation.
 Supposing the orbits of the planets to be circular, which for this purpose they may be taken to be, let the distance, period, and angular velocity of any one planet be expressed by r, P, and a, and those of any other by r', P', and a', and let the forces with which - the sun attracts them respectively be expressed by f and f'. We m shall then, according to what has been proved (2614), have

$$f = \frac{r \times a^2}{2 \times 206265}$$
 $f' = \frac{r' \times a'^2}{2 \times 206265}$;

'& and therefore

$$f:f':r\times a^2:r'\times a'^2.$$

But by the law of gravitation

$$f:f'::\gamma'^2:r^2$$

therefore

$$r'^2: r^2:: r \times \alpha^2: r' \times \alpha'^2,$$

and consequently

$$r'^3\times a'^2=r^3\times a^3.$$

But the angles described in the unit of time are found by dividing 360° by the periodic times. Therefore,

$$a = \frac{360^{\circ}}{P} \qquad a' = \frac{360^{\circ}}{P'},$$

and consequently

$$\frac{r^3}{\nu^2} = \frac{r^{\prime 3}}{\nu^{\prime 2}},$$

which is, in fact, the harmonic law.

It is easy, by pursuing this reasoning in an inverse order, to show that if the harmonic law be taken, as it may be, as an observed fact,

the law of gravitation may be deduced from it.

2623. Kepler's laws.—The three great planetary laws explained in the preceding paragraphs—1. The equable description of areas;
2. The elliptic form of the orbits; and 3, the harmonic law were discovered by Kepler, whose name they bear. Kepler deduced them as matter-of-fact from the recorded observations of himself and other astronomers, but failed to show the principle by which they were connected with each other. Newton gave their interpretation, and showed their connexion as already explained.

upon the ecliptic, although they are n The centre of the planet, twice in each 1 the ecliptic. The points at which it is of the earth's orbit are at opposite sides as seen from that luminary. At one of the the south to the north of the ecliptic, north to the south. 2625. Nodes, ascending and descendi the centre of a planet crosses the ecliptic, at which it passes from south to north bei

NODE, and the other the DESCENDING NO While the planet passes from the asci node, it is north of the ecliptic; and whil acending to the ascending node, it is south All these phenomena indicate that the the plane of the ecliptic, but in a plane it This angle cannot be great, since served to depart far from the ecliptic. which will be noticed hereafter, the obliqu do not amount to more than 70

2626. The zodiac. - The planets, there than about 8° from the ecliptic, north or limited to a zone of the heavens bounded ecliptic at this distance, north and south of 2627. Method of determining a planet's - This problem may be solved with more o a great variety of different methods 1- "

carth's diseas

be 900 - E, and will therefore be known, and thus the distances

IP and EP may be computed as in the first method.

2630. So. By the greatest and least apparent magnitudes. — If n and m' be the apparent magnitudes of an inferior planet when at afterior and superior conjunction, and e and p be the distances of the earth and planet from the sun, e-p will be the distance of the tanet from the earth at inferior, and e+p at superior conjunction **2577**); and since the apparent magnitudes are in the inverse ratio of these distances (1118), we shall have

$$\frac{m}{m'}=\frac{e+p}{e-p},$$

md consequently

$$p = \frac{m - m'}{m + m'} \times \epsilon.$$

If m + m' be the apparent magnitudes of a superior planet in opposition and conjunction, its distances at these points will be p - eand p + e, and we shall have as before

$$\frac{m}{m'} = \frac{p + e^{\cdot}}{p - e},$$

and therefore

$$p=\frac{m+m'}{m-m'}\times e.$$

2631. 4°. By the harmonic law. — This law (2614) being deduced from the law of gravitation (2616), independently of the observation and comparison of times and distances, it may be used for the determination of the distances, the times being known. Let **R** and **P** be the periodic time of the earth and planet, and e and p their distances from the sun. We shall then, by the harmonic law, have

$$\frac{p^3}{\epsilon^3} = \frac{p^2}{k^2},$$

and therefore

$$p^{s}=rac{\mathbf{P}^{s}}{\mathbf{E}^{s}} imes e^{s},$$

and thus the distance p may be found.

2632. To determine the real diameters and volumes of the bodies of the system. — The apparent diameter at a known distance being observed, the real diameter may be computed by the principle explained in 2299. The linear value of 1" at the distance being known, the real diameter will be obtained by multiplying such value by the apparent diameter expressed in seconds.

of 1" at the planet will be found (2298), which, by the greatest breadth of its gibbous disk, the 1 be obtained.

In the case of the superior planets, their diame obtained when in opposition, because then they a disk, and, being nearer to the earth than at any have the greatest possible magnitude. Their distain this position is always the difference between the earth and planet from the sun.

When the real diameters are found the volumes since they are as the cubes of the real diameters.

2633. Methods of determining the masses of solar system. — The work of the astronomer is bu formed when he has only mentioned the distances and ascertained the motions and velocities, of the the universe. He must not only measure, but pendous masses.

The masses or quantities of matter in bodies up the earth are estimated and compared by their wei the intensity of the attraction which the earth e: It is inferred that equal quantities of matter at equal the centre of the earth are attracted by equal for all masses, great and small, fall with the same yeld

The intensity of the attraction with which the upon a body at any given distance from its centre mass or quantity of matter composing the earth. the earth were suddenly increased in any proposed

the exact proportion of the quantities of ponderable matter com-

posing them.

But it will be convenient to obtain the relation between the masses and the attractions they exert at unequal distances. For this purpose, let the attractions which they exert at equal distances be expressed by f and f', and let the common distance at which those attractions are exerted be expressed by x, and let r and r' express the attractions which they respectively exert at any other distances, r and r', and we shall have, according to the general law of gravitation,

$$f: \mathbf{r} :: \frac{1}{x^4} : \frac{1}{r^4}$$

$$f': \mathbf{r}' :: \frac{1}{x^3} : \frac{1}{r^{90}}$$

and consequently

$$\frac{f}{P} \times \frac{1}{r^3} = \frac{f'}{F'} \times \frac{1}{r'^3};$$

from which it follows that

$$\frac{f}{f'} = \frac{\mathbf{F} \times \mathbf{r}^2}{\mathbf{F} \times \mathbf{r}^{\prime 2}}.$$

But since the masses M and M' are proportional to the attractions f and f', we have

$$\frac{f}{f'} = \frac{M}{M'},$$

und therefore

$$\frac{M}{M'} = \frac{F \times r^2}{F' \times r'^2};$$

that is, the attracting masses are proportional to the products obtained, by multiplying any two forces exerted by them by the squares of the distances at which such forces are exerted.

Hence in all cases in which the attractive forces exerted by any seatral masses at given distances can be measured by any known or observable motions, or other mechanical effects, the proportion of the attracting masses can be determined.

2634. Method of estimating central masses round which bodies revolve. — If bodies revolve round central attracting masses as the planets revolve round the sun, and the satellites round their primaries, the ratio of the attracting forces, and therefore that of the central masses, can be deduced from the periods and distances of the revolving bodies by the principles and method explained in 2614.

Thus if P and P be the periods of two bodies revolving round

By this principle the ratio of the attracting ascertained when the periods of any bodies reknown distances are known.

٠,

2635. Method of determining the ratio planets which have satellites, to the mass of this nothing more than a particular applicatio plained above.

To solve it, it is only necessary to ascertai tance of the planet and the satellite, and su formula determined in 2634. The arithme executed, the ratio of the masses will be deter

2636. To determine the ratio of the mass of the sun.—Since the earth has a satellite, this p by the method given in 2635.

If r and r' express the distances of the en moon, and P and P' the periods of the sun and

$$\frac{r}{r'} = 400 \quad \frac{r'}{P} = \frac{27 \cdot 30}{365 \cdot 25} = \frac{r^3}{r'^3} = 64000000 \quad \frac{r'^2}{P^3} = \frac{17}{17}$$

which being substituted, and the operations ex

$$\frac{M}{N'} = 357500.$$

2687. To determine the masses of planets we - According to what has been applying the

satellite, and of the sun upon the planet, and when the effect of the difference of distance is allowed for, the ratio of the mass of the

planet to the mass of the sun is found.

In the case of planets not attended by satellites, the effect of their gravitation is not manifested in this way, and there is no body smaller than themselves, and sufficiently near them to exhibit the same easily measured and very sensible effects of their attraction, and hence there is considerable difficulty, and some uncertainty, as to their exact masses.

2638. Mass of Mars estimated by its attraction upon the earth.-The nearest body of the system to which Mars approaches is the earth, its distance from which in opposition is nearly fifty millions of miles, or half the distance of the earth from the sun. Now, since the volume of Mars is only the eighth part of that of the earth, it may be presumed, that whatever be its density its mass must be so small, that the effect of its attraction on the earth at a distance so great must be very minute, and therefore difficult to ascertain by observation. Nevertheless, small as the effect thus produced is, it is not imperceptible, and a certain deviation from the path it would follow, if the mass of Mars were not thus present, has been observed. To infer, from this deviation, the mass of Mars is, however, a problem of much greater complexity than the determination of the mass of a planet by observing its attraction upon its satellite. The method adopted for the solution of the problem is a sort of "trial and error." A conjectural mass is first imputed to Mars, and the deviation from its course which such a mass would cause in the orbital motion of the earth is computed. If such deviation is greater or less than the actual deviation observed, another conjectural mass, greater or less than the former, is imputed to the planet, and another computation made of the consequent deviation, which will come nearer to the true deviation than the former. repeating this approximative and tentative process, a mass is at length found, which, being imputed to Mars, would produce the observed deviation; and this is accordingly assumed to be the true mass of the planet.

In this way the mass of Mars has been approximatively estimated

at the seventh part of the mass of the earth.

The smallness of this mass compared with its distance from the only body on which it can exert a sensible attraction will explain the difficulty of ascertaining it, and the uncertainty which attends its value.

2639. Masses of Venus and Mercury.—The same causes of difficulty and uncertainty do not affect in so great a degree the planet Venus, whose mass is somewhat greater than that of the earth, and which moreover comes, when in inferior conjunction, within about thirty millions of miles of the earth. The effects of the attraction is still very uncertain. Attempts have lately be imate to its value, by observing the effects of its of the comets.

2640. Methods of determining the mass of ti to its proximity and close relation to the earth, striking phenomena connected with it, the determ of the moon becomes a problem of considerable i are various observable effects of its attraction by its mass to those of the sun or earth may be com

2641. 1°. By nutation.—It will be shown he tractions of the masses of the sun and moon upo matter surrounding the equator of the terrestria a regular and periodic change in the direction earth, and consequently a corresponding change place of the celestial pole. The share which these effects being ascertained, their relative a upon the redundant matter at the terrestrial equation of the attracting masses is obtained.

2642. 2°. By the tides. — It has been shown by the attractions of the masses of the sun and n the ocean are produced. The share which each ms duction of these effects being ascertained, and the ference of distance being allowed for, the ratio of sun and moon is obtained.

2643. 3°. By the common centre of gravity the earth. — It has been stated that the centre of

rom the centres of the earth and moon will give the ratio of their nasses.

Now, the monthly motion of the earth round such a centre would necessarily produce a corresponding apparent monthly displacement of the sun. Such displacement, though small (not amounting to more than a few seconds), is nevertheless capable of observation and measurement. The exact place of the sun's centre being therefore computed on the supposition of the absence of the moon, and compared with its observed place, the motion of the earth's centre and the position of the point round which it revolves has been determined, and the relative masses of the earth and moon thus found.

2614. 4°. By terrestrial gravity. — By what has been already explained, the space through which the moon would be drawn towards the earth in a given time by the earth's attraction can be determined. Let this space be expressed by s. The linear velocity \mathbf{v} of the moon in its orbit can also be determined. Now, if r be the radius of the orbit, we shall have (2614)

$$2 r \times s = v^2,$$

und consequently

$$r = \frac{V^2}{\sqrt{g}}$$

We find, therefore, the radius vector of the moon's orbit by dividing the square of its linear velocity by twice the space through which it would fall towards the earth in the unit of time. But this radius vector is the distance of the moon's centre from the common centre of gravity of the earth and moon. The distance of that point, therefore, from the centre of the earth, and consequently the ratio of the masses of the earth and moon, will be thus found.

All these methods give results in very near accordance, from which it is inferred that the mass of the moon is not less than the seventy-fifth, nor greater than the eightieth, part of the mass of the earth, and it is consequently the twenty-eighth millionth part of the mass of the sun.

2645. To determine the masses of the satellites. — The same differalties which attend the determination of the masses of the planets not accompanied by satellites also attend the determination of the masses of satellites themselves, and the same methods are applicable to the solution of the problem. The masses of the satellites of Jupiter and the other superior planets are ascertained in relation to those of their primaries by the disturbing effects which they produce upon the motions of each other.

2646. To determine the densities of the bodies of the system.—
The masses and volumes being ascertained, the densities are found
by dividing the masses by the volumes. Thus, if D and D' be the

that in the investigation of the superficial condition of the other bodies of the solar system, the determ tensities of the forces with which they attract bo near their surfaces, is a problem of considerable in

If the mass of the earth be expressed by m, it r, and the force of gravity on its surface by g, we express the same physical quantities in relation having the form of a globe, we shall have

$$g:g'::\frac{M}{r^2}::\frac{M'}{r^2}$$

because, by the general law of gravitation, the for ratio of the masses and the inverse ratio of the squa body from their centre, and in this case the attraction supposed to be at their surfaces, those distances a diameters.

From the preceding proportion may be inferred

$$\frac{g}{g'} = \frac{M}{M'} \times \frac{r^2}{r'^2},$$

by which the superficial gravity may always be or ratios of the masses and the diameters are known.

2648. Superficial gravity on the sun. — The being 355,000 times that of the earth, while its times that of the earth, we shall have

$$g:g'::1:\frac{355,000}{12,100}=28.9.$$

It annears, therefore that the weight of a hade ale

diameter of the moon is about the fourth part of that of the h. We have, therefore, in the case of the moon,

$$g:g'::1:\frac{16}{80}=\frac{1}{5};$$

hat the superficial gravity on the moon is five times less than on earth. The man weighing 1.5 cwt. on the earth would only weigh cwt., or the lbs., if transferred to the moon.

1650. Classification of the planets in three groups. — First mp — the terrestrial planets. — Of the planets hitherto discovi three which present in several respects remarkable analogies the earth, and whose orbits are included within a circle which seds the earth's distance from the sun by no more than one-half, a been from these circumstances denominated TERRESTRIAL METS. Two of these, MERCURY and VENUS, revolve within the it of the earth; and the third, MARS, revolves in an orbit outside t of the earth, its distance from the earth when in opposition only half the earth's distance from the sun.

- 851. Second group the planetoids. A chasm having a th measuring little less than four times the earth's distance, wated, for many ages after astronomy had made considerable ress, the terrestrial planets from the more remote members of system. The labours of observers during the last half century, hiefly during the last seven years, have filled this chasm with than twenty-three planets, distinguished from all the other s of the system by their extremely minute magnitudes, and by ircumstance of revolving in orbits very nearly equal. These have been distinguished by the name of ASTEROIDS or PLANs, the latter being preferable as the most characteristic and winte.
 - 2. Third group—the major planets.—Outside the planetoids, enormous distances from the sun and from each other, revolve anets of stupendous magnitude - named JUPITER, SATURN, 18. and NEPTUNE: the two former being visible to the naked re known to the ancients; the two latter are telescopic, and scovered in modern times.

CHAP. XIII.

THE TERRESTRIAL PLANETS.

I. MERCURY.

Period. — The nearest of the planets to the sun, and that pletes its revolution in the shortest time, is MERCURY.

Mandanes manerine

me period is found to be 87.97 days.

If the earth's period be expressed by therefore, be 0.2408.

2654. Heliocentric and synodic motion centric motion is, therefore (2568),

$$a = \frac{1296000}{87.97} = 14732''.5 = 2$$

The mean daily synodic motion is (2569)

 $\sigma = \alpha - \epsilon = 14732^{\circ} \cdot 5 - 3548^{\circ} \cdot 2 = 1118$

2655. Distance determined by greatest the ellipticity of the planet's orbit, its great to some variation. Its mean amount is, hothe radius r of the planet's orbit, drawn from the point of its greatest elongation, were the earth's distance from the sun as radius,

$$r = \frac{95,000,000}{57.3} \times 22^{\circ}.5 = 37,3$$

But the radius r being, in fact, the sine of itself, the value of r is a little less, being abou 2656. By the harmonic law.—If r expr planet, that of the earth being 1, we shall h

 $r^3 = 0.2408^2 = 0.387$ The distance of the planet is, therefore, 0.38 tance of the earth being 95 millions of mile

mean distance of the planet

tance is, therefore, subject to a variation in the ratio of 5 to nearly.

mean distances of the planet from the earth are, therefore,

$$95 - 36\frac{1}{4} = 59\frac{1}{4}$$
 mill. of miles at inf. conj. $95 + 36\frac{1}{4} = 131\frac{1}{4}$ " sup. conj.

construction of seven the seven seve

. Since of the orbit relatively to that of the earth. — The Merch and a part of that of the earth are exhibited on oper take in fig. 746, where s z is the earth's distance from



Fig. 746.

the sun, and mm''m the orbit of the planet. The lines Em'' drawn from the earth touching the orbit of the planet determine the positions of the planet when its elongation is greatest east and west of the sun. The points m are the positions of the planet at inferior and superior conjunction.

2659. Apparent motion of the planet. — The effects of the combination of the orbital motions of the planet and the earth upon the apparent place of the planet will now be easily comprehended.

Since the mean value of the greatest elongation $m'' = 8 = 22\frac{1}{2}^{\circ}$, the arc $mm'' = 67\frac{1}{2}^{\circ}$, and therefore $m'' m m'' = 67\frac{1}{2}^{\circ} \times 2 = 135^{\circ}$. The times of the greatest elongations

l west therefore divide the whole synodic period into two parts, in one of which, that from the greatest elongation ough inferior conjunction to the greatest elongation west, the gains upon the earth 135°; and in the other, that from the elongation west, through superior conjunction to the greatest on east, it gains $360^{\circ} - 135^{\circ} = 225^{\circ}$. Since the parts ich the synodic period is thus divided are proportional to igles, they will be (taking the synodic period in round num-116 days).

$$\frac{135}{360} \times 116 = 43\frac{1}{2} \text{ days};$$
 $\frac{225}{360} \times 116 = 72\frac{1}{2} \text{ days}.$

And since the former interval is divided equally by the epoch of inferior, and the latter by the epoch of superior, conjunction, it follows, that the intervals between inferior conjunction and greatest elongation are 211 days, and the intervals between superior conjunction and greatest elongation are 361 days.

The interval between the times at which the planet is stationary, before and after inferior conjunction, is subject to some variation, owing to the eccentricities of the orbits both of the planet and the earth, but chiefly to that of the planet's orbit, which is considerable. If its mean value be taken at 22 days, the angle gained by the planet on the earth in that interval being

$$3^{\circ} \cdot 11 \times 22 = 68^{\circ} \cdot 4$$
,

the angular distances of the points at which the planet is stationary from inferior conjunction as seen from the sun would be 34°2, which would correspond to an elongation of about 21°, as seen from the earth. This result, however, is subject to very great variation, owing to the eccentricity of the planet's orbit and other causes.

2660. Conditions which favour the abservation of an inferior planet. — These conditions are threefold; I. The magnitude of that portion of the enlightened hemisphere which is presented to the earth. 2. The elongation. 3. The proximity of the planet to the earth.

Since it happens that the positions which render some of these conditions most favourable render others less so, the determination of the position of greatest apparent brightness is somewhat complicated. When the planet is nearest to the earth, its dark hemisphere is presented towards us (2595); besides which, being in inferior conjunction, it rises and sets with the sun, and is only present in the day-time. At small elongations in the inferior part of the orbit, its distance from the earth is not much augmented, but it is still overpowered by the sun's light, and would only appear as a thin crescent when it would be possible to see it. At the greatest elongation, when it is halved, it is most removed from the interest elongation, even though it moves to a greater distance from the earth, since it gains more by the increase of its phase than it loses by increased distance and diminished elongation.

Owing to the very limited elongation of Mercury, that planes, even when its apparent distance from the sun is greatest, sets in the evening long before the end of twilight; and when it rises before the sun, the latter luminary rises so soon after it, that it is never free from the presence of so much solar light as to render it extremely difficult to see the planet with the naked eye.

In these latitudes, Mercury is therefore rarely seen with the naked eye. It is said that Copernicus himself never saw this

a circumstance which, however, may have been owing, in a gree, to the unfavourable climate in which he resided. In titudes, where the diurnal parallels are more nearly vertical atmosphere less clouded, it is more frequently visible, and is more conspicuous, owing to the short duration of twi-

diameter,—its mean and extreme values.—
the variation of the planet's distance from the earth, its meter is subject to a corresponding change. At its mane its apparent diameter is $4\frac{1}{2}$ ", and at its least disjuic value at the mean distance being $6\frac{1}{2}$ ".

a convenient and instructive comparison by which the apangulates of other objects may be indicated, and we shall
it frequently for that purpose. The disk of the full moon
an angle of 1800" to the eye. It follows, therefore, that
arent diameter of Mercury, when it appears as a thin crescent
brior conjunction, is about the 150th part, near the greatest
on it is the 280th part, and near superior conjunction the
art, of the apparent diameter of the moon. With a magpower of 140, it would therefore, at its greatest elongation,
with a disk half the apparent diameter of the moon.

. Real diameter. — The distance of Mercury in inferior conbeing 36% millions of miles, the linear value of 1" at it (2298)

$$\frac{59,250,000}{206,265} = 287.2 \text{ miles.}$$

distance its apparent diameter is $11\frac{1}{4}$ "; and if D'express its meter, we shall have

$$\mathbf{p}' = 287 \cdot 2 + 11 \cdot 25 = 3231$$
 miles.

bservations make the diameter somewhat less, and fix it at iles.

. Volume. — If v'express the volume, that of the earth, we shall have

$$\frac{\mathbf{v'}}{\mathbf{v}} = \frac{\mathbf{p'^3}}{\mathbf{p^3}} = \left(\frac{3231}{7912}\right)^3 = \frac{1}{14 \cdot 6}$$

Fig. 747.

The volume is therefore less than the 14th part of that of the earth. If the lesser estimate of the diameter of Mercury be adopted, it will follow that its volume is about the 17th part of that of the earth. The relative volumes are represented by M and E, fig. 747.

2664. Mass and density. - Some uncer-

so that the mass is 12; times less than that
If d' and d express the densities of the p
shall therefore have

$$\frac{d'}{d} = \frac{M'}{M} \times \frac{V}{V'} = \frac{100}{1225} \times \frac{147}{10} = \frac{1}{10}$$

Other estimates make it 1.12. So that it m density of Mercury exceeds that of the eafifth.

2665. Superficial gravity. — If g' expres on the surface of Mercury, g being the forcearth, we shall have (2639)

$$\frac{g'}{g} = \frac{M'}{M} \times \frac{D'^2}{D^2} = 0.5.$$

The superficial gravity is therefore only half earth. Muscular and other forces not depe therefore twice as efficacious. The height twould fall in a second would be 96½ inches eight feet.

2666. Solar light and heat. — The apparsun is greater than upon the earth, in the sam is less; and owing to the considerable ellipticit has apparent magnitudes sensibly different Mercury's year. The apparent diameter of the earth being 30', its apparent diameter seen fro

In fig. 748, 9, the relative apparent magnitudes of the sun, as seen from the earth and from Mercury, at the mean distance and





Fig. 748.

Fig. 749.

extreme distances, are represented at E, M, M', and M''. If E be supposed to represent the apparent disk of the sun as seen from the earth, M will represent it as it appears to Mercury at the mean distance, M' at aphelion and M'' at perihelion.

Since the illuminating and heating power of the sun's rays, whatever be the physical condition of the surface of the planet, must vary in the same proportion as the apparent area of the sun's disk, it follows, that the light and warmth produced by the sun on the surface of the planet will be greater in perihelion than in aphelion, in the ratio of 9 to 4, and, consequently, there must be a succession of scasons on this planet, depending exclusively on the ellipticity of the orbit, and having no relation to the direction of its axis of rotation or the position of the plane of its equator with relation to that of its orbit. The passage of the planet through its perihelion must produce a summer, and its passage through aphelion a winter, the mean temperature of the former ceteris paribus being above twice that of the latter.

If the axis of the planet be inclined to the plane of its orbit, mother succession of seasons will be produced, dependent on such inclination and the position of the equinoctial points. If these points coincide with the apsides of the orbit, the summers and winters arising from both causes will either respectively coincide, or the summer from each cause will coincide with the winter from the other. In the former case, the intensities of the seasons and their extreme temperatures will be augmented by the coincidence, and in the latter they will be mitigated; the summer heat from each cause tempering the winter cold from the other.

If, on the other hand, the line of apsides be at right angles to the direction of the equinoxes, the summer and winter from each cause will correspond with the spring and autumn from the other, and a curious and complicated succession of seasons must ensue, depending on the degree of obliquity of the axis of the planet, compared with the effects of the eccentricity of its orbit.

In comparing the calorific influence of the sun on Mercury and

The intensity of the solar light must be grea in the ratio of four to one when the planet is it to one when in perihelion. Its effects on visit rendered the same by the manifest of the provided the same by the control of the same by the same

of the pupil of the eye. (1129.) 2667. Method of ascertaining the diurne planets. - One of the most interesting objec quiry regarding the condition of the planets is their diurnal rotation. In general, the manner seek to ascertain this fact would be, by exami telescopes the marks observable upon the disk the planet revolve upon an axis, these marks, l with it, would appear to move across the disk : other; they would disappear on one side, and, 1 tain time invisible, would reappear on the other across the visible disk. Let any one stand at common terrestrial globe, and let it be made axis: the spectator will see the geographical ma pass across the hemisphere which is turned towar successively disappear and reappear. The san course, be expected to be seen upon the seve have a motion of rotation resembling the diur globe.

2568. Difficulty of this question in the case of is a species of observation which has not yet made in the case of Mercury. Sir John Her joyed more than common advantages for teleproduct different alignment.

claims the discovery of mountains on Mercury, and even assigns their height, estimating one at 2132 yards, and another 18,978 yards.

These observations, not having been confirmed, must be considered

apochryphal.

II. VENUS.

2670. Period. — The next planet proceeding outwards from the san is Yapus, which revolves in an orbit within that of the earth, and which, after the sun and moon, is the most splendid object in the firmament.

The synodic period, ascertained by observation, is 584 days. Her period deduced from this (2589) is, therefore,

$$\frac{1}{P} = \frac{1}{865 \cdot 25} - \frac{1}{584} = \frac{1}{225}.$$

By the other methods it is more exactly determined to be 224.7

If the earth's period be taken as the unit, that of Venus will, therefore, be 0.61.

2671. Heliocentric and synodic motions. — The mean daily heliocentric motion of Venus is, therefore (2568),

$$a = \frac{1296000}{224.7} = 5768'' = 96'.13 = 1^{\circ},$$

and the mean daily synodic motion is (2569)

$$\sigma = \alpha - \epsilon = 5768'' - 3548'' = 2220'' = 37'$$
.

2672. Distance, by greatest elongation. — The mean amount of greatest elongation of Venus being found by observation to be about 45° or 46°, it follows that in that position lines drawn to the earth and sun from the planet would form the sides of a square, of which the earth's distance from the sun is the diagonal. If, therefore, the earth's distance be expressed by 1.0000, that of Venus would be 0.7071.

3673. By the harmonic law.—If r express the mean distance of the planet from the sun (2621), we have

$$r^3 = 0.61^2 = 0.719^3$$
.

Therefore r = 0.719; and since the mean distance of the earth is 95 millions of miles, we shall have

$$r' = 95,000,000 \times 0.719 = 68,300,000.$$

By more exact methods the distance is found to be 68‡ millions of miles.

2674. Mean and extreme distances from the earth.—Its distances

 $68\frac{1}{4} - 0\frac{1}{4} = 68\frac{1}{4}$ millions of miles in 1 $68\frac{1}{4} + 0\frac{1}{4} = 69\frac{1}{4}$ " a

These distances of the planet from the earth a to an increase and diminution, amounting to half due to the eccentricity of the planet's orbit, an million of miles due to that of the earth's orbit.

2675. Scale of the orbit relative to that of th



Fig. 750.

tion of the or earth is repre where sE rep distance from the mean dian orbit on the angles SE v" 1 est elongation is about 46°. gations v" E S the planet app a full disk, or or as a cresceu 2676. Api Since the m greatest elong to be 46°, the v'' 8 E = 44°. the angle v" tween the or

The intervals between inferior conjunction and greatest elongation are therefore 71½ days, and the intervals between superior conjunc-

tion and greatest elongation are 2201 days.

2677. Stations and retrogression. — From a comparison of the orbital motions and distances of the earth and planet, it is found that the epochs at which it is stationary are about twenty days before and after inferior conjunction. Now, since the planet gains 0°-61 per day upon the earth, this interval corresponds to an angle of

 $20 \times 0^{\circ} \cdot 61 = 12^{\circ} \cdot 2$

at the sun, which corresponds to an elongation of 25°.

The arc of retrogression is little less than a degree.

2678. Conditions which favour the observation of Venus.—This planet presents itself to the observer under conditions in many respects more favourable for telescopic examination than Mercury. The actual diameter of Venus is more than twice that of Mercury. It approaches nearer to the earth in the inferior part of its orbit in the ratio of 13 to 30. It elongates itself from the sun to the distance of 46°, while the elongation of Mercury is limited to 22½°. The latter is never seen, except in strong twilight. Venus, especially in the lower latitudes, is seen at a considerable elevation long after the cessation of evening and before the commencement of morning twilight, and when she has a gibbous or a crescent phase. The planet appears brightest when its elongation is about 40° in the superior part of her orbit.

2679. Evening and morning star. — Lucifer and Hesperus. — This planet for these reasons is, next to the sun and moon, the most conspicuous and beautiful object in the firmament. When it has western elongation, it rises before the sun, and is called the MORNING STAR. When it has eastern elongation, it sets after the sun,

and is called the EVENING STAR.

The ancients gave it, in the former position, the name LUCIFER

(the harbinger of day), and in the latter HESPERUS.

2680. Apparent diameter.—Owing to the great difference between its distance from the earth at inferior and superior conjunctions, the apparent diameter of this planet varies in magnitude within wide limits. At superior conjunction it is only 10", from which to inferior conjunction it gradually enlarges until it becomes 62", and in some positions even so much as 76". At its greatest clongation its apparent diameter is about 25", and at its mean distance 164".

Thus, when the planet appears as a thin crescent immediately before or after inferior conjunction, the magnitude is such that the line joining the cusps is the 30th part of the line joining the cusps of the crescent moon, and a telescope having a magnifying power no greater than 30 will show it with an apparent size equal to that

of the crescent moon to the naked eye.

sequently contended that the best position for is near superior conjunction, when its phase proper expedients it may be observed at mingrees of the sun's disk.

2682. Real diameter. — The linear value she appears as a thin crescent near her inferic

$$\frac{26,250,000}{206,265} = 127.2 \text{ mil}$$

At this distance her apparent diameter is 6 her real diameter, we shall have

$$p' = 127.2 \times 61 = 7760 \text{ i}$$

The magnitude of Venus is, therefore, nearly

2683. Mass and density.—By the methods it has been ascertained that the mass of Venu of the earth in the ratio of 113 to 100; and nearly equal, their densities are also nearly equ

2684. Superficial gravity. — All the condigravity of bodies on the surface of Venus bein so, as those which affect bodies on the earth, the

is nearly the same.

2685. Solar light and heat. — The density greater than upon the earth in the inverse rathe numbers 7 and 10, which express their different the intensity is, therefore, greater at Venus in

The relative apparent magnitudes of the sun

ations which might have been expected to demonstrate it in a tory manner have been obstructed by the causes already no-2681). Nevertheless, Cassini, in the 17th century, and er, towards the close of the 18th, with instruments very infethe telescopes of the present day, deduced from the phases a of rotation in complete accordance with the results of the cent observations.

e astronomers found that the points of the horns of the tobserved between inferior conjunction and greatest elongapeared at certain moments to lose their sharpness, and to as it were blunted. This appearance was, however, of very uration, the horn after some minutes always recovering its ses. Such an effect would obviously be produced by a local arity of surface on the planet, such as a lofty mountain, which throw a long shadow over that part of the surface which form the point of the horn. Now, admitting this to be the fit the phenomenon, it ought to be reproduced by the same in at equal intervals, this interval being the time of rotation planet. Such a periodical recurrence was accordingly as-

1. Observations of Cussini, Herschel, and Schröter. — From bservations the elder Cassini, so early as 1667, inferred the rotation of the planet to be 23th 16th, a period not very different that of the earth. Soon after this, Bianchiui, an Italian mer, published a series of observations tending to call in the result obtained by Cassini, and showing a period of 576

Sir William Herschel resumed the subject, aided by his al telescopes, in 1780, but without arriving at any satisfactory except the fact that the planet is invested with a very dense here. He found the cusps (contrary to the observations of , and, as we shall see, of more recent astronomers) always and free from irregularities. Schröter made a series of most ite observations on this planet, with a view to the determinaits rotation. He considered not only that he saw periodical s in the form of the points of the horns, but also spots, which efficient permanency to supply satisfactory indications of rota-From such observations he inferred the time of rotation to be From observations upon the horns, he inferred at the southern hemisphere of the planet was more mountainin the northern; and he attempted, from observations on the ess periodically produced on the southern point of the crescent, mate the height of some of the mountains, which he inferred unt to the almost incredible altitude of twenty-two miles.

8. Observations of M.M. Beer and Müdler—time of rota--Although the estimate of the planet's rotation resulting from servations of Schröter, corroborating those of Cassini, has been

ASTRONOMY.

y accepted by the scientific world, the question was not reas definitely settled; and a series of observations was made. Beer and Mädler, between 1833 and 1836, which went far rm the conclusions of Cassini and Schröter; and the still cent observations of De Vico at Rome may be considered as g all doubt that the period of the planet's rotation does not ch from 234.

Beer and Mädler's diagrams of Venus.—In fig. 752, esented a series of eighteen diagrams of the planet, selected much greater number made by MM. Beer at d. Mädler at is indicated above. These drawings were taken when the



In corrotoration of the observations of Schröter, it was ascertained hat the southern cusp was subject to greater and more frequent hanges of form than the northern, from which it was inferred that he southern hemisphere of the planet is the more mountainous. It is remarkable that the same character is found to prevail on the moon.

It was not only observed that the irregularities of the concave edge of the crescent were subject to a change visible from 5^m to 5^m, not that the same forms were reproduced after an interval of 23½^h,

subject to an error not exceeding from 5 to 10 minutes.

2690. More recent observations of De Vico. — In fine, De Vico, beerving at a still later date at Rome, favoured by the clear sky of laly, made several thousand measurements of the planet in its bases, the general result of which is in such complete accordance with those of MM. Beer and Mädler, that the fact of the planet's parties may now be regarded as satisfactorily demonstrated, and

hat its period does not differ much from 23th 15m.

2001. Direction of the axis of rotation unascertained. — If such the casily conceived that those which have attended the attempts is extain the direction of the axis of rotation have been much be insurmountable. The observations above described, by which is rotation has been established, supply no ground by which the rotation of the axis could be ascertained. No spot has been seen in direction of whose motion could indicate that of the axis. It as conjectured, with little probability, by some observers, that the xis was inclined to the orbit at the angle of 75°. This conjecture, lowever, has not been confirmed.

2692. Twilight on Venus and Mercury. — The existence of an atensive twilight in these planets has been well ascertained. By beerving the concave edge of the crescent which corresponds to the countary of the illuminated and dark hemispheres, it is found that he enlightened portion does not terminate suddenly, but there is a gradual fading away of the light into the darkness, produced by the mad of atmosphere illuminated by the sun which overhangs a part of the dark hemisphere, and produces upon it the phenomena of wilight.

Some observers have seen on the dark hemisphere of the planet Venus a faint reddish and grayish light, visible on parts too distant rom the illuminated hemisphere to be produced by the light of the mn. It was conjectured that these effects are indications of the play of some atmospheric phenomena in this planet similar to the aurora insertice.

In fine, it may be stated generally, that so far as relates to the bysical condition of the inferior planets, the whole extent of our ertain knowledge of them is, that they are globes like the earth,

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d and warmed by the sun; that they are invested with es probably more dense than that of the earth; and since ns render probable the existence of vast masses of clouds if not on Mercury, analogy justifies the inference that

ist on these planets.

Spheroidal form unascertained—suspected satellite. e phenomena from which the rotation, as well as the direce axis, might be inferred, is the spheroidal form of the To ascertain this by observations of the disk, it would be to see the planet with a full phase. But when the inferior eve that phase, they are near superior conjunction, and lost in the solar light. It has been nevertheless contended, Venus is most remote from her node, she is sufficiently from the plane of the ecliptic to be observed with a good

at noon when in superior conjunction. No observation, of this kind has ever yet been made, and the spheroidal

e planet is unascertained.

observers of the last two centuries concurred in maintainthey had seen a satellite of Venus. Cassini, the elder, he saw such a body near the planet on the 25th of Jan-2, and again on 27th of August, 1686; Short, the well-

$$\frac{1}{P} = \frac{1}{365} - \frac{1}{780} = \frac{1}{687}.$$

The periodic time of Mars is therefore 687 days, or, as appears by more exact methods of calculation and observation, 686.979 days.

The earth's period being taken as the unit, the period of Mars will therefore be 1.881.

2696. Distance. — To compute by the Harmonic Law the mean distance of Mars from the sun, we have therefore

$$1.88^{\circ} = 1.5246^{\circ}$$
.

The mean distance is therefore 1.5246, that of the earth being the unit, and the mean distance in miles is

$$95,000,000 \times 1.524 = 144,780,000$$

or about 1442 millions of miles.

2697. Eccentricity — mean and extreme distances from the esrth. — The eccentricity of the orbit of Mars being about 0.09, the distance is subject to a variation, the extreme amount of which is less than one-tenth of its mean value. The extreme distances

$$144\frac{3}{2} + 13 = 157\frac{3}{2}$$
 million miles in aphelion.
 $144\frac{3}{2} - 13 = 131\frac{3}{2}$ million miles in perihelion.

It appears, therefore, that the mean distances of the planet from the earth are

These distances are subject to variation, whose extreme limit is about 15 millions of miles, owing to the combined effects of the eccentricities of the two orbits. Although the mean distance of the planet in opposition from the earth is about half the distance of the sun, it may in certain positions of the orbit come within a distance of 35 hundredths of the sun's distance. In the opposition which took place in September, 1830, the distance of the planet was only 38 hundredths of the sun's mean distance.

2698. Heliocentric and synodic motions. — The mean daily Heliocentric motion of Mars is (2568)

$$a = \frac{1296000}{687} = 18'' \cdot 86 = 31' \cdot 1.$$

The mean synodic motion is therefore (2569)

$$\sigma = \bullet - \bullet = 3548 - 1886 = 16^{\circ} \cdot 62 = 27^{\circ} \cdot 7.$$

2699. Scale of orbit relatively to that of the earth. — If s, fig. 753, represent the position of the sun, and s m the distance of Mars, the orbit of the earth will be represented by E E' E'' E'.

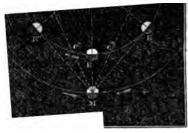


Fig. 753.

mean 1.52, press the a: 48°, 180°

Sin is 780 between position

$$\frac{48}{360} \times 780 = 104 \text{ days}$$

and the mean time between quadrature and oc

$$\frac{132}{360} \times 780 = 286 \text{ days}$$

2701. Apparent motion. — The various che positions of the planet and sun during the therefore, be easily explained. At conjunction et and sun pass the meridian to the planet being above the horizon only during After conjunction, the planet passes the meriand is therefore visible above the eastern horizon fore conjunction it passes the meridian in therefore visible above the western horizon after the planet passes the meridian in the planet passes the pla

At the time of the western quadrature, the planet passes the manifestation

said is therefore above the herizing shiely during the earlier part of the night.

The interval during which it it visible more or less in the absence of the sun, being that during which it passes from western to eastern quadrature through opposition is, in the case of Mars, 104×1000 m = 208 days.

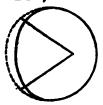
2702. Stations and retrogramion. — The elongations at which Mans is stationary, and the lengths of his are of retrogramion, vary some extent with the distances of the planet from the sun and with, which distances depend on the ellipticity of the two orbits, the direction of their major axes. In 1864, Mars will be in Marshiton on 1st March, and will be stationary on the 17th January and 10th April. The right ascension on these days will be,

17 Jan B. A	11 ^k	19 -	82° 56
•		14	86

It follows, therefore, that the extent of retrogression in right mesension will then be 14-36, which reduced to angular magnitude is

$$(14-36) \times 15 = 219' - 8°89'.$$

2703. Phases.—At opposition and conjunction the same hemisphere being turneds the earth and sun, the planet appears with a fell phase. In all other positions the lines drawn from the phase to the earth and sun, making with each other an acute angle of greater or less magnitude, the phase will be deficient of complete falces, and the planet will be gibbous; the more so the nearer it is to its quadrature, in which position the lines drawn to the earth and was make the greatest possible angle, which being the complement of zero, will be 90°—48° = 42°. Of the entire hemisphere



Te. 164

presented to the earth, 188° will therefore be enlightened and 42° dark. The corresponding form of the disk, as can easily be deduced from the common principles of projection, will be that which is represented in fig. 754, the dark part being indicated by the dotted line.

The gibbosity will be less the nearer the planet approaches to opposition or conjunction.

8704. Apparent and real diameter. — The apparent diameter of Mars in opposition varies

between rather wide limits, in consequence of the variation of its distance from the earth in that position, arising from the causes explained above. When at its mean distance at opposition, the apparatus of the causes are plained above.

the clameter D of the planet must be

$$D' = 185.7 \times 22 = 4085$$

2705. Volume. — If v' be the volume, the we have

$$\frac{\mathbf{v}'}{\mathbf{v}} = \left\{ \frac{4085}{7900} \right\}^{\bullet} = \frac{1}{7.5} = 0$$

The volume is therefore less than the seven earth. The relative volumes of Mars and that M and E, fig. 755.

2706. Mass and density. — By the metl been ascertained that the mass of Mars is being 1000.

We shall have for the density, therefore,

$$\frac{d'}{d} = \frac{145}{133} = 1.09.$$

The density is very nearly equal, therefore, t 2707. Superficial gravity.—The superficial mined by the formula (2639), we shall have

$$\frac{g'}{g} = 0.54.$$

It appears, therefore, that the force of grav. Mars is a little more than half its intensity earth.

2708. Solar light and heat. — The mean from

Since the density of the solar radiation decreases as the square of the distance increases, its density at Mars will be less than at the earth in the ratio of 4 to 9.

So far as the illuminating and heating powers of the solar rays depend on their density, they will, therefore, be less in the same

proportion.

2709. Rotation. — There is no body of the solar system, the moon alone excepted, which has been submitted to so rigorous and successful telescopic examination as Mars. Its proximity to the earth in opposition, when it is seen on the meridian at midnight with a full phase, affords great facility for this kind of observation.

By observing the permanent lineaments of light and shade exhibited by the disk, its rotation on its axis can be distinctly seen, and has been ascertained to take place in 24^h 87^m 10^h, the axis on which it revolves appearing to be inclined to the plane of the planet's whit at an angle of 28° 27'. The exact direction of the axis is,

lowever, still subject to some uncertainty.

2710. Days and nights.—It thus appears that the days and nights in Mars are nearly the same as on the earth, that the year sidversified by seasons, and the surface of the planet by zones and simates not very different from those which prevail on our globe. The tropics, instead of being 23° 28', are 28° 27' from the equator, and the polar circles are in the same proportion more extended.

2711. Seasons and climates. — The year consists of 668 Martial lays and 16 hours; the Martial being longer than the terrestrial day

in the ratio of 100 to 97.

Owing to the eccentricity of the planet's orbit, the summer on the northern hemisphere is shorter than on the southern in the ratio of 100 to 79, but owing to the greater proximity of the sun, the intensity of its light and heat during the shorter northern summer is greater than during the longer southern summer in the ratio of 145 to 100. From the same causes, the longer northern winter is less inclement than the shorter southern winter in the same proportion.

There is thus a complete compensation in both seasons in the two

hemispheres.

The duration of the seasons in Martial days in the northern hemiphere is as follows:—spring 192, summer 180, autumn 150, winter 147.

2712. Observations and researches of Messrs. Beer and Mädler.—It is mainly to the persevering labours of these eminent observers that we are indebted for all the physical information we possess respecting the condition of the surface of this planet. Their observations, commenced at an early epoch, were regularly organised at the time of the opposition of 1880, with a view to ascertain with testainty and precision the time of rotation of the planet, the position of its axis, and, so far as might be practicable, a survey of its

These observations have been continued during every opposition, in which the planet having northern declin a sufficient altitude, and was made visible by a telesconcer, of four and a half feet focal length, parallacted, and moved by clockwork, so as to keep the planet of view notwithstanding the diurnal motion of the this instrument they were enabled to use a magnifying and as the disk of the planet subtended in 1830 a of 22", it was, when thus magnified, viewed under an 0" or 110', being nearly four times the apparent diameter.

on.

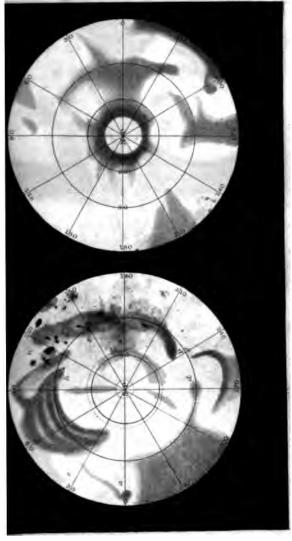
3. Areographic character. — That many of the linea ed are areographic, and not atmospheric, is established by their permanency. They are not always when visible not always equally distinct; but are observed the same forms, no matter how distant may be the injusted they may be submitted to examination. The elast has and observations of MM. Beer and Mädler, which is with the opposition of 1830, were continued with unwith the energy succeeding opposition of the planet for so far as the varying declination and the state of the way.



MARS



 $\frac{M(A|R/S)}{(1+\alpha)^{2}(1+\alpha)^{2}(1+\alpha)^{2}} = \frac{M(A|R/S)}{(1+\alpha)^{2}(1+\alpha)^{2}(1+\alpha)^{2}(1+\alpha)^{2}} = \frac{1}{12} \frac{M(A|R/S)}{(1+\alpha)^{2}(1+\alpha)^{2}(1+\alpha)^{2}} = \frac{1}{12} \frac{M(A|R/S)}{(1+\alpha)^{2}(1+\alpha)^{2}(1+\alpha)^{2}} = \frac{1}{12} \frac{M(A|R/S)}{(1+\alpha)^{2}(1+\alpha)^{2}(1+\alpha)^{2}} = \frac{1}{12} \frac{M(A|R/S)}{(1+\alpha)^{2}(1+\alpha)^{2}} = \frac{1}{12} \frac{M(A|R/S)}{(1+\alpha)^{2}} = \frac{1}$



ented the appearance of a dazzling whiteness, and one of them so exactly defined and so sharply terminated, that it seemed the full disk of a small and very brilliant planet projected upon disk, and near the edge of a larger and darker one. The apance, position, and changes of these white polar spots have sugsid to all the observers who have witnessed them, the suppositions that they proceed from the polar snows accumulated during long winter, and which, during the equally protracted summer, apposure to the solar rays, more full by 7° degrees than at the soft the earth, are partially dissolved, so that the diameter of mow circle is diminished.

he increase and diminution of this white circle takes place at hs and in positions of the axis of the planet, such as are in

plete accordance with this supposition.

716. Position of areographic meridians determined.—The leg foot-shaped spot marked p n in the southern hemisphere, was netly seen and delineated in all the oppositions. This was one be spots from the apparent motion of which the time of rotawas deduced.

be spot a in the southern hemisphere connected with a large cent spot by a sinuous line, was also one of those whose position most satisfactorily established. This spot was selected as the rvatory of Greenwich has been upon the earth, to mark the idian from which longitudes are reckoned.

he spot efh, chiefly situate in the southern, but projecting into northern hemisphere between the 90th and 105th degrees of itude, was also well observed on repeated occasions.

secording to Madler, the reddish parts of the disk are chiefly

which correspond to 40° long. and 15° lat. S.

he two concentric dotted circles marked round the south pole cate the limits of the white polar spot as seen on different occas in 1830 and 1837. The redness of this planet is much more arkable to the naked eye than when viewed with the telescope. some cases, during the observations of MM. Beer and Madler, edness was discoverable, and when it was perceived it was so; that different observers at the same moment were not agreed its existence. It was found that the prevailing colour of the was generally yellow rather than red.

reshortening, it was found that the lineaments were always seen much greater distinctness near the centre of the disk than tois its borders. This is precisely the effect which might be ex-

sd from a dense atmosphere surrounding the planet.

17. Possible satellite of Mars. — Analogy naturally suggests probability that the planet Mars might have a moon. These shants appear to be supplied to the planets in augmented num-

if such existed, must be extremely small. Jupiter is only the forty-third part of thand a satellite which would only be the ameter of Mars, would be under one hur Such an object could scarcely be discover scopes, especially if it do not recede far planet.

The fact that one of the satellites of Sa only within the last few years, renders it no that a satellite of Mars may yet be discover

CHAP. XIV.

THE PLANETOIDS.

2718. A vacant place in the planetary see epoch in the progress of astronomy it was a gression of the distances of the planets from ised by a remarkable numerical harmony, in breach of continuity existed between Mar arithmetical progression was first loosely not was not until towards the close of the last exact conditions of the law and the close do with which it was fulfilled with the area.

e succession of calculated distances from Mercury's orbit, ll exactly fulfil it in juxtaposition with the actual distances knets, the earth's distance from the sun being the unit.

	Calculated Distance from Mercury.	Actual Distance from Mercury
	0.3362	0-3362
	0-6724	0.6129
••••••	1-3448	1.1386
	2-6896 5-8792	4-8187
***************************************	10-7584	9-1517
••••••••••••	21-5168	18-7963

nparing these numbers, it will be apparent that although smon of distances does not correspond precisely with a nuseries in duple progression, there is nevertheless a certain to such a series, and at all events a glaring breach of conetween Mars and Jupiter.

ds the close of the last century, professor Bode of Berlin his question of a deficient planet, and gave the numerical on which indicated its absence in the form in which it has a stated; and an association of astronomers was formed a auspices of the celebrated Baron de Zach of Gotha, for as purpose of organising and prosecuting a course of obsertith the special purpose of searching for the supposed undispendent of the solar system. The very remarkable results we followed this measure, the consequences of which have yet been fully developed, will presently be apparent.

Discovery of Ceres.—On the first day of the present Professor Piazzi observing in the fine serene sky of Palermo, small star of about the 7th or 8th magnitude which was tered in the catalogues. On the night of the 2nd again obt, he found that its position relative to the surrounding stars bly changed. The object appearing to be invested with a haze, he took it at first for a comet, and announced it as he scientific world. Its orbit being however computed by: Gauss, of Göttingen, it was found to have a period of 12, and a mean distance from the sun expressed by 2.785, he earth being 1.

mparing this distance with that given in the preceding table a planet was presumed to be absent, it will be seen that thus discovered filled the place with striking arithmetical

Discovery of Pallas. — Soon after the discovery of Ceres.

**Bearing into conjunction ceased to be visible. In search-

for it after emerging from the sun's rays in March ers noticed on the 28th a small star in the constellation place which he had examined in the two preceding m re he knew that no such object was then apparent. I star of the seventh magnitude, the smallest which out a telescope. In the course of a few hours he for n visibly changed in relation to the surrounding stars. object proved to be another planet bearing a striking es, and what was then totally unprecedented in th ing in an orbit at very nearly the same mean distance and having therefore nearly the same period.

r. Olbers called this planet PALLAS.

721. Olbers' hypothesis of a fractured planet. — Th ce, combined with the exceptional minuteness of ets, suggested to Olbers the startling, and then, as it eared, extravagantly improbable hypothesis, that a sin he ordinary magnitude existed formerly at the distance Bode's analogy, - that it was broken into small fragm nternal explosion from some cause analogous to volca y collision with a comet,—that Ceres and Pallas were

antity far exceeding the entire inclination of any of the older

It was further observed by Dr. Olbers, that at a point near the seending node of Pallas the orbits of the two planets very nearly neided.

Thus it appeared that all the conditions which rendered these lies exceptional, and in which they differed from the other mems of the solar system, were precisely those which were consistent as the hypothesis of their origin advanced by Dr. Olbers.

2722. Discovery of Juno. — A year and a half elapsed before further discovery was produced to favour this hypothesis. Meanile, observers did not relax their zeal and their labours, and on pt. 1, 1804, at ten o'clock, P.M., Professor Harding, of Liliend, discovered another minute planet, which observation soon wed to agree in all its essential conditions with the hypothesis of bers, having a mean distance very nearly equal to those of Ceres i Pallas, an exceptional obliquity of 13°, and a considerable entricity.

This planet was named Juno.

Juno has the appearance of a star of the 8th magnitude, and a ldish colour. It was discovered with a very ordinary telescope 30 inches focal length and 2 inches aperture.

2723. Discovery of Vesta. — On the 29th of March, 1807, Dr. bers discovered another planet under circumstances precisely rilar to those already related in the cases of the former discoveries. so name VESTA was given to this planet, which, in its minute graitude and the character of its orbit, was analogous to Ceres, thus, and Juno.

Vesta is the brightest and apparently the largest of all this group planets, and when in opposition may be sometimes distinguished good and practised eyes without a telescope. Observers differ in in impressions of the colour of this planet. Harding and other reman observers consider her to be reddish; others contend that is perfectly white. Mr. Hind says that he has repeatedly extined her under various powers, and always received the impression of a pale yellowish cast in her light.

2724. Discovery of the other Planetoids.— The labours of the servers of the beginning of the century having been now prosested for some years without further results, were discontinued, and is probable that but for the admirable charts of the stars which we been since published, no other members of this remarkable cap of planets would have been discovered. These, however, III.

ng all the stars up to the 9th or 10th magnitude, in zone of the firmament 30° in width, extending to be of the celestial equator, supplied so important and ument of research, that the subject was again resume prospect of successful results. It was only necessiver, map in hand, to examine, degree by degree, twhich such bodies are known to move, and to compute heavens with the map. When a star is observe marked on the map, it is watched from hour to hight to night. If it do not change its position it that it has been omitted in the construction of the smarked upon it in its proper place. If it change must be inferred to be a planet, and its orbit is soon its observed changes of position.

hese means M. Henke, an amateur observer of Dr., discovered on the 8th December, 1845, another

lanets, which has been named Astræa.

e that time the progress of planetary discovery in the has advanced with extraordinary rapidity. Three scovered in 1847, one in 1848, one in 1849, three in 1851, and, in fine, not less than eight in 1852.

2725. Table showing the number of Planetoids discovered before let January, 1853, the names conferred upon them, their discoverers, and the dates of their discovery.

	Name.	Discoverer.	When discovered.	Place of Observation.
1 2 3 4 6 6 7 8 9 10	Corea. Pallas. Juno. Vesta. Astron. Hebs. Iris. Flore. Metis. Hygeis.	Piassi. Olbers. Harding. Olbers. Henke. Henke. Hind. Hind. Graham. De Gaspars.	Jan. 1, 1801. March 28, 1802. Sept. 1, 1804. March 29, 1807. Dec. 8, 1845. July 1, 1847. Oct. 18, 1847. April 25, 1848. April 12, 1849.	Palermo. Bremen. Lilienthal. Bremen. Dreissen (Prussis). Dreissen. London. London. London. Markree (Ireland). Naples.
11	Parthenope. Victoria (called Clio by American astronomers).	De Gasparis. Hind.	May 11, 1850. Sept. 13, 1850.	Naples. London.
18 14 15 16 17 18 19 20 21 22	Egeria. Irene.* Eunomia. Pyache. Thetia. Melpomene. Fortuna. Massalia. Lutetia. Calliope. Thalia.	De Gasparis. Hind. De Gasparis. De Gasparis. Luther. Hind. Chacornac. Goldschmit. Hind. Hind.	Nov. 2, 1850. May 19, 1851. July 29, 1851. March 17, 1852. April 17, 1852. June 24, 1852. Aug. 22, 1852. Sept. 20, 1852. Nov. 16, 1852. Nov. 16, 1852. Dec. 16, 1852.	Naples. London. Naples. Naples. Bilk (Dusseldorf). London. London. Marseilles. Paris. London. London.

This planet was discovered by M. de Gasparis four days later, at Naples, before that astronomer had received the information of the discovery of Mr. Hind.

2726. The discovery of these mainly due to amateur astronomers. — Dr. Olbers was a practitioner in medicine, Messrs. Henke, Luther, and Goldschmit, amateur observers, Mr. Hind has been engaged in the private observatory of Mr. Bishop, in the Regent's Park, and Mr. Graham in that of Mr. Cooper, at Markree, in the county of Sligo, in Ireland. It appears, therefore, that of these twenty-three members of the solar system, the scientific world owes no less than fourteen to amateur astronomers, and observatories erected and maintained by private individuals, totally unconnected with any national or public establishments, and receiving no aid or support from the state. Mr. Hind has obtained for himself the honourable distinction which must attach to the discoverer of eight of these bodies. Five are due to M. de Gasparis, assistant astronomer at the Royal Observatory at Naples.

M. Hermann Goldschmit is an historical painter, a native of Frankfort on the Maine, but resident for the last eighteen years in Paris. He discovered the planet with a small ordinary telescope, placed in the balcony of his apartment, No. 12 rue de Seine, in the

Faubourg St. Germain.

2727. Their remarkable accordance with Dr. Olbers' hypothesis.

e orbits of several of those observed in 1852 have calculated, but all those which have been computed a between the mean distances 2.2 and 3.2, that to the The magnitudes of all of these bodies, with xceptions, are too minute to be ascertained by any m rement hitherto discovered, and may be inferred wit bility not to exceed 100 miles in diameter. The lar roup is probably less than 500 miles in diameter. It herefore, to be observed in how remarkable a manu rm to the conditions involved in the hypothesis of Dr. 28. Force of gravity on the planetoids. - From the of their masses, the force of gravity on the surfaces of must be very inconsiderable, and this would accoun greater altitude of their atmospheres than is observed planets, since the same volume of air feebly attracted into a volume comparatively enormous. Muscular be more efficacious on them in the same proportion. night spring upwards sixty or eighty perpendicular for to the ground, sustaining no greater shock than would the earth in descending from the height of two or the 2730. Period.—The synodic period of Jupiter is accertained by observation to be 898 days. Hence to obtain its periodic time P, we have (2589)

$$\frac{1}{P} = \frac{1}{865 \cdot 25} - \frac{1}{898} = \frac{1}{4882 \cdot 6}$$

The period is therefore 4882.6 days, or 11.86 years.

2731. Heliocentric and Synodic motions. — The daily angular heliocentric motion of Jupiter is therefore

$$\frac{860^{\circ}}{4388} = 0^{\circ} \cdot 088 = 5'.$$

The mean angle gained daily by the earth or sun upon Jupiter, is therefore

$$0^{\circ} \cdot 9856 - 0^{\circ} \cdot 088 = 0^{\circ} \cdot 9026 = 54' \cdot 156.$$

2732. Distance. — The distance of Jupiter from the sun may be computed by means of the Harmonie Law (2621), the period being known. This method gives

$$(11.83)^3 = (5.2028)^3$$
.

The mean distance of Jupiter from the sun is therefore 5½ times that of the earth; and since the earth's mean distance is 95 millions of miles, that of Jupiter must be 494 millions of miles.

The eccentricity of Jupiter's orbit being 0.048, this distance is liable to variation, being augmented in aphelion and diminished in perihelion by 24 millions of miles. The greatest distance of the planet from the sun is therefore 518, and the least 470, millions of miles.

The small eccentricity of the orbit of this planet, combined with its small inclination to the plane of the ecliptic, is of great importance in its effect in limiting the disturbances consequent upon its mass, which, as will hereafter appear, is greater than the aggregate of the masses of all the other planets primary and secondary taken together. If the orbit of Jupiter had an eccentricity and inclination as considerable as those of the planet Juno, the perturbations produced by this mass upon the motions of the other bodies of the system, would be twenty-seven times greater than they are with its present small eccentricity and inclination.

2733. Relative scale of the orbits of Jupiter and the Earth.—
The relative magnitudes of the distances of Jupiter and the earth
from the sun, and the apparent magnitude of the orbit of the earth
as seen from Jupiter, are represented in fig. 756, where the planet
is at J, the sun at S, and the orbit of the earth E E' E'' E''.

The direction of the orbital motions being represented by the arrows, it will be evident that when the earth is at E the planet is in



opposition, at E" in conjunction, at E' in quadrature west, and at E"

in quadrature east of the sun.

2734. Annual parallax of Jupiter. — To determine the angle sir, which the semi-diameter of the earth's orbit subtends at Jupiter, or the annual parallax of the planet, it may be assumed without material inexactness, that s E is nearly equal to an arc described with J as centre, and s J as radius, and consequently (2294)

$$8JE' = \frac{57^{\circ} \cdot 3}{5 \cdot 2} = 11^{\circ}.$$

The annual parallax of Jupiter is therefore 11°, and consequently the orbit of the earth subtends at the planet an angle of 22°.

2735. Variation of distance from the earth.—Since the greatest and least distances JE" and JE of Jupiter from the earth are the sum and difference of the distances of the planet and earth from the sun, we shall have

$$J = 22$$
 494 + 95 = 589 millions of miles.
 $J = 494 - 95 = 399$ millions of miles.
 $J = 22 = 2494 - 95$ = 485 millions of miles.

The extreme distances of the planet are therefore in the ratio of 6 to 5 nearly.

By the ellipticity of the earth's orbit, the distances at opposition and conjunction may be increased or diminished by 1½ million of miles, and by that of the planet's orbit by 24 millions of miles. From both causes combined they may vary from their mean values were or less by 25½ millions of miles.

2736. Its prodigious orbital velocity.—The velocities with which the planets move through space in their circumsolar courses are on the same prodigious scale as their distances and magnitudes. It is impossible, by the mere numerical expression of these enormous magnitudes and motions, to acquire any tolerably clear or distinct notion of them. A cannon-ball moving at the rate of 500 miles an acquir, would take nearly a century to come from Jupiter to the earth, wen when the planet is nearest to us, and a steam-engine moving on railway at 50 miles an hour would take nine centuries to perform he same trip.

Taking the diameter of Jupiter's orbit at 1000 millions of miles, ts circumference is above 3000 millions of miles, which it moves over in 4333 days. The distance it travels is, therefore, 700,000 miles per day, 30,000 per hour, 500 per minute, and 8\frac{1}{2} per second,

-a speed sixty times greater than that of a cannon-ball.

2537. Intervals between opposition, conjunction, and quadrature.

— If the distance of the planet from the sun bore an indefinitely great ratio to that of the earth, the quadratures would divide the semi-synodic period into parts precisely equal; for in that case J E' and J E' would be practically parallel, and the bent line E' S E'

would become straight, and would be a discister of the math's with. Although this is not the case, the angle firsted by 93' mid-sistening less than 180° by the magnitude of the angle 2' a 2" only the intervals into which the similarymotic period is divided and not different.

We shall have the angle of a w = 180° - 22° - 168°, and w is evident that the time of gaining this angle will hear the sine proportion to the synodic period which the angle itself bears to 860°. Hence, it follows, that if s express the interval from the quadrature west to the quadrature east, and s the interval from the quadrature east to the quadrature west, we shall have

$$t = \frac{158}{860} \times 898 = 1743 \text{ days,}$$
 $t' = \frac{202}{860} \times 898 = 2283 \text{ days.}$

It follows, therefore, that the interval between exposition and quadrature is 87½ days, and the interval between conjunction and drature is 111½ days.

These are mean values of the intervals which are subject to walk

2788. Jupiter has no sensible phases. — The mere inspection of the diagram, fig. 752, will show that this planet cannot be sensible gibbous in any position. The position in which the enlighted bemisphere is in view most obliquely is when the earth is at all z", and the planet consequently in quadrature, and even the said centre of the visible hemisphere is only 11° distant from the catallog of the enlightened hemisphere (2784).

2789. Appearance in the firmament at night.—Since bettell quadrature and opposition the planet is above the horizon during a greater part of the night, and appears with a full phase, it is the favourably placed for observation during 6 months in 18 months.

2740. Stations and retrogression.—From a comparison of orbital motions and distance of Jupiter and the earth, it appears the planet is stationary at about two months before and two most after opposition; and since the earth gains upon the planet at daily rate of 0° 907, the angle it gains in two months minet be

$$0^{\circ} \cdot 907 \times 61 = 54^{\circ} \cdot 43$$
.

The angular distance of the points of station from opposition, seen from the sun, is therefore about 54°, which corresponds to elongation of 114°.

The planet is therefore stationary at about 66° on each allow its opposition.

Its are of retrogression is a little less than 10°, and the timed describing it varies from 117 to 128 days.

2741. Apparent and real diameters.—The apparent diameter of Jupiter when in opposition varies from 42" to 48", according to the relative positions of the planet and the earth in their elliptic orbits. At its mean opposition distance from the earth its apparent magnitude is 45". In conjunction the mean apparent diameter is 30", its value at the mean distance from the earth being 37\frac{1}{2}".

At the distance of 399 millions of miles the linear value of 1" is

 $\frac{399000000}{206265} = 1934 \text{ miles,}$

and consequently, the planet's diameter D' will be

 $p' = 1934 \times 45 = 87030$ miles.

According to more accurate methods, the mean diameter is ascertained to be 88640 miles. The diameter of Jupiter is therefore

11.18 times that of the earth.

2732. Jupiter a conspicuous object in the firmament—relative splendour of Jupiter and Mars.—Although the apparent magnitude of Jupiter is less than that of Venus, the former is a more conspicuous and more easily observable object, inasmuch as when in opposition it is in the meridian at midnight, and when its opposition takes place in winter, it passes the meridian at an altitude nearly equal to that which the sun has at the summer solstice. By reason, therefore, of this circumstance, and the complete absence of all solar light, the splendour of the planet is very great, whereas Venus, even at the greatest elongation, descends near the horizon before the

entire cessation of twilight.

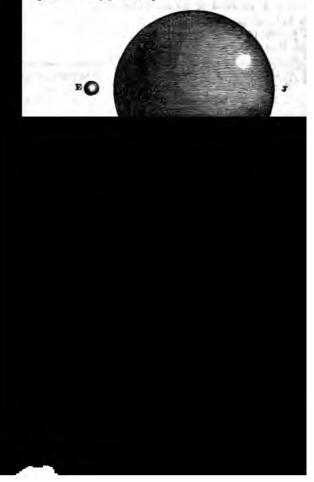
The apparent splendour of a planet depends conjointly on the apparent area of its disk, and the intensity of the illumination of its surface. The area of the disk is proportional to the square of its apparent diameter, and the illumination of the surface depends conjointly on the intensity of the sun's light at the planet, and the reflecting power of the surface. On comparing Mars with Jupiter, ere find the apparent splendour of the latter planet much greater than it ought to be, as compared with the former, if the reflecting power of these surfaces were the same, and are consequently compelled to conclude that the surface of Mars is endowed with some physical quality, in virtue of which it absorbs much more of the solar light incident upon it than that of Jupiter does. When the apparent diameter of the latter is twice that of the former, its apparent area is fourfold that of the former. But the intensity of the solar light at Jupiter is at the same time about thirteen times less than at Mars ; and if the reflective power of the surfaces were equal, the apparent splendour of Mars would be more than three times that of Jupiter. The reflective power must, therefore, be less in a sufficient proportion explain the inferior splendour of Mars, unless, indeed, the very probable supposition be admitted that there may be a source Jupiter independent of solar illumination.

2748. Surface and volume. — If s and v be the sur ume of the earth, s' and v' being those of Jupiter, we s

 $s' = 125 \times s$ $v' = 1397.4 \times v$.

e surface of Jupiter is therefore above 125 times, and it out 1400 times, that of the earth.

To produce a globe such as that of Jupiter, it would be mould into a single globe 1400 globes like that of the extra represented in fig. 757 by J and E.



The density of solar radiation being in the exact proportion of the apparent superficial magnitudes of the disks, the illuminating and heating powers of the sun will, ceteris paribus, be less in the same proportion at Jupiter than at the earth.

As has been already observed, however, this diminished power as well of illumination as of warmth, may be compensated by other

physical provisions.

2745. Rotation and direction of the axis. — Although the lineaments of light and shade on Jupiter's disk are generally subject to variations, which prove them to be, for the most part, atmospheric, nevertheless permanent marks have been occasionally seen, by means of which the diurnal rotation and the direction of the axis have been ascertained within very minute limits of error. The earlier observers, whose instruments were imperfect, and observations consequently inaccurate comparatively with those of a more recent date, ascertained nevertheless the period of rotation with a degree of approximation to the results of the most elaborate observations of the present day, which is truly surprising, as may appear by the following statement of the estimates of various astronomers:—

	H.	M.	8
Cassini (1665)	9	56	
Silvabelle			
Schröter (1786)	9	55	33
Airy	9	55	24.6
Mädler (1835)	. 9	55	26.56

The estimate of Professor Airy is based upon a set of observations made at the Cambridge Observatory. That of Mädler is founded apon a series of observations, commencing on the 3rd of November, 1834, and continued upon every clear night until April, 1835, during which interval the planet made 400 revolutions. These observations were favoured by the presence of two remarkable spots near the equator of the planet, which retained their position unaltered for several months. The period was determined by observing the moments at which the centres of the spots arrived at the middle of the disk.

The direction of the apparent motion of the spots gave the position of the equator, and consequently of the axis, which is inclined to the plane of the planet's orbit at an angle of 3° 6'.

The length of the Jovian day is therefore less than that of the

terrestrial day in the ratio of 596 to 1440, or 1 to 2.42.

2746. Jovian years.—Since the period of Jupiter is 4332.6 terrestrial days, it will consist of

4332.6 = 10484.9

Jovian days.*

The day here computed is the sidereal day, which, in the case of the superior planets, differs from the mean solar day by a quantity so insignificant that it may be neglected in such illustrations as these.

2747. Seasons.—At the Jovian equinoxes the length of terrestrial time must be 4th 57m 43.5th. Owing to the ve liquity of the plane of the planet's equator to that of t much exceeding the eighth part of the obliquity of th uator, the difference of the extreme length of the days mmer and midwinter, even at high latitudes, must neces nall. Thus at

Lat.	40°.—Longest day	H. 5 4	M. 6 49
	Difference	0	17
Lat. 60°.—Longest day	5	15 39	
	Difference	0	85

The diurnal phenomena at midwinter and midsumme rth in latitudes higher than 661° are only exhibited or ithin a small circle circumscribing the pole at a distance The extremes of temperature, so far as they depend on



JUPITER. THOM TRLESCOPIC DRAWDROW BY WADLIST & CORNECTED

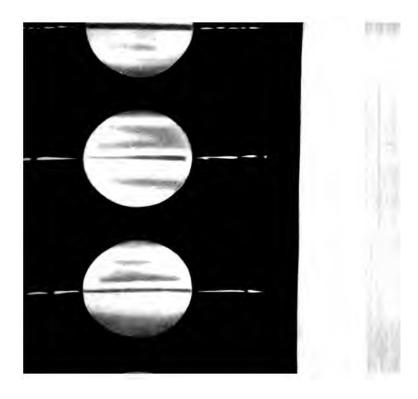
1 (6) 1 (7) 2 (6) 1 (1854 | 3 (6) 15 1834 | 4 (6) 17 1855 | 6 (6) 1 (118 16 | 6 (6) 1 (118 36)



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of the planet, the light towards the edges of the disk would radually fainter, and the edges would be nebulous and ill-The reverse is the case.

Spheroidal form of the planet. — The disk of Jupiter, magnifying powers as low as 30, is evidently oval, the s of the ellipse coinciding with the axis of rotation, and pendicular to the general direction of the belts. This fact a striking confirmation of the results attained in the nent of the curvature of the earth; and, as in the case of the degree of oblateness of Jupiter is found to be that ould be produced upon a globe of the same magnitude, rotation such as the planet is observed to have.

mean distance from the earth, the apparent diameters of are ascertained by exact micrometric measures to be-

natorial Diameterar Diameter	
Mosn diameter	_ 88 645

diameter is therefore less than the equatorial, in the ratio

that the day of Jupiter, instead of being twenty-four hours. an ten hours. This moon, therefore, has a month equal to ore than four Jovian days. In each day it passes through lete quarter; thus, on the first day of the month it passes thinnest crescent to the half moon; on the second, from moon to the full moon; on the third, from the full moon t quarter; and on the fourth returns to conjunction with

So rapid are these changes that they must be actually

they proceed.

parent motion of this satellite in the firmament of Jupiter ' rate of more than 8° per hour, and is the same as if our re to move over a space equal to her own apparent diameter. less than four minutes. Such an object would serve the of the hand of a stupendous celestial clock.

econd satellite completes its revolution in about eighty-five I hours, or about eight and a half Jovian days. It passes, , from quarter to quarter in twenty-one hours, or about an days, its apparent motion in the firmament being at the bout 4°.25 per hour; which is as if our moon were to move ace equal to nine times its own diameter per hour, or over liameter in less than seven minutes.

ovements and changes of phase of the other two moons are apid. The third passes through its phases in about 170 seventeen Jovian days, and its apparent motion is at the bout 1° per hour. The fourth and last completes its changes ours, or forty Jovian days, and its apparent motion is at of little less than 1° per hour, being double the apparent f our moon.

the inhabitants of Jupiter have four different months of ht, seventeen, and forty Jovian days, respectively.

Elongation of the satellites. — The appearance which the of Jupiter present when viewed with a telescope of modeer, is that of minute stars ranged in the direction of a line brough the centre of the planet's disk nearly parallel to tion of the belts, and therefore coinciding with that of the equator. The distances to which they depart on the one ther of the planet, are so limited that the whole system is within the field of any telescope whose magnifying power onsiderable; and their elongations from the centre of the in therefore be measured with great precision by means of micrometers.

the apparent diameter of the planet in opposition is 45", test elongations of the satellites from the centre of the dies are as follow: -

L	135/
II	215"
III	346//
IV	585"

es, therefore, that the entire system is comprised ver of about 1200" in extent, being two-thirds of the meter of the moon. If, therefore, we conceive the be centrically superposed on that of Jupiter, not on atellites be covered by it, but that which elongated in the planet would not approach nearer to the moon saixth of its apparent diameter.

the satellites were at the same time at their great they would, relatively to the apparent diameter present the appearance represented in fig. 759.



Fig. 759.

mees of the satellites, expressed in miles, are (except that of the greater than the distance of the moon from the earth.

761. Harmonic law observed in the Jovian system. — That the s law of gravitation which reigns throughout the material unis, prevails in this system, is rendered manifest by the accordance se motions and distances of the satellites with the harmonic law. he following table numerical relations establishing this are exced:—

	D	P	D ^a	Po	Da Da
I. II. IV.	60 96 154 270	48 85 172 400	216 885 3652 19,683	1849 7225 29,584 100,000	8·6 8·2 8·1 8·1

be want of exact equality in the numbers in the last column, by ithe ratio of the squares of the periods to the cubes of the distance expressed, is to be ascribed partly to using round numbers, and partly to the effects of the mutual disturbances produced he satellites upon each other and by the spheroidal form of the st itself.

162. Singular relation between the motions of the first three lites. — On comparing the periods of the first three satellites, it rident that they are in the ratio of the numbers 1, 2, and 4.

s the mean angular velocities, or, what is the same, the mean rent motions as seen from Jupiter, are found by dividing 360° he periodic times, it follows that these motions for the three lites are in the inverse ratio of 1, 2, and 4, that is, as 1, \frac{1}{4}, and \frac{1}{4}; therefore, that the mean apparent motion of the second satellite lf, and that of the third one-fourth of the mean apparent motion is first.

of follows, also, that if twice the mean motion of the third be the mean motion of the first, the sum will be three times mean motion of the second. This will be rendered evident by the second by general symbols. Let m', m'', and m''', the mean hourly apparent motions. We shall have—

$$m = \frac{1}{2} m' \qquad m'' = \frac{1}{2} m';$$

consequently

$$m' + 2m''' = m' + \frac{1}{2}m' = \frac{3}{2}m' = \frac{3}{2}m''$$
.

763. Corresponding relation between their mean longitudes.—
longitudes of satellites are referred to by their primaries as visual
res. Thus the mean longitudes of Jupiter's satellites are their

gular distances from the first point of Aries as seen from Now, it follows that the relation which has been shown between the mean motions of the first three satellites, also between their mean longitudes. Let these longitudes at peed time be l', l'', l'''; and after a given interval, during the satellites will have augmented their longitudes, let L', L'', L'''. The angles or arcs moved through in the inlies L' — l', L''' — l''', L''''; and since these will represent reportional to the mean apparent motions, we shall have—

$$(\mathbf{L}' - l') + 2(\mathbf{L}''' - l''') = 3(\mathbf{L}'' - l'');$$

ch is inferred-

$$3L'' - (L' + 2L''') = 3l'' - (l' + 2l''').$$

rs, therefore, the difference between three times the longihe second and the sum of the longitude of the first and at of the third is invariable; but what this invariable difi, does not appear from the mere relation of the periods. A servation of the positions of the three satellites at any proment, is sufficient to ascertain this difference; since whatay be at any one moment, it must always continue to be. be third satellite will therefore be 90° from the common direction the other two, and will therefore have a phase different from tirs by 90°. If one be full or new, the other will be in the arters, and vice versa.

In fine, if the first and third have a common phase, we shall have = L'''; and, consequently—

$$3 L'' - 3 L' = 180^{\circ}, L'' - L' = 60^{\circ}.$$

second will therefore have a position 60° different from the mon direction of the other two, and its phase will differ in the degree from their common phase. If one be full, the other

be gibbous; and if one be new, the other will be a crescent; breadth of the gibbous phase being 120°, and that of the cent 60°.

The student will find no difficulty in tracing the effects of this re-

on in all other phases.

In attempt has been made to trace the remarkable relation been the periods here noticed to the effects of the mutual gravitation the satellites; and Laplace has shown that, if such a relation railed nearly at any one epoch, the mutual gravitation of the llites would render it in process of time exact. There would n, therefore, to be a tendency to such a relation, as a consequence be general law of gravitation.

1764. Orbits of satellites. — The orbits of the satellites are eless of very small ellipticity, inclined to the plane of Jupiter's it at very small angles, as is made apparent by their motions ag always very nearly coincident with the plane of the planet's ator, which is inclined to that of its orbit at the small angle of

5' 30".

2765. Apparent and real magnitudes.—The satellites, although need by distance to mere lucid points in ordinary telescopes, not y exhibit perceptible disks when observed by instruments of sufent power, but admit of pretty accurate measurement. At oppoon, when the apparent diameter of the planet is 45", all the ellites subtend angles exceeding 1", and the third and fourth pear under angles of 1\frac{1}{2}" and 1\frac{1}{2}". By observing these apparent meters with all practicable precision, and multiplying them by a linear value of 1", as already determined (2741), their real dispers may be ascertained as follows:—

			Miles.
L	1//·194 x	1934 =	2309.
II	1"·070 ×	1934 =	2069.
III			
IV			

It appears, therefore, that with the exception of the second, hich is exactly equal in magnitude to the earth's moon, all the others are on a much larger scale; and one of them, the third, is greater than the planet Mercury, while the fourth is very searly

equal to it.

2766. Apparent magnitudes as seen from Jupiter. — By conparing their real diameters with their distances, the apparent diameters of the several satellites, as seen from Jupiter, may be easily ascertained. By dividing the actual distances of the satellites from Jupiter by 206,265, we obtain the linear value of 1" at such a tance; and by dividing the actual diameters of the satellites a spectively by this value, we obtain, in seconds, their apparent diameters as seen from Jupiter.

In making this calculation, however, it is necessary to talk account the magnitude of the semi-diameter of the planet; single from the surface, and not from the centre, that the actilities

viewed.

It follows, from a calculation made on these principles, that apparent magnitudes of the four satellites, seen from any part the surface not far removed from the equator of the planet, are the first 35' 30", for the second 19' 30", for the third 18' 16", all for the fourth 8' 58".

The first satellite, therefore, has an apparent diameter equal to that of the moon; the second and third are nearly equal and about half that diameter; and the apparent diameter of the other satellite is:

about the fourth part of that of the moon.

It may be easily imagined what various and interesting noctural phenomena are witnessed by the inhabitants of Jupiter, when the various magnitudes of these four moons are combined with the quick succession of their phases, and the rapid apparent motions of the first and second.

By the relation (2763) between the mean motions of the fit three satellites, they never can be at the same time on the same of Jupiter; so that whenever any one of them is absent from the firmament of the planet at night, one at least of the others met be present. The Jovian nights are, therefore, always mound except during eclipses (which take place at every revolution), and often enlightened at once by three moons of different apparent and

nitudes and seen under different phases.

2767. Parallax of the satellites.— Owing to the small propertion which the distances of the satellites bear to the semi-dismeter of the planet, the effects of their parallax, as observed from the semi-dismeter of Jupiter, are out of all analogy with any phenomena of like kind upon the earth. The nearest body in the universe to earth, the moon, is at the distance of sixty semidiameters, and horizontal parallax is consequently less than 1°; while the performance of Jupiter's satellites is only twenty-seven, and the next only six semidiameters from his centre.

method explained in 2327, the horizontal parallaxes, π , of the four satellites, may be determined, and are —

$$\pi'' = \frac{57 \cdot 3^{\circ}}{9 \cdot 6} = 6^{\circ}. \qquad \pi'' = \frac{57 \cdot 3^{\circ}}{15 \cdot 4} = 3 \cdot 6^{\circ}.$$

$$\pi''' = \frac{57 \cdot 3^{\circ}}{27} = 2 \cdot 1^{\circ}.$$

Apparent magnitudes of Jupiter seen from the satellites. he apparent diameter of the planet, seen from a satellite, s horizontal parallax (2327), it follows that the apparent of Jupiter seen from the first satellite is 19°, from the °, and from the third 7°, and from the fourth 4.25.° The Jupiter, therefore, appears to the first with a diameter imes greater, and a surface 320 times greater than that of con.

Satellites invisible from a circumpolar region of the It is easy to demonstrate in general that an object cannot om any part of the surface of a planet, which is at a disates pole less than the horizontal parallax of the object. fig. 760, be a meridian of the planet, N s its axis, o an

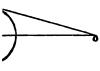


Fig. 760.

object at a distance, oc, from its centre. Suppose a line of P drawn from 0, touching the meridian at P, the angle POC will be the horizontal parallax of 0; and since the angle OFC = 90°, the angles PCO and POC taken together are 90°. But since the angle NCO is also 90°, it follows that the angle NCP, and,

the arc N P which it measures, is equal to the horizontal

is evident, that o is not visible from any part of the merireen P and N. If, therefore, a parallel of latitude be supbe described round the pole at a distance from it equal to
outal parallax of any object, such object cannot be seen
part of the circumpolar region included within such parallel.
was from this, from the values of the horizontal parallaxes
ellites found above (2732), and in fine from the fact that the
move nearly in the plane of the planet's equator, that the
ite is invisible at all parts within a parallel described round
at a distance of 9.5°, the second at 6°, the third at 8.6°,
murth at 2.1°.

Rotation on their axes. — One of the peculiarities in the our moon which distinguishes it in a remarkable manner planets, is its revolution upon its axis. It will be rememit the planets generally rotate on their axes in times some-

t analogous to that of the earth. Now, on the con n revolves on its axis in the same time that it ta e round the earth; in consequence of which adjumotions, it turns the same hemisphere continually to h.

ome observations of Sir William Herschel have rende e, that the Jovian moons also revolve on their axes or the of their respective revolutions round the planet. The ons cannot be repeated without the aid of telescopes a hose of the elder Herschel, and it may be expected Lord Rosse and others may supply further evidence stion.

771. Mass of Jupiter. — The ratio of the mass of of the sun, can be deduced from the motion of a lites, by the method explained in (2635).

f r and P express the distance and period of the planese of the satellite, and M and M' the masses of the set, we shall have—

$$\frac{M}{M'} = \left(\frac{r}{r'}\right)^3 \times \left(\frac{P'}{P}\right)^3$$

mbetituting in this formula the distances and porior

greater distances from Jupiter than that of the moon from the they nevertheless revolve in periods much shorter than that moon, and are affected by centrifugal forces, which exceed the moon in a ratio which may be determined by the pend distances, and which must be resisted by the attraction of ral mass proportionally greater than that of the earth. It be easy to show that, if the earth were attended by a similar of moons, at like distances from its centre, their periods be about eighteen times greater than those of Jupiter's

- 2. Their mutual perturbations. The mutual attraction of sees of the satellites, and the inequality of the attraction of n upon them, produce an extremely complicated system of ing actions on their motions, which has nevertheless been t with great success under the dominion of analysis by and Lagrange. This is especially the case with the three atellites, whose motions, but for this cause, would be sensibly n. The effect of these disturbing forces is nevertheless mitiand limited by the very small eccentricities and inclinations orbits of the satellites.
- 3. Density. The volume of Jupiter being greater than that earth in the ratio of 1400 to 1, while its mass is greater in erior ratio of 338 to 1 nearly, it follows, that the density of atter composing the planet is less than the mean density of the in the ratio of the above numbers. We have, therefore—

$$\frac{d'}{d} = \frac{338}{1400} = 0.2415.$$

an density is, therefore, less than one-fourth of that of the and since the mean density of the earth is 5.67 times that er, the density of Jupiter is 1.37 times that of water.

4. Masses and densities of the satellites. — The masses of ellites are determined by their mutual disturbances, by means general principle explained in (2637), and the densities are d as usual from a comparison of these masses with their so. In the following table are given the masses as compared so primary and with the earth, and their densities as compared so earth and with water.

Mann, that of Japiter as i.	Moss, that of Earth	Density, that of Earth = 1.	Density, that of Water
0-0000173	0-00576	0-02016	0-1143
0 0000232	0-00773	0-03015	0-1710
0-0000885	0-02947	0-06264	0-3970
0-0000427	0-01422	0-03925	0-2225

Thus it appears that the density of the matter composing them satellites is much smaller than those of any other bodies of the

system, whose densities are known.

It follows, therefore, that the first satellite must be composed of matter which is twice as light as cork, the density of which is 0.240; and that of the third, which consists of the heaviest matter, is not more dense than the lightest sort of wood, such, for example, as the common poplar, whose density is 0.883 (787).

It is remarkable that this extremely small degree of density is not found in the earth's satellite, the density of which, though iss than that of the earth, is still more than twice the density of water.

The planets Mercury and Mars, which are so nearly of the sum magnitudes as the third and fourth satellites, show, in a string manner, the difference of the matter composing them by the guid difference of their densities. The mean specific weight of the materials composing these planets is nearly the same as that of their which compose the earth, while the materials of the third satellite are thirteen times, and that of the fourth twenty-five times lights.

2775. Superficial gravity on Jupiter. — The gravity by which bodies placed on the surface of this planet are affected, omitting the consideration of the modifying effects of its spheroidal form and is rotation, may be computed by means of its mass, and its mean semi-diameter by the method already explained.

Let m' = J upiter's mass, that of the earth being = 1; r' = J upiter's mean semi-diameter, that of the earth being

g' = superficial gravity, that of the earth being = 1; we shall then have (2647), (2771)—

$$g' = \frac{m'}{r'^2} = \frac{338}{11\cdot 45^2} = 2\cdot 6.$$

2776. Centrifugal force at Jupiter's equator. — In the case of Jupiter, owing to the great degree of its oblateness and its rapid rotation, this force of superficial gravitation is subject to much greater variation than on the earth. To determine this variation, is will be necessary to compute the centrifugal force by which bodies placed on the equator of the planet are affected.

Let c = centrifugal force related to the terrestrial gravity the unit,

g = 16.08 feet,

v = the velocity of Jupiter's equator in feet per second due to his rotation,

we shall then have (313)-

$$c = \frac{\mathbf{v}^2}{2\mathbf{r}' \times \mathbf{q}}.$$

The value of v deduced from the equatorial diameter of the lanet (2756) and the time of rotation (2747) is 42760; and it llows, therefore, that c=0.234. Deducting this from the super-ial gravity undiminished by rotation, already computed (2775), a shall find the effective equatorial superficial gravity

$$2.616 - 0.234 = 2.382$$
.

2777. Variation of superficial gravity from equator to pole.—
be well-known theorem of Clairault, already quoted (2384), by
bich the oblateness, the variation of superficial gravity, and the
strifugal force, are connected, supplies the means of determining
is.

Let e and w, as in 2884, express respectively the fraction of its sole length by which the equatorial exceeds the polar diameter, if the fraction of its whole weight by which the weight of a body of the pole exceeds the weight of the same body at the equator, if in fine, let c express the equatorial centrifugal force as a fraction the effective equatorial superficial gravity. By the theorem of initial, these three quantities are related in the manner expressed the following formula:—

$$e + w = 2.5 c$$
.

at, from what has been already explained, e = 0.08,

$$c = \frac{c}{g'} = \frac{0.234}{2.382} = 0.096;$$

ad consequently w = 0.16.

From whence it follows that the weights of bodies are increased y 16 per cent. when transferred from the pole to the equator.

A mass of matter, therefore, which upon the earth's surface would reigh 1000 pounds, would weigh, if placed upon Jupiter's equator, 382 pounds, and if placed at his pole, would weigh 2763 pounds. The beight through which a body would fall in a second would a 16.08 × 2.382 = 38.3 feet at its equator, and 44.4 at the pole. The length of a seconds pendulum varies in the exact ratio of he forces of gravity which produce its vibration (542); and if the sagth of the seconds pendulum on the surface of the earth be aken in round numbers as 39 inches, that of a seconds pendulum a Jupiter's equator would be 39 × 2.382 = 92.91 inches, and at he poles 107.77 inches.

2778. Density must increase from the surface to the centre. — It is easy to show that the oblateness of Jupiter is incompatible with the supposition of his uniform density. It was demonstrated by Newton that, if the earth's density were uniform, its oblateness would be $\frac{1}{3}$ $\frac{1}{0}$; and the same would be true of any spheroid of uniform density, revolving on its axis in the same time. But the oblateness will be increased in the same ratio as the square of the

time of rotation and as the density are diminished. If, therefore, R express the time of rotation of Jupiter, that of the earth being I and d the mean density of Jupiter, that of the earth being I, the oblateness which the planet would have if its density were united would be—

$$e = \frac{1}{230} \times \frac{1}{R^2} \times \frac{1}{d}.$$

But $R = \frac{1}{2 \cdot 406}$ and d = 0.228; therefore

$$e = \frac{2.406^{2}}{280 \times 0.228} = 0.1104.$$

But the oblateness deduced from observation being only out follows that the density cannot be uniform.

It is easy to perceive that, if the density augmented from the centre to the surface, the effect of the centrifugal force upon a component parts of the mass would have a tendency to reason oblateness still greater than it would be with the same mass an uniform density. Since, therefore, the actual oblateness is compatible either with an uniform density, or with a density creasing from the surface to the centre, it follows that the density must increase from the surface to the centre.

The mean density of the planet being 0.228, it follows, therefore, that the mean density of the superficial stratum must be less than this, though in what proportion cannot be determined by these data.

If the mean superficial density of Jupiter bear the same proportion to the mean density of its entire mass, as the mean superficial density of the earth bears to the mean density of its entire mass, will follow, that the mean superficial density of Jupiter will be half its mean density, and will, consequently, be 0.114; and since the mean density of the earth related to that of water as the will, is 5.67, it would follow upon this supposition, that the actual mean density of the superficial stratum of Jupiter would be 0.114 = 5.67 = 0.645.

Water, which discharges so many important functions in the physical economy of the earth, has a specific gravity 2.8 times less than the mean specific gravity of the superficial stratum of the globe. If a like fluid on Jupiter, serving like purposes, be similarly related to the mean density of its surface, its specific gravity would therefore be-

$$\frac{0.645}{2.8} = 0.23,$$

which would be more than three times lighter than sulphuric ether, the lightest known liquid, and nearly equal in levity to cork.

2779. Utility of the Jovian system as an illustration of the size system. — It is not merely as a model on a small scale of the size.

system, so far as relates to the analogy presented by the motions of the satellites round Jupiter to the motion of the planets reand the sun, and the striking confirmation of the theory of gravitative afforded by the exhibition of the play of Kepler's Laws, that the Jovian system is to be regarded with interest by the physical secret-All the effects of the reciprocal gravitation of the planes one upon another, which mathematicians have succeeded in explaining upon the principles of the theory of gravitation, all the perturbations and inequalities, many of which, in the case of the planets, will take thousands of centuries to complete their periods and re-commence their course, all these are exhibited on a great, r reduced scale in the Jovian system. As the central man is reduced in a thousand-fold proportion, and the distances of the bodies rewolving round it in a still greater ratio, the cycles of the perturbations and inequalities are similarly reduced. Millions of years are reduced thousands, centuries to months, months to days, days to bours. Phenomena, the periods of which would far surpass, not the life of man only, but the whole extent of time embraced within human mecords and traditions, are reproduced and completed in this miniature system, within such moderate limits of time as to bring them within the scope of actual observation. The analyst is thus enabled to see practically verified, those conditions of equilibrium and stability, which it would take countless ages to develope in the solar system.

II. SATURN.

2780. Saturnian system. — Beyond the orbit of Jupiter a space but little less in width than that which separates that planet from the sun is unoccupied. At its limit we encounter the most extraordinary object in the system, — a stupendous globe, nearly nine hundred times greater in volume than the earth, surrounded by two, at least, and probably by several thin flat rings of solid matter, outside which revolve a group of eight moons; this entire system moving with a common motion so exactly maintained, that no one part falls upon, overtakes, or is overtaken by another, in their course around the sun.

Such is the SATURNIAN SYSTEM, the central body of which was known as a planet to the ancients, the annular appendages and satellites being the discovery of modern times.

2781. Period. - By the usual methods the period of Saturn has

been ascertained to be 10759.22 days, or 29.48 years.

2782. Heliocentric motion. — The mean heliocentric motion is

$$\frac{360^{\circ}}{29\cdot 48} = 12\cdot 23^{\circ}$$
 annually.
= $1\cdot 018^{\circ}$ monthly.
= $0\cdot 033^{\circ} = 2'$ daily.
 29^{*}

Meiricie a year and infreen days.

2784. Distance. — The mean distance fr



determined by th

(24·48)
The distance is the exactly 9:538786

exactly 9.538786 being = 1. Taking the ear

95 millions of r will then be 906 The eccentricity 0.056, this distantion, being augm diminished in per

diminished in per of its whole am distance of the p therefore 950, and lions of miles.

2785. Relative distance from the proportion of the the earth are rep where EE'E' is a se' Saturn's dist. The four position cated are,

E when the plan

The semi-diameter of the earth's orbit therefore subtends at Saturn an angle of only 6°. The apparent diameter of a globe, which would fill the entire orbit of the earth seen from Saturn, would, therefore, be no more than 12°, or twenty-four times the

apparent diameter of the sun as seen from the earth.

2787. Great scale of the orbital motion. — The distance of Saturn from the sun is therefore so enormous, that if the whole earth's orbit, measuring nearly 200 millions of miles in diameter, were filled with a sun, that sun seen from Saturn would be only about twenty-four times greater in its apparent diameter than is the actual sun seen from the earth. A cannon-ball moving at 500 miles an hour would take 91,000 years, and a railway train moving 50 miles an hour would take 910,000 years to move from Saturn to the sun. Light, which moves at the rate of nearly 200,000 miles per second, takes 5 days, 18 hours, and 2 minutes to move over the same distance. Yet to this distance solar gravitation transmits its mandates, and is obeyed with the utmost promptitude and the most unerring precision.

Taking the diameter of Saturn's orbit at 1800 millions of miles, its circumference is 5650 millions of miles, over which it moves in 10,759 days. Its daily motion is therefore 525,140 miles, and its

hourly 21,880 miles.

2788. Division of synodic period. — Since the angle \mathbf{E}' s' s = $\mathbf{6}^{\circ}$, the angle \mathbf{E} s $\mathbf{E}' = 84^{\circ}$ and \mathbf{E}' s $\mathbf{E}''' = 96^{\circ}$. Since the synodic period is 378 days, the intervals between

opposition and quadrature
$$=\frac{84}{360} \times 878 = 88.2.$$

conjunction and quadrature $=\frac{96}{360} \times 878 = 100.8.$

It appears, therefore, that in 88 days after its opposition the planet is in its eastern quadrature, and passes the meridian about 6 in the afternoon. After a further interval of 101 days it arrives at conjunction; after which it acquires western elongation, passing the meridian in the forenoon; and at 101 days from conjunction it attains its western quadrature, passing the meridian at about 6 A.M. After another interval of 88 days it returns to opposition.

2789. No phases. — It is evident from what has been explained in relation to Jupiter (2738), that neither Saturn nor any more

distant planet can have sensible phases.

2790. Variation of the planet's distance from the earth. — The distances of Saturn from the earth are therefore

$$\mathbf{s'} \mathbf{z} = 906 - 95 = 811$$
 millions of miles in opposition.
 $\mathbf{s'} \mathbf{z'''} = 906 + 95 = 1001$ millions of miles in conjunction.
 $\mathbf{s'} \mathbf{z'} = \dots = 900.6$ millions of miles in quadrature.

tances are subject to some variation, owing to the eccenf the orbits of Saturn and the earth. The amount of this
arising from the eccentricity of Saturn's orbit, is, as has
m, 100 millions of miles. The variation due to the earth's
mparatively small, being under two millions of miles.

Stations and retrogression.—From a comparison of the
otion and varying distance between the earth and Saturn,
that the stations of the planet take place at about 65 days
I after opposition. Since the earth gains upon the planet
ean rate of 0.9526° per day, the angle at the sun corg to 65 days will be

 $0.9526^{\circ} \times 65 = 61.92^{\circ};$

responds to an elongation of 113°. The planet is therefore at elongation 67° east and west of opposition. of retrogression varies from 6° 41' to 6° 55'.

Apparent and real diameter. — This planet appears as a e first magnitude, with a faint reddish light. Its apparent s, compared with that of Mars, is greater than that which their apparent magnitudes and distances, a circumstance explained, as in the case of Jupiter, by the more feebly represent the surface of Mars.

The lesser axis of the planet therefore, according to Struve, measures 71,100 miles, and the mean diameter 75,000 miles.

2793. Surface and volume. — Taking the mean diameter of the planet as 9.46, that of the earth being 1, the surface will be $9.46^{\circ} = 89.5$, and the volume $9.46^{\circ} = 847$ times greater than those of the earth.

The relative volumes of Saturn and the earth are represented in fig. 762.



Fig. 762.

2794. Diurnal rotation. — From observation on the apparent motion of the spots on the disk of the planet, it has been ascertained to have a motion of rotation upon the shorter axis of the ellipse formed by its disk in 10^h 29^m 17^h. A terrestrial day is therefore equal to 2.3 Saturnian days.

2795. Inclination of the axis to the orbit. — The general direction of the motion of rotation has been ascertained to be such, that the inclination of the equator of the plane to the plane of the orbit is 26° 48′ 40″, and its inclination to the plane of the ecliptic is 28° 10′ 47.7″.

The axis, like that of the earth, and those of the other planets, whose rotation has been ascertained, is carried parallel to itself in the orbital motion of the planet.

The consequence of this arrangement is that the year of Saturn is varied by the same succession of seasons subject to the same range

of temperature as those which prevail on our globe.

2796. Saturnian days and nights. Year.—The alternation of light and darkness is therefore nearly the same as upon Jupiter. This rapid return of day, after an interval of five hours night, seems to assume the character of a law among the major planets, as the interval of twelve hours certainly does among the minor planets.

The year of Saturn is equal in duration to 10,759 terrestrial

to the objects of their observation, one of exercise of this improved sense was the 'Saturn differed in a remarkable manner lanets in not being circular. It seemed at ong oval, approaching to the form of an ded off at the corners. As the optical ere improved, it assumed the appearance rith two smaller disks, one at each side of n fine, took the appearance of handles or a vase or jar, and they were accordingly lisk, a name which they still retain. s explained the true cause of this phenohe planet is surrounded by a ring of opaque of which it is suspended, and that what parts of the ring which lie beyond the disk le, which by projection are reduced to the ellipse near the extremities of its greater arts of the ansæ are produced by the dark ace between the ring and the planet.

es and greatly multiplied number, and inof observers, have supplied much more the form, dimensions, structure, and posi-

inary and unexampled appendage.

d, that it consists of an annular plate of which is very inconsiderable compared with arly, but not precisely concentric with the its equator. This is proved by the coinhe ring with the general direction of the apparent motion of the spots by which e planet has been ascertained.

equate power are directed to the ring preaspect, dark streaks are seen upon its surof the planet. One of these having been nence which seemed incompatible with the mospheric cause as that which has been asconjectured that it arose from a real separing into two concentric rings placed one conjecture was converted into certainty by ne dark streak is seen in the same position

It has even been affirmed by some obeen seen in the space between the rings; tion. It is, however, considered as proved, f two concentric rings of unequal breadth, her without any mutual contact.

, being always at right angles to the axis

o 258,192 hours. But since a terrestrial day is e nian days, the number of Saturnian days in the Sa t be 247,457.

Bells and atmosphere.—Streaks of light and a their general direction to the planet's equator, haven Saturn, similar, in all respects, to the belts of ding like evidence of an atmosphere surrounding the with the like system of currents analogous to the inference involves, as in the former case, the admission of the system of currents and other meteors.

Solar light and heat. — The apparent diameter of rom Saturn is 9.54 times less than as seen from the sits mean apparent diameter, as seen from the sapparent diameter, as seen from Saturn, must be

$$\frac{1923''}{9.54} = 201''.57 = 3'21''.57.$$

omparative apparent magnitudes are represented in j represents the disk of the sun as seen from the ear from Saturn. ndreds of times closer to the objects of their observation, one of a carliest results of the exercise of this improved sense was the sovery that the disk of Saturn differed in a remarkable manner rem those of the other planets in not being circular. It seemed at at to be a flattened oblong oval, approaching to the form of an ongated rectangle, rounded off at the corners. As the optical wers of the telescope were improved, it assumed the appearance a great central disk, with two smaller disks, one at each side of

a great central disk, with two smaller disks, one at each side of These lateral disks, in fine, took the appearance of handles or rs, like the handles of a vase or jar, and they were accordingly dled the ansæ of the disk, a name which they still retain. At ngth, in 1659, Huygens explained the true cause of this phenomon, and showed that the planet is surrounded by a ring of opaque alid matter, in the centre of which it is suspended, and that what ppear as ansæ are those parts of the ring which lie beyond the disk the planet at either side, which by projection are reduced to the run of the parts of an ellipse near the extremities of its greater xis, and that the open parts of the ansæ are produced by the dark ky visible through the space between the ring and the planet.

The improved telescopes and greatly multiplied number, and inreased zeal and activity of observers, have supplied much more lefinite information as to the form, dimensions, structure, and posiion of this most extraordinary and unexampled appendage.

It has been ascertained, that it consists of an annular plate of natter, the thickness of which is very inconsiderable compared with he superficies. It is nearly, but not precisely concentric with the lanet and in the plane of its equator. This is proved by the coincidence of the plane of the ring with the general direction of the belts, and with that of the apparent motion of the spots by which

the diurnal rotation of the planet has been ascertained.

When telescopes of adequate power are directed to the ring preented under a favourable aspect, dark streaks are seen upon its surace similar to the belts of the planet. One of these having been
beerved to have a permanence which seemed incompatible with the
admission of the same atmospheric cause as that which has been asigned to the belts, it was conjectured that it arose from a real sepaation or division of the ring into two concentric rings placed one
within the other. This conjecture was converted into certainty by
he discovery, that the same dark streak is seen in the same position
a both sides of the ring. It has even been affirmed by some obervers that stars have been seen in the space between the rings;
at this requires confirmation. It is, however, considered as proved,
hat the system consists of two concentric rings of unequal breadth,
see placed outside the other without any mutual contact.

The plane of the rings, being always at right angles to the axis

of the planet, is, like the axis, estried by the orbital motion of the planet parallel to itself, so that during the year of Saturn, it undergoes changes of position in relation to the radius vector of the planet, or to a line drawn from the sun analogous to those which the earth's equator undergoes. Since the plane of the rings coincides with that of the Saturnian equator, therefore, it will be directed to the sun at the epochs of the Saturnian equinoxes; and, in general, the angle which the radius vector from the sun make with the plane of the ring, will be the sun's declination as sen from Saturn. This angle, therefore, at the Saturnian solutions will be equal to the obliquity of Saturn's equator to his orbit, that is, to 26° 48' 40" (2795), and at the Saturnian equinoxes will be 0°.

2800. Position of nodes of ring and inclination to ecliptic.—
The investigation of the position of the plane of the ring in space was undertaken and conducted with great ability and success by Prof. Bessel, by means of an elaborate comparison of all the recorded observations on the phases of the ring from 1701 to 182. The result proved that the line of intersection of the plane of the ring, and, therefore, that of the equator of the plane twith the plane of the ecliptic, is parallel to that diameter of the celestil sphere, which connects the two opposite points whose longitudes at 166° 58′ 8°9″ and 246° 53′ 8°9″, the former being the longitude at the point at which the rings pass from the south to the north of the ecliptic, and which is, therefore, the ascending node of the rings. It also resulted from this investigation that the angle formed by the plane of the rings, and, therefore, of the Saturnian equator with the plane of the ecliptic, is 28° 10′ 44.7″.

These longitudes and obliquity were those which corresponded to the 1st of January, 1800. It was shown that the nodes of the ring have a retrograde motion on the celiptic at the mean rate of

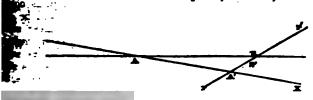
46.462" per annum.

It resulted from the observations of Professor Struve, made with the great Dorpat refractor, that the obliquity of the plane of the ring to that of the ecliptic is 28° 5′ 54″, subject to a possible enter of 6′ 24″.

The observations and measurements of these two eminent and nomers are, therefore, in as perfect accordance as the degree of fection to which the instruments of observation have been break admits.

2801. Obliquity of ring to the planet's orbit. — The positive of the plane of the ring in relation to the ecliptic being thus determined, its position in relation to that of Saturn's orbit can be appraised; and this is the more necessary to be done, inasmuch as estimated discrepancy prevails between the statements of different authorities respecting this element.

Like a, As. 764, he the according node of Saturn's orbit, and A' like making pole of the ring, AA' being consequently an arc of the line in the land of the ring, n' like the direction of the plane of the ring, n' like the orbit of the planet, of which, therefore, An



The 164

is an arc, and n the point where the plane of the ring intersects that of the orbit. It has been found that the longitude of A in 111° 56' 37.4"; and since that of A' in 166° 58' 8.9", we have AA' = 54° 56' 31.5". The angle nAA', which is the obliquity of Saturn's orbit, being 2° 29' 35.7", and the angle nA' a, the obliquity of the ring to the orbit being 28° 10' 44.7", it follows, by formulae of spherical trigonometry, that A nA' or the obliquity of the ring to the orbit of the planet, is 26° 48' 40"; that A n, or the distance of the intersection of the plane of the ring with the plane of the planet's orbit from the ascending node of the planet, is 58° 57' 80"; and, in fine, the distance nA of the same point from the ascending node of the ring is 4° 32' 30".

2802. Conditions which determine the phases of the ring.—
The relation between the phases of the ring and the position of the planet is easily ascertained. Let a be the semi-diameter of the rings as seen undiminished by projection; let b be the lesser semi-axis of the ellipse produced by the projection of the ring; and let D be the angle which the visual ray makes with the plane of the ring. We shall then have, by the common principles of projection,

$$b = a \times \sin D$$
.

But since the visual ray is the line drawn from the planet to the earth, it is evident that the angle D will be the declination of the earth as seen from the planet. Now, if L express the are of the celliptic between the earth and the ascending node of the ring as seen from the planet, and o the obliquity of the plane of the ring to the celliptic, we shall have, by the common principles of trigonometry,

mn.
$$p = \sin o \times \sin L$$
;

ioniognously.

$$\frac{b}{a} = \sin 0 \times \sin L$$

. Expt since the distance of the earth from the ascending node as III. 80

m the planet is equal to 180°, diminished by the d in from the same point as seen from the earth, L i i the preceding formula to express the latter distaning the same.

position of the planet with relation to the ascending ng be known, the preceding formula will therefore a he obliquity from the phase of the ring, or vice versa $o = 28^{\circ} 10' 44.7"$, we shall have sin. o = 0.4722 erefore have

 $\frac{b}{a} = 0.4722 \times \sin. L,$

the phases of the ring for any given distance from the computed.

The following table the ratio $\frac{b}{a}$ of the semi-axis of the by the projection of the ring, and the ratio $\frac{b}{r}$ of the semi-diameter of the planet, are given for every mode.

100	200	30°	400	500	600	70°	80°

entire breadth of the rings is visible above the disk of the at 90° from the node, the entire upper segment of the disk projected upon the ring.

n 90° to the descending node of the ring, the like phases are ted in a contrary order; and while the planet moves from mending to the ascending node, a similar series of phases are ted; the position of the plane of the ring with relation to the of the planet, however, being reversed; that which is in one terposed between the observer and the northern hemisphere planet will be interposed in the other case between him and athern hemisphere.

he diagrams, figs. 765—769, the phases of the rings indicated preceding table are exhibited.



Fig. 765.

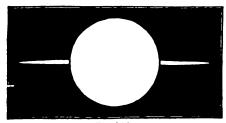


Fig. 766.

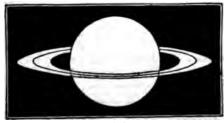


Fig. 767.



Fig. 768.



Fig. 769.

elative dimensions of the two rings, and of the planet within e represented in fig. 770, projected upon the common plane ings and the planet's equator. Each division of the subsale represents 5,000 miles.

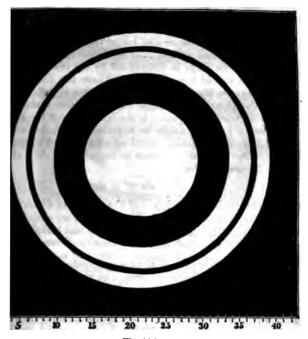


Fig. 770.

risual angle subtended at the earth by the extreme diameter external ring, when the planet is in opposition, is 48", which one thirty-seventh part of the moon's apparent diameter.

Thickness of the rings. — The thickness of the rings is mely minute, that the nicest micrometric observations have failed to supply the data necessary to determine it with ree of precision or certainty. It is so inconsiderable, that he plane of the ring is directed to the earth, and, conse, the edge alone is presented to the eye, it is invisible even lescopes of great power, or, if seen, it is so imperfectly as to elude all micrometric observation. When it was in ation in 1833, Sir J. Herschel observed it with a telescope, rould certainly have rendered distinctly visible a line of light

tieth of a second in breadth. Since the linear value of I's mean distance is about 4400 miles, it would follow the ness is less than 220 miles. Sir J. Herschel admits, how to it may possibly be so great as 250 miles.

ickness is, therefore, certainly less than the 100th part of me breadth of the two rings, and, according to the scale of efig. 756 is drawn, it would be represented by the thickleaf of the volume now before the reader.

Illumination of the ring.—Heliocentric phases.—The ion of the rings is determined by the phases under which ld be viewed from the sun. There the illuminating and I rays are identical, and their direction is that of the radius the planet. The angle which this line makes with the the Saturnian equator, is the declination of the sun as seen urn. Let this angle be expressed by D', the distance of from the Saturnian vernal equinoxial point L', and the info the Saturnian equator to the orbit o'. We shall then, former case, have

Sin.
$$D' = \sin \cdot 0' \times \sin \cdot L'$$
;

express lesser semi-axes of the ellipse to which the major d by projection, as seen from the sun, we shall have

$$\frac{b}{a'} = \sin \cdot o' \times \sin \cdot L'$$
.

ormula the ratios of B' to A and r may be determined for s of L', as in the former case. In the following table these as they have been computed, for $o' = 26^{\circ} 48' 40''$.

of the sun, as seen from the planet. The latter being only 33, the solar rays which touch the edge of the thickness may be considered as nearly parallel, and the breadth of the shadow will be nearly equal to the thickness of the ring. The shadow will therefore, in this case, be in a thin dark line, extending along the equator of the planet, fig. 771, covering a zone of the firmament whose breadth

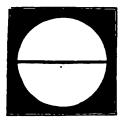




Fig. 771.

Fig. 772.

he sun. A total solar eclipse at the equator of the planet would, herefore, be produced by the shadow of the ring, and would conieue until the sun would gain or lose 44' declination.

When the planet presents the phase represented in fig. 767, its mightened hemisphere would be traversed by the shadow represented in fig. 772, and in like manner the shadows produced under the phases figs. 768, 769, are represented in figs. 773, 774.







Fig. 774.

2807. Shadow projected by the planet on the ring. — The hadow projected on the surface of the ring by the globe of the planet will vary with the sun's declination, as seen from the planet, seeing the angle at which the plane of the ring is inclined to the wis of the shadow of the planet is equal to the declination.

At the equinoxes, the declination being 0°, the plane of the ring

rough the axis of the shadow, and the breadth of ig on which the shadow falls is nearly equal to the planet, the angle of the cone of the shadow not exit is very nearly equal to the apparent diameter of t om Saturn.

press the arc of the external edge of the ring on w falls, it is evident that

Sin.
$$\frac{1}{2}a = \frac{r}{a}$$
,

ing, as before, the equatorial semi-diameter of the semi-diameter of the outer edge of the ring. The etermined being given to these, we have

Sin.
$$\frac{1}{2} \alpha = \frac{10,000}{22,287} = 0.4486$$
.

appears that a = 53° 18' 48"; and in like manner

shown that the shadow covers 84° 52' of the inner edge of the er ring.

The lateral edges of the shadow in this case are rectilinear and sibly parallel, a consequence due to the angle of the cone being

ignificant, fig. 775.

As the declination of the sun increases, the section of the cone of shadow by the plane of the ring becomes elliptical, and the edges the shadow on the ring are curved, fig. 776, while its breadth is re contracted. When the sun comes to the Saturnian solstice, I its declination is 26° 48′ 40″, the vertex of the elliptic section the cone falls upon the outer edge of the ring, and the shadow the form of an elliptic segment at the extremity of the major

s of the ellipse, fig. 777.

2808. The shadows partially visible from the earth. — It is dent that, the visual ray of an observer placed on the sun coining with the luminous ray, none of the shadows produced by the jestion of the ring on the planet or of the planet on the ring, id be visible to him, since the object producing the shadow would interposed with geometrical precision between his eye and the planet. But if the observer be transferred to the earth, the visual rails form an angle with the luminous ray, which, though it can any case exceed 6°, is sufficient, under certain circumstances has two position, to remove the observer from the direction of the simons ray to such an extent as to disclose to him a part, though thall part, of the shadow which to an observer at the sun is wholly greated.

In this manner, when the planet is in quadrature, a small part the shadow it projects upon the ring is visible on the east or on planet side of the disk, according as the sun is west or east of the sea; and in like manner, the difference between the angles which visual and luminous rays form with the plane of the ring disk, in certain cases, a small breadth of the shadow projected on planet's disk by the ring, which is accordingly seen as a thin k streak crossing the disk of the planet in contact with the ring. These phenomena prove that both the planet and the ring consist matter having no light of their own, and deriving their entire

imination from the sun.

2809. Conditions under which the ring becomes invisible from earth. — The rings of Saturn viewed from the earth may become isible, either because the parts presented to the eye are not illunated by the sun, or, being illuminated, have dimensions too

all to subtend a sensible visual angle.

It has been explained that, in every position assumed by the met in its orbital motion, one side or the other of the rings is minated with more or less intensity, except at the Saturnian ninoxes, when, the plane of the ring passing through the sun. its ge alone is illuminated. Owing to the extreme thinness of the

plate of matter composing the rings, they cease in this easy visible, except by feeble and uncertain indications observe high magnifying powers, which will be noticed hereafter. been inferred by Sir John Herschel, from observations man telescopes of great power, that the major limit of their pathickness is 250 miles. The visual angle which this the would subtend at the distance of Saturn in opposition, is (27)

 $\frac{250}{800,000,000} \times 206,265'' = 0.064''.$

The visual angle would, therefore, be less than the fifteenth a second.

The rings, therefore, disappear from this cause at Saturn noxes, which appear at intervals of 14‡ years.

When the dark side of the rings is exposed to the earth, if the property opposite sides of the plane of the ring therefore that plane must have such the sun and the earth. This can happen within a certain limited dist the planet's equipoxes.

of the earth in its orbit, the earth, as well as the sun, must be to the right of the direction of the edge of the rings, and consequently on their illuminated side; and after passing P', the earth, as well as the sun, must be to the left of the edge of the rings, and therefore will on the illuminated side. The rings, therefore, must everywhere be visible, except when the planet is at or between the points p and P'.

When the planet is at either of the points P or P', it may happen that at the same moment the earth is at the corresponding point E Ex. In that contingency the edge of the ring, being the only part exposed to the observer, would be invisible because of its mi-**Extenses,** in the same manner as when the planet is at p. ense the disappearance of the planet would be of short duration, becase the orbital motion of the earth would soon bring it on the mightened side of the ring. Thus, if when the planet is at P the earth is at E, the latter, moving much faster than the planet, advances before it, and being then on the same side of the ring with the sun, the illuminated side is exposed to the earth, and therefore visible; and if when the planet is at P the earth is at E', the latter moving towards of while the planet advances to the right of P', the earth and pleaset are both on the left of the edge of the rings, and, as before, the enlightened side of the rings is exposed to the earth, and they are therefore visible.

If, while the planet is between P and p, the earth, moving from d towards E, pass through the point to which the edge of the rings is directed, the rings will after such passage cease to be visible, because the earth will then be on their dark side. It is possible that after this, and before the planet arrives at p, the earth, moving from E towards e, overtaking the direction of the edge, may again pass through the point to which it is directed. If this happen, the rings will again become visible, because the earth will thus pass from their dark to their illuminated side.

If, in this case, while the earth moves towards E' and e', the placet pass through p, the rings will again become invisible, because, their edge passing from one side of the sun to the other, the side presented towards E' will be dark, and that towards E illuminated. If in this case the earth, moving from E' towards e', again pass through the point to which the edge of the rings is directed, it will again pass from the dark to the enlightened side, and the rings will again become visible.

The angle Eps, being the annual parallax of Saturn (2744), is 6°, and consequently EpE' or PsP' is 12°. But since the annual believentric motion of Saturn is 12°·22, the time of moving from P to P' is

 $\frac{12}{12 \cdot 22} \times 365 = 358 \frac{1}{4} \text{ days.}$

or about 61 days less than the time the earth takes to make a conplote revolution; so that while the planet moves from P to P the

earth moves through about 354° of its orbit.

It appears, therefore, that the interval during which the planet is within such a distance of its equinostial point as to render the disappearance of the rings from one or other of these several causes possible, the earth makes very nearly a complete revolution, and is erefore at one time or other in a position to meet the direction of the edges at least once, and the relative position of it and the planet may be such as to cause several disappearances of the rings within six months before and after the Saturnian equinox.

All these various phenomena were witnessed at the last Saturnian The northern surface of the ring had then been equinox in 1848. visible for nearly afteen years. The motions of the planet and the earth brought the plane of the ring to that position on the 22nd of April, in which, its edge being presented to the earth, it became is visible, the sun being still north of the plane. On the 3rd of Sp tember, the sun, passing through the plane of the ring, illuminated its southern surface, and, the earth being on the same side, the ring was visible. On the 12th, the earth again passing through the plane of the ring, its northern surface was exposed to the observe, which was invisible, the sun being on the southern side. The me continued thus to be invisible until the 18th of January, 1844, when, the earth once more passing through the plane of the ring, the southern surface illuminated by the sun came into view. This side of the ring will continue to be exposed to both the earth wh the sun until 1861-2, the epoch of the next equinox, when we succession of appearances and disappearances will take place sun and earth eventually passing to the northern side, on they will continue for a like interval

2810. Schmidt's observations and drawings of Saturn w ring seen edgeways. — At the last Saturnian equinox, which place in 1848, a series of observations was made at Bonn, sults of which have demonstrated the existence of great inequal of surface on the rings, having the character of mountains siderable elevation. The observations were made and pub accompanied by seventeen drawings of the appearance planet, its belts, and ring, by M. Julius Schmidt, of the Bu servatory.

We have selected from these drawings four, which are

Plate XI.

On the 26th of June, the planet presented an appearant closely resembling that of Jupiter, except that a dark st seen along its equator, produced by the shadow of the m

Astron. Nachr. Schumacher, Vol. xxviii. No. 650.

ing then a little above the common plane of the ring and A few feeble streaks, of a greyish colour, were visible on nisphere, which however disappeared towards the poles. A ble star was seen at the western extremity of the ring, which nosed to be one of the nearer satellites. The ring exhibited arance of a broken line of light projecting from each side lanet's disk.

this day the shadow across the planet disappeared, but was

intly seen on the 25th of July.

ing continued to be invisible until the 3rd of September, very slight indication of it was seen, but on the next night me distinctly visible with an interruption in two places, as ted in fig. 2. The bright equatorial belt was divided into qual parts by the ring, the northern portion being the nar-Three small satellites were seen in the prolongation of the 1 of the ring.

ne 5th, the ring was symmetrically broken on both sides,

e 7th, the western side was divided into three parts.

e 11th, the ring and planet presented the appearance repre-

n *fig*. 4.

broken and changing appearances of the ring on this occanonly be explained by the admission of great inequalities se, rendering some parts of the ring so thick as to be visible, are so thin as to be invisible, when presented edgeways to arver.

Observations of Herschel.—These observations of Schmidt borative of those made at a much earlier epoch by Sir W. I. who discovered the existence of appearances on the surface

ings indicating mountain inequalities.

Supposed multiplicity of rings.—Some observations made and elsewhere gave grounds for the conjecture, that the ag, instead of being double, is quintuple, and that instead ag a single division, there are four. It was even affirmed no confidence, that the ring was septuple, and consisted of moentric rings suspended in the same plane. These conjectre founded upon the supposed permanence of the black and concentric streaks which are observed upon the surface ings, and which are quite analogous to the belts of the planet. sumed permanence has not, however, been re-observed, he planet has been examined by numerous observers, with a of very superior power to those with which the observate made which formed the ground of the conjecture.

passage of Saturn diametrically across any fixed star of suffiagnitude, at the epoch of the Saturnian solstice, when the the ring is inclined at the greatest angle to the visual line,

supply the most eligible means of testing the multip f the rings; for in that case the light of the star ! ith the telescope to flash through each successive ope ring and ring, provided that the width of such open ent to allow the visual ray to clear the thickness of t 3. Ring probably triple - observations of Messrs Dawes. - Nevertheless, there are well-ascertained ap surface of the outer ring, which have been thought t nd division, and that the ring is triple. So early sor Encké noticed an appearance which indicated a ven made drawings in which such a division is indica Trans. 1838.) On the 7th September, 1843, Messi Dawes, unaware apparently of Encké's observation eet Newtonian reflector, constructed by Mr. Lassell, considered to be a division of the outer ring. hade under a magnifying power of 450, which gave d disk to the planet, and exhibited the principal di ings as a continuous, distinctly seen, black streak, und the surface of the ring. A dark line on the c he extremities of the ellipse, was not only distinctly

5. Discovery of an inner ring imperfectly reflective and lly transparent. - But the most surprising result of recent oic observations of this planet has been the discovery of a ring. ed, as it would appear, of matter reflecting light much more etly than the planet or the rings already described; and what more extraordinary, transparent to such a degree, that the the planet can be seen through it.

838, Dr. Galle, of the Berlin observatory, noticed a phenowhich he described as a gradual shading off of the inner wards the surface of the planet, as if the solid matter of the re continued beyond the limit of its illuminated surface, this ation of the surface being rendered visible by a very feeble ation such as would attend a penumbra upon it; and mea-! this obscure surface were published by him in the "Berlin stions" of that year.

subject, however, attracted very little attention until towards e of 1850, when Professor Bond, of Boston, and Mr. Dawes land, not only recognized the phenomenon noticed by Dr. aut ascertained its character and features with great precision. servations of Professor Bond were not known in England

e 4th of December; but the phenomenon was very fully and the yeen and described the Dawes, on the 29th of No. This astronomer, and the Parket of December, called the nof Mr. Lassell to the witnessed it on that evening the revatory of Mr. Dawes and descriptions of it, which appeared in Europe servations and descriptions of it, which appeared in Europe

neervations and descriptions of 11, which appeared in Europe neously with those the offessor Bond.

Is not, however, the second of the control of the contro the advantages of a lower, latitude and more serene sky. The of these observations has been the conclusive proof of the phenomenon of a semi-transparent annular appendage to this

i. Drawing of the planct and rings as seen by Mr. Dawes. planet surrounded by this compound system of rings is nted in Plate XII. The drawing is reduced from the original made by Mr. Dawes, of the planet as seen from his refractor ach aperture, at Wateringbury, in November 1852. Another ntation of the planet as seen by Mr. Lassell at Malta, in er, 1852, has been lithographed, and is almost identical with Mr. Dawes. In both, the form and appearance of the obng and its partial transparency are rendered quite manifest. incipal division of the bright rings is visible throughout its

ircumference. The black line, supposed to be a di er ring, is visible in the drawing of Mr. Dawes; bu een by Mr. Lassell.

markably bright thin line, at the inner edge of ng, which appears in Plate XII., was distinctly see

in 1851 and 1852.

inner bright ring is always a little brighter than th not, however, uniformly bright. Its illumination at the outer edge, and grows gradually fainter to dge, where it is so feeble as to render it somewhat tain its exact limit. It would seem as if the in re quality there approaches to that of the obscure ring red. The open space between the ring and the p

ne colour as the surrounding sky.

. Bessel's calculation of the mass of the rings. —] ted to determine the mass of the system of rings by on they produce upon the orbit of the sixth satel es it at 1-118th part of the mass of the planet. I the rings being too minute for measurement, no es sity of the matter composing them can be hence the density be assumed to be equal to that of t



METER, LENGT AND MEETERS FOR MOST TROMP

7.

SATURN

AN HERE IN MOVEMBER DIAS WITH A REPROPERTION OF THE BURN AFRICA.

WATERING HOLD WEAR MAILOUCHE BY W.R. DAV. E.C.



TOTAL SOLAR ECLIPSE OF 1851

XIII

 $\frac{2 \pi \sqrt{4} (4 \pi^2 + 7 \pi^2 +$

gravitation, combined with centrifugal force, causes the moon to keep revolving round the earth without falling down upon it by its gravity on the one hand, or receding indefinitely from it by the centrifugal force on the other, is well understood. In virtue of the equality of these forces, the moon keeps continually at the same mean distance from the earth while it accompanies the earth round the sun. Now it would be easy to suppose another moon revolving by the same law of attraction at the same distance from the earth. It would revolve in the same time, and with the same round facility to the first. We may extend the supposition with equal facility to the first. We may extend the supposition with equal facility to there, four, or a hundred moons, at the same distance. Nay, we may suppose as many moons placed at the same distance round the earth as would complete the circle, so as to form a ring of moons touching each other. They would still move in the same manner and with the same velocity as the single moon.

If such a ring of moons were beaten out into the thin broad flat rings which actually surround Saturn, the circumstances would be somewhat changed, inasmuch as the periods of each concentric sone would vary in a certain ratio, depending on its distance from the centre of Saturn, so that each such zone would have to revolve more rapidly than those within it, and less rapidly than those outside it. But if the entire mass were coherent, as the component parts of a solid body are, the complete ring might revolve in a periodic time less than that due to its exterior and longer than that due to its interior parts. In fact, the period of its revolution would be the period due to a certain zone lying near the middle of its breadth, exactly as the time of oscillation of a compound pendulum is that which is proper to the centre of oscillation (543). Indeed, the case of the oscillation of a pendulum and the conditions which determine the centre of oscillation afford a very striking illustration of the - physical phenomena here contemplated.

2820. Rotation of the rings.—Now the observations of Sir William Herschel on certain appearances upon the surface of the rings led to the discovery that they actually have a revolution round their common centre and in their own plane, and that the time of such revolution is very nearly equal to the periodic time of a satellite whose distance from the centre of the planet would be equal to that of the middle point of the breadth of the rings.

But if the principles above explained be admitted, it would follow that each of the concentric zones into which the ring is divided would have a different time of revolution, just as satellites at different distances have different periodic times; and it is extremely probable that such may be the case, because no observations hitherto made afford results sufficiently exact and conclusive as to either

establish or overturn such an hypothesis.

ars, therefore, in fine, that the stability of the rings is expon the same principle as the stability of a satellite.

Eccentricity of the rings. — The fact that the system of teoreentrical with the planet, resulted from some observably Messrs. Harding and Schwabe; after which the subaken up by Professor Struve, who, by delicate micrometric as and measurements executed with the great Dorpat infully established the fact, that the centre of the rings

a small orbit round the centre of the planet, being carried

the rotation of the rings.

Arguments for the stability founded on the eccentricity.—
Herschel has indicated, in this deviation of the centre of from the centre of the planet, another source of the stable Saturnian system. If the rings were "mathematically their circular form, and exactly concentric with the planet, nstrable that they would form (in spite of their centrifugal ystem in a state of unstable equilibrium, which the slightest ower would subvert—not by causing a rupture in the subthe rings—but by precipitating them, unbroken, on the the planet. For the attraction of such a ring or rings on sphere eccentrically situate within them is not the same

nand will sustain a long pole in a perpendicular position resting on the finger, by a continual and almost imperceptible variation of the point of support. Be that, however, as it may, the observed oscillation of the centres of the rings about that of the planet is in itself the evidence of a perpetual contest between conservative and destructive powers—both extremely feeble, but so antagonising one another as to prevent the latter from even acquiring an uncontrollable ascendancy, and rushing to a catastrophe."

Sir J. Herschel further observes, that since "the least difference of velocity between the planet and the rings must infallibly precipitate the one upon the other, never more to separate (for, once in contact, they would attain a position of stable equilibrium, and be held together ever after by an immense force), it follows either that their motions in their common orbit round the sun must have been adjusted to each other by an external power with the minutest precision, or that the rings must have been formed about the planet while subject to their common orbital motion, and under the full and free influence of all the acting forces."

2823. Satellites. — Saturn is attended by eight satellites, seven of which move in orbits whose planes coincide very nearly with that of the equator of the planet, and therefore with the plane of the rings. The orbit of the remaining satellite, which is the most distant, is inclined to the equator of the planet at an angle of about 12° 14′, and to the plane of the planet's orbit at nearly the same angle.

2824. Their nomenclature.—In the designations of the satellites, much confusion has arisen from the disagreement of astronomers as to the principle upon which the numerical order of the satellites should be determined. Some name them first, second, third, &c., in the order of their discovery; while others designate them in the order of their distances from Saturn. It has been proposed to remove all confusion, by giving them names, taken, like those of the planets, from the heathen divinities. The following metrical arrangement of these names, in the order of their distances, proceeding from the most distant inwards, has been proposed, as affording an artificial aid to the memory:—

Iapetus, Titan; Rhea, Dione, Tethys *; Enceladus, Mimas ———.

2825. Order of their discovery. — Since this was suggested, the eighth satellite, situate between Iapetus and Titan, has been discovered, and called Hyperion.

^{*} Pronounced Tethys.

der of their discovery was as follows :-

	Discoveryre.	Mississ
s.	Huygens, D. Caesini, Do, Do,	160 160 160
dus.	Sir W. Herschel.	17)
ion.	Messrs, Lassell and Bond.	18

ion was discovered on the same night, 19th Sep Lassell of Liverpool, and Professor Bond of the U ridge in the United States.

Their distances and periods.—The periodic tistances of these bodies from the centre of Satury the same kind of observations as already explained the satellites of Jupiter, are as follows:—

			Perio	d.	1000
Name.	D.	и.	M.	B.	Saturnian Days.
mas	0	22	37	22-9	9:18

phenomena which we have here noticed are in operation, and within such a space have these extraordinary discoveries been made. The apparent diameter of the external edge of the rings is only 44", or the fortieth part of the apparent diameter of the sun or moon; yet within that small circle have been observed and measured the planet, its belts, atmosphere, and rotation, and the two rings, their magnitude, rotation, and the lineaments of their surface.

2829. Various phases and appearances of the satellites to observers on the planet.—All that has been said of the phases and appearances of the moons of Jupiter, as presented to the inhabitants of that planet, is equally applicable to the satellites of Saturn, with this difference, that instead of four there are eight moons continually revolving round the planet, and exhibiting all the monthly changes to which we are accustomed in the case of the solitary satellite of the

earth.

The periods of Saturn's moons, like those of Jupiter, are short, with the exception of those most remote from the primary. The nearest passes through all its phases in 22½ hours, and the fourth, counting upwards, in less than 66 hours. The next three have months varying from 4 to 22 terrestrial days.

These seven moons move in orbits whose planes are nearly coincident with the plane of the rings. The consequence of this arrangement is, that they are always visible by the inhabitants of both hemispheres

when they are not eclipsed by the shadow of the planet. two inner satellites are seen making their rapid course along ternal edge of the ring, within a very small apparent distance. The motion of the nearest is so rapid as to be perceivable, at of the hour-hand of a colossal time-piece. It describes n 22½ hours, being at the rate of 16° per hour, or 16′ per; so that in two minutes it moves over a space equal to the nt diameter of the moon.

eighth, or most remote satellite, is in many respects excepand different from all the others. Unlike these, it moves in it inclined at a considerable angle to the plane of the rings. exceptional also in its distance from the primary, being reto the distance of 64 semidiameters of Saturn. The only salogous to this presented in the solar system is that of the moon, the distance of which is 60 semidiameters of the

D. Magnitudes of the satellites. — Owing to the great distance

of Saturn, the dimensions of the antellites have not been ascertained. The sixth in order, proceeding cutwards, is, however, known to be the largest, and it appears certain that its volume is little less than that of the planet Mars. The three satellites immediately within this, Rhea, Dione, and Tethys, are smaller bodies, and can only be seen with telescopes of great power. The other two, Mimas and Enceladus, require instruments of the very highest power and perfection, and atmospheric conditions of the most favourable nature, to be observable at all. Sir J. Herschel says, that at the time they were discovered by his father "they were seen to thread, like beads, the almost infinitely thin fibre of light to which the ring, there seen edgeways, was reduced, and for a short time to advance off it at either end, speedily to return, and hastening to their habitual concealment behind the body."

magnitudes of the satellites, the eighth excepted, being unascertained, nothing can be inferred with any certainty respecting their apparent magnitudes as seen from the surface of Saturn, except what may be reasonably conjectured upon analogies to other like bodies of the system. The satellites of Jupiter being all greater than the moon, while one of them exceeds Mercury in magnitude, and another is but little inferior in volume to that planet, it may be assumed with great probability of truth that the satellites of Saturn are at least severally greater in their actual dimensions than our moon.

If this be admitted, their probable apparent magnitudes as seen from Saturn may be inferred from their distances. The distance of the first, Mimas, from the nearest part of the surface of the plant, is only 94,000 miles, or about 21 times less than the distance of the moon; the distance of the second is about half that of the moon; that of the third about two-thirds, and that of the fourth about five-sixths; of the moon's distance. If these bodies, therefor, exceed the moon in their actual dimensions, their apparent magnitudes as seen from Saturn will exceed the apparent magnitude of the moon in a still greater ratio than that in which the distance of the moon from the earth exceeds their several distances from the surface of Seturn. Of the remaining satellites, little is as yell known of the seventh, Hyperion, which has only been recently discovered; and the great magnitude of the sixth, Titan, renders it probable that, notwithstanding its great distance from Sature, il may still appear with a disk not very much less than that of the moon.

2832. Horizontal parallax of the satellites.— The horizontal parallax is determined in the same manner as for the satellites of Jupiter (2767). Let the values of it, for the eight satellites pro-

coeding outwards, be expressed by n_1 , n_2 , n_3 , &c., and we shall have

$$\pi_1 = \frac{57^{\circ}3}{3\cdot36} = 17^{\circ} \qquad \pi_2 = \frac{57^{\circ}3}{4\cdot3} = 13^{\circ}3 \qquad \pi_3 = \frac{57^{\circ}8}{5^{\circ}34} = 10^{\circ}7 \qquad \pi_4 = \frac{57^{\circ}3}{6^{\circ}84} = 8^{\circ}4$$

$$\pi_6 = \frac{57^{\circ}3}{19\cdot55} = 6^{\circ} \qquad \pi_6 = \frac{57^{\circ}3}{22\cdot14} = 2^{\circ}6 \qquad \pi_7 = \frac{57^{\circ}3}{28} = 2^{\circ} \qquad \pi_8 = \frac{57^{\circ}8}{64\cdot38} = 0^{\circ}9.$$

2833. Apparent magnitudes of Saturn seen from the satellites.—It follows, therefore, that the disk of Saturn, seen from the satellites respectively, subtends visual angles varying from 34° subtended at the nearest, to 2° at the most remote.

2834. Satellites not visible in the circumpolar regions of the planet. — From what has been explained in (2769), combined with the observed fact that all the satellites except Iapetus move in the plane of the equator of the planet, it follows that they are severally invisible within distances of the poles of the planet expressed by their horizontal parallaxes. Thus, the first cannot be seen at latitudes higher than 73°; the second, 76°.4; the third, 79°.3, and so on.

2835. Remarkable relation between the periods. — The periods of the four satellites nearest to the planet have a very remarkable numerical relation. If they are expressed by P, P', P', and P''', we shall find that

$$p'' = 2 p, p''' = 2 p';$$

that is, the periods of the third and fourth are respectively double those of the first and second.

2836. Rotation on their axes. — The case of the moon, and the observations made on the satellites of Jupiter, raise the presumption that it is a general law of secondary planets to revolve on their axes in the times in which they revolve round their primary. The great distance of Saturn has deprived observers hitherto of the power of testing this law by the Saturnian system. Certain appearances, however, which have been observed in the case of the great satellite Titan, indicate, at least with regard to it, such a rotation. The variation of its apparent brightness in different parts of its orbit is very conspicuous, and the changes have a fixed relation to its elongation, the same degree of brightness always corresponding to the same position of the satellite in relation to its primary. Now this is an effect which would be explicable on the supposition that different sides of the satellite reflect light with different degrees of intensity, and that it revolves on its axis in the same time that it revolves round its primary. It has been observed that, when the entellite has eastern elongation, it has ceased to be visible, from which it has been inferred that the hemisphere then turned to the earth has so feeble a reflective power that the light proceeding from it is insufficient to affect the eye in a sensible degree. The improve-

of telescopes has enabled observers to follow it at h the entire extent of its orbit, but the diminuti on the eastern side of the planet is still so great, en with the greatest difficulty.

7. Mass of Saturn. — The mass of Saturn is ascert ption of his satellites by the method already explained express the distance of the planet from the sun ers of the orbit of a satellite, P the period of the planet the satellite for the unit, and M the mass of the su the planet for the unit, we shall have

$$M=\frac{r^3}{r^2}.$$

substituting for these symbols the numbers which the case of Saturn and his satellites, values will a mean of which is about 3500, showing that the is the 3500th part of the mass of the sun. The the earth is the 355,000th part of the mass of the that the mass of Saturn is 100 times that of the earth.

3. Density.—Since the mass of Saturn is only 1.

Let c = centrifugal force at the planet's equator related to terrestrial gravity as the unit;

g = 16.08 feet;

v = velocity of Saturn's equator in feet per second.

We shall then have (818)

$$c = \frac{\mathbf{v}^a}{21' \times g}.$$

The value of ∇ deduced from the equatorial diameter of the planet and the time of its rotation is 84,775, and it follows, therefore, that $\sigma = 0.1799$.

Deducting this from the superficial gravity, undiminished by rotation already computed (2839), we shall have

$$g'-c=1.18-0.1799=0.9501$$
;

which is, therefore, the effective gravity of Saturn's equator related

to terrestrial gravity as the unit.

2841. Variation of gravity from equator to pole.— Let e, w, and c retain their former significations (2777) (2384), and by the theorem of Clairault, already noticed, we shall have

$$e + w = 2.5 c$$

But, by what has been proved, we have

$$e = 0.097$$
 $c = \frac{c}{g' - c} = \frac{0.1799}{0.9501} = 0.189$;

from which it follows that

$$w = 2.5 \times 0.189 - 0.097 = 0.3755.$$

It follows, therefore, that a body which weighs 10,000 lbs. at Saturn's equator would weigh 13,755 lbs. if transported to his pole; and a body which weighs 100 lbs. placed upon the earth would weigh 95 lbs. on Saturn's equator.

The height through which a body would fall in a second upon

Saturn will be

$$16.08 \times 0.95 = 15.28$$
 feet at the equator; $15.28 \times 1.375 = 25.01$ feet at the pole.

The relative heights through which bodies would fall, and the lengths of pendulums, may be determined in the same manner as

already explained (2777).

2842. Prevailing errors respecting the uranography of Saturn.—
The rings must obviously form a most remarkable object in the farmament of observers stationed upon Saturn, and must play an important part in their uranography. The problem to determine their apparent magnitude, form, and position, in relation to the fixed stars, the sun, and Saturnian moons, has, therefore, been regarded

as a question of interesting speculation, if not of great scientific importance; and has, accordingly, more or less engaged the attention of astronomers. It is nevertheless a singular fact, that, although the subject has been discussed and examined by various authorities for three-quarters of a century, the conclusions at which they have arrived, and the views which have been generally expressed and adopted respecting it, are completely erroneous.

In the Berlin Jakrbuck for 1786, Professor Bode published an essay on this subject, which, subject to the imperfect knowledge of the dimensions of the rings which had then resulted from the observations made upon them, does not seem to differ materially in principle from the views adopted by the most eminent astronomes

of the present day.

2848. Views of Sir J. Herschel. — Sir John Herschel, in his Outlines of Astronomy, edit. 1849, states that the rings as seen from Saturn appear as vast arches spanning the sky from horizon to horizon, holding an almost invariable situation among the stars; and that, in the hemisphere of the planet which is on their dark side, a

solar eclipse of fifteen years' duration takes place.

This statement, which has been reproduced by almost all writers both in England and on the Continent, is incorrect in both the particulars stated. First, the rings do not hold an almost invariable position among the stars. On the contrary, their position with relation to the fixed stars is subject to a change so rapid that it must be sensible to observers on the planet, the stars seen on one side of the rings passing to the other side from hour to hour. Secondly, no such phenomenon as a solar eclipse of fifteen years' duration, or any phenomenon, bearing the least analogy to it, can take place of any part of the globe of Saturn.

2844. Theory of Mädler. — Among the continental astronomers who have recently reviewed this question, the most eminent is Dt. Mädler, to whose observations and researches science is so largely indebted for the information we possess respecting the physical characteristics.

acter of the surface of the Moon and Mars.

This astronomer maintains, like Herschel, that the rings hold a fixed position in the firmament, their edges being projected on parallels of declination, and that, consequently, all celestial objects are carried by the diurnal motion in circles parallel to them, so that in the same latitude of Saturn the same stars are always covered by the rings, and the same stars are always seen at the same distance from them.

This is also incorrect. The sones of the firmament covered by the rings are not bounded by parallels of declination, but by curve which intersect these parallels at various angles.

Dr. Mädler enters into elaborate calculations of the solar eclipses which take place during the winter half of the Saturnian year.

According to him, at a certain epoch after the autumnal equinox in sach latitude, the sun passes under the outer ring and is eclipsed by it, and continues to be thus eclipsed until, by its increasing declination, it emerges from the lower edge of that ring and passes into the opening between the rings, where it continues to be visible for an interval greater or less according to the latitude of the observer, until the further increase of its declination causes it to pass under the edge of the inner ring, where it is again eclipsed. The further increase of its declination in certain latitudes would, according to this astronomer, carry it beyond the lower edge of the inner ring, after which it would be seen below the ring uneclipsed. After the solstice in such latitudes, when the sun returns towards the celestial equator, its decreasing declination would carry it successively first under the inner and then under the outer ring. There would thus be, according to Mädler, in such latitudes two solar eclipses of long duration, one by each ring before the winter solstice; and two others of like duration, but in a contrary order, after the winter solstice. In certain latitudes, however, the declination of the lower edge of the inner ring being greater than the obliquity of the orbit to the Saturnian equator, the sun would not emerge from the inner ring, and in this case there would be only one eclipse by the inner ring, and that at mid-winter; but, as before, two, one before and the other after the solstice, by the outer ring, separated from the former by the time during which the sun passes across the interval between the rings.

Dr. Madler computes the duration of these various eclipses in the different latitudes of Saturn, and gives a table, by which it would appear that the solar eclipses which take place behind the inner ring vary in length from three months to several years, that the duration of the eclipses produced by the outer ring is still greater, and that the duration of the appearance of the sun in the interval between the rings varies in different latitudes from ten days to seven

and eight months.

2845. Correction of the preceding views. — These various conclusions and computations of Dr. Mädler, and the reasoning on which they are based, are altogether erroneous; and the solar phenomena which he describes have no correspondence with, nor any

resemblance to, the actual uranographical phenomena.

We shall now explain, so far as the necessary limits of the present volume will admit, what the actual phenomena are which would be witnessed by an observer stationed at different parts of the surface of Saturn. It will not, however, be possible to enter into the details of the reasoning upon which the conclusions are based. For this we must refer to a memoir by the author of this volume, read before the Royal Astronomical Society of London, and which will be seen in their Transactions.

^{*} See Populäre Astronomie, von Dr. J. H. Mädler. Berlin, 1852.

2846. Phenomena presented to an observer stationed at Satura's equator.— Zone of the firmament covered by the ring.— The station of the observer in this case being in the plane of the ring, and the heavens having the character of a right sphere, the ring will cover a zone of the firmament coinciding with the prime vertical, which, in this case, is also the celestial equator. It will therefore pass through the senith of the observer at right angles to his meridian, descending to the horizon at the east and west points. The only part of the system of rings exposed to view is the inner edge of the inner ring. This edge is illuminated at night by the sun at all times, except at the equinox, when the sun, being in the plane of the ring, one semicircle of the ring throws its shadow on the other; and excepting also, that are of the ring on which the shadow of the planet falls. In the day-time the edge of the ring is rather strongly illuminated by light reflected from the extensive and not very remote surface of the planet.

The thickness of the ring not being exactly ascertained, the apparent width of the zone of the firmament which it covers cannot be

determined with precision.

If, however, the major limit of 250 miles, assigned to the thickness by Sir J. Herschel, be adopted, the corresponding limit of the apparent width, obtained by the usual method of calculation, by comparing this thickness with its distance from the observer, will give 45' as the apparent breadth of the zone occupied by the ring at the zenith; and since the observer, being stationed at the point o (fig. 780) considerably removed from the centre c of the ring, is at

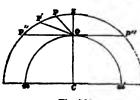


Fig. 780.

a greater distance o p" o p" from those points of the ring which meet the horizon than from that which is at the zenith, the apparent breadth of the ring will gradually decrease from the zenith z to the horizon in the same proportion as the distance of successive points P, P', &c., of the ring from the station of the observer is creases. From the known values of

the diameters of the planet and the ring already given, it is easy to show that the apparent breadth of the ring at the horizon will be less than its apparent breadth at the zenith in the ratio of 9 to 4 very nearly, that being the inverse ratio of the distance of the two points from the observer. If, therefore, the apparent breadth of the ring at the zenith z be 45', its apparent breadth at the horizon r' p' will be 20'.

It appears, therefore, that a zone of the firmament is in this case covered by the ring extending 22½' N. and S. of the equator at the senith, and 10' N. and S. of it at the horizon, and gradually decrease

ing in width from the one point to the other. It follows that two parallels of declination at 224′ N. and S. touch this zone at the points where it intersects the meridian, and lie elsewhere altogether their of it; and two other parallels, whose declination N. and S. is 10′, meet it at the horizon, and lie elsewhere altogether within it. The intermediate parallels intersect the edges of the zone at certain paints between the zenith and the horizon, and pass outside it, below and under it, above those points. It follows from this, that all bjects situate in such parallels rise clear of the ring, pass under it a certain altitude, and culminate occulted by it. All parallels of belination, whose distance from the equator is less than 10′, are attrely covered by the ring from the horizon to the zenith; and all bjects placed on such parallels are, consequently, occulted by the ing through the whole period of their diurnal motion.

2847. Solar eclipses at Saturn's equator. — These observations re applicable, of course, not only to the sun, but to all objects of hangeable declination. As to the sun, its apparent diameter at laturn being 3'·3, its disk will be in external contact with the ring at the zenith, when the declination of its centre is 24½', and in in-

ernal contact with it when its declination is 21'.

From a calculation of the rate at which the sun changes its declination at and near Saturn's equinox, derived from the ascertained obliquity of his equator to his orbit, it may be shown that it will have the declination 24½' at twenty-two days before the equinox, and the declination 21' at nineteen days before it. At twenty-two days before the equinox, therefore, a partial eclipse of the sun by the ring at the zenith will commence, which will become total at nineteen days before it.

But though total at the zenith, it will still be only partial at lower altitudes, and the sun's disk will be clear of the ring altogether when

still nearer to the horizon.

When the sun's declination still decreasing becomes 11'-65, its disk will be in external contact with the ring at the point where it rises and sets; and when its declination becomes 8'-35, it will be in internal contact, and therefore totally eclipsed. The sun will have the former declination at ten days and a half, and the latter at seven days and a half, before the equinox.

It follows, therefore, that the sun will be totally eclipsed from rising to setting, seven days and a half before, and seven days and a half after, the equinox, to an observer stationed on the equator of

the planet.

2848. Eclipses of the satellites. — The orbits of the six inner satellites, being exactly or nearly in the plane of the ring, they will be permanently eclipsed by the ring to an observer stationed on the planet's equator, unless, indeed, the apparent magnitudes of their disks exceed the apparent width of the ring. The real magnitude

of the satellites being unascertained, it is impossible to determine their apparent magnitudes; from analogy it would appear improbable that they should be so great as the apparent width of the ring even at the horison, and unless they depart to some extent, by reason of small obliquities in their orbits, from the plane of the ring all view of them must be permanently intercepted from an observer thus stationed.

The eighth satellite, however, whose orbit is inclined to the plane of the ring at an angle of about 13°, departs N. and S. of the ring to this extent, and is subject to eclipses similar to those of the sun

already described.

2849. Phenomena presented to an observer at other Saturnian latitudes. - If an observer be stationed at any point on one of the meridians of the planet, on the same side of the ring as the sun, the ring will present to him the appearance of an arch in the heavens, bearing some resemblance in its form to a rainbow; the surface, how-

ever, having an appearance resembling that of the moon.

The vertex or highest point of this arch will be upon his meridian, and the two portions into which it will be divided by the meridian will be equal and similar, and will descend to the horizon at points equally distant from the meridian. The apparent breadth of this illuminated bow will be greatest upon the meridian, and it will decrease in descending on either side towards the horizon, where it will be least. The division between the two rings will be apparent, and, except at places within a very short distance of the equator, the firmament will be visible through it.

2850. Edges of the rings seen at variable distances from celestial equator. - The distance of the edge of the bow from the celestial equator will not be every where the same, as it has been erroneously assumed to be. That part of the bow which is upon the meridian will be most remote from the celestial equator; and is descending from the meridian on either side towards the horizon, the declination of its edge will gradually decrease, so that those points which rest upon the horizon will be nearer to the equator

than the other points.

2851. Parallels of declination, therefore, intersect them. - It follows from this, that the parallel of declination which passes through the points where the upper edge of the bow meets the horizon will lie every where above it, and the parallel which passes through the point where the upper edge crosses the meridian will lie every where below that edge. This necessarily follows from the fact, that the declination of the points where the edge meets the horison is less, and that of the point where it meets the meridism greater, than that of any other point upon it.

It appears from this, that all parallels whose declinations are greater than those of the points where the edge meets the horizon,

that of the point where it crosses the meridian, must edge between the horizon and the meridian, and must below it under the point of intersection, and above it t of intersection.

litions are equally applicable to each of the edges of rings, and will serve to determine in all cases those

ch will intersect them respectively.

yes placed symmetrically in relation to meridian and from the symmetrical position of each of the edges, with a meridian and horizon, it will be apparent that the ch each parallel intersects them will be similarly placed of the meridian, having equal altitudes and equal axil W.

rm of the projection at different latitudes. — The geneposition of the bow formed by the projection of the se firmament in each latitude may be easily determined by geometrical principles. Let PB (fig. 781) be the

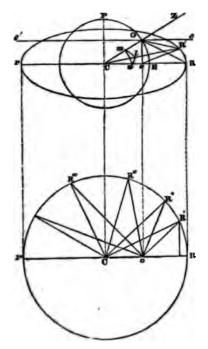


Fig. 783.

drant of the meridian of the planet passing through the observer o, and let RR' r represent one of the edg gs reduced by perspective to an oval, but shown as a cir er figure. It will be easily perceived, that the visual rough o to R carried round the circle R, R', R", &c, will surface of an oblique cone, whose base is the plane of I whose axis o c is inclined to the base at an angle of the latitude of the station. The projection of the ed v upon the firmament will then be the intersection of the this oblique cone with the celestial sphere; and it can be ted, that the point of this which is most remote from



ages in the projection of the point 2, where the plane of the ion, intersects the plane of the ring; that the other points of projection approach nearer to the celestial equator as their disfrom the meridian increases; and that they have equal declins at equal distances east and west of the meridian.

illustrate this still more fully, let NOE, fig. 782, be a quadof a meridian of the planet, o being its centre and c E its semieter. Let RR' be a section of the inner ring, made by the of the meridian continued through the ring, and let rr' be a

section of the exterior ring.

54. Rings invisible above lat. 63° 20' 38".—If we suppose an rver to travel upon the meridian from the pole N, towards the tor, it is evident that at first all view of the rings will be interproved that the point of c it will be at the latter on ed by the convexity of the met. If a line be drawn from r. 38"; and it is evident, that when the observer has descended to latitude the point r will be in his horizon, and consequently at higher latitudes it will be below his horizon, and therefore inble. It appears, therefore, that no part of the outer ring is

ble from any latitude above 63° 20' 38", and that at this latitude ingle point of the exterior ring is visible just touching the thern point of the horizon.

2855. Appearance at lat. 59° 20' 25".—If the observer now de-nd to lower latitudes, the exterior ring will begin to rise above horizon at the southern point; and it can be shown that when has descended to the latitude 59° 20' 25", his horizon will just ch the inner edge r' of the exterior ring, cutting off a segment that ring, which will be seen above the horizon.

The position of the ring thus visible above the horizon, will have

appearance of a lunar segn

32' 20".-If the observer continue 2856. Appearance at lat. 58 descend to a lower latitude, the ring will continue to rise to a eater elevation, and the interval between the rings will become fible. When he has descended to the lat, 58° 32' 20" his horizon Il just touch the outer edge of the inner ring, and a segment of interval between the rings will be visible under the arch of the ter ring, which will appear projected upon the southern firma-

The outer ring, therefore, is presented to the observer in this case a lunar bow spanning the southern firmament. It must be redeclinations of the points at which each of the mbe meridian being greater, and the declination of the ges i ints neet the horizon less, than that of any intermede p illels having declinations between these will interot the cuges severally, while all parallels whose declination is be-

ese limits will pass altogether above or altogether below

spectively, as the case may be.

Appearance at lat. 47° 33′ 51″. — When the observer ended to this latitude, the horizon will just touch the inner the inner ring, cutting off a segment of it, of which the is the base, the outer ring appearing as a bow above it, as ted in fig. 783. The same observation as to the varying



Fig. 783.

stereseted by them at every point, so that the parallels which mid will lie alternately above and below its edges as already

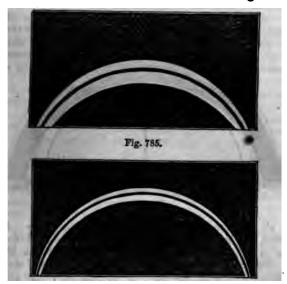


Fig. 786.



ed; some parallels, however, lying entirely above and others below it, as represented in fig. 788. It will be easy to by this, without rendering the diagrams complicated by ying upon them the arcs of the parallels, that they will be ly interlaced by these parallels, which will pass alternately and below the rings, being at one place covered by them, and her uncovered; at one point crossing the interval between



Fle. 100.

may be altogether covered by the on ascertained, by an investigation of t the bow in different latitudes, that the parallel lies altogether within the int those included between the latitudes latitudes of the planet from which the visible, the parallels which pass between within the interval, and partly above on

2859. Occultations of colestial objection all this, that, in general, celestial diurnal motion alternately above and beings; and if a parallel intersects all many cases, then the object in such a rings, will pass successively under the of them, will be visible in crossing the will culminate above them; and this wisame manner, and at precisely the san and W. of the meridian as that make

When, as happens in some cases, the parallel which comes under se conditions falls within the range of the sun's declination, that o say, when its declination is less than 26° 48' 40", the sun, ating this particular declination, will suffer four such eclipses been rising and setting,—two before and two after culmination. in some cases a parallel of declination will be covered by the er ring at the meridian, but will be clear of it near the horizon. is will take place when the declination of the parallel is greater n that of the points where the lower edge of the ring meets the izon, and less than that of the point where it meets the me-In that case, an object in such a parallel will rise and set ar of the ring, but will be occulted by it at culmination. object, therefore, will be occulted only once between rising and

An object may in like manner be occulted at or a little above the ince by the inner ring, and may culminate in the interval, or it y, after being occulted by the inner ring, pass under the outer

g and culminate occulted by it. In fine, all these various phenomena, and many others too numes and complicated to be explained here, are manifested in the arnian firmament, and the sun itself is subject to most of them. happens, in some cases, that a certain number of parallels of denation are entirely covered by the outer, and others by the inner g; and when the sun is found at any one of these parallels it will eclipsed constantly from rising to setting by one or the other

2860. Zone visible between the rings. — The zone of the heavens ible between the rings is found by calculating the visual angle stended at the station of the observer by lines drawn to the inner ze of the outer and to the outer edge of the inner ring, supposing it the thickness of the outer ring bears an inconsiderable proporn to the width of the space which separates them; and it is dent that the magnitude of this visual angle will gradually and lefinitely decrease as the observer approaches the equator, inasich as the obliquity of the visual ray to the plane of the rings lefinitely increases.

2861. Effect of the thickness of the rings on this zone.—If, hower, the thickness of the outer ring be supposed to bear any conerable ratio to the width of the space between the rings, it will ercept a portion of the visual rays included within the angle med by the rays drawn to the edges of the two rings, and the sctive opening will be found by subtracting the visual angle subided by the thickness of the outer ring from the visual angle subided by the space between the rings; and since the obliquity of e visual rays bounding the former gradually diminish in apcaching the equator, while the obliquity of the visual rays bound-111.

tter gradually increases, it is evident that the visual angle by the thickness of the outer ring continually increasing me certain latitude, become equal to the visual angle subthe space between the rings; and at that latitude accordwell as at all inferior latitudes, the thickness of the outer altogether intercept the opening, and no zone of the vill be visible through it. I have found by calculation, 00 miles be admitted as the major limit of the rings, all he heavens through the opening will be intercepted at latiow 8°; and if the probable minor limit of 150 miles be all view will be intercepted at and below the latitude of 5°. Solar eclipses by the rings. - The principles upon which oses by the rings in each latitude are calculated are, therely understood. By comparing the parallel of declination n at any time with the parallels of declination of the points ch of the edges of each of the rings meets the horizon and lian, the conditions under which it will intersect the edges will be determined, and hence it will appear that a most nd interesting body of solar phenomena, not anticipated in e works in which the uranography of Saturn has been in-I, are brought to light. In the lower latitudes the sun unon the same principles exactly as those of the sun, mutatis mutantis.

2864. Saturnian seasons. — It has been shown (2795) that the axis of the planet is inclined to the plane of its orbit at an angle of 26° 48′ 40", and is, like the axis of the earth, carried parallel to itself round the sun. The obliquity therefore which, so far as the sun is concerned, determines the extremes of the Saturnian seasons, differs by no more than 3° from that of the ecliptic. The tropics are parallels of latitude 26° 48' 40" north and south of the equa-The parallels within which the sun remains in winter below the horizon during one or more revolutions of the planet are at the latitude 63° 11′ 20″. These circles, therefore, affect the Saturnian climatology in the same manner as the tropics and polar circles affect that of the earth. The slow motion of the sun in longitude, and its rapid diurnal motion, however, must produce important differences in its effects as compared with those manifested on the earth. While the sun, as seen from the earth, changes its longitude at the mean rate of very nearly 1° per day, its change of longitude for Saturn is little more than 2' per day; and while, as seen in the terrestrial firmament, it is carried by the diurnal motion over 1° in four minutes, a Saturnian observer sees it move over the same space in less than two minutes. If the heating and illuminating power of the sun be diminished in a high ratio by the greater distance of that luminary, some compensation may perhaps arise from the rapid alternations of light and darkness.

III. URANUS.

2865. Discovery. — While occupied in one of his surveys of the heavens on the night of the 13th of March, 1781, the attention of Sir William Herschel was attracted by an object which he did not find registered in the catalogue of stars, and which presented in the telescope an appearance obviously different from that of a fixed star. On viewing it with increased magnifying powers, it presented a sensible disk; and after the lapse of some days, its place among the fixed stars was changed. This object must, therefore, be either a comet or a planet; and Sir W. Herschel, in the first instance, announced it as the former. When, however, submitted to further and more continued observation, it was found to move in an orbit nearly circular, inclined at a small angle to the plane of the ecliptic, and to have a disk sensibly circular.

It appeared, therefore, to have the characters, not of a comet, but a planet revolving outside the orbit of Saturn. It was named the "Georgium Sidus" by Sir W. Herschel, in compliment to his friend and patron George III. This name not being accepted by foreign astronomers, that of "Herschel" was proposed by Laplace, and to

some extent for a time adopted. Definitively, however, the scientific world has agreed upon the name "Uranus," by which this member of the system is now universally designated.

2866. Period, by symodic motion. — Owing to the great length of the period of this planet, those methods of determination which require the observation of one or more complete revolutions could not be applied to it. The symodic period, however, or the interval between two successive oppositions, being only 369-4 days, supplied a means of obtaining a first approximation. This gives

$$\frac{1}{P} = \frac{1}{865 \cdot 25} - \frac{1}{869 \cdot 40} = \frac{1}{80648},$$

which gives a period of 80,648 days.

2867. By the apparent motion in quadrature. — When a plant is in quadrature, its visual direction being a tangent to the make orbit, its apparent place is not affected by the earth's orbital mater. In the quadrature which precedes opposition, the earth move directly towards the planet; and in the quadrature which follows opposition, it moves directly from the planet. In neither and the planet. In the planet of planet is in quadrature, its apparent motion produce any apparent change of plant in the planet. It follows, therefore, that when a planet is in quadrature, its apparent motion is due exclusively to its own motion, and not at all to that of the earth. The daily motion of the planet as then observed is, therefore, the actual daily increment of its go-centric longitude.

But in the case of a planet such as Uranus, or even Satura, whose distance from the sun bears a large ratio to the earth's distance, the geocentric motion of the planet will not differ sensibly from the heliocentric motion; and, therefore, the geocentric daily increment of the planet's longitude observed when in quadratus may, to obtain an approximative value of the period, be taken as the daily increment of the heliocentric longitude. If this increment be expressed by l, we shall have

$$P = \frac{360^{\circ}}{l}.$$

Now, it is found that the apparent daily increment of the plant's longitude when in quadrature is 42"-28. If 860° be reduced to seconds we shall then have

$$\mathbf{P} = \frac{1296000}{42.23} = 30689.$$

By more accurate calculation, the periodic time has been determined at 80,686.82 days, or 84 years.

2868. Heliocentric motion. — The mean heliocentric motion of the planet is therefore, more exactly,

$$\frac{860^{\circ}}{84} = 4^{\circ} 17' 8'' \cdot 5 \text{ yearly;}$$

$$\frac{860^{\circ}}{84 \times 12} = 21' 25'' \cdot 7 \text{ monthly;}$$

$$\frac{1296000}{80687} = 42'' \cdot 238 \text{ daily.}$$

2869. Synodic motion. — The mean daily apparent motion of the sun being 0°9856, or 3548" 16, the mean daily synodic motion increment of elongation of Uranus will be

$$8548 \cdot 16 - 42'' \cdot 23 = 8505'' \cdot 93 = 58' \cdot 43 = 0^{\circ} \cdot 975.$$

The synodic period is therefore, more exactly,

$$\frac{360}{0.975} = 369.23$$
 days.

The earth, therefore, in 4½ days overtakes the planet, after completing each sidereal revolution.

2870. Distance. — The mean distance r of the planet from the same determined by the harmonic law, is therefore

$$r^2 = 84^2 = 7056,$$

 $r = 19.18.$

The mean distance is therefore 19:18 times that of the earth, and, consequently, the actual distance is

$$95,000,000 \times 19.18 = 1,822,100,000 \text{ miles}.$$

The distance of Uranus from the sun is therefore 1822 millions of miles, and its distance from the earth, when in opposition, is therefore 1727 millions of miles.

The eccentricity of the orbit of Uranus being 0.046, these distances are liable to only a very small variation. The distance from the sun is increased in aphelion, and diminished in perihelion by less than a twentieth of its entire amount. The plane of the orbit coincides very nearly with that of the ecliptic.

2871. Relative orbit and distance from the earth.—The relative proportions of the orbits of Uranus and the earth are represented in fig. 790, where EE'E' is the orbit of the earth, and s U the distance of Uranus from the sun. The four positions of the earth, corresponding to the opposition, conjunction, and quadratures of the planet, are represented as in the former cases.

2872. Annual parallax. - Since S U is 19.18 times S E, we shall

have for the angle

$$\mathbf{a} \ \mathbf{v} \ \mathbf{r}' = \frac{57^{\circ} \cdot 80}{19 \cdot 18} = 8^{\circ}.$$

The diameter of the earth's orbit, measuring as it does nearly 200 millions of miles, therefore subtends, at Uranus, a visual angle of only 6°; and a globe which would fill it, seen from the planet, would have an apparent diameter only twelve times greater than that of the moon.

2873. Vast scale of the orbital motion. — The distance of Uranus from the sun being above nineteen times that of the earth, and the earth being at such a distance that light, moving at the rate of nearly 200,000 miles per second, takes about eight minutes to come from the sun to the earth; it follows that it will take $19 \times 8 = 152$ minutes, or two hours and a half, to move from the sun to Uranus. Sunrise and sunset are, therefore, not perceived by the inhabitants of that planet for two hours and a half after they really take place; for the sun does not appear to rise or set until the light moving from it, at the moment it touches the plane of the horizon, reaches the eye of the observer.



Fig. 791.

2877. Solar light and heat. — The apparent diameter of the sun, as seen from Uranus, is less than as seen from the earth in the ratio of 1 to 19. The magnitude of the sun's disk at the earth being supposed to be represented by E, fig. 791, its magnitude seen from Uranus would be U.

The illuminating and warming power of the solar rays, under the same physical conditions, are therefore 19s = 361 times less at Uranus than at the earth.

2878. Suspected rings. — It was at one time suspected by Sir W. Herschel that this planet was surrounded by two systems of rings with planes at right angles to each other. Subsequent observation has not realised this conjecture.

2879. Satellites. — It has been ascertained that Uranus, like the other major planets, is attended by a system of satellites, the number of which is not yet certainly determined, and which, from, the great remoteness of the Uranian system, cannot be seen at all except by the aid of the most perfect and powerful telescopes.

Sir W. Herschel, soon after discovering this planet, announced the existence of a system of six satellites attending it, having the

periods and distances expressed in the following Table:-

	Period.				Distances in semi-diameters of
Order.	D.	н.	M.	S.	Uranus.
1 2 8	4 8 10	! 16 23	56	81-3	? 17-0 19-8 ?
4 5 6	13 88 07	11 2 12	?	12-6	22-8 45-5 ? 91-0 ?

Subsequent observations have confirmed this discovery so far only as relates to the four inner satellites. The fifth and sixth not having been re-observed, notwithstanding the vast improvement which has taken place in the construction of telescopes, and the greatly multiplied number and increased activity and zeul of observers, must be considered, to say the least, as problematical.

Of the four which have been re-observed, the second and fourth are by far the most conspicuous, and their distances and periods have been ascertained with all desirable accuracy and certainty. The first was re-observed by Mr. Lassell at Liverpool, and by M.

ve at Dorpat, in 1847. The fourth was observed about time by Mr. Lassell.

Anomalous inclination of their orbits. — Contrary to the prevails without any other exception in the motions of of the solar system, the orbits of the satellites of Uranas ed to the plane of the orbit of the planet, and therefore the ecliptic, at an angle of 78° 58′, being little less than angle, and their motions in these orbits are retrograde; say, their longitudes as seen from Uranus continually

the earth has such a position that the visual direction is at es to the line of nodes, the angle under the plane of the the visual line will be 78° 58'; and in certain positions and they will be seen, as it were, in plan. Being nearly he satellites will in such a position be visible revolving primary throughout their entire orbits, the projections not liftering from circles.

Apparent motion and phases as seen from Uranus.—The station and the direction of the axis of the planet being

IV. NEPTUNE.

2883. Discovery of Neptune. — The discovery of this planet constitutes one of the most signal triumphs of mathematical science, and marks an era which must be for ever memorable in the history

of physical investigation.

If the planets were subject only to the attraction of the sun, they would revolve in exact ellipses, of which the sun would be the common focus; but being also subject to the attraction of each other, which, though incomparably more feeble than that of the presiding central mass, produces sensible and measurable effects, consequent deviations from these elliptic paths, called PERTURBATIONS, take place, which will be more fully explained in a subsequent chapter. The masses and relative motions of the planets being known, these disturbances can be ascertained with such accuracy that the position of any known planet at any epoch, past or future, can be determined

If, therefore, it should be found, that the motion which a planet is observed to have is not in accordance with that which it ought to have, subject to the central attraction of the sun, and the disturbing actions of the surrounding planets, it must be inferred that some other disturbing attraction acts upon it, proceeding from an undiscovered cause; and, in this case, a problem novel in its form and data, and beset with difficulties which might well appear insuperable, is presented to the physical astronomer. If the solution of the problem, to determine the disturbances produced upon the orbit of a planet by another planet, whose mass and motions are known, be regarded as a stupendous achievement in physical and mathematical actione, how much more formidable must not the converse question be regarded, in which the disturbances are given to find the planet!

Such was, nevertheless, the problem of which the discovery of

Neptune has been the astonishing solution.

Although no exposition of the actual process by which this great intellectual achievement has been effected, could be comprehended without the possession of an amount of mathematical knowledge far exceeding that which is expected from the readers of treatises much less elementary than the present volume, we may not be altogether unsuccessful in attempting to illustrate the principle on which an investigation, attended with so surprising a result, has been based, and even the method upon which it has been conducted, so as to strip the proceeding of much of that incomprehensible character which, in the view of the great mass of those who consider it without being able to follow the steps of the actual investigation, is generally attached to it, and to show at least the spirit of the reasoning by which the solution of the problem has been accomplished.

For this purpose, it will be necessary, first, to explain the nature

and character of those disturbances which were observed and which could not be ascribed to the attraction of any of the known planet; and, secondly, to show in what manner an undiscovered planet revolving outside the known limits of the solar system could produce such effects.

2884. Unexplained disturbances observed in the motion of Uranus. — The planet Uranus, revolving at the extreme limits of the solar system, was the object in which were observed those disturbances which, not being the effects of the action of any of the known planets, raised the question of the possible existence of another

planet exterior to it, which might produce them.

After the discovery of the planet by Sir W. Herschel, in 1781, its motions, being regularly observed, supplied the data by which is elliptic orbit was calculated, and the disturbances produced upon a by the masses of Jupiter and Saturn ascertained; the other planet of the system, by reason of their remoteness, and the comparative minuteness of their masses, not producing any sensible effects Tables founded on these results were computed, and ephemerical constructed, in which the places at which the planet ought to be found from day to day for the future were duly registered.

The same kind of calculations which enabled the astronomer that to predict the future places of the planet, would, as is evident equally enable him to ascertain the places which had been occupied by the planet in times past. By thus examining, retrospectively, the apparent course of the planet over the firmament, and comparing its computed places at particular epochs with those of stars which had been observed, and which had subsequently disappeared, it was ascertained that several of these stars had in fact been Uranus itself whose planetary character had not been recognised from its apparance, owing to the imperfection of the telescopes then in use, as from its apparent motion, owing to the observations not having been sufficiently continuous and multiplied.

In this way it was ascertained, that Uranus had been observed and its position recorded as a fixed star, six times by Flansterivis., once in 1690, once in 1712, and four times in 1715;—023 by Bradley in 1753, once by Mayer in 1756, and twelve times by

Lemonnier between 1750 and 1771.

Now although the observed positions of these objects, combined with their subsequent disappearance, left no doubt whatever of the identity with the planet, their observed places deviated sensity from the places which the planet ought to have had according to the computations founded upon its motions after its discovery a 1781. If these deviations could have been shown to be irregular and governed by no law, they would be ascribed to errors of observation. If, on the other hand, they were found to follow a regular course of increase and decrease in determinate directions, they would

he seembad to the agency of some undiscovered disturbing cause. shome action at the epochs of the ancient observations was different

its action at more recent periods.

be ancient observations were, however, too limited in number to discontinuous to demonstrate in a satisfactory manner the rregularity or the regularity of the deviation. Mevertheless, the freumstance raised much doubt and misgiving in the mind of Bouvard, by whom the tables of Uranus, based upon the modern bservations, were constructed; and he stated that he would leave o futurity the decision of the question whether these deviations were due to errors of observation, or to an undiscounted disturbing gent. We shall presently be enabled to appreciate the aspecity

of this reserve.

The motions of the planet continued to be assiduously observed, and were found to be in accordance with the tables for about fourteen years from the date of the discovery of the planet. About the year 1795, a slight discordance between the tabular and observed places began to be manifested, the latter being a little in advance of the former, so that the observed longitude L of the planet was greater than the tabular longitude L'. After this, from year to year, the advance of the observed upon the tabular place increased, so that the excess L - L' of the observed above the tabular longitude was continually augmented. This increase of L - L' continued until 1822, when it became stationary, and afterwards began to decrease. This decrease continued until about 1830-31, when the deviation L-L' disappeared, and the tabular and observed longitudes again agreed. This accordance, however, did not long prevail. The planet soon began to fall behind its tabular place, so that its observed longitude L, which before 1831 was greater than the tabular longitude L', was now less; and the distance L' - L of the observed behind the tabular place increased from year to year, and still increases.

It appears, therefore, that in the deviations of the planet from its computed place, there was nothing irregular and nothing compatible with the supposition of any cause depending on the accidental errors of observation. The deviation, on the contrary, increased gradually in a certain direction to a certain point; and having attained a maximum, then began to decrease, which decrease still

The phenomena must, therefore, be ascribed to the regular agency

of some undiscovered disturbing cause.

2885. A planet exterior to Uranus would produce a like effect. -It is not difficult to demonstrate that deviations from its computed place, such as those described above, would be produced by a planet revolving in an orbit having the same or nearly the same plane as that of Uranus, which would be in heliocentric conjunction

planet at the epoch at which its advance beyond its con-

BCDEF, fig. 792, represent the arc of the orbit of Uranus by the planet during the manifestation of the perturba-



Fig. 792.

ne manifestation of the perturbations. Let N N' represent the orbit of the supposed undiscovered planet in the same plane with the orbit of Uranus. Let a, b, c, d, e, and f, be the positions of the latter when Uranus is at the points A, B, C, D, E, and F. It is, therefore, supposed that Uranus when at D is in heliccentric conjunction with the supposed planet, the latter being then at d.

The directions of the orbital motions of the two planets are indicated by the arrows beside their paths; and the directions of the disturbing forces* exerprincedly reduce this advance, until it bring back the planet to the ace it would have occupied had no disturbing force acted; after ish, the retardation being still continued, the planet will fall bethe place it would have had if no disturbing force had acted

it is evident that these are precisely the kind of disturbing s. which act upon Uranus; and it may, therefore, be inferred the deviations of that planet from its computed place are the micel indications of the presence of a planet exterior to it, moving as achit whose plane either coincides with that of its own orbit inclined to it at a very small angle, and whose mess and disname such as to give to its attraction the degree of intensity ne-

ne heen observed. nee, however, the intensity of the disturbing force depends cintly on the quantity of the disturbing mass and its distance, in easy to perocive that the same disturbance may arise from difnunt meanes, provided that their distances are so varied as to comsate for their different weights or quantities of matter. A double at a fourfold distance will exert precisely the same attraction. question, therefore, under this point of view, belongs to the s of indeterminate problems, and admits of an infinite number solutions. In other words, an unlimited variety of different tracts may be assigned exterior to the system which would cause chances observed in the motion of Uranus, so nearly similar to pheerved as to be distinguishable from them only by observamore extended and elaborate than any to which that planet had possibly have been submitted since its discovery.

6. Researches of Messre. Le Verrier and Adams.—The idea king these departures of the observed from the computed place income so the data for the solution of the problem to accertain position and motion of the planet which could cause such devipercentage of the same time, to two astronomers, neither an at that time had attained either the age or the scientific which would have raised the expectations of achieving the

emishing discovery of modern times.

Le Verrier, in Paris, and Mr. J. C. Adams, Fellow and Asis Tutor of St. John's College, Cambridge, engaged in the instiesties, each without the knowledge of what the other was doing, believing that he stood alone in his adventurous and, as would the problem, but did so with a completeness that filled the sith astonishment and admiration, in which none more arlissed than those who, from their own attainments, were best to appreciate the difficulties of the question. ion, as has been observed, belonged to the class of in-

nate problems. An infinite number of different e assigned which would be equally capable of produ I disturbances. The solution, therefore, might be rect, but practically unsuccessful. To strip the qu possible of this character, certain conditions were : stence of which might be regarded as in the higher Thus, it was assumed that the disturbing plane or nearly in the plane of that of Uranus, and the the ecliptic; that its motion in this orbit was in n as that of all the other planets of the system, th to the order of the signs; that the orbit was an e nall eccentricity; and, in fine, that its mean dista was, in accordance with the general progression of by Bode, nearly double the mean distance of Uran idition, combined with the harmonic law, gave the antage of the knowledge of the period, and therefo eliocentric motion.

ming all these conditions as provisional data, the uced to the determination, at least as a first appronass of the planet and its place in its orbit at a give would be capable of producing the observed altern

·	La Verrier.	Adams.
Esseh of the elements. Hean longitude at the epoch. Mean distance of planet from the sun Securitiety of the orbit. Longitude of perhellon. Heas (sun = 1)	1 Jan. 1947. 316° 47'-4 36'1839 0-107610 284° 45'-8 0-00010727	1 Jan. 1846. 323° 2' 37:2474 0:120615 209° 11' 0:001500S

2888. Its actual discovery by Dr. Galle of Berlin. - On the 23rd of September, 1846, Dr. Galle, one of the astronomers of the Royal Observatory at Berlin, received a letter from M. Le Verrier, senouncing to him the principal results of his calculations, informing him that the longitude of the sought planet must then be 326°, and requesting him to look for it. Dr. Galle, assisted by Professor Encké, accordingly did "look for it," and found it that very night. It appeared as a star of the 8th magnitude, having the longitude of 326° 52', and consequently only 52' from the place assigned by M. Le Verrier. The calculations of Mr. Adams, reduced to the same date, gave for its place 329° 19', being 2° 27' from the place where it was actually found.

2889. Its predicted and observed places in near proximity. —

To observe the relative proximity of these remarkable predictions to the actual observed place, let the arc of the ecliptic, from long. 323° to long. 330°, be represented in fig. 793. The place assigned by M. Le Verrier for the sought planet is indicated by the small circle at L, that assigned by Mr. Adams by the small circle at A, and the place at which it was actually found by the dot at N. The distances of L and A from N may be appreciated by the circle which is described around the dot N, and which represents the apparent disk of the moon.

The distance of the observed place of the planet from the place predicted by M. Le Verrier was less than two diameters, and from that predicted by Mr. Adams less than five diameters, of the lunar disk.

2890. Corrected elements of the planet's orbit. - In obtaining the elements given above, Mr. Adams based his calculations on the observations of Uranus made up to 1840, while the calculations of M. Le Verrier were founded on observations continued to 1845. On subsequently taking into computation the five years ending 1845, Mr.



Tie. 793.

ncluded that the mean distance of the sought planet would exactly taken at 33.33.

xactly taken at 33.33.

he planet had been actually discovered, and observations at continuance were made upon it, the following proved to be exact elements:—

	Gereswich.
the elements citude of epoch	1 Jan. 1847, M. Noon. 328° 32′ 44″ 2 30°0367. 000871946. 47° 12′ 6″ 50. 130° 4′ 20″ 81. 1° 46′ 58″ 97. 164 6181 years. 2°18688.

Discrepancies between the actual and predicted elements.—Now it will not fail to strike every one who devotes the ation to this interesting question, that considerable discrepist, not only between the elements presented in the two solutions of this problem, but between the actual elements covered planet and both of these solutions. There were ag some who, viewing these discordances, did not hesitate that the discovery of the planet was the result of chance, as was claimed, of mathematical reasoning, since, in fact, a discovered was not identical with either of the two planets

w such a conclusion from such premises, however, betrays

problem. Both, however, differed from the true planet in parars which did not affect the conditions of the problem. All e were circumscribed within those limits, and subject to such itions as would make them produce those deviations or disturbs which were observed in the motions of Uranus, and which

red the immediate subject of the problem.

392. Comparison of the effects of the real and predicted planets. t may be satisfactory to render this still more clear, by exhibiting nmediate juxtaposition the motions of the hypothetical planets MM. Le Verrier and Adams and the planet actually discovered, s to make it apparent that any one of the three, under the supd conditions, would produce the observed disturbances. We accordingly attempted this in fig. 794, where the orbits of

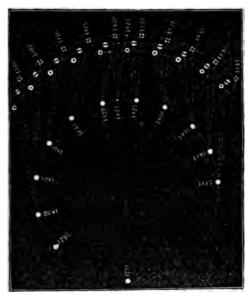


Fig. 794.

inus, of Neptune, and of the planets assigned by MM. Le Verrier Adams are laid down, with the positions of the planets respecly in them for every fifth year, from 1800 to 1845 inclusively. s plan is, of course, only roughly made; but it is sufficiently at for the purposes of the present illustration. The places of anus are marked by O, those of Neptune by O, those of M. Le rrier's planet by Θ , and those of Mr. Adams's planet by Θ .

be observed that the distances of the two planets assigned Le Verrier and Adams, as laid down in the diagram, from the distance of the planet Neptune than the mean given in their elements differ from the mean distance of

This is explained by the eccentricities of the orbit, the elements of both astronomers, are considerable, being eighth in one and a ninth in the other, and by the posi-

he supposed planets in their respective orbits.

masses of the three planets were equal, it is clear that the with which Le Verrier's planet would act upon Uranus, less than that of the true planet, and that of Adams's I more so, each being less in the same ratio as the square ance from Uranus is greater than that of Neptune. But nets are so adjusted that what is lost by distance is gained reater masses, this will be equalised, and the supposed I exert the same disturbing force as the actual planet, so tes to the effects of variation of distance. It is true that, at the arcs of the orbits over which the observations exdistances of the three planets in simultaneous positions very where in exactly the same ratio, while their masses essarily be so; and, therefore, the relative masses, which oduce perfect compensation in one position, would not do This cause of discrepancy would operate, however, actual conditions of the problem, in a degree altogether able, if not insensible.

either within the path of Neptune, or between it and that of Adams's planet, or, in fine, beyond this - within certain assignable limits.

2893. No part of the merit of this discovery ascribable to chance. -That the planets assigned by MM. Le Verrier and Adams are not identical with the planet to the discovery of which their researches have conducted practical observers is, therefore, true; but it is also true that, if they or either of them had been identical with it, such excessive amount of agreement would have been purely assidental, and not at all the result of the sagacity of the mathe-All that human sagacity could do with the data presented by observation was done: Among an indefinite number of possible planets capable of producing the disturbing action, two were assigned, both of which were, for all the purposes of the in-

quiry, so nearly coincident with the real planet as inevitably and immediately to lead to its discovery.

2894. Period. — After a complete revolution of the earth, Neptune is found to advance in its course no more than 2°.187, and consequently its period is -

$$P = \frac{360}{2 \cdot 187} = 164.6$$
 years,

or, more exactly, 164.618 years.

2895. Distance. — Its mean distance R, therefore, may be determined by the harmonic law:

$$R^3 = (164.6)^2 = 27093 = (30.04)^3$$
.

2896. Relative orbits and distances of Neptune and the earth. — It appears, then, in fine, that the system possesses another member still more remote from the common centre of light, heat, and attraction. In fig. 795, the earth's orbit is represented at EE"; and a part of that of Neptune, on the same scale, is represented at N. The actual distance of N from s is thirty times that of E from 8.

The mean distance of Neptune from the sun is, therefore,

2,850,000,000 miles.

2897. Apparent and real diameter. - The apparent diameter of the planet, seen when in opposition, is about 2".8. Its distance from the earth being then,

$$2850 - 95 = 2755$$
 mill. miles,

and the linear value of 1" at this distance being

$$\frac{2755000000}{206265} = 13,313 \text{ miles,}$$



Fig. 795.

e actual diameter of the planet will be

 $13313 \times 2.8 = 37,276$ miles.

The diameter of the planet is, therefore, a little greater the Uranus, about half that of Saturn, and about four and mes that of the earth.

According to Mr. Hind, the apparent diameter is only is real diameter 31,000 miles; numbers which, he says, ced from careful measurements with some of the most results.

propean telescopes.

2898. Satellite of Neptune. — A satellite of this planet vered by Mr. Lassell in October, 1846, and was afterwarved by other astronomers both in Europe and the United ne first observations then made raised some suspicions a esence of another satellite as well as of a ring analogous

Saturn. Notwithstanding the numerous observers, and t ful instruments which have been directed to the planet s te of these observations, nothing has been detected which y tendency to confirm these suspicions.

The existence of the satellite first seen by Mr. Lassell her not only been fully established but its motion

of the planet. M. Struve, calculating by the principles explained, has found that the mass of Neptune is the h part of the mass of the sun; and since its diameter is as 20th, and its volume the 8000th, part of that of the sun, ity will be about five-ninths that of the sun, and about the part of the density of the earth.

r estimates make the mass less. According to Professor t is the 19,400th, and according to Mr. Hind the 17,900th, mass of the sun.

. Apparent magnitude of the sun at Neptune. — The apparenter of the sun, as seen from Neptune, being 80 times less am the earth, is,

$$\frac{1800''}{30} = 60''.$$

sun, therefore, appears of the same magnitude as Venus seen string or evening star. relative apparent magnitudes are exhibited in fig. 796, at z

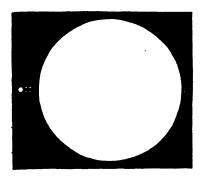


Fig. 796.

ruld, however, be a great mistake to infer that the light of at Neptune approaches in any degree to the faintness of Venus at the earth. If Venus, when that planet appears raning or evening star, with the apparent diameter of 60", all disk (instead of one halved or nearly so, like the moon paarters), and if the actual intensity of light on its surface ual to that on the surface of the sun, the light of the planet be exactly that of the sun at Neptune. But the intensity light which falls on Venus is less than the intensity of the the sun's surface in the ratio of the square of Venus' dispetate of the sun's semidiameter, upon the supposition that

is propagated according to the same law as if it issued from centre; that is, as the square of 37 millions to the square million nearly, or as 37^2 : $\frac{1}{4}$; that is, as 5476 to 1. If, the surface of Venus reflected (which it does not) all the dent upon it, its apparent light at the earth (considering more than half its illuminated surface is seen) is about mes less than the light of the sun at Neptune.

therefore, as is the apparent magnitude of the sun at Nepintensity of its daylight is probably not less than that uld be produced by about 20,000 stars shining at once in nent, each being equal in splendour to Venus when that

brightest.

ition to these considerations, it must not be forgotten that estimates of the comparative efficiency of the illuminating ng power of the sun is based upon the supposition that his eceived under like physical conditions; and that many connodifications in the physical state of the body or medium which the light falls, and in the structure of the visual nich it affects, may render light of an extremely feeble inefficient as much stronger light is found to be under other

id, to the vulgar mass, unexpected appearance, and the singular benomena which often attend them, strike the popular mind with re and terror. To the astronomer, geographer, and navigator, they beerve important uses, among which the determination of terresial longitudes, the more exact estimation of the sun's distance on the earth (which is the standard and modulus of all distances the celestial spaces), and, in fine, the discovery of the mobility light, and the measure of its velocity, hold foremost places.

When one of the extremes of the series of the three bodies high thus assume a common direction is the sun, the intermediate by deprives the other extreme body, either wholly or partially, of a illumination which it habitually receives. When one of the tremes is the earth, the intermediate body intercepts, wholly or stially, the other extreme body from the view of observers situate; places on the earth which are in the common line of direction, at the intermediate body is seen to pass across the other extreme ady as it enters upon and leaves the common line of direction. The phenomena resulting from such contingencies of position and irection are variously denominated ECLIPSES, TRANSITS, and OCLITATIONS, according to the relative apparent magnitudes of the interposing and obscured bodies, and according to the circumstances this attend them.

2903. General conditions which determine the phenomena of inreposition when one of the extreme objects is the earth. — If the

interposing and intercepted objects have disks of sensible magnitude, the effects attending their interposition will depend on the magnitude of the diameters of their disks and the apparent distance between their centres.

Let D express the apparent distance between the centres of the two disks. Let r be the semidiameter of the nearer, and r' that of the more distant disk.

2904. Condition of no interposition. — If D be greater than r + r', as represented at A, fig. 797, the disks must be entirely outside each other, and consequently no interposition can take place. The nearest points of the edges of the disks are, in this case, at a distance equal to the difference between D and r + r', that is, D—(r + r').

External contact.—If D = r + r', as at B, the disks will touch without interposition. This is called the position of EXTERNAL CONTACT.

2905. Partial interposition.—If D be less than r+r', the nearer disk will be partially interposed, as at c. In this case, the greatest breadth of













Fle. 797.

ared part of the more remote disk is (r + r')—D. It is that the less the distance D is, the greater will be this and the greater the part obscured.

Internal contact of interposing disk. —If the interposing less than the more distant, it will reduce the latter to a the points of the horns of which meet, as represented at D = r' - r, that is, when the distance between the centres to the difference of the apparent semi-diameters.

Centrical interposition of lesser disk.—If in the same centres coincide, as at E, the nearer disk, covering all the ortion of the more distant, will leave uncovered around it a ing or annulus of visible surface, the breadth of which will

fference r-r' of the semi-diameters.

Complete interposition.—If the nearer disk be greater than remote, and the distance p between the centres be not han r-r', the difference of the semi-diameters, the more isk will be completely covered, and will continue so until es separate to a greater distance than r-r', as represented σ .

I. SOLAR ECLIPSES.

position will take place (2905). The greatest breadth of the obscured parts of the solar disk will in this case be equal to the difference between the sum of the apparent semi-diameters and the distance between the centres of the two disks, that is, (r + r') - D.

2911. Magnitude of eclipses expressed by digits. — If the apparent diameter of the obscured object be supposed to be divided into twelve equal parts, each of these parts in reference to eclipses is called a DIGIT, and the magnitude of an eclipse is expressed by the number of digits contained in the greatest breadth of the obscured part of the disk. Thus the magnitude of the eclipse will be found by dividing r + r' - p by $\frac{2r}{12}$ or by $\frac{r}{6}$.

2912. Total solar eclipse.— To produce a total solar eclipse, it is necessary, 1st, that the apparent diameter of the moon should be equal to or greater than that of the sun, and 2dly, that the apparent places of their centres should approach each other within a distance not greater than r'-r, the difference of their apparent semi-diameters. When these conditions are fulfilled, and so long as they continue to be fulfilled, the eclipse will be total (2908).

The greatest value of the apparent semi-diameter of the moon being 1006", and the least value of that of the sun being 945", we shall have

$$r'-r=61''.$$

The greatest possible duration, therefore, of a total solar eclipse will be the time necessary for the centre of the moon to gain upon that of the sun $61'' \times 2 = 122''$. But since the mean synodic motion of the moon is at the rate of 30'' per minute, it follows that the duration of a total solar eclipse can never exceed four minutes.

2913. Annular eclipses. — When the apparent diameter of the moon is less than that of the sun, its disk will not cover that of the sun, even when concentrical with it. In this case, a ring of light would be apparent round the dark disk of the moon, the breadth of which would be equal to the difference of the apparent semi-diameters, as represented at E, fig. 792. When the disks are not absolutely concentrical, the distance between their centres being, however, less than the difference of their apparent semi-diameters, the dark disk of the moon will still be within that of the sun, and will appear surrounded by a luminous annulus, but in this case the ring will vary in breadth, the thinnest part being at the point nearest to the moon's centre; and when the distance between the centres is reduced to exact equality with the difference of the apparent semi-diameters, the ring becomes a very thin crescent, the points of the horns of which unite, as represented at D, fig. 792.

eatest breadth of the crescent will be in this case equal to ence of the apparent diameters of the sun and moon.

reatest apparent semi-diameter of the sun being 16' 18", east apparent semi-diameter of the moon being 14' 44", the possible breadth of the annulus when the eclipse is centrical

$$r-r'=16'18''-14'44''=1'34''=94''$$

about the 20th part of the mean apparent diameter of the

reatest interval during which the eclipse can continue anthe time necessary for the centre of the moon to move ly over $94'' \times 2 = 188''$, and, since the mean synodic at the rate of 30'' per minute, this interval will be about

$$\frac{188}{30} = 6.26 \text{ minutes}$$

six minutes and a quarter.

Solar eclipses can only occur at or near the epoch of new -This is evident, because the condition which limits the distance between the centres of the disks to the sum of m, fig. 798, represent sections of the sun, earth, and moon, made by the plane which passes through their centres. Let a line P m s be drawn, touching the sun and moon, but so that they shall lie on opposite sides of it. It is evident that to an observer at P, the dark disk of the moon would touch that of the sun externally; for the apparent distance between the centres would be measured by the angle s P M, which is equal to the sum s P s, the apparent semi-diameter of the sun, and M p m that of the moon.

From the point s let lines be supposed to be

From the point s let lines be supposed to be drawn, touching the earth at p and p'. It is evident that, to an observer situate between p and p', the apparent distance of the centres of the moon and sun would be greater than the sum of their apparent semi-diameters, and they would therefore be separated at the nearest points of their disks by a space equal to the excess of this distance above the sum of the apparent semi-diameters.

Adopting the signs already used, let r express the apparent semi-diameter of the sun, r' that of the moon, and D the apparent distance between their centres, we shall have D greater than r + r' for every point from P to p', and the excess will increase continually from P to p'.

On the other hand, for every point between P and p, D will be less than r + r', and the sun will be eclipsed, the magnitude of the eclipse augmenting gradually from P to p.

phenomena varying therefore indefinitely with the position beerver upon the earth, it is necessary, in order to render ediction practicable, to select a fixed position for which they calculated, formulæ being established, and tables prepared, the difference between the appearances there and at any d place may be computed. The fixed point selected for this is the centre E of the earth.

angular distance between the centres of the disks of the sun on, as seen from any place, such as P for example, is called *ppurent* distance at that place, and their angular distance, as om the centre E of the earth, is called their *true* distance. PM is the apparent distance between the centres at P, and

ŗ. 798.

eir true distance. It will be easy to show the relation ts between these two distances.

principles of elementary geometry we have

$$=$$
 soM $=$ PSE, soM $=$ POE $=$ MPS + PME, uently

SEM = MPS + PME - PSE.

ngle PME is the diurnal parallax of the moon, and PSE sun, estimated in the plane of the figure. If these be by ω' and ω respectively, and the apparent and true disween the centres by D and D' respectively, the above relace

$$D'=D+\omega'-\omega,$$

quently

$$D'-D=\omega'-\omega;$$

say, the true distance exceeds the apparent by as much as ax of the moon exceeds that of the sun.
place P, from which the disks appear in external contact,

$$D=r+r'$$

ore-

$$\mathbf{D}'-(r+r')=\omega'-\omega;$$

tly, when external contact takes place, we have

$$D'=r+r'+\omega'-\omega;$$

e true distance between the centres is equal to the sum of nt diameters added to the difference of the parallaxes. plify the explanation, we have here supposed the place of ody will depend partly on the shape and magnitude of the opaque ody itself, and partly on that of the body from which the light roceeds.

2917. Method of determining the form and dimensions of the indow. — In the cases which are actually presented in astronomy, is luminous body being the sun, and the opaque body a planet or itellite, both are globes, and the former of much greater dimensas than the latter. It is easy to show that in such case the hadow will be a cone, projected to a certain distance behind the paque body. The length of this cone, and the angle formed at its strex, may be computed, when the real diameters of the sun and is body which forms the shadow, and the distance of the one from is other, are known.

Let $b \ b'$ and $a \ a'$, fig. 799, represent a section of the sun and the

opaque body. Suppose the lines b a and b' a' drawn touching these. Let them be continued until they meet at f. If similar lines be supposed to be drawn through all points surrounding both globes, they will include a cone the diameter of whose base is b b', whose sides are b f and b' f, and whose vertex is f. It will be evident that the sun's rays will be excluded from all that part of the cone which is between a a' and the vertex f. This part of the cone, therefore, having the section of the opaque body at a a' for its base, and the point f for its vertex, is the shadow. To ascertain the length l of the shadow, let r and

To ascertain the length l of the shadow, let r and r' express the semi-diameters of the sun, and the body a a' respectively, and let d express the distance b a between them. We shall then have, by the principles of elementary geometry,

$$r:r'::l+d:l,$$

and consequently,

$$r \times l = r' \times l + r' \times d,$$

and therefore,

$$l \times (r - r') = r' \times d, \quad l = \frac{r' \times d}{r - r'};$$

that is, the length of the shadow is found by multiplying the distance from the sun by the semi-diameter of the body which forms the shadow, and dividing the product by the difference between the semi-diameters.

To determine the semi-angle a f e of the cone, we have

$$afe = 206265'' \times \frac{r'}{l}.$$

Fig. 190,

Method of determining the limits of the penumbra.—If he drawn transversely, such as b a' and b' a, and be convend the points a and a', the sun's rays will be partially from the space included between p a and f a. Any point a p will receive light from all points of the sun's disk. In thus illuminated be moved gradually from p towards eccive less and less of the sun's light, since the globe a d' ore and more interposed between it and the sun. Thus, a led at d' receives light only from those points of the sun between c and b, the rays proceeding from all points bend c being intercepted by a a'. As the point o' is moved the corresponding point c moves towards b, so that the the sun from which it receives light constantly decreases rrives at the boundary a f of the shadow, where all the intercepted.

ht being thus partially intercepted from the space bounded es a p and a f, this space is called the PENUMBRA. gle p a f, which measures the penumbra, is equal to the le b a b, subtended by the sun at the object which forms

w.

Total and partial solar eclipses explained by the lunar.

The moon projects behind in a conical shadow, the s of which can be ascertained by the methods explained if the moon comes between the sun and the earth, must do near conjunction, if it be not far removed from of its orbit, this shadow will be projected on a part of the e of the earth which is turned to the sun, provided its greater than the moon's distance as represented in far.

which the axis of the shadow is directed. This case is represented in fig. 801, where f represents the vertex of the moon's shadow.

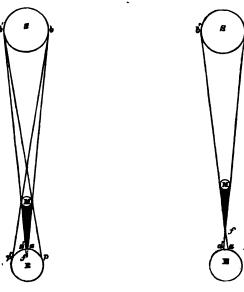


Fig. 800.

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Fig. 801.

At all places within the circle upon the earth, of which $a\,a'$ is the diameter, there will be a annular eclipse, and at the centre of the circle the eclipse will be centrical, the annulus being of uniform breadth. Outside this circle, so far as the penumbra extends, the eclipse will be partial, its magnitude decreasing as the distance of the place from the centre of the circle increases, until at the limit of the penumbra the phenomena ceases to be exhibited.

2921. Possibility of annular eclipses proved. — To establish the possibility of an annular eclipse, and to show the relative positions of the earth and moon, in their respective orbits, when such a phenomenon takes place, it must be considered that it is necessary that the length of the moon's shadow be less than the moon's distance from the earth. By substituting for r and r', in the general formula for the value of l (2917), the actual values of the semi-diameters of the sun and moon, we find

$$\frac{r'}{r-r'} = \frac{1076}{441000} = \frac{1}{440}.$$

me limits of the sun's distance d being d'' = 96,600000, d' = 93,400000,

st and least values of I, the length of the moon's

 $l'' = 96,600000 \times \frac{1}{440} = 219545,$ $l' = 93,400000 \times \frac{1}{440} = 212272.$

extreme distances of the moon from the centre of the

 length of the shadow, the diameter of the circular shadow proed upon the earth, which is the section of the conical shadow, bout the 100th part of the moon's diameter, or about 20 miles, th, however, is increased by the effect of the curvature of the h, and considerably so by the obliquity of its surface to the axis he shadow.

n the same manner it may be shown, that the diameter of the le over which the eclipse may be annular, measured at right les to the axis of the shadow, is about the sixth part of the diamof the moon, which in like manner is augmented by curvature

obliquity.

922. Solar ecliptic limits. — The moon's orbit being inclined to ecliptic, at an angle of 5°, and, consequently, the distance of the n's centre from the ecliptic varying in each month from 0° to while the interposition of the moon between any place on the h and the sun requires that the apparent distance of their centres ald not exceed the sum of their apparent semi-diameters, which much exceed half a degree, it is clear that an eclipse can represent happen except when, at the time of conjunction, the apparent nace of the moon's centre from the ecliptic is within that limit; a lition which can only be fufilled within certain small distances so moon's nodes.

here is a certain distance from the moon's node, beyond which lar eclipse is impossible, and a certain lesser distance, within the that phenomena is inevitable. These distances are called the

PCLIPTIC LIMITS.

he mere inspection of fig. 799, will show that no solar eclipse take place unless some part of the globe of the moon pass within lines b a and b' a', which touch externally the globes of the sun earth. It follows, therefore, that the major limit of the distance he moon's centre from the ecliptic, or its latitude at the time of unction, which is compatible with the occurrence of an eclipse, b' a', or what is the same, the angle m' a' a'. Let this angle be ressed by b', and we have

$$\mathbf{L} = m' a' n' + n' a' s + s a' o'$$

by the principle of geometry,

$$sa'o'=a'o'e-a'se,$$

therefore,

$$L = m' a' n' + n' a' s + a' o' e - a' s e.$$

m'a'n' and n'a's are the apparent semi-diameters of the sun moon, and a'o'e and a'se are their horizontal parallaxes, respectly. If the former be expressed by s and s', and the latter by h k', we shall have

$$\mathbf{L} = \mathbf{s} + \mathbf{s}' + \mathbf{h}' - \mathbf{h}.$$

s, therefore, that a solar eclipse cannot take place, unless de of the moon at conjunction be less than the sum of the semi-diameters of the sun and moon, added to the difference horizontal parallaxes.

nce all these quantities vary between a certain major and a ninor limit, an eclipse will be possible or certain, according oon's latitude at conjunction is within the one limit or the f the latitude be within the major limit, a solar eclipse may be; and if the several quantities have such values as fulfill e condition, it will take place. If the latitude be within or limit, an eclipse must take place; because, whatever be ues, they must fulfil the condition.

Extreme and mean values of semi-diameters and horizondiaxes of sun and moon.— The extreme and mean values quantities, which are very important in the theory of and other parts of practical astronomy, are given in the folable:—

No. of the last		
Greatest.	Least.	Mess.

mns =
$$5^{\circ} 8' 48''$$
 ms = $1^{\circ} 34' 14''$ m's' = $1^{\circ} 24' 19''$,
ns = $1^{\circ} 34' 14'' \times \frac{57 \cdot 30}{5 \cdot 15} = 17^{\circ} 27' 48''$,
ns' = $1^{\circ} 24' 19'' \times \frac{57 \cdot 30}{5 \cdot 15} = 15^{\circ} 37' 36''$.

us it appears, that when the distance from the node at opposition greater than 17° 27′ 48″, an eclipse cannot, and when less than 6′ 16″, must take place. Between these limits it may or may coccur, according to the magnitude of the parallaxes and apparent meters.

Since the sun takes more than a month to move through 32° of ecliptic, it follows that at least one conjunction must take place thin 16° of each node, and that one solar eclipse, at least, must are near each node, and therefore two, at least, annually. But it by happen that two solar eclipses shall occur at the same node, it this will take place if the moon be in conjunction at more than 1,0°, and less than 15° 37′ 36″, from the node; for in that case, it is be again in conjunction in 29½ days, in which time the sun will two through 29°, and will therefore be at 14½° on the other side the node, and therefore within the ecliptic limit.

Thus, it is possible that two solar eclipses may take place at each le, and, therefore, four within the year. But even more is posle; for, as will hereafter appear, the nodes of the moon's orbit re a retrograde motion on the ecliptic, the consequence of which that the sun arrives at each node in less than a year after it has t passed through it, and consequently another solar eclipse may pen, before the lapse of a solar year, at the same node at which ifirst occurred.

2924. Limits for total and annular eclipses.—It is evident that total or annular eclipse can be witnessed, unless the globe of the on be fully within the tangents b a and b' a', fig. 799. That s may take place, the apparent distance of the moon's centre m' m d' must be less than n' o' by the moon's semi-diameter m' n', that we shall have

$$L = n' a' o' - n' a' m' = s a' b' + s a' o' - n' a' m';$$

1, from what has been explained above, this becomes

$$\mathbf{L} = \mathbf{s} - \mathbf{s}' + \mathbf{h}' - \mathbf{h}.$$

By assigning to these quantities the values which render L

$$L = 62'44'' = 1°2'44''$$

I when least,

$$L = 52'49'';$$

and according to the method previously applied, we find a sponding distance from the nodes

> $Ns = 11^{\circ} 37' 36''$ $N's' = 9^{\circ} 47' 19''$.

A total or annular eclipse is therefore possible, if co takes place within 11° 37′ 36″, and certain, if it takes pla 9° 47′ 19″ of the node. It will be total or annular, ace the apparent diameter of the moon is greater or less that the sun.

2925. Appearances attending total solar eclipses.— I consequence of the diffusion of knowledge is, that while the vague sense of wonder, with which singular phenometure are beheld, it increases the feeling of admiration at the nious laws, the development of which renders easily is effects apparently strange and unaccountable. It may be what a sense of astonishment, and even terror, the tempor pearance of an object like the sun or moon must have pran age when the causes of eclipses were known only to the Such phenomena were regarded as precursors of divine verificate of the constantion swead among them but the effects of the constantion swead among them but the

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observed by Mr. Francis Baily, that immediately before the saing, or after the end of complete obscuration, the crescent ared as a band of brilliant points separated by dark spaces, so



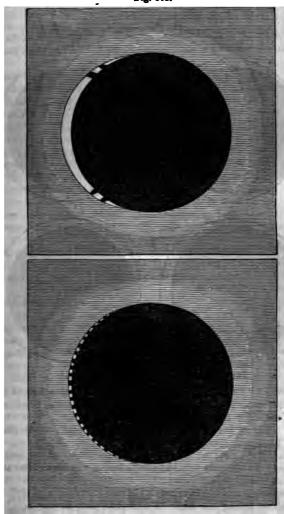


Fig. 804.

e to it the appearance of a string of brilliant "beads." The non, which has since been frequently re-observed, thence the name of "Baily's beads."

er observation showed, that before the formation of the the horns of the crescent were sometimes interrupted and y black streaks thrown across them.

phenomena are roughly sketched in figs. 803, 804.

Fig. 805.

Fig. 806.

ound. The white parts between the teeth will appear like a necke of white pearls.

The fact, that in some cases the beads have not been seen, or if in, appeared in a less conspicuous manner, may be explained by greater or less prevalence of mountainous masses, on that part the moon's surface which forms the edge of its disk at different less.

The beads, in general, disappear suddenly, at the moment of the nmencement of total obscuration, and reappear on the other side the lunar disk, with a somewhat startling, instantaneous effect, at moment the total obscuration ceases.

2928. Flame-like protuberances. — Immediately after the commement of the total obscuration, red protuberances, resembling mes, appear to issue from the edge of the moon's disk. These pearances, which were first noticed by Vassenius, on the occasion the total solar eclipse which was visible at Göttenberg on 3rd sy, 1733, have been re-observed on the occurrence of every total ar eclipse which has taken place since that time, and constitute s of the most curious and interesting effects attending this class phenomena.

2929. Solar eclipse of 1851.—A total eclipse of the sun took ce on the 28th July, 1851, which became a subject of systematic servation by the most eminent astronomers of the present day. considerable number of English observers, aided by several eigners, distributed themselves in parties at different points along path of the shadow, so that the chances of the impediments at might arise from unfavourable conditions of the atmosphere that be diminished. The reports and drawings of these various servers have been collected by the Royal Astronomical Society, it published in their transactions.

The Astronomer Royal, with two assistants, Messrs. Dunkin and imphreys, authorised by the Board of Admiralty, selected certain rts of Sweden and Denmark as the most eligible station. Prosor Airy observed at Göttenberg, Mr. Dunkin at Christiana, and r. Humphreys, assisted by Mr. Miland, at Christianatad.

2930. Observations of the Astronomer Royal. — The weather on a whole proved favourable at Göttenberg. We take from the port of the Astronomer Royal the following highly interesting risculars of the progress of the phenomenon.

"The approach of the totality was accompanied with that indescribably sterious and gloomy appearance of the whole surrounding prospect ich I have seen on a former occasion. A patch of clear blue sky in the sith became purple-black while I was gazing at it. I took off the higher wer, with which I had scrutinized the sun, and put on the lowest power agnifying about 34 times). With this I saw the mountains of the moon resulty well. I watched carefully the approach of the moon's limb to the 1's limb, which my graduated dark glass enabled me to see in great per-

fection; I saw both limbs perfectly well defined to the line becoming narrower and the cusps becoming sharper tortion or prolongation of the limbs. I saw the manner wance up to the sun's, and the light of the sun glamma hollows between the mountain peaks, and saw these tinguished one after another in extremely rapid any of the appearances which Mr. Baily has described overed, and immediately slipping off the dark glappearances represented at a b c d, fig. 1, Pl. XIII.

16 Before alluding more minutely to these, I must I have no means of ascertaining whether the dark in the eclipse of 1842; I am inclined to think the may say appalling, obscurity, I saw the grey growth whether because in 1851 the sky was much (so that the transition was from a more lumin ness nearly equal in both cases), or from what of the darkness in 1851 appeared to me much My friends who were on the upper rock, to what great difficulty in descending. A capilla about a quarter of an hour before the totality to read the minutes of the chronometer-facility and the constant of the chronometer-facility.

"The corona was far broader than that

"I again looked round, when I saw a scene of unexpected beauty. The southern part of the sky, as I have said, was covered with uniform white cloud: but in the northern part were detached clouds upon a ground of clear sky. This clear sky was now strongly illuminated to the height of 30° or 35°, and through almost 90° of aximuth, with rosy-red light shining through the intervals between the clouds. I went to the telescope, with the hope that I might be able to make the polarization-observation, (which, as my apparatus was ready to my grasp, might have been done in three or four seconds,) when I saw that the sierra, or rugged line of projections, shown at (f), had arisen. This sierra was more brilliant than the other prominences, and its colour was nearly scarlet. The other prominences had perhaps increased in height, but no additional new ones had arisen. The appearance of this sierra, nearly in the place where I expected the appearance of the sun, warned me that I ought not now to attempt any other physical observation. In a short time the white sun burst forth, and the corona and every prominence vanished.

"I withdrew from the telescope and looked round. The country seemed,

"I withdrew from the telescope and looked round. The country seemed, though rapidly. yet half unwillingly, to be recovering its usual cheerfulness. My eye, however, was caught by a duskiness in the south-east, and I immediately perceived that it was the eclipse-shadow in the air travelling away in the direction of the shadow's path. For at least six seconds this shadow remained in sight, far more conspicuous to the eye than I had

anticipated."

2931. Observations of Messrs. Dunkin and Humphreys.—
Owing to the unfavourable state of the atmosphere, the observations of the other members of the Admiralty party were not so
attisfactory as those of its chief. Nevertheless, both observers saw
the red prominences, though imperfectly, as compared with the
results of the observations of the Astronomer Royal. Baily's beads
were seen by Mr. Dunkin, as well before as after the total obscuration. Their appearance was of intense brilliancy, compared by
the observer to a diamond necklace. Their effect on the observer
was "quite overpowering," being unprepared for a sight so magnificent.

At Christianstad, the planets VENUS, MERCURY, and JUPITER, and the stars ARCTURUS and VEGA, were visible during the totality

of the eclipse.

2932. Observations of W. Gray, at Tune, near Sarpsborg.—
This gentleman also saw Baily's beads, both before and after the total obscuration. He saw four of the red projections, three of which are represented in fig. 2, pl. xiii., the fourth resembling c and d in form, and diametrically opposite to a in position on the moon's limb. The apparent height of a was estimated at 1½', and its breadth 62", but the altitude of this afterwards increased to 1½'. There was a dark shade in the curved portion, which gave it are memblance to a gas flame. The remainder, however, was rose-red, not uniform, and very pale, like the innermost parts of the petals of a rose. The red prominence opposite to a had an apparent altitude of 1', and a deeper red colour. The prominences c and d were estimated at about 50" in size.

g the totality, the light seemed like that of an ev at an hour and a half after sunset.

Observations of Messrs. Stephenson and And hsvaarn.—Baily's beads were seen both before and curation. The crescent, before disappearing, was ad of light, which broke up into fragments, and wh i, it gave the idea of globules of mercury rushing er along the edge of the moon. In a second or t appearance of the crescent, a rose-coloured flame e limb of the moon, which in form resembled a sic It increased rapidly, and then two other rose-color s, above and below it, started out, differing in sh y of the same character. Besides these, there were them as elsewhere, around the moon's edge otl and other indistinct lines. The height of the princ was estimated at about the twentieth of the moon t is, about 14'. The chief prominences looked like es, and the lurid points and lines reminded the obse eams of cooling lava.

Observations of Mr. Lassell at Trollhättan Falls.—
e red prominences seen in the former total eclipses

stimated its length at 45" of arc, and on attentively watching it towards the end of totality, I saw it materially lengthened (probably to 2'), the moon having apparently left more and more of it visible as she travelled scross the sun. It was always curved, and I did not remark any change of form, nor the slightest motion during the time the sun was hidden. my this extraordinary prominence four seconds after the end of totality, but at this time it appeared detached from the sun's limb, the strong white light of the corona intervening between the limb and the base of the prominence.

"About 10° south of the above object, I saw, during the totality, a detached triangular spot of the same colour, suspended, as it were, in the light of the corona, which gradually receded from the moon's dark limb, as she moved onwards, and was, therefore, clearly connected with the sun. Its form and position, with respect to the large prominence, continued exactly the same so long as I observed it. On the south limb of the moon appeared a long range of rose-coloured flames, which seemed to be affected

with a tremulous motion, though not to any great extent.

"The bright rose-red of the tops of these projections gradually faded towards their bases, and along the moon's limb appeared a bright narrow line of a deep violet tint: not far from the western extremity of this long range of red flames was an isolated prominence, about 40" in altitude, and another of similar size and form, at an angle of 145° from the north towards the east: the moon was decidedly reddish-purple at the beginning of totality, but the reddish tinge disappeared before its termination, and the disk assumed a dull purple colour. A bright glow, like that of twilight, indicated the position where the sun was about to emerge, and three or four seconds later the beads again formed, this time instantaneously, but less numerous, and even more irregular, than before. In five seconds more the sun reappeared as a very fine crescent on the sudden extinction of the beads."

2936. Observations of Mr. Dawes near Engelholm. - Mr. Dawes observed the beads, and found all the circumstances attending their appearance such as to leave no doubt as to the truth of the cause generally assigned to them. He observed the corona a few seconds after the commencement of the totality, and estimated its extreme breadth at half the moon's diameter, the brightness being greatest near the moon's limb, and gradually decreasing outwards. The phenomena of the red protuberances, witnessed by Mr. Dawes, are so clearly and satisfactorily described by him, that we think it best here to give the account of them in his own words,-

"Throughout the whole of the quadrant, from north to east, there was no visible protuberance, the corona being uniform and uninterrupted. Between the east and south points, and at an angle of about 175° from the north point, appeared a large red prominence of a very regular conical form, fig. 6. When first seen, it might be about 1½ in altitude from the edge of the moon, but its length diminished as the moon advanced.

The position of this protuberance may be inaccurate to a few degrees, being more hastily noticed than the others. It was of a deep rose colour,

and rather paler near the middle than at the edges.

"Proceeding southward, at about 145° from the north point, commenced a low ridge of red prominences, resembling in outline the tops of a very arregular range of hills. The highest of these probably did not exceed

his ridge extended through 50° or 55°, and reached, therefore to 7° from the north point, its base being throughout formed by the defined edge of the moon. The irregularities at the top of the emed to be permanent, but they certainly appeared to undelsta west towards the east; probably an atmospheric phenomenon, as was in the west.

about 220° commenced another low ridge of the same character, and in the about 250°, less elevated than the other, and also less in outline, except that at about 225° a very remarkable proterose from it to an altitude of 1½′, or more. The tint of the low is a rather pale pink; the colour of the more elevated prominence dedly deeper, and its brightness much more vivid. In form it ed a dog's tusk, the convex side being northwards, and the concave uth. The apex was somewhat acute. This protuberance, and the connected with it, were observed and estimated in height towards of the totality.

mall double-pointed prominence was noticed at about 255°, and low one with a broad base, at about 263°. These were also of the pured tint, but rather paler than the large one at 225°.

tost directly preceding, or at 270°, appeared a bluntly triangular dy, suspended, as it were, in the corona. This was separated from a's edge when first seen, and the separation increased as the moon d. It had the appearance of a large conical protuberance, whose s hidden by some intervening soft and ill-defined substance, like

37. Effects of total obscuration on surroun y. - Although the different parties of observe. ith of the moon's shadow were not equally fortunin opposition, r unclouded sky, they were all enabled to observers latitude, ffects of the total obscuration upon the surroundingpparent country. Dr. Robertson of Edinburgh, Dr. Robinson conical , and some others, witnessed the eclipse from an island oft, it of Norway, in lat. 61° 21', at a point in the path of the an. The precursory phenomena corresponded with those her observers. The atmosphere was, however, obbed by other observers. I by clouds, which appeared to rush down in streams from lace of the sun. The sea-fowl flocked to their customary of rest and shelter in the rocks. The darkness at the moment al obscuration was sudden, but not absolute; for the clouds left an open strip of the sky, which assumed a dark lurid e, which changed to a greenish colour in another direction, shed upon persons and objects a faint and unearthly light. and candles, seen at fifty or sixty yards distance, were as e as in a dark night, and the redness of their light presented a ge contrast with the general green hue of every thing around "The appearance of the country," says Dr. Robertson, a through the lurid opening under the clouds, was most ap-The distant peaks of the Tostedals and Dorieffeld mounwere seen still illuminated by the sun, while we were in utter less. Never before have we observed all the lights of heaven arth so entirely confined to one narrow strip along the horizon, ever that peculiar greenish hue, and never that appearance of darkness in the place of observation, and of excessive distance

r. Hind says, that during the obscuration "the entire landscape verspread with an unnatural gloom; persons around him assumed earthly cadaverous aspect; the distant sea appeared of a lurid red; outhern heavens had a sombre purple hue, the place of the sun; indicated only by the CORONA; the northern heavens had an se violet hue, and appeared very near. On the east and west e northern meridian, bands of light of a yellowish crimson r were seen, which gradually faded away into the unnatural is of the sky at greater altitudes, producing an effect that can r be effaced from the memory, though no description could a just idea of its awful grandeur."

e verge of the horizon, caused in this case by the hills there; more highly illuminated as they receded by a less and less

is several places in Prussia, where the heavens were unclouded up the total obscuration, a great number of the more conspicuous, as well as the planets Jupiter, Venus, and Mercury, were le. Several flowering plants were observed to close their blos-

40". This ridge adding about 197° from the partitioned over the wine objects and the wine objects are wined to the wine objects and the wine objects and the wine objects are wined to the wine objects and the wine objects are wined to the wine objects and the wine objects are wined to the wine objects and the wine objects are wined to the wine objects are wined to the wine objects and the wine objects are wined to the wine objects are wined to the wine objects are wined to the wine objects and the wine objects are wined to the wi

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jously flying about disappeared,

posphere. — Many of the phoneses afford strong correboratory atmosphere, extending to a very of the sun, the probability of 10).

y, surrounding the dark disk of s observed to be concentrie with the latter is concentrie with the hm's disk, it appears to be es-

non-luminous atmosphere faintly reflecting the sun's light.

The corona supplies no exact data by which the height of the solar atmosphere thus faintly reflecting light can be ascertaised; let Sir J. Herschel thinks, that from the manner in which the distinution of light is manifested on the sun's disk, being by no mean sudden on approaching the borders, but extending to some distance within the disk, the height must not only be great in an absolute sense, but must even be a very considerable fraction of the san's semi-diameter; and this inference is strongly confirmed by the luminous corona surrounding the eclipsed disk.

2939. Probable causes of the red emanations in total solar eclipses.—It appears to be agreed generally among astronomers that the red emanations above described are solar, and not lunar. If they be admitted then to be solar, it is scarcely possible to imagine them to be solid matter, notwithstanding the apparent constancy of their form in the brief interval during which at any one time they are visible; for the entire duration of their visibility has never yet been so much as four minutes. To admit the possibility of their being solar mountains projecting above the luminous atmosphere surrounding the sun, and rising to the height in the extension and non-luminous atmosphere forming the corona necessary to explain their appearance, we must suppose their height to amount to nearly a twentieth part of the sun's diameter, that is, to 44,600 miles.

The fact that they are gaseous and not solid matter appears, therefore, to be conclusively established by their enormous my nitude, the great height above the surface of the sun at which they are placed, their faint degree of illumination, and the circumstance of their being sometimes detached at their base from the visible limb of the sun. These circumstances render it probable that the remarkable appearances are produced by cloudy masses of extensive special shell of non-luminous gaseous matter, surrounding and rising about the luminous surface of the sun to a great altitude.

II. LUNAR ECLIPSES.

Deciring the sum of the section of the shadow, it deprived of the sun's light, and will therefore be eclipsed. circumstances and conditions attending such a phenomenon evidently on the dimensions of the section at the moon's distance, and the position of the relation to it.

Dimensions of the earth's shadow. — Let s, h, s', and k', as before, the apparent semi-diameters and horizontal paralf the sun and moon, and let s express the semi-angle ef a' conical shadow, and s' the apparent semi-diameter o a' n of ion of the shadow at the moon's distance. By the common les of geometry we shall then have

$$s = s - h$$
 $s' = h' - s = h + h - s$.

express the length $\alpha' f$ of the shadow, in semi-diameters of th. We shall then have (2297)

$$\mathbf{L} = \frac{206265}{\mathbf{s}} = \frac{206265}{\mathbf{s} - \mathbf{h}},$$

being expressed in seconds. mean value of s - h being 952", we shall have

$$L = 206.$$

in its orbit round the sun, this conical shadow is therefore tly projected in a direction contrary to that of the sun. The f. fig. 794, of the cone is always in the plane of the ecliptic, vertex f describes an orbit which lies in the plane of the , outside that of the earth, at a distance somewhat above 206 ameters of the earth. Any body, therefore, which may to be in the plane of the ecliptic, or sufficiently near to it, thin this distance of the path of the earth, will be deprived sun's light while it is within the limits of the cone. The eing the only body in the universe which passes within such see of the earth, is therefore the only one which can be thus d.

he distance of the moon, which is less than one-third of the of the shadow, the section of the dark cone is a circular disk, parent semi-diameter of which, according to what has just roved, subtends an angle, the mean and extreme values of

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which will be found by giving to the quantities which enter the preceding formula for s', their mean and extreme values.

The greatest value of s' will be found by subtracting the less value of the sum of the horizontal parallaxes, and it is therefore and

$$s' = 61'27'' - 15'45'' = 45'42''$$
.

Its least value is found by subtracting the greatest value of the subsemi-diameter from the least values of the horizontal parallaxes, and it is therefore

The mean value of s' is, in like manner,

$$s' = 57'47'' - 16'2'' = 41'45''$$
.

The section of the shadow may therefore be regarded as a dark disk, whose apparent semi-diameter varies between 37'49" and 45'42", and the true place of whose centre is on a point or the coliptic 180° behind the centre of the sun. A lunar eclipse is produced by the superposition, partial or total, of this disk on that of the moon, and the circumstances and conditions which determine such an colipse are investigated upon the principles already explained.

By the solar tables, the apparent position of the centre of the san from hour to hour, may be ascertained, and the position of the centre of the section of the shadow may thence be inferred. From the lunar tables, the position of the moon's centre being in like manner determined, the distance between the centres of the section of the shadow and the moon's disk can be ascertained. When this distance is equal to the sum of the apparent semi-diameters of the moon's disk and the section of the shadow, the eclipse will begin; the means when the distance is least will be the middle of the celipse, and the line of greatest obscuration; and when the distance between the centres increasing becomes again equal to the sum of the apparent semi-diameters, the eclipse will terminate. The computation of all these conditions, and the time of their occurrence, presents no other difficulty than those of ordinary arithmetical calculation.

The magnitude of the eclipses is measured, like that of the sum by the difference between the sum of the semi-diameters and distance between the centres.

The occurrence of a total eclipse, and the moment of its commencement, if it take place, are determined by the distance between the centre of the shadow and that of the moon becoming equal to the difference between the semi-diameter of the shadow and that the moon. Thus, a total eclipse will take place if the moon's latituding L in opposition be less than

$$L = s' - s' = (h + h') - (s + s');$$

that is, less than the difference between the sum of the horizont parallaxes and the sum of the semi-diameters. Since the sum of the horizontal parallaxes, even when least, is much greater than the sum of the apparent semi-diameters, even when greatest, a total eclipse of the moon is always possible, provided the centre of the moon approaches near enough to the centre of the shadow, and for the same reason an annual lunar eclipse is impossible.

2943. Lunar ecliptic limits. — That a lunar eclipse may take place, it is necessary that the moon, when in opposition, should approach the ecliptic within a distance less than the sum of the apparent semi-diameters of the moon and the section of the shadow. Let its latitude in opposition be L, the limiting value of this will be

$$\mathbf{L}' = \mathbf{h} + \mathbf{h}' + \mathbf{s}' - \mathbf{s}.$$

If the latitude of the moon be less than this (which is the sum of the semi-diameters of the moon and shadow) an eclipse must take place.

But, as in the case of solar eclipses, the quantities composing this being variable, the limit itself is variable. If such values be assigned to the component quantities as to render L' the greatest possible, we shall obtain the latitude within which an eclipse is possible. If such values be assigned, as will render L' the least possible, we shall obtain the latitude within which an eclipse is inevitable.

To obtain the major limit, we must take the greatest value of h, k', and s', and the least value of s. This will give

$$L' = 61'27'' + 16'46'' - 15'45'' = 1°2'28'';$$

and to obtain the minor limit, we must assign the least values to k, k', and s', and the greatest to s, which will give

$$\mathbf{L}' = 54' \, 7'' + 14' \, 44'' - 16' \, 18'' = 52' \, 83''.$$

The corresponding distances from the node, determined in the same manner as in the case of the solar ecliptic limits, will be, for the major limit,

$$ns = 11^{\circ} 34' 38''$$

and for the minor limit,

$$n' s = 9^{\circ} 24' 22''$$
.

If the moon in opposition be within 11° 34′ 38″ of its node, therefore, a lunar eclipse may take place, and will do so, if the apparent diameters and parallaxes have the necessary values; but if it take place within 9° 24′ 22″ of the node, an eclipse must take place, because the same quantities must be within the requisite limits.

Since the sun moves through these limits on each side of the bode, in from 18½ to 22½ days, it may happen that within the time 37

ion may take place at either node, and consequently that elipse may take place within the year.

Limits for a total eclipse. — It has been explained that a se can only take place when the moon's latitude in oppoess than

$$L = (h + h') - (s + s').$$

rmine the limit within which a total eclipse is possible, we gn to h + h' its greatest, and to s + s' its least, value.

$$\mathbf{L}' = (61'27'') - (30'29'') = 30'58''.$$

ace from the node corresponding to this is therefore

$$N s = (30' 58'') \times \frac{57 \cdot 30}{5 \cdot 15} = 5^{\circ} 44' 21''.$$

ermine the limit within which a total eclipse is inevitable, assign to h + h' its least, and to s + s' its greatest, value.

$$\mathbf{L}'' = (54' \ 7'') - (33' \ 4'') = 21' \ 3'',$$

orresponding distance from the node is

ust, and five may, take place within the year, while not e latter may occur. Nevertheless, the number of lunar exhibited at any given place on the earth is greater than lar eclipses, because, although the latter occur with so much equency, they are seen only within particular limits on the rface.

Effects of the earth's penumbra. — Long before the moon hin the sides of the cone of the shadow, it enters the penud is partially deprived of the suns light, so as to render ination of its surface sensibly mee faint. When once it thin the line a'p', fig. 799, forming the external limit of mbra, it ceases to receive lightfrom that part of the sun near the limb b. As it advaces closer to a'f, the edge e shadow, more and more of he solar rays are intercepted rth; and when it approaces the edge, it is only illumia thin crescent of the sun visible from the moon over the he earth at a'. It mighoe thus inferred, that the obscu-

ration of the mooris so extremely gradual, that it would be impossie to perceive the limitation of the shadow and permitra. Nevertheless, such is the splendour of the olar light, that the thinnest crescent of the sun, to hich the part of the moon's surface near the edge of the earth's shadow is exposed, produces a dege of illuminate which contrasts so strongly withe shadow as to the hate boundary of the latter so distinct, that the phenomenary of the latter so distinct, that the phenomenary of the most striking widences of the resents one of the shadow being the shadow and the shadow being the shadow and the shadow being the shadow as to the shadow being the shadow and the shadow being the shadow being the shadow being the shadow and the shadow being the shadow and the shadow being the shadow as the shadow being the shadow being the shadow as the shadow as the shadow being the shadow as the shadow

2948 Effects of refraction of the earth's atmosphere n total eclipse. — If the earth were not surround with an atmosphere capable of refracting the sun' light, the disk of the moon would be absolutely invible after entering within the edge of the shdow. For the same reason, however, that we entinue to see the sun's disk, and receive its rays after it has really descended below the horizon, an observer placed upon the moon, and therefore the surface of the moon itself, must continue to receive the sun's rays after the interposition of the edge of the earth's disk as seen from the moon. This refracted light falling upon the moon after it has entered within the limits of the shadow, produces upon it a peculiar illumination, corresponding in faintness and colour to

hus transmitted through the earth's atmosphere.

To render this more clear, let ee, fig. 809, represent a diameter of the earth at right angles to the axis f of the shadow, and let a a' represent the limits of the atmosphere. Let sef be the ray proceeding from the edge of the sun, and forming therefore the boundary of the shadow, considered without reference to the atmosphere. But the solar rays in passing through the convex shell of air, between a and e, are affected as they would be by a convex lens composed of a trusparent refracting medium (1028), and are therefore rendered convergent, so that the ray se, instead of passing directly to m, will be not inwards towards m', while the ray which really passes from e to j is one which comes in the direction se, and therefore from a point ithin the sun's disk. The moon's disk, therefore, or any point of t which is within the angle mem, will receive this refracted light and will be illuminated by it in accordance with its colour and integity.

The deflection which a sol-ray suffers in passing through the atmosphere towards e on the se of the sun, is equal to the borzontal refraction, and as, according to the principles of optics (1031), it suffers an equal refraction it cassing out on the other side, the total deflection, which is measured, the angle $m \in m'$, is twice the horizontal refraction. But the me, value of the horizontal refraction being 33', the mean value of thangle $m \in m'$ will be 66'. But since the greatest value of $m \in o$ is $5' \cdot 42'' \cdot (2942)$, it follows that the refracted ray $e \cdot m'$ will fall upon the section of the shadow at point beyond the shadow, it follows that the entire section will be polyton less illuminated by the light the refracted: the intensity of such illumination increases from the entre towards the borders.

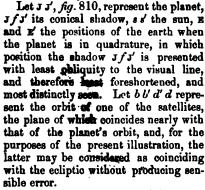
2949. The lunar disk visible during tol obscuration. - When the moon's limb first enters the shadow at 1, the contrast and glar of the part of the disk still enlightened b'the direct rays of the sun render the eye insensible to the more t-ble illumination produced upon the cclipsed part of the disk by the refracted rays. As however, the celipse proceeds, and the magnitud of the part of the disk directly enlightened decreases, the eye, parly relieved from the excessive glare, begins to perceive very faintly the eclipsed limb, which is nevertheless visible from the beginning in a telescope When he entire dist in which it appears with a dark grey bue. has passed into the shadow, it becomes distinctly visible, showing gradation of tints from a bluish or greenish on the outside to gradually increasing red, which, further in, changes to a colour resembling that of incandescent iron when at a dull red heat. As the lunar disk approaches the centre of the shadow, this red line is spread all over it. Its illumination in this position is sometimes so strong as to throw a sensible shadow, and to render distinctly in the telescope the lineaments of light and shadow upon its

se effects are altogether similar to the succession of tints ped in our atmosphere at sunset, and arise, in fact, from the cause, operating, however, with a two-fold intensity. The ays traversing twice the thickness of air, the blue and green are more effectually absorbed, and a still more intense red is ad to the tints transmitted. Without pursuing these consesfurther here, the student will find no difficulty in tracing n the effects of sunset and of sunrise, and of evening and g twilight.

CLIPSES, TRANSITS, AND OCCULTATIONS OF THE JOVIAN SYSTEM.

. The motions of Jupiter and his satellites, as seen from the earth, exhibit, from time to time, all the

effects of interposition.



From E suppose the visual lines E J and E J' to be drawn, meeting the path of the satellite at d and g, and at a' and b', and, in like manner, let the corresponding visual lines from E' meet it at d' and g', and at a' and b'. Let c and c' be the points where the path of the satellite crosses the limits of the shadow, and b' and b' the points where it crosses the extreme solar rays which pass along those limits.

If *l* express the length *J f* of the shadow, *d* the distance of the planet from the sun in semi-diameters of the



Fig. 810.

planet, and r and r' the semi-diameters of the sun and the planet respectively, we shall have (2917)

$$l=d\times\frac{r'}{r-r'}.$$

But

$$d = 11227$$
 $r = 441000$ $r' = 4400$,

and therefore

$$l = 11227 \times \frac{44}{441 - 44} = 1247;$$

that is to say, the length of the shadow is 1247 semi-diameters of the planet. Now, since the distance of the most remote satellite is not so much as 27 semi-diameters of the planet (2760), and since the orbits of the satellites are almost exactly in the plane of the orbit of the planet, it is evident that they will necessarily pass through the shadow, and almost through its axis, every revolution, and the lengths of their paths in the shadow will be very little less than the diameter of the planet.

The fourth satellite, in extremely rare cases, presents an exertion to this, passing through opposition without entering the shadow. In general, however, it may be considered that all the satellites is opposition pass through the shadow.

2951. Effects of interposition. — The planet and satellites exhibit, from time to time, four different effects of interposition.

2952. 1st. Eclipses of the satellites. — These take place when the satellites pass behind the planet. Their entrance into the shadow, called the *immersion*, is marked by their sudden extinction. Their passage out of the shadow, called their emersion, is manifested by their being suddenly relighted.

2953. 2nd. Eclipses of the planet by the satellites. — When the satellites, at the periods of their conjunctions, pass between the lines s J and s' J', their shadows are projected on the surface of the planet in the same manner as the shadow of the moon is projected on the earth in a solar eclipse, and in this case the shadow may be seen moving across the disk of the planet, in a direction parallel w its belts, as a small round and intensely black spot.

2954. 3rd. Occultations of the satellites by the planet. — When a satellite, passing behind the planet, is between the tangents II d' and II J' b', drawn from the earth, it is concealed from the observer on the earth by the interposition of the body of the planet. It suddenly disappears on one side of the planet's disk, and as suddenly reappears on the other side, having passed over that part of its orbit which is included between the tangents. This phenomenes is called an occultation of the satellite.

2955. 4th. Transits of the satellites over the planet. - When s

a, being between the earth and planet, passes between the ts EJ and EJ', drawn from the earth to the planet, its disk is ed on that of the planet, and it may be seen passing across, sall brown spot, brighter or darker than the ground on which ejected, according as it is projected on a dark or bright belt. strance of the satellite upon the disk, and its departure from denominated its ingress and egress.

3. All these phenomena manifested at quadrature. — When net is in quadrature, and the shadow therefore presented to ual ray with least effect of foreshortening, all these several nena may be witnessed in the revolution of each satellite.

nena may be witnessed in the revolution of each satellite.

earth being at E or E', the visual line E J or E' J' crosses the

ry x' or x of the shadow at a distance x' J' or xJ from the

which bears the same ratio to its diameter as the distance of

from the sun bears to the distance of the earth from the

is evident from the figure. But Jupiter's distance from the

ng five times that of the earth, it follows that the distance

ive diameters, or ten semi-diameters, of the planet. But

he distance of the first satellite is only six, and that of the

somewhat less than ten, semi-diameters of the planet, it fol
at the paths of these two will lie within the distance x J

planet being in quadrature 90° behind the sun, the earth at E, and the entire section cc' of the shadow, at the disof the third and fourth satellites (which are 15 and 27 semiers of the planet respectively), will be visible to the west of net, so that when these satellites, moving from b, as indiy the arrow, pass through the shadow, their immersion and n will be both manifested on the west of the planet, by their disappearance and reappearance on entering and emerging e shadow at c and c'. But the section of the shadow, at the s of the first and second satellites, being nearer to the planet z', will be visible only at its western edge, the planet interthe visual ray directed to the eastern edge. The immererefore, of these will be manifested by their sudden disape on the west of the planet, at the moment of their ion; but the view of their immersion will be intercepted by ly of the planet, and they will only reappear after having behind the planet.

third and fourth satellites, after emerging from the shadow of appearing to be relighted, will again be extinguished when me to the visual ray EJa', which touches the planet. The of passing this ray is that of the commencement of their ion by the planet. They will continue invisible until they the other tangential visual ray EJ'b', when they will sudsappear to the east of the planet, the occultation ceasing.

In the cases of the first and second antillities, the communication of the occultation preceding the termination of the scilipse, if it and perceived, the antillite at the moment of the interposition of the edge of the planet not having yet emerged from the similar. In these cases, therefore, the disappearance of the antillite at the same menoement of the eclipse, and its respectives at the terminated of the occultation, alone are perceived, the communication of the unfalled being concealed by the occultation, which has already communication and the disappearance at the commencement of the occultation being prevented by the eclipse not yet terminated.

When the satellite, proceeding in its orbit, arrives at k', its shadow falls upon the planet, and is seen from the earth, at k, to move across its disk as a small black spot, while the planet move from k' to k.

When the planet arrives at g, it passes the visual ray EJ, and while it moves from g to d, its disk is projected on that of the planet, and a transit takes place, as already described.

Thus, at quadrature, the third and fourth satellites present accessively all the phenomena of interposition: Ist, an eclipse of the satellite to the west of the planet shows both immersion and emersion; 2nd, an occultation of the satellite by the planet, the disappearance and reappearance being both manifested; 3rd, the eclipse of the planet by the satellite; and 4th, the transit of the satellite over the planet.

2957. Effects modified at other elongations. — There is a certain limit, such as e, at which the emersion of the third and fourth satellites is intercepted, like that of the first, by the body of the planet. This is determined by the place of the earth from which the visual ray e J c' is directed to the eastern edge of the section of the shadow at the planet's distance. Within this limit the phenomena for the third and fourth satellites are altogether similar to those already explained in the case of the first and second satellites seen from E.

When the earth is between s and s' no eclipses can be witnessed. Those of the satellites are rendered invisible by the interposition of the planet, and those of the planet by the interposition of the satellites.

When the earth is at e' and E', the phenomens are similar to those manifested at e and E, but they are exhibited in a different order and direction. The occultation of the satellite precedes its eclipse, and the latter takes place to the east of the planet. Its like manner, the transit of the satellite precedes the eclipse of the planet.

The student, aided by the diagram, and what has been explained, will find no difficulty in tracing these and other consequences.

2958. Phenomena predicted in Nautical Almanack.—The times of the occurrence of all them several phenomena are calculated and predicted with the greatest precision, and may be found registered in the Nautical Almanack, with the diagrams for each month, to aid the observer. The mean time of their occurrence at Greenwich is there given, so that if the time at which any of them are observed to occur in any other place be observed, the difference of such local time and that registered in the Almanack will give the longitude of the place east or west of the meridian of Greenwich.

2959. Motion of light discovered, and its velocity measured by means of these eclipses. — Soon after the invention of the telescope, Roemer, an eminent Danish astronomer, engaged in a series of observations, the object of which was the discovery of the exact time of the revolution of one of these bodies around Jupiter. The mode in which he proposed to investigate this was, by observing the successive selipses of the satellite, and noticing the time between them,

Now if it were possible to observe accurately the moment at which the satellite would, after each revolution, either enter the shadow, or emerge from it, the interval of time between these events would mable us to calculate exactly the velocity and motion of the satellite. It was, then, in this manner that Roemer proposed to ascertain the motion of the satellite. But, in order to obtain this estimate with the greatest possible precision, he proposed to continue his observations for several months.

Let us, then, suppose that we have observed the time which has clapsed between two successive eclipses, and that this time is, for example, forty-three hours. We ought to expect that the eclipse would recur after the lapse of every successive period of forty-three

pôlite.

Imagine, then, a table to be computed in which we shall calculate and register before-hand the moment at which every successive callege of the satellite for twelve months to come shall occur, and let us conscive that the earth is at A, at the commencement of our characters; we shall then, as Roemer did, observe the moments at which the colleges occur, and compare them with the moments registered in the table.

Let the earth, at the commencement of these observations, be supposed at E, fig. 756, where it is nearest to Jupiter. When the earth, has moved to E', it will be found that the occurrence of the ealigns in a kittle later than the time registered in the table.

La the earth moves from E" towards E", the actual occurrence of the enlipse is more and more retarded beyond the time of its computed commence, until at E", in conjunction, it is found to occur about sixteen minutes later than the calculated time.

By observations such as these, Roemer was struck with the fact that his predictions of the eclipses proved in every case to be wrong. It would at first occur to him that this discrepancy might arise from some errors of his observations; but, if such were the case, it might be expected that the result would betray that kind of irregularity which is always the character of such errors. Thus it would be expected that the predicted time would sometimes be later, and sometimes carlier, than the observed time, and that it would be later and earlier to an irregular extent. On the contrary, it was observed, that while the earth moved from z to z'', the observed time was continually later than the predicted time, and regularly increased. This was an effect, then, too regular and obsistent to be supposed to arise from the casual errors of observation; it must have its origin in some physical cause of a regular kind.

The attention of Roemer being thus attracted to the question to determined to pursue the investigation by continuing to observe the celipses. Time accordingly rolled on; and the earth, transporter

the astronomer with it, moved from z" to z'.

It was now found, that though the time observed was later than the computed time, it was not so much so as at E"; and as the earth again approached opposition, the difference became less and less, until, on arriving at E, the position of opposition, the observed

eclipse agreed in time exactly with the computation.

From this course of observation it became apparent that the lateness of the eclipse depended altogether on the increased distance of the earth from Jupiter. The greater that distance, the later was the occurrence of the eclipse as apparent to the observers, and of calculating the change of distance, it was found that the delay of the eclipse was exactly proportional to the increase of the earth distance from the place where the eclipse occurred. Thus, what the earth was at E'', the eclipse was observed sixteen minutes, a about 1000 seconds, later than when the earth was at E. The diameter of the orbit of the earth, EE'', measuring about the hundred millions of miles, it appeared that that distance product a delay of a thousand seconds, which was at the rate of two hundred thousand miles per second. It appeared, then, that for every two hundred thousand miles that the earth's distance from Jupiter was increased, the observation of the eclipse was delayed one second.

Such were the facts which presented themselves to Roemer. How were they to be explained? It would be absurd to suppose that the actual occurrence of the eclipse was delayed by the increased distance of the earth from Jupiter. These phenomena depend only on the motion of the satellite and the position of Jupiter's shades, and have nothing to do with, and can have no dependence on the position or motion of the earth, yet unquestionably the time the appear to occur to an observer upon the earth, has a dependence of

the distance of the earth from Jupiter.

To solve this difficulty, the happy idea occurred to Roemer that because it which we see the extinction of the satellite by its ratio into the shadow is not, in any case, the very moment at ish that event takes place, but sometime afterward, vis., such an twil as is sufficient for the light which left the satellite just before extinction to reach the eye. Viewing the matter thus, it will imparent that the more distant the earth is from the satellite, left ger will be the interval between the extinction of the satellite, and the arrival of the last portion of light which left it at the light at the moment of the extinction of the satellite is that of light at the earth is the moment the commencement of the light at the carth is the moment the commencement of the light at the carth is the moment the commencement of the light is observed.

Thus Roemer, with the greatest felicity and success, explained and the observed times of sellipses; but he saw that these circumstances placed a great discery at his hand. In short, it was apparent that light is proposed through space with a certain definite speed, and that the sumstances we have just explained supply the means of measuring

s velocity.

We have shown that the eclipse of the satellite is delayed one and more for every two hundred thousand miles that the earth's sance from Jupiter is increased, the reason of which obviously is, a light takes one second to move over that space; hence it is parent that the velocity of light is at the filter in round numbers, two hundred thousand miles per second.

By more exact observation and calculation the velocity is found be 192,000 miles per second, the time taken in crossing the

the orbit being 16m. 26 6s.

2960. Eclipses of Saturn's satellites not observable. — Owing to sobliquity of the orbits of the Saturnian satellites to that of the many, eclipses only take place at or near the equinoxes of the inet, the satellites revolving nearly in the common plane of the satellites revolving nearly in the common plane of the satellites revolving nearly in the common plane of the satellites are difficult of observation as to be practically useless for the determination of longitudes, and have, consequently, received but little interes.

IV. TRANSITS OF THE INFERIOR PLANETS.

2961. Conditions which determine a transit. — When an inferior met, being in inferior conjunction, has a less latitude or distance method that the sun's semi-diameter, it will be less distant the sun's centre than such semi-diameter, and will therefore within the sun's disk. In this case, the planet being between the sun's disk and the sun, its dark hemisphere being turned towards a seith, it will appear projected upon the sun's disk as an in-

tensely black round spot. The apparent motion of the planet being then retrograde, it will appear to move across the disk of the sun from cost to west in a line sensibly parallel to the ecliptic.

Such a phenomenon is called a TRANSIT, and as it can only take place with planets which pass between the earth and sun, it is

limited to Venus and Mercury.

Notwithstanding the very small obliquity of the orbits of these planets, it is evident that transits can only take place when the

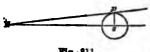


Fig. 811.

planet is within an extremely small distance of its node. Let n be the node, fig. 811, s the centre of the sun's disk on the ecliptic, at the distance N s from the node at which the edge p of the disk just touches the

orbit Np of the planet. It is evident that a transit can only take place when the sun's centre is at a less distance than N s from the node.

Let o express the obliquity p N s of the planet's orbit. The mess value of the semi-diameter sp of the sun being 16' or 0°-266, we shall have (2294)

$$Ns = 0^{\circ} \cdot 266 \times \frac{57 \cdot 3}{9} = \frac{15^{\circ} \cdot 24}{9}$$

The obliquity of Mercury's orbit being 7", we shall have

$$ns = \frac{15^{\circ} \cdot 34}{7} = 2^{\circ} \cdot 18 = 2^{\circ} \cdot 10',$$

and that of Venus' orbit being 3°.39, we shall have

$$Ns = \frac{51^{\circ} \cdot 24}{3 \cdot 39} = 4^{\circ} \cdot 5 = 4^{\circ} \cdot 30'.$$

Thus the distances from the node within which the transits take place, the planet being in conjunction, are 2° 11' for Mercury, and 4° 30' for Venus.

2962. Intervals of the occurrence of transits. - The transits of Mercury and Venus are phenomena of rare occurrence, especially those of Venus, and they are separated by very unequal intervals The following are the dates of the successive transits of Mercury during the latter half of the present century :-

1845	May 8.
1848	Nov. 9.
1861	Nov. 11.
1868	Nov. 4.
1878	May 6.

Those of Venus occur only at intervals of 8, 122, 8; 105, 8, 122, &c., years. Two only will take place in the present century -- in 1874 and 1882.

2963. The sun's distance determined by the transit of Venue. The transits of Venus have acquired immense interest and importance, from the circumstance of their supplying data by which the sun's distance from the earth can be determined with far greater precision than by any other known method. The transits of Mercury would supply like data, but owing to the greater distance of that planet from the earth when in inferior conjunction, the conditions affecting the data are not nearly so favourable as those supplied by Venus.

The details of this celebrated problem are much too complicated, and involve calculations too long and intricate, to admit of being fully explained here, but there is no difficulty in rendering the prin-

ciple and spirit of the solution intelligible.

It will be observed that although the exact determination of the absolute distances of the planets from the sun be attended with some difficulty, there is none in the determination of their relative dis-The observation of their synodic motions, which may be made with great precision, supplies the data necessary for the solution of this problem (2593), and it is thus ascertained that the distances of the earth and Venus from the sun are in the ratio of 1000

It follows, therefore, that when Venus is directly interposed between the earth and sun, as she always must be when a transit takes place, the ratio of her distances from the cash and sun is that of 277 to 728.

Let v, fig. 812, represent the place of the planet at conjunction, and let ee and s s' be two lines taken at right angles to the plane of the ecliptic, and, therefore, to the direction of the planet's motion. The planet v, viewed from any points, such as p and p', upon the line e e', will be seen as projected on corresponding points P and P of the line s s'. Now it is evident that the distance between the points P and P' will bear to the distance between the points p and p' the same ratio as VP bears to ∇p , that is, 728 to 277, or 2.61 to 1. If, therefore, the distance between the points

p and p' upon the earth be known, or can be as: certained (which it always may be), the distance between the corresponding points P and P on the sun will be

$$PP' = pp' \times 2.61.$$

If the points P and P were visibly marked upon the sun, so that the apparent distance between them



could be exactly measured with the micrometer, the linear value of 1" at the sun would be ascertained; for if a express, in seconds the apparent distance between P and P' thus ascertained, we should have for the linear value s of 1"

$$s = \frac{p \, p'}{4} = \frac{p \, p' \times 2.61}{4}.$$

"Supplied with this datum, the distance d of the sun from fie earth would be (2294)

 $d = \frac{p p' \times 2.61}{2} \times 206265.$

If the places of observation p and p' be not placed when a lime at right angles to the ecliptic, its projection on such a line on the ascertained by computation, and may be substituted for it.

It is evident, therefore, that the problem is reduced to the datamination of the apparent angle subtended at the earth by the two points of the sun's disk P and P', upon which the planet is projected when viewed from the two places p and p' upon the earth.

But since the black spot formed by the projection of the plant is in continual motion on the disk of the sun, it would be impressible to determine its position at any given moment with the degree of precision necessary to compare observations of this delicate had made at distant places on the earth. Besides which, to render the observations made at precisely the same moment of absolute time comparable, it would be necessary that the difference of the longitudes of the stations be known with a degree of precision not attainable under the circumstances.

A happy expedient, however, has been imagined by which the difficulty has been effectually surmounted. It will be remembered that the motion of the planet v is at right angles to the plane of the diagram, and therefore to the line ss' supposed to be drawn upon the disk of the sun. The apparent paths of the projections P and P' of the planet on the sun's disk will therefore be also stright angles to this line ss', and parallel to each other, being it

fact, both parallel to the ecliptic.

Fig. 813.

Let 8 s', fig. 813, represent the disk of the sea which is at right angles to the line joining the earth and planet with the sun's centre, and therefore to the plane of fig. 812. Let P and P', fig. 813, represent two points, upon which the plane is simultaneously projected, as viewed from P and P', fig. 812. Let 8 s', fig. 813, be that is ameter of the sun's disk which is in the plane of the ecliptic. The apparent paths of the pre-

jections of the planet on the sun's disk will be parallel to s s', and will therefore be m n and m'n'. Now, if the planet, as it moves,

were to leave a permanent mark upon the disk of the sun, indicating the line its projection followed, seen from each place, it would be an easy matter to measure the apparent distance PF between these lines, and thus solve the problem. No such permanent mark, nor

any other visible indication, however, exists.

F

The synodic motion of the planet, that is to say, its motion relatively to the sun, however, being computed and known with the utmost precision, this motion has, with the greatest felicity and success, been used as a means of estimating the distances between the chords mn and m'n' of the sun's disk, along which the planet appears to move. The time taken at each place by the planet to move ever the chords mn and m'n' being exactly observed, and the rate of the apparent motion of the planet being exactly known, the number of seconds in each of the chords can be ascertained. From these data the length of PF may be computed. We shall have

$$c P^2 = c m^2 - m P^2$$

 $c P'^2 = c m'^2 - m' P'^2$

The distances cP and cP being thus determined, their difference

will be PP, which will therefore be known.

To determine with the necessary precision the duration of the transit at each place of observation, it is necessary to ascertain the exact moment at which the centre of the planet's disk crosses the limb of the sun at the beginning and end of the transit; but as the centre of the planet's disk is not marked by any visible or distinguishable point, this cannot be directly observed. It is ascertained by noting, as precisely as possible, the times of external and internal contact of the planet's disk with the limb of the sun, both at the beginning and end of the transit. The middle of the interval between external and internal contact in each case, is the moment of the passage of the centre of the planet's disk over the limb.

It is evident that the solution of this problem includes the determination of the horizontal parallax of the sun; for the linear value of 1" at the sun as seen from the earth is the same as the linear value of 1" at the earth as seen from the sun. By the method just explained, this is found to be at the mean distance, 466 miles, and since the horizontal parallax s of the sun is the angle which the

semi-diameter of the earth subtends at the sun, it is

$$\pi = \frac{3968}{466} = 8'' \cdot 5$$

and the distance itself of the sun is

$$d = 206265 \times 466 = 96,119,490$$
 miles.

In the practical application of this method, various circumstances are taken into account, such as the effects of the diurnal rotation of the earth, &c.

V. OCCULTATIONS.

2964. Occultation defined. — When any calestial object, the smarcepted, is concealed by the interposition of another, it is said to be OCCULTED, and the phenomenon is called OCCULTATION.

Strictly speaking, a solar eclipse is an occultation of the sun by the moon, but usage has given to it, by exception, the name of m

eclipse.

2965. Occultations by the moon. — The phenomena of this class, which possess greatest astronomical interest, are those of stars and planets by the moon. That body, measuring about half a degree in diameter, moves in her monthly course so as to occult every object on the firmament which is included in a zone extending to a quarter of a degree at each side of the apparent path of her cauta. All the stars whose places lie in this zone are successively occultate, and disappearances and reappearances of the more conspicuous one, as well as those of the planets which may be found within the limits of the same zone, present some of the most striking effects which are witnessed by observers.

The astronomical amateur will find in the Nautical Almenecks table in which all the principal occultations, both of stars and

planets, are predicted.

The disappearance takes place always at the limb of the moon,

which is presented in the direction of its motion.

From the epoch of full moon to that of new moon the moon moves with the enlightened edge foremost, and from new moon to full moon with the dark edge foremost. During the former interval, therefore, the objects occulted disappear at the enlightened edge, and reappear at the dark edge, and during the latter period they disappear at the dark, and reappear at the enlightened edge.

The disappearances and reappearances when the moon is a crecent are especially remarkable. If the disappearance take place at the convex edge, notice of its approach is given by the visible proximity of the star, which, at the moment of contact, is saddedly extinguished. Its reappearance is more startling, for it seems to be suddenly lighted up at a point of the firmament nearly half a degree from the concave edge of the crescent. If the disappearance take place at the dark edge, it is much more striking; the star appearing to "go out" of itself at a point of the sky where nothing interferes with it.

The moon's horizontal parallax amounting to nearly twice is diameter, the part of the firmament on which it is projected and which is its apparent place, differs at different parts of the earth. In different latitudes the moon, therefore, in the course of the month, appears to traverse different zones of the firmament, and consequently to occult different stars. Stars which are occulted in

certain latitudes are not occulted at all at others, and of those which are occulted, the durations of the occultations and the moments and places of disappearance and reappearance are different.

To render this more intelligible, let N s, fig. 814, represent the

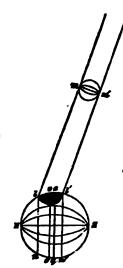


Fig. 814.

earth, n being its north, and s its south Let mm' represent the moon, and m* and m'* the direction of a star which is occulted by it. It must be observed, that the distance of the star being practically infinite compared with the diameter of the moon, the lines m* and m'* are parallel. Let these lines be supposed to be continued to meet the earth at I and I. Let similar lines, parallel to these, be imagined to be drawn through all points of a section of the moon made by a plane at right angles to the direction of the star passing through the moon's centre. lines would form a cylindrical surface, the base of which would be the section of the moon, and it would be intersected by the surface of the earth, a portion of which would be included within it, one half of which is represented by the darkly shaded part of the earth between l and l'. clear that the star will be occulted by the moon to all observers situated within this space.

While this cylindrical space is carried by the moon's orbital motion from west to east, the surface of the earth included between the parallels of latitude l n and l' n', is also carried from west to east, but much more rapidly, by the diurnal rotation, so that the places between these parallels are continually overtaking the cylindrical space which limits the occultation.

It is evident that beyond ln and l'n', which are called the "limiting parallels," no occultation can take place. At l and l' the star is seen just to touch the moon's limb without being occulted, but within those limits it will be occulted. The middle parallel o o', between the limiting parallels, is that at which a central occultation is seen, and where therefore the duration is greatest.

The occultation may be seen from any place upon the earth which lies within the shaded zone, and will be seen provided the phenomenon occur during the night, and that the star at the time be above the horizon at such an altitude as to render the event observable.

In the Nautical Almanack these "limiting parallela" for every conspicuous occultation are tabulated, as well as the data necessary

to enable an observer at any proposed latitude to ascertain previously

whether any particular occultation will be observable.

2966. Determination of longitudes by lunar occultations.—In common with all phenomena which can be exactly predicted, and whose manifestation is instantaneous, occultations of stars by the moon are eminently useful for the exact determination of longitudes. The frequency of their occurrence greatly increases their utility in this respect, and although, for nautical purposes, the observe cannot always choose his time of observation, and therefore cannot be left dependent on them, they come in aid of the lunar method as verifications; and for geographical purposes on land, are among the best means which science has supplied. The times of the disppearance and reappearance, as observed, being compared with the Greenwich times tabulated in the Nautical Almanack, the difference of the longitudes is inferred after applying the necessary corrections.

2967. Occultations indicate the presence or absence of an absence of an absence of an absence around the occulting body. — When a star is occulted by the disk of the moon or planet, its brightness, previously to its disappearance, would be more or less dimmed by the atmosphere surrounding such object, if it existed. Such a gradual decrease of brightness previously to disappearance, as well as a like increase of brightness after reappearance, is observable in occultations by the

disks of planets, but never by the disk of the moon.

It is hence inferred that the planets have, and the moon has not,

an atmosphere.

It might be objected that the lunar atmosphere may not have sufficient density to produce any sensible diminution of brightness. Another test has, however, been found in the effect which the refraction of an atmosphere would have in decreasing the duration of an occultation (2483). No such decrease being observed, it is

inferred that no atmosphere exists around the moon.

2968. Singular visibility of a star after the commencement of occultation. — Some observers, of sufficient weight and authority to command general confidence, have occasionally witnessed a phonomenon in occultations which has been hitherto unexplained. According to them, it sometimes happens that after the occulted star has passed behind the limb of the moon it continues to be seen, and even for a considerable time, notwithstanding the actual interpsition of the body of the moon. If this be not an optical illusion, and if the visual rays actually come straight to the observer, they must pass through a deep fissure in the moon. Such a supposition is compatible with the rare, and apparently fortuitous, occurrence of the phenomenon.

2969. Suggested application of lunar occultations to result double stars. — Sir J. Herschel thinks that these occultations would supply means of ascertaining the double character of some

ters, the individuals suspected to compose which are too close ogether to be divided by any telescope. He thinks, nevertheless, hat they might disappear in perceptible succession behind the dge of the moon's disk. It does not seem to be easy to conceive ow such an effect can be expected in a case where the most powrful telescopes have failed to resolve the stars.

2970. Occultations by Saturn's rings. — In the case of stars sculted by Saturn's rings, a reappearance and second disappearance may be seen in the open space between the ring and the planet. It as been affirmed also, that a momentary reappearance of a star, in he space which intervenes between the rings, has been witnessed. This observation does not, however, seem to have been repeated, otwithstanding the recent improvements in the telescope, and the screened number of observers. The passage of the planet, in a avourable phase of the ring, through the neighbourhood of the silky way, which is so thickly strewed with stars, would afford an enortunity of testing this, and might also supply precise evidence, contive or negative, upon the question of the existence of more than we concentric rings. If other black streaks seen upon the surface I the ring be, like the principal one, real openings between a muliple system of rings, the stars sprinkled in such countless numbers wer the regions of the galaxy, and the adjacent parts of the firmanent, would be seen to flash between ring and ring, as the planet mass before them. Such observations, however, would require in he telescope the very highest attainable degree of optical perfection.

CHAP. XVII

TABULAR SYNOPSIS OF THE SOLAR SYSTEM.

2971. Planetary data. - Having explained, individually, the arrounstances attending the physical condition and motion of the bedies of the system, it remains to bring them into juxtaposition, to view them collectively, and to supply, in tabulated forms, those numerical data which at any given time determine their positions and motions.

- Such data may be resolved into three classes: --

L Those which determine the orbit.

II. Those which determine the place of the body in the orbit.

III. Those which determine the conditions which are independent

as the orbit.

I. Data which determine the form, magnitude, and position of the orbits of the planets.

2972. Form of the orbit determined by the eccentricity.—It is well understood (2606) that the form of an ellipse depends on the eccentricity; all ellipses with the same eccentricity, however they may differ in magnitude, having the same form.

Let a = the mean distance, c = the distance of the costs of the orbit from the centre of the sun, and e = the cocentricity. We

shall then have

$$e = \frac{c}{a},$$
 $c = a \times e.$

٠ (

Ą:

The values of e, in the cases of all the principal planets, its cury excepted, are less than \mathbf{r}_0^1 . In the case of Mercury, it is also \mathbf{r}_0^1 , and in the larger planets \mathbf{r}_0^1 .

In the case of the planetoids, the eccentricities are subject great and exceptional variation, amounting in one case to ; and

others being less than wo.

2978. Magnitude determined by semi-axis major. — As the eccentricity determines the form, the semi-axis determines the magnitude, of the orbit. This quantity forms in other respects a very important planetary element, since upon it is dependent also, by the Harmonic law, the periodic time, and, consequently, the mean are

gular and mean linear velocity in the orbit.

2974. Position of the plane of the orbit.— The plane of the orbit must always pass through the centre of the sun, which is therefore the common point at which the planes of all the planes of orbits intersect. But to define the position of the plane of say orbit something more is necessary. If the plane of the earth's orbit be provisionally assumed as a fixed plane (which, however, is not, as will appear hereafter), the positions of the planes of the orbits of the planes, severally, with relation to it, will be determined, 1st, by the angle at which they intersect it, and, 2ndly, by the direction of the line of intersection.

2975. Inclinations of the orbits. — The angles which the plane of planets' orbits form with the plane of the ecliptic are generally less than 3°. Of the principal planets, Mercury forms an exception to this, having an inclination of 7°. The planetoids are also exceptional, the orbit of one having an inclination of 34½°; the inclination of 34½°; the inclination of 34½°;

tions of the others varying between 16° and 1°.

2976. Line of nodes.— The inclination is not enough to determine the position of the plane of the orbit, for it is evident that at infinite variety of different planes may be inclined at the same and to the ecliptic. If, however, the direction of the line of intersection of the plane of the orbit with the plane of the ecliptic (which lies must always pass through the centre of the sun) be also defined.

the position of the plane of the orbit will be determined. This line of intersection is called the *line of nodes*, being the direction is which the nodes of the planet's orbit are seen from the sun. If an observer be imagined to be stationed at the centre of the sun, he will be in this line, and the nodes will be viewed by him in opposite directions along this line, the ascending node (2625) being viewed in one direction, and the descending node in the other.

2977. Longitude of ascending node. — It has been customary to define the direction of the line of nodes by the angle which the direction of the ascending node, seen from the sun, makes with the direction of the "first point of Aries," or, what is the same, by its

beliocentric longitude.

The position of the plane of the orbit is, therefore, determined by its inclination and the longitude of the ascending node.

2978. Longitude of perihelion. — These data, however, are still insufficient to determine the position of the orbit. They would be sufficient if the orbit were circular, since a circle is symmetrical with relation to its centre. But the orbit being an ellipse, the major axis may have an infinite variety of different directions, all of which shall pass through the sun's centre, and all of which shall be in the same plane. After defining, therefore, the position of the plane of the orbit, it is necessary to determine the position of the orbit upon that plane, and this is determined by the direction of its major axis, just as the plane itself was determined by the direction of the line of nodes, and as the latter was determined by the heliocentric longitude of the ascending node; the position of the orbit upon its plane is determined by the heliocentric longitude of perihelion (2608).

2979. Five elements which determine the orbit. — The orbit of a planet is, therefore, determined, in form, magnitude, and position, by the five following data, which are called its ELEMENTS:—

1.	The semi-axis, or mean distance	a
2.	The eccentricity	e
	The inclination	
4.	The longitude of the ascending node	,
5.	The longitude of perihelion	π

The eccentricity is sometimes expressed by the angle ϕ , of which is the sine, which is called the "angle of eccentricity."

2980. Elements subject to slow variation — Epoch. — If the elements of the orbit were invariable, they would be always known when once ascertained. But it will appear hereafter, that although for short intervals of time they may, without sensible error, be regarded as constant, some of them are subject to slow variations, which, after long intervals, such, for example, as centuries, com-

TABLE I.

Data which determine the magnitude, fun,

		Semi-axis.		Eccentr	ucity.	
Planet.	Sign.	α				
MERCURY	ğ	0-3870985	0-2056063	11	l á	1:
VENUS	ç	0.7233317	0.0068618	0	23	12
EARTH	ė	1.0000000	0.01679226	0	57	10
MARS	3	1-523691	0-0932168		90	19
PLANETOIDS:	0	2,000		10	1 ~	1
Ceres	0	2-766921	0-0763660	4	97	1 mi
Pallas	0	2.772896	0-2394280	18	40	1B
Juno	0	2-669095	0-2560780	14	50	pi)
Vesta	0	2:361702	0.0888410	5	5	154
Astræa	0	2-577400	0-1887517	10	52	à
Hebe	0	2-425368	0-2020077	11	38	40
Iris	0	2.385310	0-2323515	13	26	100
Flora	(9)	2-201727	0.1567974	9	1	130
Metis	0	2.386897	0.1228221	7	1	284
Hygeia	(1)	3-151388	0.1009159	5	47	598
Parthenope	(11)	2:448097	0-0980302	5	43	20
Victoria (Clio)	(12)	2.335003	0-2181980	12	25	332
Egeria	(13)	2.582492	0.0862748	4	57	0
Irene	(1)	2-581951	0-1697575	9	46	20
Eunomia	(16)	2-650918	0.1893392	10	47	23
Psyche	(16)	2-932951	0-1309378	7	81	20
Thetis	(17)	2:343192	0.0464569	6	24	20.02
Melpomene	18	2-295713	0-2159123	12	28	ā
Massalia	100	2:375851	0.1338916	7	41	40
Fortuna	60)	2.445902	0-1555438	9	3	粉章
Lutetia	1	2-604770	0-3398105	19	52	4
Calliope	@	1	1	1	-	-
Thalia	3	1	2	10	-	-
Themis	(3)	1	1	1	-	-
Phocea *	(9)	1	1	1	-	-
Proserpine	(20)	1	7	2	-	-
TUPITER	24	5-202767	0.0481621	2	45	40
SATURN	72	9-538850	0.056T505	. 3	13	
URANU8	H	19-1824	0.0466	2	40	15
NEPTUNE	Ψ	30-04	0-0087195	0	29	\$95

This planetoid was discovered on the 6th of April, 1863 (since p. 315 of the tory, and on the preceding day, April 5th, Themis was discovered by M. 6st.

TABLE I. and position of the Planetary Orbits.

Name and the same

, 1	elination	Ba .	Lo	ngitude i	of *	E J	ongitude Perihelipa	lo L	Epoch.
	4			P			*		M. T. Paris,
0	6	5	45	57	38	74	20	42	1 Tennes 1000
3	23	29	74	51	41	128	43	6	1 January, 1800.
0	0	0	0	0	0	99	30	29	
1	51	8	47	59	38	332	22	51	
10	87	12	80	49	50	148	2	54	2-0 July, 1852.
84	87	20	172	45	14	121	24	11	2-0 July, 1852.
13	3	17	170	56	28	54	18	55	24-0 September, 1852.
Ť	. 8	25	105	23	14	250	44	3	3-0 November, 1852.
5	19	23	141	27	48	135	42	32	29-5 April, 1851.
14	46	32	138	31	55	15	15	26	13·0 July, 1852.
5	28	16	259	44	5	41	20	22	8-0 June, 1852.
	53	3	110	20	53	32	49	45	24-0 March, 1852.
	35	55	68	28	58	71	83	11	40 June, 1852.
8	47	11	287	88	27	218	2	29	28-5 September, 1851.
4	36	54	124	59	54	317	8	51	13·0 July, 1852.
8	23	7	235	29	31	301	55	18	0-0 January, 1851.
16	33	7	43	17	40	118	17	17	15.0 March, 1852.
9	5	33	86	51	33	178	26	58	13-0 July, 1852.
11	43	50	298	53	19	27	13	24	13.0 October, 1852.
8	8	37	150	36	43	11	28	9	31·0 March, 1852,
8	42	32	128	5	50	271	25	26	1.0 May, 1852.
10	10	38	149	54	23	15	35	53	10·0 July, 1852.
0	50	16	203	20	8	144	1	40	0-0 October, 1852.
1	33	18	211	0	9	31	16	13	23-5 September, 1852.
8	19	49-9	78	28	43.4	309	53	194	0-0 Dec. 1852, M. T. Ber
7	-	-	2	-	-	1	-	-	
1	-	-	1	-	-	1	-	-	0.00
1	-	-	1	-	-	1	-	-	
1	-	-	1	-	-	1	-	-	
1	-	-	1	-	-	1	-	-	
1	18	52	98	25	45	11	7	38	1 January, 1800.
2	29	86	111	56	7	89	8	20	
0	46	28	72	59	21	167	30	24	**
1.	46	50	130	6	52	47	14	37	4

was printed), by M. Chacornac, (the discoverer of Massalia), at the Marsellles Observaak Maples. Proceeping was discovered on the 5th of May by Luther. pletely change the orbits. These variations have been calculated with surprising precision, and are, moreover, found to be periodical although their periods are in general of such magnitude as to surpass not only the limits of human life, but those of all human record.

Since, therefore, the planetary objects are thus subject to a low but constant change, it is necessary in assigning their element, to assign also the date at which the orbits had these elements. What the rates at which the elements severally vary are known, their values at any assigned date being given, their values at any there date, anterior or posterior, can be determined.

The date at which the elements of the orbits have had the raise

assigned to them is technically called the EPOCH.

2981. Table of the elements of the orbits. — In the present table are given the elements of the planetary orbits, severally, at the epochs assigned in the last column. Those of the more recently discovered planets must be regarded as provisional, and subject to

such corrections as future observations may suggest.

The elements are taken from the tables published by the Fresh Board of Longitude, with the exception of those of the recent discovered planetoid LUTETIA, the elements of which are given provisionally, from those calculated by M. George Rumker, Jan of Hamburg. (Comptes Rendus de l'Acad. des Sc. t. xxxv. p. 810.)

To illustrate the relative mean distances of the planets from the sun, and from each other, we have delineated, nearly in the proper proportions, the mean distances of the principal planets and

the planetoids or asteroids, in fig. 815.

II. Data to determine the place of the planet.

2982. By the epoch and the mean daily motion. — The obtice being defined in magnitude, form, and position, it is necessarily supply the data by which the position of the planet in it at my assigned time may be found. It will be sufficient for this to see the position which the planet had at the EPOCH, and the persent time, from which the mean daily motion of the planet can be inferred. By means of this motion, the mean place of the planet for any given time anterior or posterior to the epoch can be determined.

2983. The equation of the centre. — To find the true placed the planet, a further correction, however, is necessary velocity of the planet referred to the sun is not a greatest at perihelion and least at aphelion. The difference the position which the planet would have, as seen from its angular motion were uniform, and that which it actuary



called the "equation of the centre," and tables are computed by which this correction for each planet may be made, so that, the mean place of the planet in its orbit being determined, the true place may be found.

2984. Table of the data necessary to determine the place of the planet. — In the following table are given the data which are necessary to determine the mean place of each of the planets for any given time. In the first column is given the mean longitude of the planet at the EPOCH assigned in Table L, and in the second column is given the mean daily increment of heliocentric longitude.

The SIDEREAL PERIOD, or the time which the planet takes to make a complete revolution round the sun, is given in days and years in the third and fourth columns.

If the equinoctial points were fixed, the sidereal period would be equal to the interval between two successive returns of the planet to the same equinoctial point. But the equinoctial points are subject, as will appear hereafter, to a very slow retrograde motion, in virtue of which the first point of Aries, from which right ascensions and longitudes are measured, moves annually from east to west upon the ecliptic through a space a little less than a degree. A planet, therefore, departing from the vernal equinoctial point, and moving constantly from west to east, will return to that point before it completes its revolution, inasmuch as that point moving in the contrary direction meets it before its return to the point of departure.

It follows from this, that the interval between two successive returns to the vernal equinoctial point is a little less than the sidereal period. This interval is called the *equi*noctial period, and is given in the fifth column of Table II.

The synodic period is given in the last column.

2985. Table of extreme and mean distances from sun and earth.—In Table I., the

Fig. 815.

TABLE II.

Data which determine the places of the Planets in their respective Orbits at a given time.

Name.	Lon	poch.	at	Dally Motion.	-61	Per	Margaria.	APRIL REL
Name.				Α -	Sidere	al.	Equipment .	Spends.
MERCURY VENUS. EARTH MARS PLANETOIDS: Flora Melpomene. Victoria (Cilo) Thetis. Vesta Massaila Iris. Metis Hele Fortuna Parthenope Astrea Irene Egeria Lutetia Eunomia Juno Ceres Pallas Payche Hygeia Calliope Thalia Themis Phocea Procerpine	146 100 233 174 302 7 199 35 13 85 255 47 323 356 61, 47 22 145 123 149 123 149 123 149 123 149 123 149 123 149 123 149 149 149 149 149 149 149 149 149 149	133 444 553 5 466 144 422 3 559 177 455 229 443 225 100 421 455 —	18 56 30 34 5 20 5 5 26 22 33 44 4 8 55 52 7 10 31	14732419 5767-668 3548-193 1886-518 1086-0790 1020-0708 994-4325 989-2240 977-6178 968-5970 963-1396 963-1396 853-2337 854-9642 844-0179 822-07-61 813-0926 770-9242 768-6413 706-3977 634-2404 ?	Days — F. 87 96826 224 70080 305-25637 680 97964 1193-281 1270-498 1303-255 1310-116 1325-609 1337-601 1346-9400 1377-935 1397-135 1397-135 1515-850 1515-850 1516-493 1515-850 1526-9403 1515-850 1516-9403 1516	Years—P, 0 2408 0 6152 1 0000 1 8807 7 3 2968 3 4785 3 5650 3 6570 3 6520 4 1300 4 1503 4 2040 4 3650 4 5595 4 6100 5 5 220 5 5 342 1	Tops.	001- 1105 1205 1205 1205 1205 1205 1205 1205 1205
JUPITER SATURN URANUS NEPTUNE	81 123 178 335	54 6 30 8	49 29 87 58	298-989 120-435 42-233 21-554	4332-58480 10759-2198 30686-8205 60127-	11-86 29-46 84-01 164-62	4330-6105 10740-7324 30589-3573 59743-	3084 3780 3097 3674

mean distances α of the several planets from the sun are expressed in numbers, of which the earth's mean distance is the unit. It is necessary, however, to compute the actual mean distances in such known units, such as miles. To obtain these it is only necessary to multiply the actual mean distances of the earth in miles by the numbers in the column α of Table I.

It is also necessary to assign the actual limits of the varying tances of the planets as well from the earth as from the sun. These are easily determined by the data in Table I.

2986. Perihelion and aphelion distances.—Let the extress at mean distances of the earth from the sun, expressed in million distances, be

d = mean distance d' = least distance d'' = greatest distance:

we shall then have, according to what has been already explained and proved.

$$d=95$$
, $d'=95\times (1-e)$, $d''=95\times (1+e)$,

the value of e in the case of the earth being 0.01679226.

Let the mean and extreme distances of a planet from the sun be in like manner expressed by D, D', D" in millions of miles, and we shall have

$$\mathbf{D} = 95 \, a, \quad \mathbf{D}' = 95 \, a \times (1 - e), \quad \mathbf{D}'' = 95 \, a \times (1 + e).$$

The distance s of a planet from the earth at superior conjunction being equal to the sum of the distances of the earth and planet from the sun, we shall have

$$s = D + d$$
.

This will vary, because the distances from the sun vary. It will be gradest when the earth and planet are both in aphelion, and least when they are both in perihelion. If s", therefore, express the greatest, and s' the least possible, distance of the planet when in conjunction, the mean being expressed by s, we shall have

$$s'' = D'' + d''$$
 $s' = D' + d'$.

The distance of an inferior planet from the earth, when in inferior conjunction, is found by subtracting the planet's distance from the sun from the earth's distance. If o express the mean distance of the planet in inferior conjunction from the earth, we shall have

$$o = d - D$$
.

The distance will vary according to the relative positions of the axes of the elliptic orbits, and will evidently be greatest when the earth is in perihelion and the planet in aphelion. If o' and o' then express, as before, the greatest and least possible distances of the planet in inferior conjunction, we shall have

$$o'' = d'' - p'$$
 $o' = d' - p''$.

The distance of a superior planet in opposition is found by subtracting the earth's from the planet's distance; and it may in like manner be shown that the mean and extreme distances of the planet in opposition from the earth will be

$$0 = D - d$$
 $0'' = D'' - d'$ $0' = D' - d''$.

In the following table the mean and extreme distances of the planets successively from the sun and earth are given as computed by these several formulæ. The method of computation is indicated at the head of each column. (See Table on next page.)

TABLE III.

Distances from the Sun and from the Earth in millions of

and the same	Dist	ance from t	Sun.	Distance from Earth.					
20-1			50	At super	rier conjunc	tion.	Al opp		
Name,	Greatest.	Lesst.	Mean	Greatest.	Least.	Mean.	Greatest.		
	D" = 95a (1 + e)	D' = 95a (1 - e)	D = 95a	=D"+d"	S' =D' +d'	S = D+d	=D''-d'		
MERCURY VENUS EARTH	44·32 60·18 96·59 158·24	29-32 68-24 93-41 131-26	36-77 68-71 95-00 144-75	140-91 165-77 254-83	122-73 161-66 224-67	131-77 163-77 239-77	67:27 25:35 64:83		
PLANETOIDS: Flora		205-89 170-99 178-45 212-28 204-44 195-49 173-97	209-17 218-08 221-82 222-61 224-30 225-71 226-61	340.87	299-30 264-40 260-86 305-69 297-85 288-90 267-38	304-77 313-77 316-77 319-77 329-77 321-77	119-04 177-76 176-80 139-53 150-87 162-52 125-84		

TABULAR SYNOPSIS OF THE SOLAR SYSTEM.

TABLE IV.

Data affecting the Planet, which are independent of its Orbit.

	Real Diameter.		Ap	parent D sm	eter.	8	urface.	Volume,		
	Earth's	Miles.	Greatest.	Lear.	Mean.	Earth's=	Millions Square Miles.	Earth's = 1.	Bittieza Cubie Miles.	
	Δ	8	δ 0''×206265	, -	∂ D×206265	$\Delta' = \Delta^2$	$\delta = \Delta' \times \mathbf{E}'$	Δ" Δ'	δ" = Δ"×E"	
CURY	0-315	2,950	12-4	4-3	8-4	0-139	2-734	0-0519	0-0135	
s	0 956	7,800	66-4	6-3	36 4	0-972	15-540	0-958	0-249	
я	1-000	7,912	-		-	1-000	19-660	1-000	0-260	
s	0-518	4,100	24-4	3-3	14-0	0-268	5-271	0 139	0-036	
ER.	11-150	85,640	48-9	30-0	39-0	125-000	2458-330	1397-400	363-330	
BN .	9-501	75,000	20-5	14-6	17-6	90-250	1775-000	857-400	223-000	
US .	4 360	34,500	4-3	8-5	3-9	19-000	373-660	62-900	21-550	
UNE	4-740	37,500	2-8	2-6	2.7	22-460	441-700	107-200	- 27-600	
	111-450	882,000	1947-6	1883-5	1915-5	12410-000	244066-000	1354333-000	359925-000	
·	0-272	2,153	1982-5	1776-5	18:3 7	0-074	1:456	0-020	0.0052	

		Mass	Density.		Diag	Apparent Diameter of Suu.		R	Rotation.		Inclimation of Axis to Orbit,			Ob- late- ness.	
	Earth's	Sun's	Trivilions Tons.	Earth'	Water's	Earth = 1.		Earl Earl		Ī					
	Δ""		ð'''	=	x'	1	1915		ı	T		0	0 +		
	354906	9	Δ× 6069	Δ''' Δ'''	± 2×5 67	ā	a	$\frac{1}{a^2}$	ħ	m					
TRY	0-175	2025810	1063	3-45	19-56	2-550	1947	6-67	24	5	07		-	-	7
	0.885	401211	6369	0-92	5-22	1-350	2647	1-91	23	21	21	,	-	-	1
ı.,	1 000	354936	6009	1-00	5-67	1-000	1915	1-00	23	56	4	23	28	0	1 299
	0-132	2080807	804	0-95	5-39	0-656	1256	0-43	24	37	22	28	27	0	167
B.	238-475	1048-70	2054200	0:24	1-36	0-192	366	0-037	9	55	25	3	5	30	13
N.	101-066	3512	613300	0-12	0-68	0-105	201	0.011	10	29	17	26	48	40	111
s .	14-2:5	24500	86505	0-17	0-97	0-052	100	0 003	9	30	07	7	-	-	ì
NE	18-900	1 18780	114700	0-17	0-97	0 033	61	0.001	7	-	-	7	-	_	2
	354976-000	1	2154100000	0:26	1-47	-	-	-	607	4	0	-	-	-	0
	0-0125	28394880	38-8	0-62	3 52	1 000	1915	1-00	655	44	0	_	-	-	0

	Sup Gr	ordelal avity.	Orbital Velocity.			Voinc Boss at Eq	استثل	Gara	
	Barth's = 1.	Fall Fool in 1 Second.	Earth's — L	Miles per Hour,	Fact per Second.	Miles Pr How.	Į	Terre- trial Gravity = L	2/1/1
	<u>√</u> Δ*	£×16-00	¥ √a	7: 7 × 6000	₹'. × 586 *' × 586	3×3-MIS	`	0 1 100×2	7 10-00 ×6
MERCURY	0-60	804	1-60	110796	169400	37 0	548	-14	-
VERCUS	+#0	14-65	1-1	810 0 0	119800	1040	1540	=	-
BARTH	1-00	10-08	1-00	68F 8 0	101096	1040	1886	1	139
MARS	954	304	0-61	65812	\$1860	883	788	- 1 - 1	a
JUPITER .	548	39-40	0-44	30803	44297	99 1986	41956	44	**
SATURN .	1-18	19-00	0-92	22906	26715	25440	200 10	1	10
URANUS .	0-75	12-06	0.23	15730	23070	11410	16736	100100	9453
NEPTUNE	0-84	13-56	0-18	1257C	18435	,	,	1007333	0-13B
SUN	98-58	450-47	-	-	-	4561	6694	-	-
моом	0:169	-72	0-033	2265	3338	10-3	16-13	1006	119

given in the several columns of Table IV. have been already explained. Some of them, however, require further elucidation.

2988. Method of computing the extreme and mean apparent diameters. — The real diameters & being ascertained by the methods explained in (2299), the extreme variation of the apparent diameter may be found from a comparison of the real diameter with the extreme and mean distances D', D, D, given in Table III. We have thus (2294)

$$a'' = \frac{\delta}{D''} \times 206265$$
, $a' = \frac{\delta}{D'} \times 206265$, $a = \frac{\delta}{D} \times 206265$.

2989. Surfaces and volumes. — The surface of the earth consists of 197 millions of square miles, and its volume of 259,800 millions of cubic miles. Let these numbers be expressed respectively by x and x''. Since, then, the surfaces of spheres are as the square, and their volumes as the cubes, of their diameters, if Δ' express the surface and Δ'' the volume of a planet related to those of the earth as an unit, and δ'' the volume in billions of cubic miles, we shall have

$$\Delta' = \Delta^2,$$
 $\Delta'' = \Delta^3$
 $\delta' = \Delta' \times E'$ $\delta'' = \Delta'' \times E''.$

2990. The masses. — The masses of the planets in relation to the sun being ascertained by the several methods explained in (2633), et seq., and the ratio of that of the sun to the earth being ascertained to be 354936 to 1, let Δ''' express the mass related to that of the earth, and Σ''' to that of the sun as the unit. We shall then have

$$\Delta'''=\frac{\Sigma'''}{854936}.$$

By which Δ''' may be inferred from Σ''' .

The actual weight of the earth in trillions of tons being 6069 (2394), let the weight of any other mass in trillions of tons be ", and we shall have

$$\delta''' = \Delta''' \times 6069.$$

2991. The densities. — The mean densities being the quotients obtained by dividing the volumes by the masses, and the mean density of the earth related to that of water as the unit being 5.67 (2393), let the mean density of any of the other bodies related to that of the earth as the unit be x, and related to water x', and we shall have

$$x = \frac{\Delta'''}{\Delta''} \qquad x' = x \times 5.67.$$

2092. Certain data not exactly ascertained. — It will be useful to observe that, in the determination of several of these, the results of the observations and computations of astronomers are to a certain extent at variance, and a corresponding uncertainty attends such data, as well as all conditions which depend on them or are derived by calculation from them. This is more especially the case with the masses of those planets which are unaccompanied by satellites, and consequently with the densities which are ascertained by dividing the masses by the volumes.

As an example of the masses and densities of some planets.—
As an example of the character and extent of these discrepancies, we give the following estimates of the masses of some of the principal planets expressed as fractions of the mass of the sun. The column E contains the values assigned by Professor Encké, from a comparison of all the authorities, except that of Neptune, which is given on the authority of Professor Pierce. The column E contains the values adopted by the French Board of Longitude, and the columns L and M the values given in the treatises lately published in Germany by Professors Littrow and Mädler.

	P.	7.	L.	M.
MERCURY	1	1 202-5010	1	l Account
VENUS	401830	401847	405471	401718
EARTH	300661	36:036	365000	3440
URANUS	9580337	9660327	2545020	
NEPTUNE	94905 1 18780	94000 1 14446	21000 1	34 H

It will be observed that in Table IV., as well as in the preceding tables, the quantities are in all cases reduced to, and expressed in, those actual standard measures and weights with which all persons are familiar. The utility of this was very foreibly expressed and very happily illustrated by the Astronomer Royal, in the popular lectures delivered by him at Ipswich.

2994. Intensity of solar light and heat. — Since the intensity of solar radiation decreases as the square of the distance from the sna decreases, if γ expresses its intensity at the mean distance of any planet relative to its intensity at the earth as the unit, we shall have

$$\gamma = \frac{1}{a^2}$$
.

2995. Superficial gravity. — The superficial gravity of a spherical body being in proportion to its mass, divided by the square of its semi-diameter, and the height through which a body falls upon the surface of the earth in one second being 16.08 feet, let g' express the superficial gravity of a spherical body related to that of the earth as the unit, and let f' express the height through which a body submitted to it would fall in one second, and we shall have

$$g' = \frac{\Delta'''}{\Lambda^2}, \qquad f' = g' \times 16.08.$$

2996. Orbital velocities.—It is easy to show that it follows as a necessary consequence of the harmonic law, that the mean orbital velocities of the planets are in the inverse ratio one to another of the square roots of the distances; for since these velocities are proportional to the circumferences, or, what is the same, the semi-diameters of the orbits, divided by the periods, they are proportional to $\frac{a}{P}$; but since, by the harmonic law, P^{2} is proportional to a^{3} , the velocities will be proportional to $\frac{a}{\sqrt{a^{3}}}$, or, what is the same, to $\frac{1}{\sqrt{a}}$, that is, inversely proportional to the square roots of the mean distances.

This being understood, and the mean orbital velocity of the earth

expressed in miles per hour being 68,890, let v be the mean velocity of a planet related to that of the earth as the unit, and v' its mean velocity in miles per hour, and we shall have

$$\mathbf{v} = \frac{1}{\sqrt{a}}, \quad \mathbf{v}' = \mathbf{v} \times 68890;$$

and since the ratio of miles per hour to feet per second is that of 5280 to 3600, if v" be the velocity in feet per second, we shall have

$$\mathbf{v''} = \frac{528}{360} \times \mathbf{v'}.$$

2997. Superficial velocity of rotation. — The superficial velocity of a planet at its equator in virtue of its diurnal rotation is found by comparing the circumferences of its equator with the time of its rotation. By the elementary principles of geometry, the circumference of a circle whose diameter is δ , is $\delta \times 3.1415$, and if τ express the time of rotation in hours, we shall have for v, the velocity of rotation in miles per hour

$$v = \frac{\delta \times 3.1415}{T};$$

which may be reduced to feet per second, as before, by

$$v'=v\times\frac{528}{360}.$$

2998. Solar gravitation. — The general law of gravitation supplies easy and simple means by which the force of the sun's attraction at the mean distance of each of the planets may be brought into immediate comparison with the known force of gravity at the surface of the earth.

Let this latter force be expressed by g. It will decrease in the same ratio as the square of the distance of the body affected by it increases. The distance of the sun being 24,000 semi-diameters of the earth, the intensity of the attraction which the earth's mass would exert at that distance would be

$$\frac{g}{24000 \times 24000} = \frac{g}{576,000000}.$$

But the mass of the sun being 354,936 times that of the earth, it will at the same distance exert an attraction 354,936 times greater. The intensity of the attraction, therefore, which the sun exerts at the earth's mean distance will be

$$g \times \frac{354936}{24000^8} = \frac{g}{1626};$$

and the intensity of its attraction at the mean distance of the other planets being still inversely as the squares of the distances, will be found by dividing this by a^2 . So that if G express this attraction, and F the height, in thousandths of an inch, through which a body placed at each distance would fall in one second, we shall have

$$G = \frac{g}{1626 \, a^9}$$
 $F = 16080 \times 12 \times G = 192960 \, G.$

By the numbers given in the column a, it is there to be understood that a mass of matter which, placed upon the surface of the earth, would weigh the number of pounds expressed by the descendant or of the fractions severally, would, if submitted only to the sun's attraction at the respective mean distances of the plants, gravitate to the sun with the force of one pound. Thus, a mass which on the earth's surface would weigh 1626 lbs. would weigh only one pound if exposed to the sun's attraction in the absence of the earth. In like manner, a mass which upon the earth's surface would weigh 1467333 lbs., or 655 tons, would, if exposed to the sun's attraction at the mean distance of Neptune, weigh only one pound, so extremely is the intensity of solar attraction enfeabled by the enormous increase of distance.

The numbers given in the column r have a more absolute sense, and express in thousandths of an inch the actual spaces through which a body would be drawn in one second of time by the sun's attraction at the mean distances of the planets severally.

IV. TABULATED ELEMENTS OF THE SATELLITES.

2999. The elements of the orbits, and other physical data relating to the satellites of Uranus, Jupiter, and Saturn, so far as they have been discovered, are given in Tables V., VI., and VII. After the explanations which have been given above respecting the corresponding data of the primary planets, no difficulty will be found in comprehending those tables, and the manner of computing them.

TABLE V.

Elements of the Uranian System.

	1.	11.	111.	IV.	▼.	¥1.
Time of revolution (days) Greatest cloudation Distance from Uranus in semi-diameter	5-993 13''-12	8 • 707 83 · · · 19	10-961 36***71	13-466 44***56	\$8-976 \$8***74	141-01
lanet Distance from Urarus in moles Orbital velocity, moles per hour 4 feet per second 4 1	13-12 226320 :0056 14746	17-02 2930-0 6825 15945	19-86 ? 349416 8178 11995	22-75 392450 1636 11200	45-61 ? 7:6080 6398 7:17	91-917 15-988 984
Gravitation towards Uranus, terres risk gravity = 1	<u>1</u>	383	830	697	27 00	
in I second	541	500	364	277	70	-

TABLE VI.

Elements of the Jovian System.

	I.	m.	III.	IV.
	W. T. G.	M. T. G.	M. T. G.	M. T. G.
Epoch	1 Jan. 1801. 1-7691 136"	l Jan. 1801. 3-5512 815"] Jan. 1801. 7-1546 346''	1 Jan. 1801. 16-63-86 585''
Distance from Jupiter in cont-diameter of planet.	6-0485 958600	9-4235 4-26500	15 3502 680000 Sma 1	25-9978 1 15/000 Small
Econtricity	0	0	and variable	and variable
Apparent diameter seen from earth	1" 194 89' 40"	1""0:0	1"-747 18" 16"	1***496 8* 58**
Beel diemeter in somi-diemeter, Jupiter Bellet • • • • •	0-026 2300	0 02.3 2019	0-088 3878	0-0326 2501
Man-Betht=1 · · · · ·	77:16	1294	34	70
# Juplier's m 1 - · · · ·	67 <u>100</u>	43 00	11300	25(20
Shootly Earth's = 1 · · · · ·	40,6	23-3	मंड मंड	25-5
™ Water's == 1 · · · · ·	6-75	1 · 65	1 2-52	449
Orbital velocity, miles per hour	31772 56865	90716 46163	2451 3 36952	17743 98093
Genritation towards Jupiter, ter. gr. = 1	- <u>1</u> -	36-3	90	968
" fall inches in I second	13-82	5-46	2-146	0-748
proper to each	00 0' 0"	00 81, 90,	00 15. 20.	00 14, 28,,
Jupiter's equator Time of retrograde revolution of nodes, years	00 0. Q.	29-9142	0° 6' 2'' 141'7880	531-0000

TABLE VII.

Elements of the Saturnian System.

	L. Manais.	II. Esceladus.	III. Tethys.	IV. Dione.	V. Rhea.	VI. Tima	VII, Hyperion.	VIII. Japotus.
Ejneh	M. T. G. 1790-0	M. T. G. 1836-0	M. T. G. 1826-0	M. T. G. 1836-0	M. T. G. 1836-0	M. T. G. 1830-0	M. T. G.	M. T. G. 1790-0
	0945	1-870	1-966	2-739	4-517	15-946	22-67	79-230
	34"-4 3-3607	43''-1	59′′·4 5-3396	68***4 6-8398	96***5 9-5528	921"·4 92·1450	980**?	643-6 64-350
	196020	161790	200236 0-04?	256500 0-02?	359225 0-08 7	870440 0-029314	1050000	9414660
	, 24005	? 80876	540?	49°? 94516	96°-7 90783	256° 38′ 11′′ 13636	? 132215	7968
	61313	45325	97776 40793	36967	20/65	19886	17920	11980
Salare, terrestrial gravity = 1 · ·	30-00	166	36-46	4177	11-48	430	700	370E
forms, inches in Jeografi Moss long, at epoch	5780. 28. 48 18-18	670 41' 98"	7-68 813° 43° 48°	4- 62 327° 40' 48''	2-67 363°44' 0''	0-441 137° 21' 34"	0-276	0-062 269° 37' 48''

CHAP. XVIII.

COMETS.

I. COMETARY ORBITS.

3000. Prescience of the astronomer. - For the civil and political historian the past alone has existence,—the present he rarely as prehends; the future never. To the historian of science it is per mitted, however, to penetrate the depths of past and future with equal clearness and certainty : facts to come are to him as present and not unfrequently more assured than facts which are passed. Although this clear perception of causes and consequences chanterises the whole domain of physical science, and clothes the natural philosopher with powers denied to the political and moral inquire, yet foreknowledge is eminently the privilege of the astronome. Nature has raised the curtain of futurity, and displayed before him the succession of her decrees, so far as they affect the physical universe, for countless ages to come; and the revelations of which she has made him the instrument, are supported and verified by never-ceasing train of predictions fulfilled. He "shows us the things which will be hereafter," not obscurely shadowed out in figures and in parables, as must necessarily be the case with other revelations, but attended with the most minute precision of time place, and circumstance. He converts the hours as they roll into an ever-present miracle, in attestation of those laws which his Creater through him has unfolded; the sun cannot rise — the moon cannot wane - a star cannot twinkle in the firmament, without beits witness to the truth of his prophetic records. It has pleased in "Lord and Governor" of the world, in his inscrutable wisdom," baffle our inquiries into the nature and proximate cause of that derful faculty of intellect — that image of his own essence which is has conferred upon us; nay, the springs and wheelwork of animal and vegetable vitality are concealed from our view by an importrable veil, and the pride of philosophy is humbled by the spectral of the physiologist bending in fruitless ardour over the dissection of the human brain, and peering in equally unproductive inquiry on the gambols of an animalcule. But how nobly is the darker which envelopes metaphysical inquiries compensated by the for of light which is shed upon the physical creation! There all? harmony, and order, and majesty, and beauty. From the chand social and political phenomena exhibited in human recordsnomena unconnected to our imperfect vision by any discovernia law, a war of passions and prejudices, governed by no appared

purpose, tending to no apparent end, and setting all intelligible order at defiance — how soothing and yet how elevating it is to turn to the splendid spectacle which offers itself to the habitual contemplation of the astronomer! How favourable to the development of all the best and highest feelings of the soul are such objects! the only passion they inspire being the love of truth, and the chiefest pleasure of their votaries arising from excursions through the imposing scenery of the universe - scenery on a scale of grandeur and magnificence, compared with which whatever we are accustomed to call sublimity on our planet dwindles into ridiculous insignificancy. Most justly has it been said, that nature has implanted in sur bosoms a craving after the discovery of truth; and assuredly that glorious instinct is never more irresistibly awakened than when our notice is directed to what is going on in the heavens. "Quoniam cadem Natura cupiditatem ingenuit hominibus veri inveniendi, quod facillime apparet, cum vacui curis, etiam quid in cœlo fiat, scire avemus; his initiis inducti omnia vera diligimus; id est, adelia, simplicia, constantia; tum vana, falsa, fallentia odimus."*

8001. Strikingly illustrated by cometary discovery. — Such reflections are awakened by every branch of the science which now engages us, but by none so strongly as by the history of cometary discovery. Nowhere can be found so marvellous a series of phenomena foretold. The interval between the prediction and its ful-filment has sometimes exceeded the limits of human life, and one generation has bequeathed its predictions to another, which has been filled with astonishment and admiration at witnessing their literal

accomplishment.

3002. Motion of comets explained by gravitation.—In the vast framework of the theory of gravitation constructed by Newton, places were provided for the arrangement and exposition not only of all the astronomical phenomena which the observation of all preceding generations had supplied, but also for a far greater mass which the more fertile and active research of the generations which succeeded him have furnished. By this theory, as we have seer all the known planetary motions were explained, and planets previously unseen were felt by their effects, their places ascertaine and the telescope of the observer guided to them.

But transcendently the greatest triumph of this celebrated thec was the exposition it supplied of the physical laws which govern motions of cometá, as distinguished from those which prevail amo

the planets

8008. Conditions imposed on the orbits of bodies which are ject to the attraction of gravitation.—It is proved in the practions demonstrated in the first book of Newton's Principia, w

^{*} Cio. de Fin. Bon. et Mal. ii. 14.

ASTRONOMY.

ons form in substance the groundwork of the entire theory ation, that a body which is under the influence of a central e intensity of which decreases as the square of the distance, must move in one or other of the curves known to geosthe "conic sections," being those which are formed by section of the surface of a cone by a plane, and that the attraction must be in the focus of the curve; and in order that such curves are compatible with no other law of attractions therefore be taken as conclusive evidence of the existing law, it is further demonstrated that whenever a body is to move round a centre of attraction in any one of these hat centre being its focus, the law of the attraction will be gravitation; that is to say, its intensity will vary in the in-

verse proportion of the square of the distance of the moving body from the centre of force.

Subject to these limitations, however, a body may move round the sun in any orbit, at any distance, in any plane, and in any direction whatever. It 816, the forms of a very eccentric ellipse, a b a' b', a parap p', and an hyperbola a h h', having s as their common and it will be convenient to explain in the first instance the magnitude of some important lines and distances connected lesse orbits.

4. Elliptic orbit. — Ellipses or ovals vary without limit in eccentricity. A circle is regarded as an ellipse whose eccenis nothing. The orbits of the planets generally are ellipses, ving eccentricities so small that, if described on a large scale r proper proportions on paper, they would be distinguishable ircles only by measuring accurately the dimensions taken in it directions, and thus ascertaining that they are longer in a

direction than in another at right angles to it. A very ic and oblong ellipse is delineated in fig. 816, of which a a' major axis. The focus being s, the perihelion distance d is d the aphelion distance d' is s a', the mean distance a being half the major axis. The eccentricity e, being expressed by merical ratio of the distance of the focus s from the centre e semi-axis, we shall have

$$\frac{s c}{a} = e, s c = a \times e.$$

evident from what has been just stated, then, that we shall

$$d = a - a \times e = a \times (1 - e),$$

nsequently

$$a=\frac{d}{1-\epsilon};$$

Ю

$$d' = a + a \times e = a \times (1 + e) = d \times \frac{1 + e}{1 - e}$$

ce it is evident that, if the perihelion distance and eccentricity m, the semi-axis a and the aphelion distance d' can be com-

the properties of the ellipse, the distance of any point from us s can be computed, if the perihelion distance d, the eccence, and the angular distance of the point from perihelion be Let a express this angular distance, which is, in fact, the formed by two lines, one d, drawn from s to a, and the other a to the actual place of the body in the ellipse. It is proved metry that the value of a may be determined in all cases by mula.

$$z = d \times \frac{1 + e}{1 + e \times \cos a};$$

to may, if the perihelion distance be first multiplied by the

eccentricity increased by 1, and the product then divided by the number found by adding to 1 the product of the eccentricity and the cosine of the angular distance of the body from perihelion, the quotient will be the distance of the body from the focus s.

From this general formula, therefore, the expression for the distance of the body from the focus in every position can be found. Thus at 90° from perihelion we have

$$\cos a = \cos 90^{\circ} = 0$$
,

and therefore the distance s l, which we shall call l, is

$$l = d \times (1 + e).$$

If we suppose $= 180^{\circ}$, we shall reproduce the expression for the aphelion distance d', for cos. $180^{\circ} = -1$; and therefore

$$d' = d \times \frac{1+\epsilon}{1-\epsilon}$$

It will be useful also to observe that the cos. a is positive when all

less, and negative when a is greater, than 90°.

The number which is expressed by e is necessarily less than I. since it is a fraction whose numerator s c is less than its denominator c a. The more eccentric the ellipse is, the more nearly equal will s c be to c a, and consequently the more nearly equal to I will be the eccentricity e.

The distance l, being greater than the perihelion distance d, in the ratio of 1 + e to 1, it will therefore be always less than twist this distance, inasmuch as 1 + e is always less than 2; but the more eccentric the ellipse is, the more nearly will I approach to twice the perihelion distance d. Thus, for example, if $\epsilon = 0.999$, we should have $l = d \times 1.999$, which falls short of twice the perhelion distance by not more than the 1000th part of that distance.

The curvature of the ellipse continually increases from the mean distance to perihelion, and consequently decreases from perihelist to the mean distance, being equal at equal angular distances from

perihelion as seen from the sun.

It is evident that if a body move in a very eccentric ellipse, and as that represented in fig. 816, whose plane coincides exactly nearly with the common plane of the planetary orbits, it may intersect the orbits of several or all of the planets, as it is represented to do in the figure, although its mean distance from the sun may less than the mean distance of several of those which it thus into The aphelion distance of such a body may, therefore, greatly exceed that of any planet, while its mean distance may be less the that of the more distant planets.

3005. Parabolic orbits. — The form of a parabolic orbit having the same perihelion distance as the elliptic orbit is represented app, in fig. 816. This orbit consists of two indefinite branches

similar in form, which unite at perihelion a. Departing from this point on opposite sides of the axis a a', their curvature regularly and rapidly decreases, being equal at equal distances from perihelion. The two branches have a constant tendency to assume the direction and form of two straight lines parallel to the axis a a'. To actual parallelism, and still less to convergence, these branches, however, never attain, and consequently they can never reunite. They extend, in fine, like parallel straight lines, to an unlimited distance without ever reuniting, but assuming directions when the distance from the focus bears a high ratio to the perihelion distance, which are practically undistinguishable from parallelism.

It is demonstrated in geometry, that if d express the perihelion distance and z the distance of the body at the angular distance a

from the perihelion, we shall have

$$z=\frac{2}{1+\frac{2}{\cos a}};$$

that is to say, the distance z is found by dividing twice the perihelion distance by 1 added to the cosine of the angular distance from perihelion.

It must be mentioned, however, that when a is greater than 90°, the cosine is negative, and its value must then be subtracted from 1

to obtain the divisor.

To find the distance l of the body at 90° from perihelion, let $= 90^{\circ}$, and consequently cos. a = 0. Therefore

$$l=2d;$$

that is to say, the distance at 90° from perihelion is twice the

perihelion distance.

One parabolic orbit differs from another in its perihelion distance. The less this distance is, the less will be the separation at a given distance from s between the parallel directions to which the indefinite branches pp' tend. This distance may have any magnitude. The body in its perihelion may graze the surface of the sun, or may pass at a distance from it greater than that of the most remote of the planets, so that, although it be subject to solar attraction, it would in that case never enter within the limits of the solar system at all.

A body moving in such an orbit, therefore, would not make, like one which moves in an ellipse, a succession of revolutions round the sun; nor can the term periodic time be applied at all to its motion. It enters the system in some definite direction, such as p'p, as indicated by the arrow, from an indefinite distance. Arriving within the sensible influence of solar gravitation, the effects of this attraction are manifested in the curvation of its path, which gradually increases as its distance from the sun decreases, until it arrives at perihelion, where the attractive force, and consequently the curvature, attain

their maxima. The extreme velocity which the body attains at this point produces, in virtue of the inertia of the moving mass, a centrifugal force, which counteracts the gravitation, and the body, after passing perihelion, begins to retreat; the solar gravitation and the curvature of its path decreasing together, until it issues from the system in a direction pp', as indicated by the arrows, which is nearly a straight line, and parallel to that in which it entered. In such an orbit a body therefore visits the system but once. It extens in a certain direction from an indefinite distance, and, passing through its perihelion, issues in a parallel direction, passing to an unlimited distance, never to return.

8006. Hyperbolic orbits. — This class of orbits, like the parbolas, consist of two indefinite branches, which unite at perihelias, which at equal distances from perihelion have equal curvatures, and which, as the distance from perihelion increases, approach indenitely in direction and form to straight lines; but, unlike the parbolic orbits, the straight lines to whose direction the two branches approximate are divergent and not parallel.

Such an orbit having the same perihelion distance as the ellipse and parabola, is represented by $a \ h \ h'$, fig. 816.

If z express, as before, the distance of the body from s, when its angular distance from perihelion is a, and if e express a certain number, which, instead of being less, as in the case of the ellipse, is greater than 1, we shall have

$$z = d \times \frac{1 + e}{1 + e \times \cos a}$$

a formula identical with that which expresses the value of s in the case of the ellipse, the difference being merely in the relation which the number e bears to 1.

It is easy to perceive that when the perihelion distance is the same, the value of z for any proposed angular distance from perhelion is greater in the hyperbola than in the ellipse, and that walue in the parabola is intermediate, being less than in the hyperbola and greater than in the ellipse.

The parabola is, therefore, included between the ellipse of hyperbola, and the less the number e falls short of 1 for the ellips, and exceeds it for the hyperbola, the nearer will the three orbits in relation to each other at those parts which are not very removed from perihelion.

The distance l of the body which moves in the hyperbola at \mathfrak{M}^{\bullet} from perihelion, is

$$l=d\left(1+e\right),$$

the same as for the ellipse. If I express this distance for the ellips,

I for the parabola, and I' for the hyperbola, and I express the value of I for the hyperbola, we shall have

$$egin{aligned} l &= d \times (1 + e) \\ l' &= 2 d \\ l'' &= d \times (1 + e'), \end{aligned}$$

and consequently the distances between the parabola and each of the other orbits at 90° from perihelion, measured in the direction of all, will be

$$\vec{l}' - l = d \times (1 - \epsilon)$$
 $\vec{l}'' - \vec{l}' = d \times (\epsilon' - 1)$

It is evident, therefore, that, whatever be the fraction by which stalls short of 1, and by which e' exceeds 1, the same will be the fraction of the perihelion distance by which the parabola at this point is separated from the other orbits.

It will be recollected that, when a exceeds 90°, the cos. a becomes

negative, and, consequently we would then have

$$z = d \times \frac{1 + e}{1 - e \times \cos a}.$$

Now, as the cos. a, which is 0, when $a = 90^{\circ}$ increases, the product $e \times \cos$. a, which, after passing 90°, is very minute, will also increase, and, consequently, the divisor $1 - e \times \cos$. a will decrease. This will evidently cause a proportionate increase of z. As the product $e \times \cos$. a approaches to 1, the divisor decreasing, the value of z rapidly increases; and when $e \times \cos$. a becomes actually = 1, z becomes infinite.

The geometrical interpretation of this analytical contingency is, that each branch of the orbit, in receding from the centre of attraction s, approaches indefinitely to coincidence with certain straight lines, which make, with the direction of perihelion, an angle, the cosine of which has such a value, that $e \times \cos s = 1$, that is, an angle whose cone is $\frac{1}{s}$.

If two straight lines, therefore, be drawn from s, making an angle with the axis a a', whose cosine is $\frac{1}{e}$, these lines will be the directions into which the two branches of the hyperbolic orbit have a constant tendency to run. They will, therefore, be the limit of the divergence of the branches h h'.

It is evident, therefore, that the more the number e exceeds 1, the greater will be the angle of divergence of the two branches h h', and the less it exceeds 1, the nearer will the hyperbolic branches h h' approach to the parabolic branches p p'.

In the fig. 816, the orbits circular, elliptic, parabolic, and hyper-

bolic are necessarily represented as being all in the same plane. It must, however, be understood, that so far as any conditions are imposed upon them by the law of gravitation, they may seemly be in any planes whatever, inclined each to the other, at any angle whatever, from 0° to 90°, with their mutual intersection or lines of nodes in any direction whatever, and that the bodies may may in these several orbits, in any directions, how opposed soerer to each other.

3007. Planets observe in their motions order not exacted law of gravitation. — When the theory of gravitation was first pounded by its illustrious author, no other bodies, save the plan and satellites then discovered, were known to move under fluence of such a central attraction. These bodies, hower plied no example of the play of that celebrated theory in . latitude. They obeyed, it is true, its laws, but they did may They displayed a degree of harmony and order far exceed the law of gravitation exacted. Permitted by that law to me any of the three classes of conic sections, their paths were sively elliptical; permitted to move in ellipses infinitely ver their eccentricities, they moved exclusively in such as differed also insensibly from circles; permitted to move at distances subordinated to no regular law, they move in a series of orbits at distances in creasing in a regular progression; permitted to move at all consisable angles with the plane of the ecliptic, their paths are inclined it at angles limited in general to a few degrees; permitted, in fac, to move in either direction, they all agreed in moving in the direction in which the earth moves in its annual course.

Accordance so wondrous, and order so admirable, could not be fortuitous, and, not being enjoined by the conditions of the law of gravitation, must either be ascribed to the immediate dictates of the Omnipotent Architect of the universe above all general laws, or to some general laws superinduced upon gravitation, which had compute the sagacity of the discoverer of that principle. If the former apposition were adopted, some bodies, different in their physical directors from the planets, primary and secondary, and playing different parts and fulfilling different functions in the economy of the universe, might still be found, which would illustrate the play of gravitation in its full latitude, sweeping round the sun in all found of orbit, eccentric, parabolic, and hyperbolic, in all planes, at all distances, and indifferently in both directions. If the latter superition were accepted, then no other orbit, save ellipses of small eccentricity, with planes coinciding nearly with that of the celiptic

would be physically possible.

3008. Comets observe no such order in their motions.—The theory of gravitation had not long been promulgated, nor as you mean generally accepted, when the means of its further verification.

were sought in the motion of comets. Hitherto these bodies had seen regarded as exceptional and abnormal, and as being exempt lingether from the operation of the law and order which prevailed a manner so striking among the members of the solar system. o little attention had been given to comets, that it had not been stainly ascertained whether they were to be classed as meteoric or mmical phenomena; whether their theatre was the regions of the mosphere, or the vast spaces in which the great bodies of the uni-Their apparent positions in the heavens on various mae move. sessions of the appearances of the most conspicuous of them, had swartheless been from time to time for some centuries observed ad recorded with such a degree of precision as the existing state f astronomical science permitted; and even when their places were ot astronomically ascertained, the date of their appearance was geneally preserved in the historic records, and in many cases the condellations through which they passed were indicated, so that the seems of obtaining at least a rude approximation to their position 1 the firmament were thus supplied.

3009. They move in conic sections, with the sun for the focus. uch observations, vague, scattered, and inexact as they were, suphed, however, data, by which, in several cases, it was possible to ompute the real motion of these bodies through space, their posions in relation to the sun, the earth, and the planets, and the aths they followed in moving through the system, with sufficient pproximate accuracy to conclude with certainty that they were one r other of the conic sections, the place of the sun being the focus.

This was sufficient to bring these bodies under the general operaion of the attraction of gravitation.

It still remained, however, to determine more exactly the specific haracter of these orbits. Are they ellipses more or less eccentric? r parabolas? or hyperbolas? Any of the three classes of orbits rould, as has been shown, be equally compatible with the law of ravitation.

8010. Difficulty of ascertaining in what species of conic section comet moves. - It might be supposed that the same course of obarvation as that by which the orbit of a planet is traced would be pplicable equally to comets. Many circumstances, however, attend is latter class of bodies, which render such observations impossile, and compel the astronomer to resort to other means to determine seir orbits.

A spectator stationed upon the earth keeps within his view each I the other planets of the system throughout nearly the whole of s course. Indeed, there is no part of the orbit of any planet in hich, at some time or other, it may not be seen from the earth. ivery point of the path of each planet can therefore be observed; ad, although without waiting for such observation, its course might

ned, yet it is material here to attend to the fact, that the it may be submitted to direct observation. The different so, present peculiar features, by which each may be dis-Thus, as has been explained, they are observed to be odies of various magnitudes. Their surfaces are marked r modes of light and shade, which, although variable and till, in each case, possess some prevailing and permanent by which the id tity of the object may be established, there no of Lans of determining it. planets, comets do not present to us those individual above mentioned, by which their identity may be deter-None of them have been satisfactorily ascertained to be odies, nor indeed to have any definite shape. It is certain of them possess no solid matter, but are masses consome nearly transparent substances; others are so surrith this apparently vaporous matter, that it is impossible, eans of observation which we possess, to discover whether r enshrouds within it any solid mass. The same vapour is envelopes the body (if such there be within it) also rom us its features and individual character. Even the repour itself if repour

that which it pursues after it ceases to be visible, would be as certainly and precisely known as if it could be traced by direct obser-

vation throughout its entire orbit.

3011. Hyperbolic and parabolic comets not periodic. — If it be ascertained that the are in which the comet moves while it is visible is part of an hyperbola, such as gag, it will be inferred that the comet, coming from some indefinitely distant region of the universe, has entered the system in a certain direction, h'A, which can be inferred from the visible are gag," " hat it must depart to another indefinitely distant region of the Liverse following the direction hh', which is also ascertained from the visible are g a g.

If, on the other hand, it be ascertained that the visible arc, such as g' a g', be part of a parabola, then, in like manner, by the properties of that curve, it will follow that it entered the system coming from an indefinitely distant region of the universe in a certain direction p'p, which can be inferred from the visible arc g' a g', and that after it ceases to be visible, it will issue from the system in another determinate direction, pp, parallel to that which it entered.

The comet, in neither of these cases, would have a periodic character. It would be analogous to one of those occasional meteors which are seen to shoot across the firmament never again to reappear. The body, arriving from some distant region, and coming, as would appear, fortuitously within the solar attraction, is drawn from its course into the hyperbolic or parabolic path, which it is seem to pursue, and escapes from the solar attraction, issuing from the system never to return. The phenomenon would in each case be occasional, and, in a certain sense, accidental, and the body could not be said properly to belong to the system. So far as relates to the comet itself, the phenomenon would consist in a change of the direction of its course through the universe, operated by the tempomany action of solar gravity upon it.

8012. Elliptic comets periodic like the planets. — But the case is very different, the tie between the comet and the system much more intimate, and the interest and physical importance of the body transcendently greater, when the arc, such as g'' a g'', proves to be part of an ellipse. In that case the invisible part of the orbit being inferred from the visible, the major axis $a \, a'$ would be known. The comet would possess the periodic character, making successive revo-Intions like the planets, and returning to perihelion a after the proper periodic time, which could be inferred by the harmonic law from the magnitude of its major axis.

Such a body would then not be, like those which follow hyperbolic or parabolic paths, an occasional visitor to the system, connected with it by no permanent relation, and subject to solar gravicon only accidentally and temporarily. It would, on the contrary, he as permanent, if not as strictly regular, a member of the system

the planets, though invested, as will presently appear, with

ely different physical character.

therefore, be easily conceived with what profound interest ere regarded before the theory of gravitation had been yet ablished or generally accepted, and while it was, so to on its trial. These bodies were, in fact, looked for as the

whose testimony must decide its fate.

Difficulties attending the analysis of cometary motions. s, however, which seemed almost insurmountable, opposed s to a satisfactory and conclusive analysis of their motions. ses rendered the observations upon their apparent places mber and deficient in precision. The arcs g a g, g a g, y" of the three classes of orbit, in any of which they might hout any violation of the law of gravitation, were very ncident in the neighbourhood of the place of perihelion a. r example, in almost all the cases which presented themessible to conceive three different curves, an eccentric ch as a b a' b', a parabola, such as p' p a, and an hyperh as h'ha, so related that the arcs gag, g'ag, and ould not deviate one from another to an extent exceeding inevitable in cometary observations. Thus any one of

s; and would arrive at its perihelion at exactly the same point d after exactly equal intervals.

w, although the disturbing actions of the planets near which ght pass, in departing from and returning to the sun, must be sted to be much more considerable than when one planet acts another, as well because of the extreme comparative lightness s comet, as of the great eccentricity of its orbit, which someactually or nearly intersects the paths of several planets, and ially those of the larger ones, yet still such planetary attracare only disturbances, and cannot be supposed to efface that ster which the orbit receives from the predominant force of memonse mass of the sun. While, therefore, we may be prefor the possibility, and even the probability, that the same his comet, on the occasion of its successive re-appearances, may g.a path g" a g" in passing to and from its perihelion, differing se extent from that which it had followed on previous appearyet in the main such differences cannot, except in rare and snal cases, be very considerable, and for the same reason the rals between its successive periods, though they may differ, it be subject to any very great variation.

15. Periodicity, combined with the identity of the paths while a stablishes identity.—If then, on examining the various is whose appearances have been recorded, and whose places wisible have been observed, and on computing from the apparances the arc of the orbit through which they moved, it be that two or more of them, while visible, moved in the same the presumption will be that these were the same body re-apage after having completed its motion in an elliptic orbit; nor a this presumption of identity be hastily rejected because of missences of any discrepancies between the observed paths, or sequality of the intervals between its successive re-appearances, as such discrepancies can fairly be ascribed to the possible bences produced by planets which the comet might have en-

in its path.

16. Many comets recorded—few observed.—Many comets, pix, have been recorded, but not observed. Historians have appear, and even described their appearances, and in some cases indicated the chief constellations through which such bodies I, although no observations of their appearent places have been aitted by which any close approximation to their actual paths be made. Nevertheless, even in these cases, some clue to identification is supplied. The intervals between their appearance is a highly probable test of identity. Thus if comets intervally recorded to have appeared at intervals of fifty years remarkance affording evidence of the diversity of these objects),

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cessive returns of an elliptic comet having that interval as its

. Classification of the cometary orbits. - The appearances t 400 comets had been recorded in the annals of various es before the end of the seventeenth century, the epoch sigby the discoveries and researches of Newton. In most cases, r, the only circumstance recorded was the appearance of the accompanied in many instances with details bearing evident of exaggeration respecting its magnitude, form and splendour. e few cases, the constellations through which the object passed ively, with the necessary dates, are mentioned, and in some, till, observations of a rough kind have been handed down. uch scanty data, eagerly sought for in the works preserved in t countries, sufficient materials have been collected for the ation, with more or less approximation, of the elements of its of about sixty of the 400 comets above mentioned. e the time of Newton, Halley, and their contemporaries rs have been more active, and have had the command of ents of considerable and constantly increasing power; so ery comet which has been visible from the northern hemithe earth since that time has

M. Encké of Berlin succeeded in calculating its entire erring the invisible from the visible part — and found riod was about twelve hundred days. This calculation 1 by the fact of its return in 1822, since which time has gone by the name of Encké's comet, and returned

we asked, How it could have happened that a comet which volution in a period so short as three years and a quarter, have been observed until so recent an epoch as 1818? plained by the fact that the comet is so small, and its able even when in the most favourable position, that it a seen by the aid of the telescope, and not even with this, her certain conditions which are not fulfilled on the occurry perihelion passage. Nevertheless, the comet was n three former occasions, and the general elements of its ded, although its elliptic, and consequently periodic chance recognised.

paring, however, the elements then observed with those let now ascertained, no doubt can be entertained of their

'able of the elements of the orbit. — In the following table he elements of the orbit of this comet, as computed from ations made upon it at each of its three appearances in 5, and 1805, before its periodic character was discovered, eleven subsequent appearances up to 1852.

TABLE I.

Elements of the Orbit of Encké's Comet to 1852.

6,	Eccen- tricity.	Perihelion Dutance.	Aphelica Distance.	Longitude of Perihelion.	Longitude of Ascending Node.	Inclination	Time of Peribelion		
	$d' = a \times (1-\epsilon)$		$d^{**} = a \times (1 + \epsilon)$	π	y	ı			
-1	-		-	0 , "	0	0		A. m	
- 1	0.8484	0-3349	4-0512	156 38	334 8	13 36	Jan. 30.	21 7	
- 1	0-1-159	0.3344	4 0916	156 41 20	334 39 22	13 42 30	Dec. 21.	10 44	
-1	0.5462	0-5404	4.0860	156 47 24	334 20 10	13 33 30	Nov. 21.	6 19	
- 1	0-8486	0.3353	4-0929	156 59 12	334 33 19	13 36 54	Jan. 27.		
-1	0-8445	0.3460	4-1028	157 11 44	334 25 9	13 20 17	May 23. Sept. 16.	6 43	
п	0.5449	0.3449	4-1017	157 14 31	334 27 30	13 21 24	Jan. 9.	18 3	
-1	0.5446	0.3455	4 1023	157 17 53	334 29 32	13 20 34	May 21,	23 3	
-1	0-1454	0.34.15	4.1003	157 21 1				8 4	
- 1	D 8450	0 3444	4:10:10	157 23 29	334 34 59	13 21 15	Aug 26, Dec. 19,	0 2	
- 1	0.8452	0 3440	4-1004	157 27 4		13 20 26	April 12.	0 3	
п	0.5448	0 3450	4-0998		334 39 10			15 1	
- 1	D-8474	0-3391	4-1049	157 44 21	334 19 34	13 7 34	Nov. 20.	3+	
н	0.8478	0-3371	4 0 23			13 7 55	Mar. 14.	20	
П	0-8477	0.0374	4.0530	157 51 2	334 23 21	13 7 67	mar. 14.	M. T. B.	

tion of this comet is direct; and its period in 1852 was ears, which is subject to a slight variation.

vident that between 1786 and 1795 there were two,

between 1795 and 1805 two, and, in fine, between 1805 and 1819

three, unobserved returns to perihelion.

It appears, therefore, that, excepting the oval form of the orbit, the motion of this body differs in nothing from that of a phase whose mean distance from the sun is that of the nearest of the planetoids. Its eccentricity is such, however, that when in parihelia it is within the orbit of Mercury, and when in aphelion it is estile the most distant of the planetoids, and at a distance from the sun

equal to four-fifths of that of Jupiter.

8020. Indications of the effects of a resisting medium. altogether anomalous in the motions of the bodies of the system, and indicating a consequence of the highest physical inportance, has been disclosed in the observation of the mo It has been found that its periodic time, and come comet. its mean distance, undergoes a slow, gradual, and apparently a decrease. The decrease is small, but not at all uncertain amounted to about a day in ten revolutions, a quantity which a not by any means be placed to the account either of errors of e vation or of calculation; and, besides, this increase is increase whereas errors would affect the result sometimes one way and a times the other. The period of the comet between 1786 and 1795 was 12081 days; between 1795 and 1805 it was 12074 days; between 1805 and 1819 it was 1207 4 days; in 1845 it was 1205 days; and, in fine, in 1852 it was 1204 days.

The magnitude of the orbit thus constantly decreasing (for the cube of its greater axis must decrease in the same proportion as the square of the period), the actual path followed by the comet must be a sort of elliptic spiral, the successive coils of which are very does together, every successive revolution bringing the comet nearer and

nearer to the sun.

Such a motion could not arise from the disturbing action of the planets. These forces have been taken strictly into account in the computation of the ephemerides of the comet, and there is still found this residual phenomenon, which cannot be placed to their account, but which is exactly the effect which would arise from any physical agency by which the tangential motion of the comet would be feebly but constantly resisted. Such an agency, by diminishing the tangential velocity, would give increased efficacy to the sale attraction, and, consequently, increased curvature to the comet's path; so that, after each revolution, it would revolve at a less distant from the centre of attraction.

3021. The luminiferous ether would produce such an effect—It is evident that a resisting medium, such as the luminiferous ether (1225) is assumed to be in the hypothesis which forms the basis of the undulatory theory of light, would produce just such a phasemenon, and, accordingly, the motion of this comet is regarded as

strong evidence tending to convert that hypothetical fluid into a real

physical agent.

It remains to be seen whether a like phenomenon will be developed in the motion of other periodic comets. The discovery of these bodies, and the observation of their motions, are as yet too recent to enable astronomers, notwithstanding their greatly multiplied number, to pronounce decisively upon it.

8022. Comets would ultimately fall into the sun. - If the exintence of this resisting medium should be established by its observed effects on comets in general, it will follow that, after the lapse of a certain time (many ages, it is true, but still a definite interval), the comets will be successively absorbed by the sun, unless, as is not improbable, they should be previously vaporised by their near approach to the solar fires, and should thus be incorporated with his apphere.*

3823. Why like effects are not manifested in the motion of the planets.—It may be asked, If the existence of a resisting medium be admitted, whether the same ultimate fate must not await the hasets? To this inquiry it may be answered that, within the limits of past astronomical record, the ethereal medium, if it exist, has had no sensible effect on the motion of any planet. That it might have a perceptible effect upon comets, and yet not upon planets, will not be surprising, if the extreme lightness of the comets compared with their bulk be considered. The effect in the two cases may be compared to that of the atmosphere upon a piece of swan's down and upon a leaden bullet moving through it. It is certain that whatever may be the nature of this resisting medium,

In the efforts by which the human mind labours after truth, it is curious to observe how often that desired object is stumbled upon by accident, or spectrum at by reasoning which is false. One of Newton's conjectures respecting comets was, that they are "the aliment by which suns are sustained;" and he therefore concluded that these bodies were in a state of pregressive decline upon the suns, round which they respectively swept; and that into these suns they from time to time fell. This opinion appears to have been cherialed by Newton to the latest hours of his life: he not aly consigned it to his immortal writings; but, at the age of eighty-three, conversation took place between him and his nephew on this subject, which has come down to us. "I cannot say," said Newton, "when the comet of 1680 will fall into the sun: possibly after five or six revolutions; but whenever that time shall arrive, the heat of the sun will be raised by it to such a point, that our globe will be burnt, and all the animals upon it will perish. The new stars observed by Hipparchus, Tycho, and Kepler, must have proceeded from such a cause, for it is impossible otherwise to explain their sudden splendour." His nephew then asked him, "Why, when he stated in his writings that comets would fall into the sun, did he not also state those vast fires they must produce, as he supposed they had done in the stars?"—"Because," replied the old man, "the confingrations of the sun concern us a little more directly. I have said, however," added he, smiling, "enough to enable the world to collect my opinion."

, for many hundred years to come, produce the slightest a effect upon the motions of the planets.

Corrected estimate of the mass of Mercury. — The masses in general are, as will be explained, incomparably smaller of the smallest of the planets; so much so, indeed, as to oppreciable ratio to them. A consequence of this is, that effects of their attraction upon the planets are altogether the disturbing effects of the masses of the planets upon very considerable. These disturbances, being proportional urbing masses, may then be used as measures of the latter, a movement of the pith-ball in the balance of torsion sup-

s comet near its perihelion passes near the orbit of Merwhen that planet at the epoch of its perihelion happens the same point, a considerable and measurable disturbance ted in the comet's motion, which being observed supplies of the planet's mass.

mbination of the motions of the planet and comet took er very favourable circumstances, on the occasion of the

passage of the comet in 1838, the result of which, ac-

asure of the physical forces to which that instrument is

This comet had been observed in 1772 and in 1806; but in the elliptic form of its orbit, and consequently its periodicity, was not discovered. Its return to perihelion was predicted and observed in 1832, in 1846, and in 1852; but that which took place in 1838 escaped observation, owing to its unfavourable position and extreme faintness.

The elements of the orbit, deduced from the observations made on each of its appearances to 1846 inclusive, are given in Table II. We have not yet obtained calculations of its elements from observations made in 1852. It was first seen in that year by Professor Secchi at Rome, on September 16th, and continued to be seen for three weeks. It was preceded in right ascension about two minutes of time by a still fainter comet, whose real distance from it must have been about a million and a quarter of miles.

TABLE II. Elements of the Orbit of Biela's Comet to 1846.

	Mean Distance, Earth's == 1	Ecora- tricity.	Peribelion Distance.	Aphelion Distance.	Longitude of Peribelion,	Longitude of Ascending Node.	Inclination	Time of Perihelion Passage.
1773 1606 1888 1488	9-1998 3-5671 3-5615	0-6769 0-7458 0-7466	d' = a × (1 - e) 0-9118 0-9068 0-9025	4"3 6-23 6-23	97 21 0 109 32 23 109 45 50	9 263 24 0 251 15 15 251 29 12	0 , ,, 17 39 0 13 36 45 15 33 51	Feb 8, I 0 Jan 1, 23 52 Mar. 18, 10 3
1946 1946	3-f01-0 3-6-150	0-7616 9-7563	0-8792 . 0-8587	6-30 6-18	110 0 95 109 5 31	248 15 18 245 47 51	13 19 47 12 39 45	Nov. 26, 1 41 Feb. 11. 0 43

3026. Possibility of the collision of Biela's comet with the earth.

— One of the points at which the orbit of Biela's comet intersects the plane of the ecliptic, is at a distance from the earth's orbit less than the sum of the semi-diameters of the earth and the comet. It follows, therefore (2905), that if the comet should arrive at this point at the same moment at which the earth passes through the point of its orbit which is nearest to it, a portion of the globe of the earth must penetrate the comet.

It was estimated on the occasion of the perihelion passage of this comet in 1832, that the semi-diameter of the comet (that body being nearly globular, and having no perceptible tail) was 21,000 miles, while the distance of the point at which its centre passed through the plane of the ecliptic, on the 29th of October in that year, from the path of the earth was only 18,600 miles. If the centre of the earth happened to have been at the point of its orbit nearest to the centre of the comet on that day, the distance between the centres of the two bodies would have been only 18,600 miles, while the semi-diameter of the comet was 21,000 miles; and the semi-diameter of the earth being, in round numbers, 4000 miles, it would follow

ach a contingency the earth would have plunged into the he depth of

21,000 + 4000 - 18,600 = 6400 miles,

cceeding three-fourths of the earth's diameter. ssibility of such a catastrophe having been rumoured, ular alarm was excited before the expected return of the 1832. It was, however, shown that on the 29th Ocearth would be about five millions of miles from the point , and that on the arrival of the earth at that point the ald have moved to a still greater distance.

Resolution of Biela's comet into two. - One of the most ary phenomena of which the history of astronomy affords ple, attended the appearance of this comet in 1846. It at occasion seen to resolve itself into two distinct comets, om the latter end of December, 1845, to the epoch of its ince in April, 1846, moved in distinct and independent The paths of these two bodies were in such optical juxtanat both were always seen together in the field of view of ope, and the greatest visual angle between their centres 16th. After this the companion gradually faded away, and disappeared previously to the final disappearance of the original comet on 2nd April.

It was observed also that a thin luminous line or arc was thrown cross the space which separated the centres of the two nuclei, espeially when one or the other had attained its greatest brightness, he are appearing to emanate from that which for the moment was he brighter.

After the disappearance of the companion, the original comet have out three faint tails, forming angles of 120° with each other, use of which was directed to the place which had been occupied by

he companion.

It is suspected that the faint comet which was observed by Prof. Seechi to precede Biela's comet in 1852, may have been the common thus separated from it, and if so, the separation must be permanent, the distance between the parts being greater than that

which separates the earth from the sun.

3029. Faye's comet.—On the 22nd November, 1843, M. Faye, of the Paris Observatory, discovered a comet, the path of which soon appeared to be incompatible with the parabolic character. Goldschmidt showed that it moved in an ellipse of very limited limensions, with a period of 72 years. It was immediately obzerved as being extraordinary, that, notwithstanding the frequent returns to perihelion which such a period would infer, its previous appearances had not been recorded. M. Faye replied by showing that the aphelion of the orbit passed very near to the path of Inpiter, and that it was possible that the violent action of the great mass of that planet, in such close proximity with the comparatively light mass of the comet, might have thrown the latter body into its present orbit, its former path being either a parabola or an ellipse, with such elements as to prevent the comet from coming within visible distance. M. Faye supported these observations by reference to a more ancient comet, which we shall presently notice, to which a like incident is supposed with much probability, if not certainty, to have occurred.

8030. Re-appearance in 1850-1 calculated by M. Le Verrier.—
The observations which had been made in 1843, at several observatories, but more especially those made by M. Struve at Pultowa, who continued to observe the comet long after it ceased to be observed elsewhere, supplied to M. Le Verrier the data necessary for the calculation of its motion in the interval between its perihelion in 1843 and its expected re-appearance in 1850-1, subject to the listurbing action of the planets, and predicted its succeeding peri-

helion for the 3rd of April, 1851.

Aided by the formulæ of M. Le Verrier, Lieutenant Stratford alculated a provisional ephemeris in 1850, by which observers

enabled more easily to detect the comet, which was the ssary as the object is extremely faint and small, and not f being seen except by means of the most perfect tele-By means of this ephemeris, Professor Challis, of Camulating the comet on the night of the 28th November very the place assigned to it in the tables. Two observations then made upon it, which, however, were sufficient to Le Verrier to give still greater precision to his formulæ, ng a definite numerical value to a small quantity which is left indeterminate. Lieutenant Stratford, with the forcorrected, calculated a more extensive and exact ephemeling to the last day of March, and published it in January, the Nautical Almanack.

net, though extremely faint and small, and consequently observation, continued to be observed by Professor Challis reat Northumberland telescope at Cambridge, and by M. Pultowa, and it was found to move in exact accordance oredictions.

De Vico's comet.—On the 22nd August, 1844, M. de he Roman Observatory, discovered a comet whose orbit fterwards proved by M. Fave to be an ellipse of moderate which M. Villarcenux proved to move in an elliptic orbit, with a period of about 61 years. The next perihelion passage of this comet will take place in the end of 1857, or the beginning of 1858.

3034. Elliptic comet of 1743.—A revision of the recorded observations of former comets by the more active and intelligent seal of modern mathematicians and computers, has led to the discovery of the great probability of several among them having revolved in elliptic orbits, with periods not differing considerably from those of the comets above mentioned. The fact that these comets have not been re-observed on their successive returns through perihelion, may be explained, either by the difficulty of observing them, owing to their unfavourable positions, and the circumstance of observers not expecting their re-appearance, their periodic character not being then suspected; or because they may have been thrown by the disturbing action of the larger planets into orbits such as to keep them continually out of the range of view of terrestrial observers.

Among those may be mentioned a comet which appeared in 1743, and was observed by Zanetti at Bologna; the observations indicate an elliptic orbit, with a period of about 5½ years.

3035. Elliptic comet of 1766.—This comet, which was observed by Messier, at Paris, and by La Nux, at the Isle of Bourbon, revolved, according to the calculations of Burckhardt, in an ellipse with a period of 5 years.

3036. Lexell's comet.—The history of astronomy has recorded one singular example of a comet which appeared in the system, made two revolutions round the sun in an elliptic orbit, and then disap-

peared, never having been seen either before or since.

This comet was discovered by Messier, in June, 1770, in the constellation of Sagittarius between the head and the northern extremity of the bow, and was observed during that month. It disappeared in July, being lost in the sun's rays. After passing through its perihelion, it re-appeared about the 4th of August, and continued to be observed until the first days of October, when it finally disappeared.

All the attempts of the astronomers of that day failed to deduce the path of this comet from the observations, until six years later, in 1776, Lexell showed that the observations were explained, not, as had been assumed previously, by a parabolic path, but by an ellipse, and one, moreover, without any example at that epoch,

which indicated the short period of 51 years.

It was immediately objected to such a solution, that its admission would involve the consequence that the comet, with a period so short, and a magnitude and splendour such as it exhibited in 1770,

been frequently seen on former returns to perihelion; o record of any such appearance was found. Lexell replied, by showing that the elements of its orbit, om the observations made in 1770, were such, that at its phelion, in 1767, the comet must have passed within a the planet Jupiter fifty-eight times less than its distance un; and that consequently it must then have sustained on from the great mass of that planet more than three e energetic than that of the sun; that consequently it n out of the orbit in which it previously moved into the oit in which it actually moved in 1770; that its orbit pre-1767 was, according to all probability, a parabola; and, at consequently moving in an elliptic orbit from 1767 to having the periodicity consequent on such motion, it ess moved only for the first time in its new orbit, and had ne within the sphere of the sun's attraction before this

further stated, that since the comet passed through its which nearly intersected Jupiter's orbit, at intervals of and it encountered the planet near that point in 1767, the the planet being somewhat above 11 years, the planet gle revolution and the comet after two revolutions must

assuming as data the observations recorded in 1770, Laplace showed that before sustaining the disturbing action of Jupiter in 1767, the comet must have moved in an ellipse, of which the semi-axis major was 13.293, and consequently that its period, instead of being 5½ years, must have been 48½ years; and that the eccentricity of the orbit was such, that its perihelion distance would be but little less than the mean distance of Jupiter, and that consequently it could never have been visible. It followed also, that, after suffering the disturbing action of Jupiter in 1779, the comet passed into an elliptic orbit, whose semi-axis major was 7.3; that its period was consequently 20 years; and that its eccentricity was such, that its perihelion distance was more than twice the distance of Mars, and that in such an orbit it could not become visible.

- 8089. Revision of these researches by M. Le Verrier. This investigation has recently been revised by M. Le Verrier,* who has shown that the observations of 1770 were not sufficiently definite and accurate to justify conclusions so absolute. He has shown that the orbit of 1770 is subject to an uncertainty, comprised between certain definite limits; that tracing the consequences of this to the positions of the comet in 1767 and 1779, these positions are subject to still wider limits of uncertainty. Thus he shows that, compatibly with the observations of 1770, the comet might in 1779 pass either considerably outside, or considerably inside Jupiter's orbit, or might, as it was supposed to have done, have passed actually within the orbits of his satellites. He deduces in fine the following general conclusions:
- 1. That if the comet had passed within the orbits of the satellites, it must have fallen down upon the planet and coalesced with it; an incident which he thinks improbable, though not absolutely impossible.
- 2. The action of Jupiter may have thrown the comet into a parabolic or hyperbolic orbit, in which case it must have departed from our system altogether, never to return, except by the consequence of some disturbance produced in another sphere of attraction.
- 3. It may have been thrown into an elliptic orbit, having a great axis and long period, and so placed and formed that the comet could never become visible; a supposition within which comes the solution of Laplace.
- 4. It may have had merely its elliptic elements more or less modified by the action of the planet, without losing its character of short periodicity; a result which M. le Verrier thinks the most probable, and which would render it possible that this comet may still be identified with some one of the many comets of short period,

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^{*} See Mem. Acad. des Sciences, 1847, 1848.

activity and sagacity of observers are every year dis-

itate such researches, M. Le Verrier has given a table, all the possible systems of elliptic elements of short period comet would have assumed, subject to the disturbing upiter in 1779, and taking the observations of 1770 within ble limits of error.

her demonstrates, that the orbit in which the comet moved by to the disturbing action of Jupiter upon it in 1767, could not have been a parabola or hyperbola, but must an ellipse, whose major axis was considerably less than a Laplace deduced from the insufficient observations of He shows that, before that epoch, the peribelion distance met could not, under any possible supposition, have exceet times the earth's mean distance, and most probably fied between 1½ and 2 times that distance; and that the major of the orbit could not have exceeded 4½ times the ean distance, a magnitude 3 times less than that assigned e calculations of Laplace.

Process by which the identification of periodic comets may .—It must not, however, be supposed that it is sufficient

somets of Faye, De Vico, and Brorsen; tracing back their histories during their unseen motions for three-quarters of a century, and ascertaining the effects of the disturbing actions which they must severally have sustained from revolution to revolution, until he brought them to the epoch of 1779. On comparing the orbits thus determined with those of the table of possible orbits of Lexell's comet, he has shown that none of them can be identical with it, however strongly some of the elements of their present orbits may raise such a presumption.

3042. Probable identity of De Vico's comet with the comet of 1678.—The comet of De Vico having presented striking analogies with a comet which was observed by Tycho Brahe and Rothmann in 1585, and one observed by La Hire in 1678, M. Le Verrier has applied like principles to the investigation of these questions.

MM. Laugier and Mauvais observed that the elements of De Vico's comet presented such a resemblance to that of Tycho Brahe, as almost to decide the question of their identity. M. Le Verrier, tracing back the comet of De Vico to 1585, has shown that its orbit at that epoch was so different from that of the comet of Tycho, as to be incompatible with any plausible inference of their identity.*

He has shown, however, by like reasoning, that there is a high degree of probability that the comet of De Vico is identical with

that observed by La Hire in 1678.

8043. Blainplan's comet of 1819.— M. Blainpan discovered a comet at Marseilles on 28th November, 1819, which was observed at Milan until 25th January, 1820. The observations reduced and calculated by Prof. Encké gave an elliptic orbit with a period a little short of 5 years. Clausen conjectures that this comet may be identical with that of 1743. It has not been seen since 1820.

3044. Pons's comet of 1819.—A comet was discovered by M. Pons on June 12th, 1819, which was observed until July 19th. Prof. Encké assigned to it an elliptic orbit, with a period of 51 years.

3045. Pigott's comet of 1783.—A comet, discovered by Mr. Pigott at New York in 1783, was shown by Burckhardt to have an

elliptic orbit, with a period of 51 years.

\$046.— Peters's comet of 1846.—On the 26th June, 1846, a comet was discovered at Naples by M. Peters, which was subsequently observed at Rome by De Vico, and continued to be seen until 21st July. An elliptic orbit is assigned to this comet, with a period of from 13 to 16 years, some uncertainty attending the observations. The re-appearance of this comet may be expected in 1859, 1860.

[&]quot; Mém. Acad. des Sciences, 1847.

bular synopsis of the orbits of the comets which revolve rn's orbit.—In Table III. we have given the elements en comets above mentioned.

TABLE III.

the Motion of the Elliptic Comets which revolve within the Orbit of Saturn.

Mean		Perihelion	Aphelion	Daily Motions				
Distance, Earth's = 1.	Eccen- tricity.	D wince, Earth's = 1.	Distance,	Mean Distance.	At Perihe- lion.	At Aphrica.		
4		d'=a× (1−e)	d"= 4X		-			
2-2148 3-5245	0-8477 0-7570	0-3370 0-8564	4-0527 6-1906	1076-5 536-3	46497 9082	315.3 179.7		
3-8118 3-1028 3-1465	0 5559 0 6173 0 7945	1-6926 1-1863 0-6501	5-9310 6-0194 5 6429	476-6 648-8 635-7	2418-5 5264-1 14890	956-9 947-6 197-7		
3-4618 3-0913 2-9337	0-6609 0-7213 0 8640	1-1740 0-8615 0-3990	5-7497 6-3211 5-4670	550 9 652 8 706-1	4799-7 8406 38175	197-1 199-7 270-4 270-5		
3·1560 2·8490 3 1602	0-7861 0-6867 0-75-2	0-6745 0-8926 0-7-36	5 6375 4-8060 5-5468	632-8 737-8 631-6	13855 7516-4 10300	259 S 259 S 200 S		

have an analogy to those of the planets. Their inclinations, with one exception, are within the limits of those of the planets. Their eccentricities, though incomparably greater than those of the planet, are, as will presently appear, incomparably less than these of all other comets yet discovered. Their mean distances and pasts (with the exception of the last two in the table,) are within the

limits of those of the planetoids.

3050. Planetary character of their orbits.—The comparison of the numbers given in Table III. with those which will be given hereafter, in the tables of the elements of other elliptic counts, and the comparison of the diagrams of their orbits with those of elem, will show in a striking manner, to how great an extent the critic of this group of comets possess the planetary character. Business moving round the sun in the common direction, their inclination, with a single exception, are within the limits of those of the planet. It is true that their eccentricities have an order of magnitude materials greater; but on the other hand, it will be seen presently that they are incomparably less than the eccentricities of all other periods comets yet discovered. Their mean distances and periods plane them in direct analogy with the planetoids.

Moderate as are the eccentricities as compared with those of other comets, they are sufficiently great to impart a decided oval form to the orbits, and to produce considerable differences between the perihelion and aphelion distances, as will be apparent by isspecting the numbers in the columns d' and d''. It appears by these, that while the perihelion of Encké's comet lies within the orbit of Mercury, its aphelion lies outside the orbit of the most remote of the planetoids, and not far within that of Jupiter. The perihelion of Biela's comet, in like manner, lies between the critic of the earth and Venus, while its aphelion lies outside that of Jupiter. In the case of Faye's comet, the least eccentric of the group, the perihelion lies near the orbit of Mars, and the aphelia

outside that of Jupiter.

It must be remembered that the elliptic form of these orbits has only been verified by observations on the successive returns to perhelion of the first five comets in the table. The elliptic elements

of the others may, so far as is at present known, have been clied by disturbing causes.

The angular motions at the mean and extreme distances from the sun, given in the columns a, a' and a" have been computed, on the principles already explained, by the formulæ

$$a = \frac{1,296,000}{365 \cdot 25 \times P'}$$
 $a' = a \times \frac{a^2}{a'''}$ $a'' = a \times \frac{a^2}{a'''}$

The same numbers which express these angular motions, also express in all cases the intensities of solar light and heat in the

several positions of the comet; and also the apparent motion of the sun, as seen from the comet; and a comparison of these with the corresponding numbers related to any of the planets, will illustrate in a striking manner how different are the physical conditions by which these two classes of bodies are affected; and this will be more and more striking, when the other groups of comets have been noticed.

Taking the comet of Encké as an example, it appears that while its mean daily motion is 1076" or 18', its motion in aphelion is only 5', and in perihelion nearly 13°. Its motion in perihelion, the light and heat it receives from the sun, and the apparent motion of the sun as seen from it, are therefore severally more than 150 times greater in perihelion than in aphelion.

III. Elliptic Comets, whose mean distances are nearly EQUAL TO THAT OF URANUS.

8051. Comets of long periods first recognised as periodic.—It might be expected, that comets moving in elliptic orbits of small dimensions, and consequently having short periods, would have been the first in which the character of periodicity would be discovered. The comparative frequency of their returns to those positions near perihelion, where alone bodies of this class are visible from the earth, and the consequent possibility of verifying the fact of periodicity, by ascertaining the equality of the intervals between their successive returns to the same heliocentric position, to say nothing of the more distinctly elliptic form of the arcs of their orbits in which they can be immediately observed, would afford strong ground for such an expectation; nevertheless in this case, as has happened in so many others in the progress of physical knowledge, the actual results of observation and research have been directly contrary to such an anticipation; the most remarkable case of a comet of large orbit, long period, and rare returns, being the first, and those of small orbits, short periods, and frequent returns, the last whose periodicity has been discovered.

8052. Newton's conjectures as to the existence of comets of long periods.—It is evident that the idea of the possible existence of comets with periods shorter than those of the more remote planets, and orbits circumscribed within the limits of the solar system, never occurred to the mind either of Newton or any of his contemporaries

or immediate successors.

In the third book of his PRINCIPIA, he calls comets a species of planets, revolving in elliptic orbits of a very oval form. But he continues, "I leave to be determined by others the transverse diameters and periods, by comparing comets which return after long intervals of time to the same orbits.'

nteresting to observe the avidity with which minds of a der snatch at such generalisations, even when but slen-nded upon facts. These conjectures of Newton were soon oted by Voltaire: "Il y a quelque apparence," says he, y on comets, "qu'on connaîtra un jour un certain nombre tres planètes qui sous le nom de comêtes tournent comme ur du soleil, mais il ne faut pas espérer qu'on les connais-

gain, elsewhere, on the same subject:-

"Comêtes, que l'on craint à l'égal du tonnerre, Cessez d'épouvanter les peuples de la terre ; Dans une ellipse immense achevez votre cours, Remontez, descendez près de l'astre des jours."

Halley's researches. - Extraordinary as these conjectures e appeared at the time, they were soon strictly realised. ndertook the labour of examining the circumstances at-I the comets previously recorded, with a view to discover ny, and which of them, appeared to follow the same path. that a comet which had been observed by himself, by and their contemporaries in 1682, followed a path while

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ently that the comet ought not to be expected to appear until the d of 1758, or the beginning of 1759. It is impossible to imagine y quality of mind more enviable than that which, in the existing the of mathematical physics, could have led to such a prediction. In impossible for Halley to fer to the world a demonstration of the event which he foretold. He therefore," says M. de Pontecoulant, "could only announce rese felicitous conceptions of a sagacious mind as mere intuitive proceptions, which must be received as uncertain by the world, however he might have felt them himself, until they could be verified the process of a rigorous analysis."

Subsequent researches gave increased force to Halley's prediction; it appeared from the ancient records of observers, that comets ad been seen in 1456* and 1378, whose elements were identical

ith those of the comet of 1682.

8054. Great advance of mathematical and physical sciences tween 1682 and 1759.—In the interval of three-quarters of a mtury which elapsed between the announcement of Halley's prection and the date of its expected fulfilment, great advances were ade in mathematical science; new and improved methods of instigation and calculation were invented; and, in fine, the theory gravitation was pursued with extraordinary activity and success trough its consequences in the mutual disturbances produced upon to motions of the planets and satellites, by the attraction of their

The extraordinary length and brilliancy which was ascribed to the tail pen this occasion, have led astronomers to investigate the circumstances ader which its brightness and magnitude would be the greatest possible; ad, upon tracing back the motion of the comet to the year 1456, it has sen found that it was then actually under the circumstances of position ith respect to the earth and sun most favourable to magnitude and splenour. So far, therefore, the results of astronomical calculation corroborate is records of history.

^{**}The appearance of this comet in 1456, was described by contemporary sthorities to have been an object of "unheard-of magnitude;" it was acompanied by a tail of extraordinary length, which extended over sixty agrees (a third of the heavens), and continued to be seen during the whole 'the month of June. The influence which was attributed to this appearance, renders it probable that in the record there exists more or less of taggeration. It was considered as the celestial indication of the rapid access of Mohammed II., who had taken Constantinople, and struck terror to the whole Christian world. Pope Calixtus II. levelled the thunders of the church against the enemies of his faith, terrestrial and celestial, and the same bull exorcised the Turks and the comet; and in order that the amony of this manifestation of his power should be for ever preserved, he related that the bells of all the churches should be rung at midday—a stom which is preserved in those countries to our times. It must be imitted that, notwithstanding the terrors of the Church, the comet puried its course with as much ease and security as those with which Moammed converted the church of St. Sophia into his principal mosque.

masses one upon mother. As the epoch of the expected return of the comet to its perihelion approached, therefore, the scientific world resolved to divest, as far as possible, the prediction, of that vagueness which necessarily attended it, owing to the imperfect state of science at the time it was made, and to calculate the exact effects of these planets whose masses were sufficiently great in accelerating or retarding its motion while passing them.

3056. Exact path of the comet on its return and time of in perihelion calculated and predicted by Clairant and Lalande. This inquiry, which presented great mathematical difficulties, and involved enermous arithmetical labour, was undertaken by Clairant and Lalande: the former, a mathematician and natural philosopher, who had already applied with great success the principles of grattation to the motions of the moon, undertook the purely analyzed part of the investigation, which consisted in establishing certain general algebraical formulæ, by which the disturbing actions exertably the planets on the comet were expressed; and Lalande, an ement practical astronomer, undertook the labour of the arithmetical computations, in which he was assisted by a lady, Madame Leputs, whose name has thus become celebrated in the annuals of science.

These elaborate calculations being completed, Clairant present the result of their joint labours, in a memoir, to the Academy of Sciences of Paris,* in which he predicted the next arrival of the comet at perihelion, on the 18th April, 1759; a date, howeve, which, before the re-appearance of the comet, he found resent change to the 11th of April, and assigned the path which the

The name of Madame Lepaute does not appear in Clairaut's meast; suppression which Lalande attributes to the influence exercised by antiflady to whom Clairaut was attached. Lalande, however, quotes lettend Clairaut, in which he speaks in terms of high admiration of "la saute calculatrice." The labours of this lady in the work of calculating (fixed also assisted Lalande in constructing his Ephemerides) at length at the end her sight, that she was compelled to desist. She died in 1788, the attending on her husband, who had become insane. See the artists of the year 1833.

^{*}When it is considered that the period of Halley's comet is about sweety-five years, and that every portion of its course for two successive public was necessary to be calculated separately in this way, some notice my be formed of the labour encountered by Lalande and Madame Lepass. "During six months," says Lalande, "we calculated from morning in night, sometimes even at meals; the consequence of which was, that contracted an illness which changed my constitution for the remainder my life. The assistance rendered by Madame Lepaute was such, the without her we never could have dared to undertake this enormous labour, in which it was necessary to calculate the distance of each of the two planets, Jupiter and Saturn, from the comet, and their attraction we that body, separately, for every successive degree, and for 150 years."

raid follow while visible, as determined by the following

ion. Long. of node. Long. of perils. Perilsel, dist. Direction. 7' 58° 50' 808° 10' 0.58 retrograde.

Remarkable anticipation of the discovery of Uranus.—
noing his prediction Clairaut stated, that the time assigned
pproaching perihelion might vary from the actual time to
it of a month; for that independently of any error either
ethods or process of calculation, the event might deviate
less from its predicted occurrence, by reason of the attracn undiscovered planet of our system revolving beyond the
Saturn. In twenty-two years after this time, this conjecrealised by the discovery of the planet Uranus, by the late
am Herschell, revolving round the sun one thousand milmiles beyond the orbit of Saturn!

Prediction of Halley and Clairaut fulfilled by re-appearthe comet in 1758-9.—The comet, in fine, appeared in r 1758, and followed the path predicted by Clairaut, which out little from that which it had pursued on former appearwill be seen by a comparison of the elements as given th those since ascertained. It passed through perihelion .3th March, within 22 days of the time, and within the the possible errors assigned by Clairaut.

Disturbing action of a planet on a comet explained.—
eral effects of a planet in accelerating or retarding the mocomet are easily explained, although the exact details of the
sees are too complicated to admit of any exposition here.

fig. 818, represent the place of the disturbing planet, and f the comet. The attraction of the planet on the comet be a force directed from c towards P, and by the principle



Fig. 818.

of the composition of forces is equivalent to two components, one c m in the direction of the comet's path, and the other c n perpendicular to that path. If the motion of the comet be directed from c towards m, it will be accelerated; and if it be directed from c towards m', it will be retarded by that component of the planet's attraction which is directed from c to m. The other com-

I me being at right angles to the comet's motion, will have t effect either in accelerating or retarding it. pears, therefore, in general, that, if the direction of the motion o me make an acute angle with the line of P drawn hanet, the planet's attraction will accelerate it; and if its direction o st make an obtase angle with the lines o p, it will retard it.

This being understood, the disturbing action of a planet such as Jupiter or Saturn on a comet such as Halley's may be easily conprehended. In fig. 819, the orbit of the counct is represented at



Fig. 819.

AcPc" in its proper proportions, A being the major axis, P the place of perihelion, A that of aphelion, act a that of the focus in which the sun is placed. The small circle described round a represents in its proper proportions the orbit of the earth, who distance is about twice that of the comet when the latter is at perihelion. The circle p p' p" represents in its proper proportions the orbit of Jupiter, which, for illustration, we shill consider as the disturbing planet.

It will be apparent on the men inspection of the diagram, that lises drawn from the planet, whatever be its place, to any point whatever of the comet's path between its aphelion A and the point m', where it arrives at the orbit of the planet in approaching the sun, will make acute angles with the direction of the comet's motion, and that, consequently, the comet will be accelerated by the action of the planet. In like manner it is apparent that lines drawn from the planet, whatever be its place, to any point whatever of the comet's path between m and the aphelion A, will make ob

tuse angles with the direction of the comet's motion, and, consequently, the comet will be retarded by the action of the planet is

departing from the sun, from m to A.

In that part of the comet's path which lies within the planet's orbit, the action of the planet alternately accelerates and retards it, according to their relative position. If the planet be at p, suppose po drawn so as to be at right angles to the path of the comet. Between m' and o the action of the planet at p will accelerate the comet, and after the comet passes s it will retard it. In like manner if the planet be at p'', it will first retard the motion of the comet proceeding from m' towards A, and will continue to do so until the line of direction becomes perpendicular to that of the comet's motion, after which it will accelerate it.

It appears, therefore, that during the period of the comet, the disturbing action of the planet is subject to several changes of direction, owing partly to the change of position of the comet and partly to that of the planet; and the total effect of the disturbing action of the planet on the comet's period is found by taking the difference between the total amount of all the accelerating and all the retarding actions.

In the case of the planet Jupiter and Halley's comet, the former makes nearly seven complete revolutions in a single period of the comet; and consequently its disturbing action is not only subject to several changes of direction, but also to continual variation of in-

tensity, owing to its change of distance from the comet.

Small as the arc m' P m of the comet's path is which is included within the orbit of Jupiter, the fraction of the period in which this are is traversed by the comet is much smaller, as will be apparent by considering the application of the principle of equable areas (2599) to this case. The time taken by the comet to move over the arc m' P m is in the same proportion to its entire period, as the area included between the arc m' P m and the lines m's and m s is to the entire area of the ellipse A P.

To simplify the explanation, the orbit of the comet has here been supposed to be in the plane of that of the disturbing planet. If it be not, the disturbing action will have another component at right angles to the plane of the comet's orbit, the effect of which will be

a tendency to vary the indication.

3060. Effect of the perturbing action of Jupiter and Saturn on Halley's comet between 1682 and 1759.—The result of the investigation by Clairaut showed, that the total effect of the disturbing action of Jupiter and Saturn on Halley's comet between the perihelions in 1682 and in 1759, was to increase its period by 618 days as compared with the-time of its preceding revolution, of which increase, 100 days were due to the action of Saturn, and 518 to that of Jupiter.

Clairant did not take into account the disturbing action of the earth, which was not altogether inconsiderable, and could not allow for those of the undiscovered planets Uranus and Neptune. The effects of the action of the other planets, Mars, Venus, Mercury,

and the planetoids, are in these cases insignificant.

3061. Calculations of its recura in 1835-6.—In the interval of three-quarters of a century which preceded the next re-appearance of this comet, science continued to progress, and instruments of observation and principles and methods of investigation were still further improved; and, above all, the number of observers was greatly augmented. Before the epoch of its return in 1835, its motions, and the effects produced upon them by the disturbing action of the several planets, were computed by MM. Damoiseau, Ponte-

111.

Rosenberger, and Lehmann, who severally predicted its perihelion:—

Damoiseau	4th N	lov. 1835.
Pontecoulant	7th	44
Rosenberger	11th	44
Lehmann		44

Predictions fulfilled.—These predictions were all published y 1835. The comet was seen at Rome on the 5th Auposition within one degree of the place assigned to it for in the ephemeris of M. Rosenberger. On the 20th Aucame visible to all observers, and pursued the course, with deviation, which had been assigned to it in the ephemeving at its perihelion on the 16th Nov., being very nearly tween the four epochs assigned in the predictions. This, passing south of the equator, it was not visible in latitudes, but continued to be seen in the southern hemi-

til the 5th of May 1836, when it finally disappeared, no eturn until the year 1911.

Tabular synopsis of the motion of Halley's comet.—In is given a synopsis of the elements of the orbit of this duced from the observations made on each of its seven

or Encké, and was found to be an ellipse of such dimensions ve a period of 75½ years, equal to that of Halley's comet.

i. Olbers' comet of 1815.—On the 6th of March 1815, Dr. discovered at Bremen, a comet whose orbit, calculated by or Bessel, proved to be an ellipse, with a period of 74 years. ext perihelion passage of this comet is predicted for the 9th

ruary 1887.

3. De Vico's comet of 1846. — On the 28th of February M. de Vico discovered a comet at Rome, whose orbit, calcuy MM. Van Deiuse and Pierce, appears to be an ellipse, with

d of 72-73 years.

1. Brorsen's comet of 1847. — A comet was discovered by ween at Altona, on the 20th of July 1847; the orbit of calculated by M. d'Arrest, appears to be an ellipse, with a of 75 years.

3. Westphal's comet of 1852. — On the 27th of June, 1852, t was discovered by M. Westphal at Gottingen, and was soon ards observed by M. Peters at Constantinople. The calcuof its orbit proves it to be an ellipse, with a period of about rs.

3. Tabular synopsis of the motions of these six comets. — In V. are presented the data necessary to determine the motions e six comets:--

TABLE V.

is of the Motion of the Elliptic Comets, whose mean Distances are nearly equal to that of Uranus.

	Mean		_						Aphelion			Dai	ily Motio	۵.	
ignation.	Dutane Earth's	e.	Ecces- tricity.			Perihelion Distance.			A phe Dusta	lion nce.	At Mean Distance.		At Peribe- lion,	At Aphe- lios,	
	•			•		ď = (1 -		7	(14	4 X (- e)	•		•	6 "	
1616)	17-987 17-995 17-633 14-538 17-779 16-690	6	0-9674 0-9546 0-9518 0-9644 0-9796 0-9248			0-5866 0-7771 1-2129 0-6831 0-4879 1-2510			35-3680 83-4140 34-0550 34-3510 35-0710 31-9700		46:3 50:7 47:9 46:4 47:3 52:4		43510 94505 10135 22943 62950 22965	29 19-3 19-6 19-6 19-9 19-9 14-8	
Period, Years.			Longitude of Perchelion.			Longitude of Avend- ing Node.			Inclination.		Time of Peribelion Passage.		Direction of Motion,		
	P		*	_	_	•	_	_	<u>.</u>	_					
1612)	76-680 70-068 74-040 73-260 74-970 67 770	304 92 149 90 79	91 18 1 94 19 12	 32 41 56 46 46 16	55 253 83 77 309 346		9 2 34 36 49 55	0 17 73 44 84 19	45 67 29 67 8	5 5 55 13 25 32	Nov. 15, 11 Sept. 15, 11 April 25, 1 Mar. 5, 18 Sept. 9, 18 Oct. 12, 11	815. 815. 46.	A. m 22 41 7 41 25 54 14 1 13 1	D D D	

3070. Diagram of their orbits. — In fig. 820, is presented a plan of their orbits. plan of their orbits. — In fig. 820, is present and drawn according to the scale indicated. This figure shows, in a manner sufficiently exact for the named. sufficiently exact for the purposes of illustration, the relative mes nitudes and forms of the nitudes and forms of the six orbits, as well as the directions of the several axes with relation to the six orbits, as well as the directions of the several axes with relation to the several axes with the several axes with relation to the several axes with t several axes with relation to that of the first point of Aries.



3071. Planetary characters are nearly effaced in these orbits—
By comparing the elements given in Table V., and the forms and
studes of the orbits shown in the diagram, with the forms and By comparing the elements given in the diagram, with the forms and magnitudes of the orbits shown in the diagram, with those of the magnitudes of the orons among the real state of the orons are stated in Table III, and the state of the planetary characteristics. first group of elliptic contents the planetary characteristics not stated in the planetary characteristics not stated in the state of t

posing the second group, revolve in the common direction of the planets, and this is the only planetary character observable among them. The inclinations, no longer limited to those of the planetary orbits, range from 18° to 74°. The eccentricities are all so extreme, that the arc of the orbit near perihelion approximates closely to the parabolic form, and, in fine, the most remarkable body of the group, the comet of Halley, revolves in a direction contrary to the common

motion of the planets.

But it is more than all in the elongated oval form of their orbits, that this group of comets differs, not only from the planets, but from the first group. While their perihelia are at distances from the an, between those of Mars and Mercury, their aphelia are from two to five hundred millions of miles outside the orbit of Neptune. Thus, the comet of Halley, for example, in perihelion, is at a distance from the sun less than that of Venus; but at its aphelion, its distance exceeds that of Neptune by a space greater than Jupiter's distance from the sun. The mean angular motion of this comet is nearly the same as that of Uranus; but its angular motion in perihelion is three times that of Mercury; while its angular motion in aphelion is little more than half that of Neptune.

The corresponding variations of solar light and heat, and of the

may be easily inferred.

IV. ELLIPTIC COMETS, WHOSE MEAN DISTANCES EXCEED THE LIMITS OF THE SOLAR SYSTEM.

2072. Tabular synopsis of twenty-one elliptic comets, of great recutricity and long period.—Although the periodicity of this class of comets has not yet in any instance been certainly established by observations made upon their successive returns to perihelion, the observations made upon them during a single perihelion passage indicate an arc of their orbit, which exhibits the elliptic form so unequivocally, as to supply computors and mathematicians with the data necessary to obtain, with more or less approximation, the value of the eccentricity, which, combined with the perihelion distance, gives the form and magnitude of the comet's orbit.

By calculations conducted in this manner, and applied to the observations made on various comets which have appeared since the latter part of the seventeenth century, the elliptic orbits of twenty-one of these bodies have been computed, and are given in the order of the dates of their perihelion passages in the table on p. 510.

Of this group the least eccentric is No. 15, which passed its perihelion in 1840. This comet was discovered at Berlin by M. Bremiker, and its orbit was calculated by Götz, and proved to be an ellipse, having the elements given in the table, subject to no greater

TABLE VI.

f the Motions of the Elliptic Comets whose mean Distances exceed the Limits of the Solar System.

Mesa Di	stance.	Eccen. Minor	Perihe-		Distance.	Daily Molios.			
3.57	3	Eccen- tricity.	Minor Axis.	Distance Earth's	V. Brazille	MODE.	At	At -	At
Earth's	Nep-		Major Axis = 1.	= t.	Earth's	Nep-	Mean Distance.	Perihe-	Apha lion.
	= i.	100		$d = a \times (1 - e)$	d'=a × (1−ε)	= L		a'	4"
427-6437	14-2547	0 99998		0 00622		1	04	528333	0-001
33:0310	1-1010	0-98320		0-55340	855-2 65-5	28-5	18 7	18-5	4-75
217-4074	7 2469	0-99540		0-49830	433-8	14-5	0-11	58-5	0-28
163-4575	5-4450	0-99920		0-12250	326-8	10-9	1-7	116-6	0-€
1787-9200	59-5973	0.911994	M 1	0.09680	3575-5	119-1	0.047	4479 6	0.01
56-2000	1.9000	0.97340		1-4951	110-9	3.7	8-43	34	2-16
143-8562	4-7952	0.99550	M 0	0.6504	287-0	9 66	2-06	21-9	0.52
211-0225	7-0340	0-99510		1-0354	421-0	14-0	1-16	13:2	0.37
91-5068	3-0503	0.99270		1.5821	181-4	6-0	4-05	2-5	1-03
309-5000	10.3200	0-99630	1	1-1451	617-7	20-6	0-65	13.2	1-16
267-9440	8-9314	0-99540		1-2409	5346	17.8	0.61	13-21	0.25
189-6187	6:3206	0-99930		0.1378	379-0	12 6	1.36	714-71	0.34
536-0000	51-2000	0-99940-		0-9215	5070-0	102-3	0-069	46-5	0-011
577-1099	19-2370	0.99790		1-2214	1155-0	38-4	0-26	20-0	0.08
49-1110	1-6370	0-96990		1-4808	96-7	3-2	10-3	31	2-66
56.0000	18-6000	0-99990		0-0056	111-9	3-7	9-44	262125-0	
2138 0000	71-2600	0-99960		0 8554	4274-0	142-5	0.06	61-6	0-00
39-7600	1:3200	0.98990		0-4016	79-1	2-6	1.41	3.8	
194 8000	64-9000	0-99240		1-4807	388-1	12-9	1-3	6-3	0-33

b, which passed its perihelion in 1793, has an orbit, accordate calculations of D'Arrest, nearly similar both in form and 29, as will be seen by comparing the numbers given in the More uncertainty, however, attends the estimation of these 3-

comets which approached nearest to the sun were the great of 1680 and 1843, Nos. 1 and 16 in the table, both memoretheir extraordinary magnitude and splendour.

elements of that of 1680, given in the table, are those which sulted from the calculations of Professor Enoké, based on observations of the comet which have been recorded. The sof the great comet of 1843 have resulted from the comes of Mr. Hubbard. Both are subject to considerable uncertaind must be accepted only as the best approximations that obtained.

is not subject, however, to the same uncertainty, is the linary proximity of these bodies to the sun at their reperihelia. The perihelion distance of the comet of 1680 put 576,000 miles—and that of 1843, 538,000 miles, semi-diameter of the sun being 441,000 miles, it follows distance of the centres of those comets respectively from ace of the sun at perihelion must have been only 235,000 000; so that if the semi-diameter of the nebulous enveloper of them exceeded this distance, they must have actually he sun.

velocity of the orbital motion of these bodies in aphelion by the table to be such, that the comet of 1680 would volved round the sun in a minute, and that of 1843 in little n two minutes, if they retained the same angular motion lished.

listance to which the comet of 1680 recedes in its aphelion imes greater than that of Neptune. The apparent diameter un seen from that distance would be 2", and the intensity that and heat would be 730,000 times less than at the earth; heir intensity at the perihelion distance would be 26,000 eater, so that the light and heat received by the comet in lion would be $26,000 \times 730,000 = 18,980$ million times less perihelion.

reatest aphelion distances in the table are those of Nos. 5, 17, the comets of 1780, 1830, and 1844, amounting to 0 to 140 times the distance of Neptune; the eccentricities from unity by less than To 0. These orbits, though the results of calculation, must be regarded as subject to able uncertainty.

3073. Plan of the form and relative magnitude of the orbits. — To convey an idea of the form of the orbits of the comets of this group, and of the proportion which their magnitude bears to the dimensions of the solar system, we have drawn, in fig. 821, an ellipse, which may be considered as representing the form of the orbits of the comets Nos. 15, 6, 9, 12, and 1, of the Table VI.

If the ellipse represent the orbit of the comet No. 15, the circle a will represent on

the same scale the orbit of Neptune.

If the ellipse represent the orbit of the comet No. 6, the circle b will represent the orbit of Neptune.

If the ellipse represent the orbit of No. 9, the circle c will represent the orbit of Neptune.

If the ellipse represent the orbit of No. 12, the circle d will represent the orbit of

COMPTS.

TABLE VIII.

Elements of the Orbits of Comets ascertained or presented to be parabolic.

Time of Perihelion Passage.	Perili. Dist. Earth's = 1.	Longitude of Perihelion	Long. of As-	Inclination.	Direction.
A. m. J. B. C. 570. Winter. 0 0 2. 136. April 29 0 0 3. 58. July 0 0 4. 11, Liewiner 8 19 12 5. A. D. Go. Jamary 14 4 48 5. 14. March 19 2 34 7. 240. November 9 32 54 8. 539. October 30 14 51 8. 539. October 30 14 51 10. 699. August 23 0 29 10. 67 August 25 0 29 10. 67 August 2	Very small { 1-01 0-80 0-58 0-445 0-720 0-372 0-541 0-502 0-803 0-603	0 150 to 120 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 270 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	10 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	R R D RRR D D R D D R
13. 837. February 25. 23 51 14. 881. December 39 3 59 18. 588. Sephenaber 11 3 51 18. 588. Sephenaber 11 3 51 18. 588. Sephenaber 11 3 51 18. 589. Sephenaber 11 3 51 18. 5106. April 1 0 0 0 12. 1927. 1928. Pebruary 55 0 0 0 12. 1927. 1928. Pebruary 15 0 0 0 12. 1927. Sephenaber 21 21 27 192. 1928. Junery 30 7 13 192. 1928. Junery 30 7 13 192. 1928. Junery 30 7 13 192. 1928. Junery 30 15 192. 1929. Junery 40 192 193. 1930. Junery 40 193 1930. Junery 193 1930. 1930. Junery 193 1930. 1937. Junery 193 1930. 1930. Junery 193 1930. 1937. Junery 193 1930. 1930. Junery 193 1930. 1937. Junery 193	0-580 0-582 0-583 0-583 0-583 0-983 0-983 0-983 0-983 0-983 0-983 1-600 0-983 1-600 0-983	299 3 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	200 25 0 0 0 125 50 0 0 0 125 50 0 0 0 125 50 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	10 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	RE DODDERHEDE RUREDEDDEDRORDED DODDERRORDDDDRORRDDDRRDDRRDDRRDDDRRD

ne of Peribelion Passage.	Perih, Dist, Earth's = 1.	Longitude of Perihelion,	Long. of As-	Inclination
A. m.	-	0 . #	0 1 11	0 .
47. March 5 7 11	2-1955	277 2 0	147 18 50	79 6
15, April 28 18 44	0.8404	215 23 29	232 51 50	85 28
48, June 18 21 15	0.6254	278 47 10	33 8 29	67 3
57. October 21 7 65	0-3375	122 58 0	214 12 50	12 50
S. June 11 3 18	0-2154	267 38 0	230 50 0	68 19
9. November 27 2 19	0.7985	53 24 20	139 39 24	78 59
59. December 16 21 4	0.9660	138 24 35	79 50 45	4 51
2. May 28 8 2	1-0091	104 2 0	348 33 5	85 38
64. February 12 13 42	0.9995	15 14 52	120 4 33	52 53
6. February 17 8 41	0.5053	143 15 25	244 10 50	40 50
10. November 22 5 39	0.5282	208 22 44	108 42 10	31 25
3. September 5 14 34	1-1269	75 10 68	121 5 30	61 14
9. January 4 2 4	0-7132	67 14 27	25 4 10	32 50
November 28 20 21	0.5153	246 52 0	141 1 0	72 3
ii. July 7 4 32	0-1768	239 11 25	63 0 38	81 43
1. November 29 12 32	0.9610	16 3 28	77 22 52	27 13
54. January 21 4 47	0.7079	90 44 24	56 49 21	51 9
5. January 27 7 49	I-1434	109 51 56	264 12 15	70 14
5. April 5 8 59	0-4273	297 29 33	64 53 36	87 31
6. July 7 21 51	0-4101	159 25 36	194 22 40	50 54
7. May 10 19 49		7 44 9	106 51 35	48 15
88. November 10 7 25	1-0630	99 8 7	156 56 43	12 27
58. November 20 7 16	0.7573	22 49 54	352 24 29	64 30
0. January 15 5 6	0.7581	60 14 12	176 11 46	31 54
90. Janu ry 28 7 36	1.0633	111 44 37	267 9 37	56 58
io. May 21 5 47	0.7850	273 43 27	33 11 2	63 54
2. January 13 13 35	1-29/10	36 29 42	190 46 15	39 46
2. December 27 6 5	0.9663	135 50 24	281 16 17	49 1
93. November 4 20 12	0-4034	228 42 0	108 29 0	60 21
16. April 2 19 48	1-5792	192 44 13	17 2 16	64 54
97. July 9 2 31	0.5266	49 27 8	329 15 37	50 40
98. April 4 11 32	0.4848	104 59 0	122 9 0	43 52
98. December 31 13 17	0-7795	34 27 27	249 30 30	42 26
9. Beptember 7 5 39	0-8369	3 39 46	99 32 47	50 56
0. December 25 21 31	0-6258	190 20 12	326 49 11	77 1
I. August 5 13 23	0:2617	183 49 0	44 28 0	21 20
D. Kondonskop (1) 40	1-0644	993 6 4	910 AE 80	EM IN

VI. PARABOLIC COMETS.

3075. Tabular synopsis of the parabolic comets.—In the annexed Table (VIII.) are given the elements of the orbits of 161 comets, whose paths in passing through the system have been either parabolas or ellipses of eccentricities so extreme as to be undistinguishable from parabolas in that part of their orbits at which they were capable of being observed.

VII. DISTRIBUTION OF COMETARY ORBITS IN SPACE.*

8076. Distribution of the cometary orbits in space. — In reviewing the vast mass of data collected by the labours of observers, ancient and modern, and which, so far as we have been enabled to see grounds for classification, are marshalled in the series of tables which are given above, it is natural to look for some evidence of a prevalent law in the motions of these bodies. The absence of all analogy to the planetary orbits, except in the case of the first group of elliptic comets consigned to Table III., has been already indicated; but, although no analogy to the planetary motions may exist, it does not follow that the cometary motions may not be governed by some laws of their own, the nature and character of which can only be discovered by carefully conducted induction.

3077. Relative numbers of direct and retrograde comets. — It has been shown that of the nineteen comets included in the first and second groups, which possess in the most marked degree the planetary character, one only is retrograde. Here is, then, the indication of a law, so far as regards the direction of the motion of

the comets of these groups.

To ascertain whether traces of the same law are discoverable in the other classes of comets, let the other tables be examined and compared.

Of the twenty-one comets included in Table VI. there are,

Direct	10
Retrograde	11
	_

There is, therefore, among these no indication of the prevalence of any law in relation to the direction of the motion.

Of the seven hyperbolic comets in Table VII. there are,

••••••••••••••••••••••••••••	
•	;

^{*} This section contains the substance of a paper by the author, which has been printed in the Proceedings of the Royal Astronomical Society.

Here	the law	of di	rect m	otion	re-app	ears;	but th	e nun
all to	supply	groun	d for	any s	afe ind	luction		
Of 16	30 paral	bolic o	comets	inclu	ded in	Table	VIII	. there

Direct	
	156
Direction unascertained	4
	100

Here the tendency leans to retrograde motion, but still gree sufficiently decided to supply safe ground for a constead of taking as the basis of the induction the 160 nets, we take the entire number of 203 comets of a secretained, we shall find,

scertained, we shall find,	
Direct	
	203

t must, therefore, be concluded that, notwithstanding

3079. Directions of the nodes and perihelia. — Taking, in like manner, the longitudes of the nodes and the perihelia, we find that those of every hundred comets are distributed in longitude as follows:—

	• •	Number of Nodes.	Number of Perihelia
oo t	o 30°	8:35	0.80
30	60	8.85	7:30
60	90	11.85	12-25
90	120	8:35	11.70
120	150	1.35	8:25
130	160	7-90	2:90
160	210	9-90	8.85
210	240	8-90	7.80
a 3	270	7:40	10-70
270	300	4.90	1275
300	380	8-35	10-30
300	360	6-90	8.40
		100-00	100-00

An uniform distribution would give 8.33 nodes to each arc of 80°. The number in the third sign between 60° and 90° is nearly 12, and in the seventh sign between 180° and 210° nearly 10, both considerably exceeding the mean share.

The distribution of the perihelia is still more unequal. There is an evident tendency to crowd into the arcs between 60° and 120°, and between 240° and 300°. The number of perihelia due to an arc of 60° is 16.66. Now the actual number found between 60° and 120° is 23.95, about 50 per cent. above the mean. Between 240° and 330° there are 33.75 perihelia, where, as the number due to an arc of 90° is 25, the actual number being 35 per cent. above the mean.

8080. Distribution of the points of perihelion. — Considering how much the visibility of a comet from the earth depends on its perihelion distance, and that beyond a certain limit of such distance a comet cannot be expected to be seen at all, it cannot be expected that the law, if any such there be, which governs the distribution of the points of perihelion round the sun can be discovered with any degree of certainty. Nevertheless, it will not be without interest to show the distribution of the points of perihelion of the known comets in relation to their distances from the sun.

If the centre of the sun be imagined to be surrounded by spheres having semi-diameters increasing successively by a constant increment of 20 millions of miles, the number out of every hundred known comets whose perihelia lie between sphere and sphere will

be as follows :-

100				Number
Within	20			
Between	20	and	40	
***************************************	40	**	60	2
	60	44	80	
	80	**	100	2
	100	44	120	
	120	66	140	
	140	16	160	
	160		180	
	180		220	
	220	**	240	

is evident that the small proportion of the perihelia de the sphere, whose radius is 120 millions of miles bed to the fact that comets moving in such orbits we observation: but it may, perhaps, be assumed the bus, the comets whose perihelia lie within a sphere earth's orbit have nearly equal chances of being observed are nearly proportional to the have been observed are nearly proportional to the second s

It is evident then that the density of the perihelia increases rapidly in approaching the sun. If the numbers in the last column of the table be compared with the inverse powers of the distance, it will be found that this increase of density is more rapid than the inverse distance, but less so than the inverse distance squared.

VIII., PHYSICAL CONSTITUTION OF COMETS.

3081. Apparent form — Head and Tail. — Comets in general, and more especially those which are visible without a telescope, present the appearance of a roundish mass of illuminated vapour or nebulous matter, to which is often, though not always, attached a train more or less extensive, composed of matter having a like appearance. The former is called the HEAD, and the latter the TAIL of the comet.

8082. Nucleus. — The illumination of the head is not generally uniform. Sometimes a bright central spot is seen in the nebulous matter which forms it. This is called the NUCLEUS.

The nucleus sometimes appears as a bright stellar point, and sometimes presents the appearance of a planetary disk seen through a nebulous haze. In general, however, on examining the object with high optical power, these appearances are changed, and the object seems to be a mere mass of illuminated vapour from its borders to its centre.

3083. Coma. — When a nucleus is apparent, or supposed to be so, the nebulous haze which surrounds it and forms the exterior part of the head is called the coma.

8084. Origin of the name. — These designations are taken from the Greek word *σομή (komé) hair, the nebulous matter composing the coma and tail being supposed to resemble hair, and the object

being therefore called zouriths (kometes), a hairy star.

3085. Magnitude of the head. — As the brightness of the coma gradually fades away towards the edges, it is impossible to determine with any great degree of precision its real dimensions. These, however, are obviously subject to enormous variation, not only in different comets compared one with another, but even in the same comet during the interval of a single perihelion passage. The greatest of those which have been submitted to micrometrical measurement was the great comet of 1811, Table VI. No. 8, the diameter of the head of which was found to be not less than 1½ millions of miles, which would give a volume greater than that of the sun in the ratio of about 2 to 1. The diameter of the head of Halley's comet when departing from the sun, in 1836, at one time measured 357,000 miles, giving a volume more than sixty times that of Jupiter. These are, however, the greatest dimensions which have been observed in this class of objects, the diameter rarely exceeding 200,000 miles, and being generally less than 100,000.

8086. Magnitude of the nucleus.—Attempts have been miles where nuclei were perceivable, to estimate their magnitude, midiameters have been assigned to them, varying from 100 to 500 miles. For the reasons, however, already explained, these results

must be regarded as very doubtful.

Those who deny the existence of solid matter within the commaintain that even the most brilliant and conspicuous of these bodies, and those which have presented the strongest rescribions to planets, are more or less transparent. It might be supposed that a fact so simple as this, in this age of astronomical activity, call not remain doubtful; but it must be considered, that the continuation of circumstances which alone would test such a question of rare occurrence. It would be necessary that the centre of the comet, although very small, should pass critically the a star, in order to ascertain whether such star is visible through it. With comets having extensive comes without nuclei, this has starting occurred; but we have not had such satisfactory examples it the more rare instances of those which have distinct nuclei.

In the absence of a more decisive test of the occultation of a set by the nucleus, it has been maintained that the existence of a set nucleus may be fairly inferred from the great splendour which he attended the appearance of some comets. A mere mass of vapor could not, as is contended, reflect such brilliant light. The fel-

lowing are the examples adduced by Arago:-

In the year 48 before Christ, a comet appeared which was said to be visible to the naked eye by daylight. It was the comet which the Remain considered to be the soul of Casar transferred to the heavens after his assassination.

In the year 1402 two remarkable comets were recorded. The first we so brilliant that the light of the sun at noon, at the end of March, did so prevent its nucleus, or even its tail from being seen. The second appeared in the month of June, and was visible also for a considerable time before sunset.

In the year 1532, the people of Milan were alarmed by the appearant of a star which was visible in the broad daylight. At that time Versi was not in a position to be visible, and consequently it is inferred that this star must have been a comet.

The comet of 1577 was discovered on the 18th of November by Tycks Brahe, from his observatory on the isle of Huene, in the Sound, before sunset.

On the 1st of February, 1744, Chizeaux observed a comet more brilled than the brightest star in the heavens, which soon became equal in spledour to Jupiter, and in the beginning of March it was visible in the present of the sun. By selecting a proper position for observation, on the 1st of March it was seen at one o'clock in the afternoon without a telescope.

Such is the amount of evidence which observation has supplied respecting the existence of a solid nucleus. The most that can be said of it is, that it presents a plausible argument, giving some pre-

bability, but no positive certainty, that comets have visited our system which have solid nuclei, but, meanwhile, this can only be maintained with respect to few: most of those which have been seen, and all to which very accurate observations have been directed, have afforded evidence of being mere masses of semi-transparent matter.

3087. The tail. - Although by far the great majority of comets are not attended by tails, yet that appendage, in the popular mind, is more inseparable from the idea of a comet than any other attribute of these bodies. This proceeds from its singular and striking appearance, and from the fact that most comets visible to the naked eye have had tails. In the year 1531, on the occasion of one of the visits of Halley's comet to the solar system, Pierre Apian observed that the comet generally presented its tail in a direction opposite to that of the sun. This principle was hastily generalized, and is even at present too generally adopted. It is true that in most cases the tail extends itself from that part of the comet which is most remote from the sun; but its direction rarely corresponds with the direction which the shadow of the comet would take. Sometimes it has happened that the tail forms with a line drawn to the sun a considerable angle, and cases have occurred when it was actually at right angles to it.

Another character which has been observed to attach to the tails of comets, which, however, is not invariable, is, that they incline constantly toward the region last quitted by the comet, as if in its progress through space it were subject to the action of some resisting medium, so that the nebulous matter with which it is invested, suffering more resistance than the solid nucleus, remains behind it

and forms the tail.

The tail sometimes appears to have a curved form. That of the comet of 1744 formed almost a quadrant. It is supposed that the convexity of the curve, if it exists, is turned in the direction from which the comet moves. It is proper to state, however, that these circumstances regarding the tail have not been clearly and satisfac-

torily ascertained.

The tails of comets are not of uniform breadth or diameter; they appear to diverge from the comet, enlarging in breadth and diminishing in brightness as their distance from the comet increases. The middle of the tail usually presents a dark stripe, which divides it longitudinally into two distinct parts. It was long supposed that this dark stripe was the shadow of the body of the comet, and this explanation might be accepted if the tail was always turned from the sun; but we find the dark stripe equally exists when the tail, being turned sideward, is exposed to the effect of the sun's light.

This appearance is usually explained by the supposition that the

hollow, conical shell of vapour, the external subsesses a certain thickness. When we view it, a considerable thickness of vapour at the edges, and ratively small quantity at the middle. Thus upon of a hollow cone, the greatest brightness would a, and the existence of a dark space in the middle accounted for.

alls of comets are not always single; some have ap times with several separate tails. The comet opeared on the 7th or 8th of March, had six to in breadth, and from 30° to 44° in length. The I defined and tolerably bright, and the spaces between lark as the other parts of the heavens.

dark as the other parts of the heavens.

ils of comets have frequently appeared, not only of
gth, but extending over considerable spaces of the
be easily understood that the apparent length depipon the real length of the tail, and the position in
ted to the eye. If the line of vision be at right
ngth will appear as great as it can do at its exi
f it be oblique to the eye, it will be foreshortened,
ording to the angle of obliquity. The real leng

rocal effects of their gravitation, and those of any known bodies in the system could be observed. But although the disturbing action of the planets on these bodies is conspicuous, and its effects have been calculated and observed, not the slightest effect of the same kind has ever been ascertained to be produced by them, even upon the smallest bodies in the system, and those to which comets have approached most nearly.

In fine, notwithstanding the enormous number of comets, observed and unobserved, which constantly traverse the solar system in all conceivable directions; notwithstanding the permanent revolution of the periodic comets, whose presence and orbits have been ascertained; notwithstanding the frequent visits of comets, which so thoroughly penetrate the system as almost to touch the surface of the sun at their perihelion, the motions of the various bodies of the system, great and small, planets major and minor, planetoids and satellites, go on precisely as if no such bodies as the comets approached their neighbourhood. Not the smallest effects of the attraction of such visitors are discoverable.

Now since, on the other hand, the disturbing effects of the planets upon the comets are strikingly manifest, and since the comets move in elliptic, parabolic, or hyperbolic orbits, of which the sun is the common focus, it is demonstrated that these bodies are composed of ponderable matter, which is subject to all the consequences of the law of gravitation. It cannot, therefore, be doubted that the comets do produce a disturbing action on the planets, although its effects are inappreciable even by the most exact observation. Since, then, the disturbances mutually produced are in the proportion of the disturbing masses, it follows that the masses of the comets must be smaller beyond all calculation than the masses even of the smallest bodies among the planets primary or secondary.

The volumes of comets in general exceed those of the planets in a proportion nearly as great as that by which the masses of the planets exceed those of the comets. The consequence obviously resulting from this, is that the density of comets is incalculably small

Their densities in general are probably thousands of times less than that of the atmosphere in the stratum next the surface of the earth.

8089. Light of comets. — That planets are not self-luminous, but receive their light from the sun, is proved by their phases, and by the shadows of their satellites, which are projected upon them, when the latter are interposed between them and the sun. These tests are inapplicable to comets. They exhibit no phases, and are attended by no bodies to intercept the sun's light. But, unless it could be shown that a comet is a solid mass, impenetrable to the solar rays,

the non-existence of phases is not a proof that the bedy does ast receive its light from the sun.

A mere mass of cloud or vapour, though not self-luminous, but rendered visible by borrowed light, would still exhibit no effect of this kind: its imperfect opacity would allow the solar light to effect its constituent parts throughout its entire depth—so that, like a this fleecy cloud, it would appear not superficially illuminated, but no ceiving and reflecting light through all its dimensions. With respect to comets, therefore, the doubt which has existed is, whether the light which proceeds from them, and by which they become with is a light of their own, or is the light of the sun ahining upon them, and reflected to our eyes like light from a cloud. Among arrespected by Arago merits attention.

It has been already shown (1131 et seq.), that the apparent brightness of a visible object is the same at all distances, supposing its real brightness to remain unchanged. Now if comets show with their proper light, and not by light received from the sun, their apparent brightness would not decrease as they would recede from the sun, and they would cease to be visible, not because of the faintness of their light, but because of the smallness of their apparent magnitude. Now the contrary is found to be the case. As the comet retires from the sun its apparent brightness rapidly decreases, and it ceases to be visible from the mere faintness of its

light, while it subtends a considerable visual angle.

3090. Enlargement of magnitude on departing from the sun-It will doubtless excite surprise, that the dimensions of a count should be enlarged as it recedes from the source of heat. It has been often observed in astronomical inquiries, that the effects, which at first view seem most improbable, are nevertheless those which frequently prove to be true; and so it is in this case. It was log believed that comets enlarged as they approached the sun; and this supposed effect was naturally and probably ascribed to the heat of the sun expanding their dimensions. But more recent and exact observations have shown the very reverse to be the facts. Comet increase their apparent volume as they recede from the suu; and this is a law to which there appears to be no well-ascertained esception. This singular and unexpected phenomenon has been attempted to be accounted for in several ways. Valz ascribed it the pressure of the solar atmosphere acting upon the comet; that atmosphere being more dense near the sun, compresses the cond and diminishes its dimensions; and, at a greater distance, being relieved from this coercion, the body swells to its natural bulk. A very ingenious train of reasoning was produced in support of this theory. The density of the solar atmosphere and the elasticity of the comet being assumed to be such as they might naturally be say

posed, the variations of the comet's bulk are deduced by strict reasoning, and show a surprising coincidence with the observed change in the dimensions. But this hypothesis is tainted by a fatal error. It proceeds upon the supposition that the comet, on the one hand, is formed of an elastic gas or vapour; and, on the other, that it is impervious to the solar atmosphere through which it moves. To establish the theory, it would be necessary to suppose that the elastic fluid composing the comet should be surrounded by a nappe or envelope as elastic as the fluid composing the comet, and yet wholly impenetrable by the solar atmosphere.

After several ingenious hypotheses * having been proposed and successively rejected for explaining this phenomenon, it seems now agreed to ascribe it to the action of the varying temperature to which the vapour which composes the nebulous envelope is exposed. As the comet approaches the sun, this vapour is converted by intense heat into a pure, transparent, and therefore invisible elastic fluid. As it recedes from the sun, the temperature decreasing, it is partially and gradually condensed, and assumes the form of a semi-transparent visible cloud, as steam does escaping from the valve of a steam boiler.. It becomes more and more voluminous as the distance from the source of heat, and therefore the extent of condensation, is augmented.

3091. Professor Struve's drawings of Encké's comet. — Professor Struve made a series of observations on the comet of Encké, at the period of its re-appearance in 1828, and by the aid of the great Dorpat telescope, made the drawings given in Pl. XIV., figs. 1 and 2.

Fig. 1 represents the comet as it appeared on the 7th November, the diameters a b and c d measuring each 18'. The brightest part of the comet extended from a to x, and was consequently eccentric to it, the distance of the centre of brightness from the centre of magnitude being x K. Between the 7th and the 30th November, the magnitude of the comet decreased from that represented in fig. 1 to that represented in fig. 2; but the apparent brightness was so much increased, that at the latter date it was visible to the naked eye as a star of the 6th magnitude. The apparent diameter was then reduced to 9'.

On November 7th a star of the 11th magnitude was seen through the comet, so near the centre z of brightness that it was for a moment mistaken for a nucleus. The brightness of the star was not in the least perceptible degree dimmed by the mass of cometary matter through which its light passed.

It was evident that the increase of the brightness of the comet

[•] For several of these, see Sir J. Herschel's memoir, Proceedings of Astronomical Society, vol. vi. p. 104.

on the 30th November, must be ascribed to the contraction, and consequent condensation, of the nebulous matter composing it in receding from the sun, for its distance from the earth on the 7th November, when it subtended an angle of 18', was 0.515 (the earth's mean distance from the sun being =1); while its distance on the 30th, when it subtended an angle of 9', was only 0.477. Its cubical dimensions must, therefore, have been diminished, and the density of the matter composing it augmented in more than an eightfold proportion.

8092. Remarkable physical phenomena manifested by Halley's comet. — The expectation so generally entertained, that, on the occasion of its return to perihelion in 1835, this comet would afford observers occasion for obtaining new data, for the foundation of some satisfactory views respecting the physical constitution of the class of which it is so striking an example, was not disappointed. It no sooner re-appeared than phenomena began to be manifested, preceding and accompanying the gradual formation of the tail, the observation of which has been most justly regarded as forming a memorable epoch in astronomical history.

Happily, these strange and important appearances were observed with the greatest zeal, and delineated with the most elaborate and scrupulous fidelity by several eminent astronomers in both hemispheres. MM. Bessel, at Konigsberg, Schwabe, at Dessau, and Struve, at Pultowa, and Sir J. Herschel and Mr. Maclear, at the Cape of Good Hope, have severally published their observations, accompanied by numerous drawings, exhibiting the successive transformations presented under the physical influence of varying temper-

ature, in its approach to and departure from the sun.

The comet first became visible as a small round nebula, without a tail, and having a bright point more intensely luminous than the rest eccentrically placed within it. On the 2d October, the tail began to be formed, and, increasing rapidly, acquired a length of about 5° on the 5th; on the 20th it attained its greatest length, which was 20°. It began after that day to decrease, and its diminution was so rapid, that on the 29th it was reduced to 3°, and on the 5th November, to 2½°. The comet was observed on the day of its perihelion by M. Struve, at the Observatory of Pultowa, when no tail whatever was apparent.

The circumstances which accompanied the increase of the tail from 2d October, until its disappearance, were extremely remarkable, and were observed with scrupulous precision, simultaneously by Bessel, at Konigsberg, by Struve, at Pultowa, and by Schwabe, at Dessau, all of whom made drawings from time to time, delineating

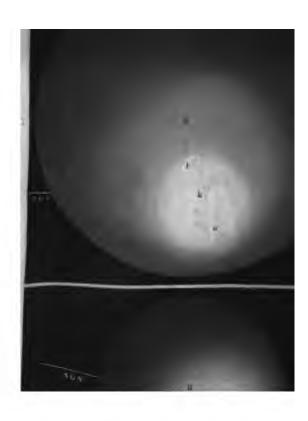
the successive changes which it underwent.

. On the 2nd, the commencement of the formation of the tail took place by the appearance of a violent ejection of nebulous matter



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APTEN FOR OF THE



HALLEY'S COMET, 1835

APPROACHING THE SUN FROM DRAWING BY



1, eg. 32/2 - dis 3 ; 2/25.



1 that part of the comet which was presented towards the sun. ejection was, however, neither uniform nor continuous. fiery matter issuing from the crater of a volcano, it was thrown at intervals. After the ejection, which was conspicuous, accordto Bessel, on the 2nd, it ceased, and no efflux was observed for ral days. About the 8th, however, it recommenced more vioy than before, and assumed a new form. At this time Schwabe ed an appearance which he denominates a "second tail," preed in a direction opposed to that of the original tail, and, theretowards the sun. This appearance seems, however, to be rded by Bessel merely as the renewed ejection of nebulous

er which was afterwards turned back from the sun, as smoke ld be by a current of air blowing from the sun in the direction

he original tail.

rom the 8th to the 22nd, the form, position, and brightness of nebulous emanations underwent various and irregular changes,

last alternately increasing and decreasing.

.t one time two, at another three, nebulous emanations were rved to issue in diverging directions. These directions were inually varying, as well as their comparative brightness. Somes they would assume a swallow-tailed form, resembling the e issuing from a fan gas-burner. The principal jet or tail was observed to oscillate on the one side and the other of a line vn from the sun through the centre of the head of the comet, stly as a compass needle oscillates between the one and the r side of the magnetic meridian. This oscillation was so rapid, the direction of the jets was visibly changed from hour to The brightness of the matter composing them, being most nse at the point at which it seemed to be ejected at the nucleus, ad away as it expanded into the coma, curving backwards, in direction of the principal tail, like steam or smoke before the d.

093. Struve's drawings of the comet approaching the sun in 5. - These curious phenomena will, however, be more clearly zeived by the aid of the admirable drawings of M. Struve, which have reproduced with all practicable fidelity, in Plates XV., I., and XVII. These drawings were executed by M. Kruger, eminent artist, from the immediate observation of the appeares of the comet with the great Fraunhoffer telescope, at the towa Observatory. The sketches of the artist were corrected by astronomer, and only adopted definitively after repeated compa-The original drawings are preserved in the ns with the object. ary of the observatory.

094. Its appearance 29th September. — Plate XV., fig. 1, reents the appearance of the comet on the 29th September. was difficult to be recognised, appearing to be composed of very 01

po

feeble nebulous matter. The nucleus passed almost centrically over magnitude, without in the slightest degree affecta star of th rightness. The star was distinctly seen through ing its : the comet. Another transit of a star took place the

a is the scale, according to which this drawing has been

Appearance on O his is represented in fig. 2,

same scale. comet changed not .. its magnitude and form, but also its since September 25. On that day the direction of the tail at of the parallel of declination through the head. On Oc-3, it was inclined from that parallel towards the north at a angle, and, instead of being straight, was curved. The dismeter of the head was increased in the ratio of 2 to 3, and the length of the tail in the ratio of nearly 1 to 3.

3096. Appearance on October 8. - Plate XVI. fig. 1. This

drawing is made on the subjoined scale of seconds.

On the 5th, 6th, and 7th, the comet underwent several changes; the nucleus became more conspicuous. On the 6th, a fan-formed flame issued from it, which disappeared on the 7th, and re-appeared on the 8th with increased splendour, as represented in the figure. The nucleus appeared like a burning coal, of oblong form, and yellowish colour. The extent of the flame-like elongation was about The feeble nebula surrounding the nuclei extended much beyond the limits of the drawing, but, being overpowered by the moonlight, could not be measured.

3097. Appearance on October 9.—Plate XVI. fig. 2, same scale, represents the nucleus and flame-like emanation, which entirely changed their form and magnitude since the preceding night. The tail (not included in the drawing) measured very nearly 2°. The flame consisted of two parts, one resembling that seen on the 8th, and the other issuing like the jet from a blow-pipe in a direction at right angles to it. The figure represents the nucleus and flame #

they appeared at 21^h sid. time, with a magnifying power of 254. 3098. Appearance on October 10. — Plate XVI. fig. 3, on the same scale. The tail, which still measured nearly 20, was now much brighter, being visible to the naked eye, notwithstanding PUBLIC LIBE A FY

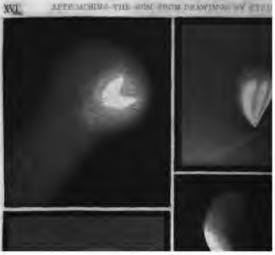
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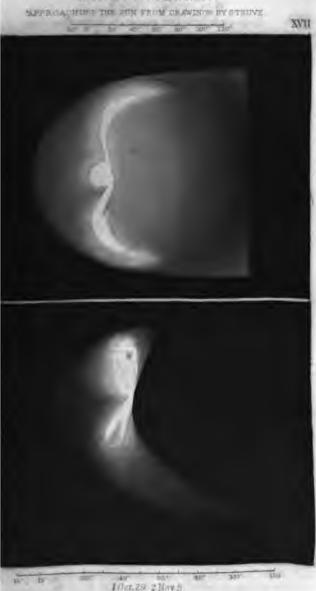
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HALLEY'S COMET. 1835.

APPRING THE GOA SHOW DRAWINGS WY STAD



HALLEY'S COMET, 1835



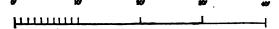
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g moonlight. The coma was evidently broader than the tail. flaming nucleus is represented in the drawing as it appeared r a magnifying power of 86, with a field of 18' diameter, the e of which was filled with this coma. The diameter of the r must, therefore, have been more than 18'. The drawing was n at 21 h. s. t.

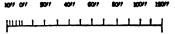
199. Appearance on October 12. — Plate XVI. fig. 4, on the scale. The comet appeared at 0 h.—25 m. s. t., for a short val, in uncommon splendour, the nucleus and flame, however, being visible, as represented in the drawing. The greatest nt of the flame measured 64".7. Its appearance was most beautresembling a jet streaming out from the nucleus like flame a blow-pipe, or the flame from the discharge of a mortar, ated with the white smoke driven before the wind.

100. Appearance on October 14. — Plate XVI. fig. 5, on the scale. The principal flame was now greatly enlarged, extend-to the apparent length of 134". Its deflection and curved form most remarkable.

101. Appearance on October 29.—A cloudy sky prevented all rvation for 12 days. On the 27th, the comet appeared to the d eye as bright as a star of the third magnitude, the tail being netly visible. The coma surrounding the nucleus appeared as iform nebula. The tail was curved, and of great length; but, g to the low altitude at which the observation was taken, it i not be measured. On the 29th, however, the comet was pred under much more favourable conditions, and the drawings, a XV. fig. 3, and Plate XVII. fig. 1, were made. The former seents the entire comet, including the whole visible extent of ail, and is drawn to the annexed scale of minutes. The latter



ments the head of the comet only, and is drawn to the annexed of seconds.



t 20² 30² s. t., the head presented the appearance represented in a XVII. fig. 1. The chief coma was almost exactly circular, and a diameter of 165". With a power of 198, the nucleus aped as in the figure, the diameter being about 1".25 to 1.50. flame issuing from the nucleus, curved back like smoke before wind, was very conspicuous. The appearance of the formation of tail as it issues from the nucleus was remarkably developed.

ppearance on November 5. - Plate XVII. fig. 2. This presents the nucleus and flame issuing from it on the ale of seconds.

0	20*	40**	60"	80*	100**	120
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per nucleus was found to measure about 2"-3. Two e seen issuing from it in nearly opposite directions, and I towards the same side. The brighter flame, directed e north, was marked by strongly defined edges. sted towards the south, was more feeble and ill-defined.

Sir J. Herschel's deductions from these phenomena. - Sir l, who also observed this comet himself at the Cape of e, makes from all these observations the following in-

the matter of the comet vaporised by the sun's heat jets, throwing the comet into irregular motion by its nd thus changing its own direction of ejection. this ejection takes place principally from the part pre-

an aspect altogether different from that under which it was seen before its perihelien. It had evidently, as Sir J. Herschel thinks, undergone some great physical change, which had operated an entire

transformation upon it.

"Nothing could be more surprising than the total change which had taken place in it since October. . . . A new and unexpected phenomenon had developed itself, quite unique in the history of comets. Within the well-defined head, somewhat eccentrically placed, was a vivid nucleus resembling a miniature comet, with a head and tail of its own, perfectly distinct from and considerably exceeding in intensity the nebulous disk or envelope which I have above called the 'head.' A minute bright point, like a small star, was distinctly perceived within it, but which was never quite so well defined as to give the positive assurance of the existence of a solid sphere, much less could any phase be discovered."*

3105. Observations and drawings of Messrs. Maclear and Smith. The phenomena and changes which the comet presented from its reappearance on the 24th of January, until its final disappearance, have been described with great clearness by Mr. Maclear, and illustrated by a beautiful series of drawings by that astronomer and his assistant, Mr. Smith, in a memoir which appeared in the tenth volume of the Transactions of the Royal Astronomical Society, from which we reproduce the series of illustrations given on Plates XVIII.

and XIX.

• 3106. Appearance on January 24. — The comet appeared as in fig. 1, visible to the naked eye as a star of the second magnitude. The head was nearly circular, and presented a pretty well-defined planetary disc, encompassed by a come or halo of delicate gossamer-like brightness. The diameter of the head, without the halo or come, measured 131", and with the latter 492".

3107. Appearance on January 25. — Fig. 2. Circular form broken, and magnitude increased. Three stars seen through the

coma and one through the head.

3108. Appearance on January 26. — Fig. 3. Magnitude again increased, but come diminished.

3109. Appearance on January 27. — Fig. 4. Comet began to assume the parabolic form, and increase of magnitude continued.

- 3110. Appearance on January 28. Fig. 5. The come or halo quite invisible, but the nucleus appeared like a faint small star. The magnitude of the comet continued to increase. The observer fancied he saw the faint outline of a tail.
- 3111. Appearance on Junuary 30. Fig. 6. The form of the comet now became decidedly parabolic. The breadth across the head was 702", being greater than on the 24th in the ratio of 49 to

^{*} Cape Observations, p 397.

to 10, which corresponds to an increase of volum 1 to 3, supposing the form to remain unchanged mated that the extension in length gave a superficial atio of 35 to 1, which would correspond to a muc tation of volume.

Appearance on February 1. — Fig. 7. Further itude, the form remaining the same.

Appearance on February 7. - Plate XIX. fig. as on this night rendered faint by the effect of moo Appearance on February 10. - Fig. 9. Further A star visible through the body of the comet. Appearance on February 16 and 23. - Figs. gnitude went on increasing, while the illumination d more faint, and this continued until the comet's nce; the outline, after a short time, became so faint the surrounding darkness, leaving a bland nebulor oright centre enveloping the nucleus.

Number of comets. - According to Mr. Hind, the ts which have appeared since the birth of Christ in century is as follows: I., 22; II., 23; III., 44; VI., 25; VII., 22; VIII., 16; IX., 42;



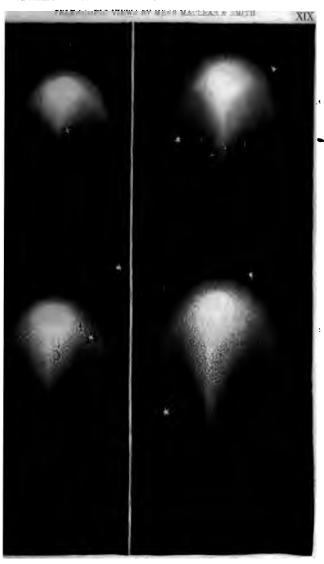
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HALLEYS COMET DEPARTING FROM THE SUN IN B

III TELEROOPE VIEWS BY MEST MACLEAR & BUTTE

HALLEYS CORET DEPARTING FROM THE SUN IN 1836.



1 Feb 7 2 fe li r 3 Feb 16 4 Feb 21.

CHAP. XIX.

THEORY OF VARIABLE ORBITS.

3119. Conditions under which elliptic orbits are described.—
If any number of bodies P, P', P'', &c., moving with any velocities in any directions whatever, be exposed to the influence of the attraction of a central body s, in a fixed position, such attraction varying in its intensity inversely as the square of the distance of the attracted body from s; and if at the same time the several bodies P, P', P'', &c., exert no attraction upon each other or upon the central body, s; these bodies P, P', P'', &c., will each of them revolve in an ellipse of which the centre of the attracting body s is the focus. Each of these elliptic orbits will be invariable in form, magnitude, and position, and so long as such a system would be exposed to the influence of no other force than the central attraction of s, each of the bodies P, P', P'', &c., would continue to revolve round s in the same invariable orbit.

The general proposition here enunciated was demonstrated by Newton in the first book of his celebrated work entitled the PRINCIPIA.

3120. Forces other than the central attraction would destroy the elliptic form. — If, however, the bodies composing such a system were exposed to the influence of any other attraction, whether proceeding from each other or from any cause exterior to and independent of the system, the motions of P, P', P'', &c., would no longer take place in such elliptic orbits. Their paths would, in that case, depend on the directions, intensities, and law of variation of those other attractions, whether internal or external, to the operation of which they are exposed. If such forces have intensities which bear any considerable proportion to the intensity of the central attraction exercised by s. the elliptic form impressed on the orbits by the latter would be altogether effaced, and the bodies P, P', P'', &c., would be thrown into new and wholly different paths, the problem to determine which would be one of the greatest physical complexity and mathematical difficulty.

8121. But when these forces are feeble compared with the central attraction, the elliptic form is only slightly affected. — But if the forces, whether internal or external, to the operation of which the system is exposed, have intensities incomparably more feeble than the central attraction exercised by s upon P, P', P'', &c., then, as may be readily conceived, the influence of s in imparting the elliptic form to the paths of P, P', P'', &c., around it, will still in the main

45 *

prevail. These paths will not, in strictness, be ellipses, but, owing to the comparatively small effect of the disturbing forces, they will deviate from the elliptic form, which in the absence of such fixes they would rigorously assume, in a degree so alight as to be only perceptible when the most exact methods of observation and measurement are brought to bear upon them, and in many cases at even then until the effects of such feeble forces have been allowed to accumulate during a long succession of revolutions.

3122. This is the case in the system of the Universe.—Now is happens that the Great Architect of the Universe has so constructed it, that in all cases whatever, without a single known exception, the forces which are independent of the central attraction s, whether they be those which arise between the bodies composing the system, or whether they proceed from causes exterior to and independent of them, are under the conditions last mentioned. In no case do their intensities exceed very small fractions, such as an hundredth, and more generally not a thousandth, of the central attraction. Hence it is that the ellipticity of the orbits is so preserved, their magnitudes so maintained, and their positions so little variable, that is cases the most exact means of observation, and in general long periods of time, are necessary to discover and measure the change produced upon them.

3123. Hence proceed great facilities of investigation and calculation.—Hence arise consequences of vast importance in the development of the laws of nature and the progress of physical knowledge. The problem presented by a system subject only to such feels interferences with the influence of the central attraction, is incomparably more simple and easy of solution than would be that of a system in which interfering attractions of much greater relative intensity might prevail. Methods of investigation and calculation, as well as modes of observation, are applicable in the one case, which would be altogether inadmissible in the other; and results are obtained and laws developed which would, under the more complicated conditions of the other problem, be utterly unattainable.

3124. Perturbations and disturbing forces. — The central attraction, therefore, being in all cases regarded as the chief presiding physical power by which the system is held together, and by which its motions in the main are regulated, the orbits of the revolving bodies P, P', P'', &c., are first calculated as if they depended solely upon the central attraction of s. This gives a first, but very class, approximation to them. The forces by which they are affected, independent of the central attraction of s, are then severally takes into account, and the deviations, minute as they always are, from the elliptic paths first determined, are exactly calculated. These deviations are called DISTURBANCES or PERTURBATIONS; and the

forces which produce them are called DISTURBING OF PERTURBING FORCES.

3125. Method of variable elements.—The instantaneous ellipse. -Let a body P be supposed to revolve in a certain orbit, subject to the central attraction F of a certain mass s, and at the same time to a disturbing force D much more feeble than F in its intensity. There are two ways in which the problem to determine the exact path of P may be approached. 1st. The body P may be regarded as under the influence of two forces F and D, of given intensities and directions; and its actual path may be investigated by the principles of mathematical and physical analysis. This path would, in every case presented in nature, be a very complicated curve of no regular form, although in its general shape and outline it would differ very little from an ellipse having its focus at s. 2ndly. Instead of attempting to determine the exact geometrical character of this complicated curve, the body P may be regarded as revolving round s in an ellipse, the form, position, and magnitude of which are subject to a slow and continuous variation. To comprehend this method of considering the motion of P, let the disturbing force D be imagined to be suspended at any proposed point of P's path. From the moment of such suspension, P would move in an exact and invariable ellipse, having 8 as its focus. The form, position, and magnitude of this ellipse, or, what is the same, its elements, that is, its major axis, eccentricity, longitude of perihelion, inclination, and longitude of node, would be exactly deducible from P's distance from s at the moment of suspension of the disturbing force, its velocity, and the direction of its motion. The problem of its determination in such case would have nothing indeterminate. One, and but one, ellipse, could, under such conditions, be described.

If the disturbing force D be imagined to be suspended at another moment and at a different point in the path of P, another and a different ellipse would be in the same manner described by P after such suspension. If the interval between the two moments of such supposed suspension be not considerable, as, for example, when they occur at different parts of a single revolution of P round s, the two ellipses will not in general have any appreciable difference in any of their elements, from which it follows, that when a single or even several revolutions of P round 8 are only considered, the path of P may in general be regarded as an ellipse of fixed position and invariable form and magnitude, such as P would describe independently of the influence of D. But if the interval between the two moments of supposed suspension be very great, as, for example, when it extends to a long series of revolutions of P round s, then the disturbing effects of D, having accumulated from revolution to revolution, will become very sensible and measurable, and the two ellipses may differ one from the other in any or all of their elements,

extent more or less considerable according to the intensity

ion of the disturbing force D.

ipse in which P would thus move, if at any point of its ction of the disturbing force were thus suspended, is called ANTANEOUS ELLIPSE."

ng to this second method of viewing the effects of disturbtherefore, the body P, which is subject to their action, is
s moving in an elliptic orbit of which s is the focus; but
is supposed from moment to moment to change its posi, and magnitude in a certain minute degree. The perturing thus, as it were, transferred from the body P to the
th it describes, the body being supposed to move as a bead
e on a fine wire, while the wire itself, being flexible, would
various forms, the bead still moving along it, the method
denominated as that of "VARIABLE ELEMENTS."

the method of considering the effects of disturbing forces s adopted by Newton, under the title of moveable orbits, ill generally adopted as the most simple, clear, and conpeans of investigating and explaining the phenomena of

one

Feebleness of the disturbing forces in the cases presented or system explained.—In the cases which are presented in system of the world, the extremely feeble intensities of bing forces, compared with those of the central attractions, ome cases from the vastness of the masses of the central with those of the disturbing bodies; in others, from the of the distance of the central compared with that of the

assume it provisionally for the present in our exposition of the general effects of the disturbing forces which prevail among the bodies of the system; premising, however, that other conditions besides the consideration of relative masses and proximity will be necessary for the exact estimation of the effects of the disturbing forces.

3127. Order of exposition. — In the present chapter we shall then explain generally, without reference to any particular disturbing or disturbed body, the effects produced by disturbing forces upon the elements of the orbit of the disturbed body; and in the succeeding chapters we shall show the application of the general principles thus established to the most important cases of perturbation presented in the solar system.

3128. Resolution of the disturbing force into rectangular components. — From whatever cause the disturbing force may arise, it can always be resolved into three components, each of which is at right angles to the other two; and its effects may be investigated by ascertaining the separate effects of each of these components, and then combining the results thus obtained.

The resolution of any force into three rectangular components parallel to three lines or axis, arbitrarily chosen, is a process of great utility in mathematical physics, and one which is based upon the general principles of the composition and resolution of force,

formerly so fully explained and illustrated (144) et seq.

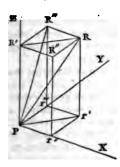


Fig. 822.

To render this more clearly intelligible, let P, fig. 822, be the position of the disturbed body at any proposed time, and let the direction of the disturbing force D be PR, its intensity being such that, if no other force acted on P, it would cause that body to move over PR in the unit of time. Let PZ, PX, and PY be the three axes at right angles to each other, taken at pleasure in any directions along which the disturbing force D is to be resolved. Suppose three lines, RR', RR'', and RR", drawn from R parallel to these three axes, PZ, PY, and PX, so as to form the rectangular, die-shaped solid, called a parallelopiped, represented in the figure.

Now, by the principles of elementary geometry, it appears that R R' P' is a rectangle, of which PR is the diagonal. It follows, therefore (154), that the disturbing force D, represented by PR, is equivalent to two forces represented by PR' and Pr'. But Pr''' r' being also a rectangle, the component Pr' is equivalent to two components represented by Pr'' and Pr''', directed along the axes PX and PR respectively.

it appears that the disturbing force D, represented by PR, ed into three components, represented by PR' directed , Pr" directed along PX, and Pr" directed along PY re-. If the angles at which the direction PR of the disturbis inclined to the three axes PX, PY, and PZ be known, it obtain arithmetical expressions for these three components

e angles RPX, RPY, and RPZ, at which PR is inclined to PX, PY, and PZ respectively, be expressed by a, B, and y; the three components Pr", Pr", and PR' be expressed by I z respectively. Since the angles Pr" R, Pr" R, and each 90°, it will follow that

 $\cos \alpha \times D$, $Y = \cos \beta \times D$, $Z = \cos \gamma \times D$;

e by the figure we have

 $PR^2 = PR'^2 + RR'^2$, $RR'^2 = R'R''^2 + RR''^2$, $PR^2 = PR'^2 + R'R''^2 + RR''^2$,

 $D^2 = X^2 + Y^2 + Z^2$.

ace at the moment the disturbing force is supposed to act, such agent being in effect the direction of P's motion at that moment. If one of the axes, PY, for example, be taken in the direction of e radius vector, the other will necessarily be that of a line drawn rough P in the plane of the orbit perpendicular to the radius

If one of the axes, PX, for example, be taken in the direction the tangent, the other will necessarily be that of the normal the orbit, at the point at which the disturbing force is supposed act.

3130. Orthogonal component. — In referring to these several sthods of resolving the disturbing force, it will conduce to brevity d clearness to give the several components distinct designations licative of the directions which they have in relation to the plane the orbit, and to the position of the disturbed body in its orbit or this purpose we shall adopt the designations which have been ready proposed for them by elementary writers.

The component which is perpendicular to the plane of the orbit the disturbed body will then be distinguished as the ORTHOGONAL

IMPONENT of the disturbing force.

8131. Radial and transversal components.—If the other two imponents be taken in the directions of the radius vector, and of a me in the plane of the orbit at right angles to it, we shall call the rmer the RADIAL and the latter the TRANSVERSAL COMPONENT.

3132. Tangential and normal components.— If the other two emponents be taken in the directions of the tangent and normal 'the orbit, we shall call the former the TANGENTIAL and the latter IN NORMAL COMPONENT.

3133. Orthogonal component affects the inclination and it is evident that of these components the orthogonal alone in have any disturbing effect upon the plane of P's orbit. The other imponents being all in that plane, can have no tendency to move is disturbed body P into any other plane. The orthogonal comment, however, being at right angles to the plane in which P is soving, must have a direct tendency to carry P out of that plane, a the one side or the other, according to the direction in which it its.

This component therefore, and this alone, affects the inclination P's orbit, and the longitude of its node. The kind of effect it roduces on these elements will be explained hereafter.

3134. Radial and transversal components affect the central atraction and angular motion.—To explain in general the effect
roduced on P's motion by the radial and transversal components of
se disturbing force, let Pc, fig. 823, be the radial, and Pa the
ransversal component, the diagonal Pr being therefore the part of
he disturbing force which acts in the plane of P's orbit.

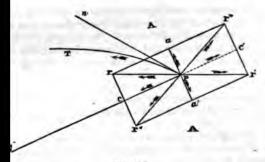


Fig. 823.

ident that the radial component P c, as here represented, the effect of augmenting the attraction by which P is vards s, and that the transversal component P a, being at es to the radius vector, will have a tendency to increase ar velocity of P round s, since this angular velocity is by the motion of P, at right angles to P s, the radius P s posed to be given.

components, however, may be otherwise directed in relae radius vector. If, for example, the element of the disorce which acts in the plane of P's orbit have the direction adial component will be P c', and its transversal P a'. The cting directly against s's attraction on P, would have a ten-

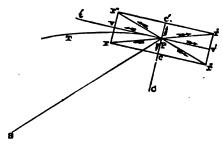


Fig. 824.

of the motion of P, as have been explained in relation to the radial and transversal sub-components, and which will be easily comprehended by the fig. 824.

3186. Positive and negative components. — It will conduce at once to brevity and clearness to distinguish each of the components of the disturbing force according to its direction, with reference to the motion of the disturbed body, the direction of the central attraction, and the plane of the disturbed orbit. We shall therefore consider the transversal or tangential component as positive or + when it acts in the direction of P's motion, and therefore tends to accelerate it; and negative or - when it acts in the contrary direction, and therefore tends to retard it. We shall in like manner consider the radial or normal compoment as positive or + when it acts towards the concave side of P's orbit, and therefore tends to augment the central attraction, and negative or - when it has the contrary direction, and tends to diminish the central attraction. In fine, we shall consider the orthogonal component positive or + when it is directed towards the plane which is adopted as the plane of reference, and negative or — when it is directed from that plane.

3137. In slightly elliptic orbits, the normal and radial components, and the tangential and transversal, coincide.—It is evident that when the elliptic orbit is but slightly eccentric, and therefore very nearly circular, the radial and normal components are very nearly identical in their direction; and, in like manner, the transversal and tangential components are nearly coincident. As this is the case with all the orbits to be considered in this chapter, we shall, without again recurring to this point, consider these components as practically identical.

We shall then explain, in the first instance, without special reference to any particular disturbing body, the effects which are produced upon the orbit of P, 1st, by the radial component;

2ndly, by the transversal component; and 3rdly, by the orthogonal component of any disturbing force whatever.

I. EFFECTS OF THE RADIAL COMPONENT OF THE DISTURBING FORCE.

3138. Equable description of areas not disturbed by it. - The equable description of areas round the centre being independent of the law of central attraction, and involving no other condition, except that the revolving body should be affected by no forces except such as have directions passing through the fixed centre (2599), it will not be affected by the radial component, the direction of which necessarily passes through that point.

3139. Its effect on the mean distance and period. - If M express the central mass, a the mean distance, and P the period proper to the instantaneous ellipse, we shall have, according to what has been

proved (2634), $M = \frac{a}{p^2}$. Now the radial component either aug-

ments or diminishes the central attraction, according as it is positive or negative. This is equivalent to a momentary increase or diminution of the central mass M, which would be attended by a corresponding increase or diminution of $\frac{a^3}{p^2}$; that is, of the ratio of the

cube of the mean distance to the square of the periodic time in the

instantancous ellipse.

3140. If the radial component vary according to any condition which depend solely on the distance, it will not change the form at magnitude of the instantaneous ellipse. - It has been established as a principle of high generality by mathematicians, that if the varation of the central force depend only on the distance of the revolving body from the centre of attraction, the orbital velocity of the body, or the space it moves through in the unit of time, will also depend solely on the distance. Now, from this, combined with the general principle of equable areas, it may be inferred that, under such conditions, the apsides of the instantaneous ellipse will be always at the same distances from the centre of attraction. For the apsides must be always at those particular distances, and no other, at which the velocity (which by the supposition depends on the distance) mutiplied by the distance is equal to twice the area which the revolving body describes in the unit of time, that being necessarily the case of the common principles of elementary geometry when the direction of the motion is at right angles to the radius vector. therefore always give the same values for the radii vectores w

are at right angles to the tangent, or what is the same, to the tances of the apsides of the instantaneous ellipse from the focu-But it is clear that, if the distance d' d' of the apsides fr

focus be always the same, the major axis 2a, and the eccentricity $\frac{c}{a}$, will also be always the same; for we shall have

$$2 a = d' + d'', \qquad 2 c = d'' - d', \qquad \epsilon = \frac{d'' - d'}{d'' + d''}$$

Although the instantaneous ellipse be thus invariable in its form and magnitude, under the conditions here assumed, it does not, however, follow that it is equally invariable in its position. It may, and does, as will presently appear, in certain cases, revolve round

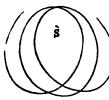


Fig. 825

the centre of attraction, its major axis continually shifting its direction, so that the real path of the disturbed body will be such as is represented in fig. 825.

3141. Effect of a gradually increasing or decreasing radial component.—If the radial component, whether it be positive or negative, were by its continual increase or decrease to cause the effective central attraction continually to increase, the revolving

body P would be brought every revolution nearer and nearer to the central body s; and if it caused the effective central attraction continually to decrease, the contrary effect would be produced. In one case, the angular motion of the revolving body would be continually accelerated; and, in the other case, continually retarded.

3142. Effects on the period and mean motion more sensible than those on the mean distance.— If the mean distance by means of such radial disturbances as here described should be varied in an extremely small proportion, such, for example, as that of one part in a million in each revolution, such a change would become sensible, even to the most delicate instruments of observation, only after the lapse of centuries. The continual change effected on the period, and thereby on the mean motion, would, however, tell in a sensible manner on the mean place of the body in a comparatively short time.

3143. Its effect on the position of the apsides.— The effect of the radial component on the direction of the major axis of the orbit, will vary with the part of the orbit at which the disturbed body is found at the moment the disturbing force acts upon it.

3144. It diminishes or increases the angle under the radius vector and tangent, according as it is positive or negative.—It must be considered that, in general, the radial component, when +, has a tendency to diminish the angle n P s, fig. 818, formed by the direction P n of P's motion and the radius vector 8 P; and, when -, to increase it. This will be nearly self-evident on inspecting the

fig. 826. If P p represent the arc of the orbit which P is going to describe at the moment that the force R acts upon it; and if R be supposed to be +, and therefore to have a tendency to increase the energy of the force directed to c; it is evident that in the unit of time the force which previously deflected P to p, will now deflect it still more to p' or p"; so that the arc of the new orbit P p' or P p" will be more inclined to P c, that is, it will

make a less angle with it.

If, on the contrary, R be negative, it will tend to diminish the intensity of the central force, and therefore to lessen the obliquity, or increase the angle n PC under the tangent and the radius vector.

It raises or depresses the empty focus of the elliptic orbit below the axis, according to the position of the disturbed is elliptic orbit.—Let s, fig. 827, be the place of the cens' the empty focus of the instantaneous ellipse, and P, P', e disturbed body at different parts of the ellipse. It may d that, in an ellipse of small eccentricity, the radial comill produce no sensible effect on the orbital velocity of P.

'sPs', it follows that the decrease of tPs will cause a decrease twice the magnitude in the angle sPs'; and, since the direction 'sP is fixed, that of Ps' must be deflected towards Ps, so that Ps' ill change its position to Ps. But, since the major axis of the lipse is not affected by the disturbing force, and since, by the properties of the ellipse, Ps+Ps' is equal to the major axis, it follows as the disturbing force will not change the length of Ps'. To imprehend, therefore, the effect of the disturbance, we have only imagine the line Ps to turn on P, as a centre towards Ps, and to ke the position Ps. In effect, the empty focus will be transferred, the radial component, from s' to s.

Now, as the disturbed body approaches nearer to mn, the line trough s' at right angles to the major axis, the line Ps', drawn om it to the empty focus, approaches more and more to the director of the perpendicular ms'; and the point to which the empty was would be transferred by the disturbing force, is less and less smoved from the axis; and when the disturbed body is at m, that was is displaced by the disturbance to another point upon the axis

carer to perihelion p than s'.

After passing m, the disturbed body, at r', for example, being sted upon as before by a positive radial component, the effect will to deflect Ps' towards Ps'; but in this case, the angle Ps's eing obtuse, the new position s' of the empty focus will lie above le axis.

If we take the disturbed body at P', the empty focus will be ansferred to s', a point still above the axis. As the disturbed ody approaches n, the point to which the empty focus is transferred omes nearer and nearer to the axis, and lies upon it when the dis-

arbed body is at n.

Thus, it appears, that while the disturbed body moves from m, brough aphelion a to n, the point to which the empty focus would e transferred by a positive radial component would move from the xis to a certain distance above it, and would again return to the xis when the disturbed body would arrive at n.

After passing n, let us suppose the disturbed body at any point ". For the same reasons the line p" s' will be deflected from "s, and the empty focus will be transferred to s", a point below

ne axis.

Thus it appears, in general, that while the disturbed body moves rom m through a to n, the empty focus is transferred to points nore or less above the axis, and while it moves from n, through p m, it is transferred to points more or less below it.

3146. Effects of a positive radial component on the apsides. — It sevident, therefore, that a positive radial component will change be direction of the apsides, or of the major axis of the instantations education given at each point to the major

46 *

g that of the line drawn from s, through the new position pty focus, it will be evident, from what has just been exhat while the disturbed body moves from m through a to w direction of the axis s s', s s', &c., will be such, that the selion will lie below p, and the new aphelion above a nts would, therefore, be removed from their original places, tion contrary to the motion of P. The motion imparted to ld then be regressive.

the disturbed body moves from n through p to m, the new of the axis s s, s s", &c., must be such that the new peril lie above p, and the new aphelion below a. These points erefore, be removed from their original places, in the dithe motion of P. The motion imparted to them would

orogressive.

t appears, that, with a positive radial component, the axis bit, or the line of apsides, has a progressive motion while ing body passes over the arc n p m, and a regressive motion asses over the arc m a n.

Effects of a negative radial component on the position of If the radial component be negative, it is evident that

will be precisely the opposite of those here stated; that

through the arc npm, and progressive while it moves through the

3148. Diagram indicating these effects.—In fig. 828 we have indicated by the feathered arrows the direction of P's motion, and by the arrows with a cross upon their shafts the direction of the motion of the apsides when the radial component is positive. Its motion, when negative, will be indicated by supposing it to take place in directions contrary to those in which the latter arrows point.

3149. This motion of the apsides bears a very minute proportion to that of the disturbed body.—It must not, however, be supposed that these alternate progressive and regressive motions of the apsides bear any considerable proportion to P's motion; they are, on the contrary, incomparably smaller; so that, although while P moves from Q' to p, p is moving in the same direction, it is moving with so small a velocity that P arrives at p, and passes it almost as soon as if p were not moving at all: and the same observation will apply to the regressive motion.

3150. Diagram illustrating the motion of the apsides. — The successive positions assumed by the orbit subject to the disturb-

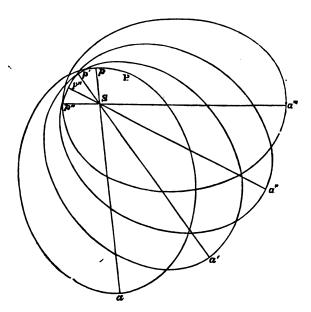


Fig. 829.

of a positive radial component, while P passes from are represented in fig. 829, where p, p', p'', p'', represuccessive positions of the point of perihelion, and t'', the successive positions of the point of aphelion. If be imagined to revolve in the other direction from to $p ext{ s} ext{ a}$, the motion will be that which it would receive disturbing action of the positive radial component while hrough the arc q a q, fig. 829.

This motion of the apsides increases as the eccentricity bit diminishes, other things being the same.—It is not o perceive that this effect of the radial component in a motion of revolution progressive or regressive to the sides is greater, ceteris paribus, when the orbit of the

body is less eccentric.

ill be evident by the mere inspection of figs. 830 and fig. 830, the orbit of the disturbed body, of which part, has but small eccentricity; and the action of the force at p deflects the body into the arc represented



by the dotted line. To find the new position of perihelion, it is only necessary to take c as a centre, p c as a radius, and to describe a circle. The middle point p' of the dotted arc of the new orbit included within this circle, will be the position of the new perihelion. If we take the case of a much more eccentric orbit, represented in fig. 831, it will be evident that the arc of the orbit included within the circle for the same degree of deflexion, will be less than in fig. 830; and consequently its middle point, which is the new perihelion, will be proportionally

nearer to p.

3152. Effect of the radial component on the eccentricity.—
By what has been explained (3145), as to the change of position of the empty focus, the effect of the radial component in all cases on the eccentricity will be easily understood. The magnitude of the major axis not being affected, the variation of the eccentricity will be proportional to that of the distance of the empty focus from s. But, since the distances of P from the two foci are not affected by the disturbing force, the distance between the foci will be increased or diminished, according as the angle sPs', fig. 827, is increased or diminished by the disturbing force. But, from what has been explained it is clear that, while P moves from perihelion p to aphelion a, the angle sPs' is diminished; and while it moves from aphelion a to perihelion p, that angle is increased by the disturbing force.

It follows, therefore, that a positive radial component will diminish the eccentricity while P moves from perihelion to aphelion, and will increase it while it moves from aphelion to perihelion; and it is evident that a negative radial component will produce

the contrary effect.

The effect produced on the eccentricity may also be understood by the following considerations: — While the revolving body P, fig. 828, passes from perihelion to aphelion, its distance Ps from the central body s continually increases; and while it passes from aphelion to perihelion, on the other hand, its distance P's from the central body continually diminishes. Now, it is evident that the more eccentric the elliptic orbit is, the more rapid will be the increase of the radius vector in the one case, and its decrease in the other. Any influence, therefore, which will have a tendency to diminish that rate of increase or decrease of the radius vector will have the effect of diminishing the eccentricity of the orbit; and, on the other hand, any influence which would have the contrary effect of augmenting this rate of increase or decrease, would have the effect of augmenting the eccentricity.

Now, it is evident that a positive radial component, having necessarily the effect of increasing the energy of the central attraction, will necessarily diminish the rate at which P departs from

ing from perihelion to aphelion, and will consequently, g to what has been just explained, have the effect of ing the eccentricity of the orbit; but the same positive omponent, continuing to act while P passes from perio aphelion, will augment the rate at which the radius ecreases, and will therefore increase the eccentricity.

FFECTS OF THE TRANSVERSAL COMPONENT OF THE DISTURBING FORCE.

It accelerates or retards the orbital motion. — In orbits small eccentricity, such as alone are here considered, the ector is never inclined to the tangent drawn in the direction action, at an angle much less or much greater than 90°, phelion to perihelion this angle is always a little less or, being least at the extremity of the minor axis; and rihelion to aphelion it is always a little greater than ang greatest at the extremity of the minor axis.

the transversal component being always at right angles adius vector, it follows that, when it is positive, it forms acute, and when negative a very obtuse angle with the motion of P, and that a negative transversal component will increase it,—an effect quite the opposite of what might be at first view expected.

3155. It produces progression of the apsides from perihelion to aphelion, and regression from aphelion to perihelion, when positive; and the contrary when negative.—The principle here announced, which is of considerable importance, may be demonstrated and illustrated in several ways.

1. It has just been shown, that a positive transversal component augments the orbital velocity, and that in the instantaneous ellipse the orbital velocity proper to each point continually increases from aphelion to perihelion, and continually decreases from perihelion to aphelion. By augmenting the velocity, therefore, the positive transversal component imparts to P in all cases a velocity proper to a point nearer to perihelion, and therefore in effect brings perihelion nearer to P than it would have been if the disturbing force did not act. It follows, therefore, that when P is moving from aphelion to perihelion, the point of perihelion, being made to approach it, will have a motion contrary to that of P, and therefore regressive; and when P is moving from perihelion to aphelion, the point of perihelion, still approaching P, must follow it, and therefore have a motion in the same direction, or progressive.

It is evident that a negative transversal component must produce the contrary effects, and would therefore impart a progressive motion to the apsides when P moves from aphelion to perihelion, and a regressive motion when it moves from perihelion to aphelion.

It will be apparent, that at the very points of perihelion and aphelion where the effects of a transversal component on the position of the axis, whether positive or negative, change from progression to regression, or vice versa, the actual effect upon the direction of the line of apsides will be nothing.

2. The same principle may be demonstrated as follows: -

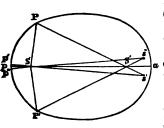


Fig. 832.

By what has been already shown (3154), a positive transversal component increases the major axis of the instantaneous ellipse. Let p Pa P', fig. 832, represent that ellipse, the body being supposed to move in the direction p P' a P.

Let s be the central body, and s' the other focus of the ellipse. By the properties of that curve we shall have

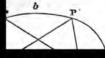
$$8P + 8'P = 2a$$
.

e velocity of P be augmented by the effect of a positive component, the major axis 2 a, and consequently s' P, ce of the empty focus of the orbit from P, must also be The disturbing force will therefore transfer that focus ch point as s' upon the continuation of the line Ps', and, y, the new direction of the major axis will be p's s' inss, and it will therefore revolve round s with a regressive

isturbed body be at P', moving from perihelion to aphelion, focus will in like manner be transferred to s", and the tion of the axis being p" s s", it will have a progressive and s.

be evident that a negative transversal component must

ne contrary effects. Its effect on the eccentricity. - It is easy to show that a



ansversal component will augment the eccentricity when the distance of P from s is less, and will diminish it when greater, than the mean distance, and that a negative transversal component will have the contrary effect.

sed by a positive transversal component between the mean and perihelion, and by a negative one between the mean and aphelion; and that it will be diminished by a positive al component between mean distance and aphelion, and by e one between mean distance and perihelion.

it appears that if a positive transversal component of the g force were to act constantly on a planet during the entire n, it would cause the eccentricity of the instantaneous ellipse ly to increase from perihelion to the end of the lesser axis, would attain its major limit. From that point it would until the planet arrives at aphelion, where it would attain limit. From that it would again increase until the planet me to the other extremity of the minor axis, where it would tain its major limit, after which it would again decrease planet would arrive at perihelion, where it would attain minor limit.

been erroneously stated, in some astronomical works, that is at which the eccentricity would attain its major limit by e, would be the extremities of a perpendicular to the major ing through the empty focus of the orbit.*

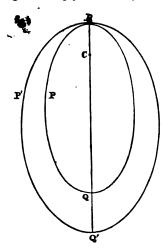
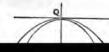


Fig. 834.

Its effects on the major axis at the apsides. — Let p P Q, i, be the undisturbed orbit, p being perihelion and Q. Now, if we suppose the revolving body at perihelion p

receive the action of the positive transversal componention increasing its velocity will throw it into an arc such ich would include p P within it, and the revolving body equently move in the orbit p P'Q' instead of the orbit which it would have revolved had it been undisturbed. I herefore, which would result from the perturbing actic ositive transversal force at P, would be one in which the psides would have the same direction, but in which the phelion Q' would be more remote from c than the point of of the undisturbed orbit. The effect therefore is, that hanging the direction of the line of apsides, the transversal augmented by the disturbing force.

Let us now consider the effect of a positive transversal certing upon the revolving body at aphelion. Let Q, fig he aphelion, and p the perihelion, of the undisturbed of evolving round the central body c. A positive transverse



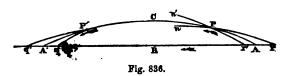
body c. A positive transversacting at Q, accelerating the v before, will cause the body to an orbit Q r'p' having the sec for its remote focus, and the undisturbed orbit within

III. — EFFECTS OF THE ORTHOGONAL COMPONENT OF THE DISTURBING FORCE.

3158. It changes the plane of the orbit—plane of reference.—It has been already explained, that the effect of this component is to produce a change in the position of the plane of P's orbit. In order, therefore, to express such change of position, it is necessary that some fixed plane be selected with relation to which the position of the plane of P's orbit may be expressed. Such a plane may be chosen arbitrarily, and we shall denominate it generally the plane of reference.

The position of the plane of P's orbit then will depend on its line of intersection, and its inclination to the plane of reference.

8159. Nodes of disturbed orbit on plane of reference.—Let ABA' and ACA', fig. 836, represent respectively the plane of reference and that of P's orbit, seen in the same manner as we are accustomed to view the equator and ecliptic; A being the



ascending node corresponding to the vernal equinoctial point, and A' the descending node corresponding to the autumnal equinoctial point, and c being that point of the semicircle which corresponds to the solstitial point, and which is, therefore, the point most remote from the plane of reference. We shall call A C the first quadrant, counting from the ascending node; C A' the second quadrant; and the corresponding quadrants of the other half of the orbit the third and fourth quadrants.

3160. Effect of orthogonal component varies with distance from node.—Now let us suppose the body subject to perturbation to be at some point such as P in the first quadrant, and to receive there the action of a positive orthogonal component, the direction of P's motion being indicated by the arrow. Since this positive component has a tendency to draw P towards the plane of reference, it is evident that the motion which P will receive, by its action, must cause it to proceed in a direction between PC and a line drawn from P perpendicular to the plane of reference, that is, in such a direction as Pn inclined to PC and below it.

If the body subject to perturbation be in the second quadrant, as at r', it will for a like reason, after the disturbing action,

direction Pq, slightly inclined to P'A' and below it. thogonal component be negative, it will be apparent the body would, a er the action of the disturbing force, that direct a Pn, slightly inclined to Pc and above like manner, at P' it would move in the direction 'y inclined to P' A' and a little above it.

of these disturbances will change both the nodes and

s progress or regress according as the component or positive. - If n P be continued backwards, it will the plane of reference at a point r beyond its former It is evident, therefore, that in this case the ascendwould regress upon the plane of reference. If the arc like manner continued to meet the plane of reference point q will be in like manner behind A'. Thus the ion of the descending node will be behind its former nd, consequently, in this case also the node regresses. ars, therefore, that wherever, in the semi-circle ACA', a thogonal component acts, its effect will be to impart to the ressive motion. ne reasoning will equally apply to the cases in which P is

d and fourth anadrant . and therefore generally it may be

ponent decreases the obliquity when the disturbed body is in the first and third quadrants, and increases it when in the second of fourth; and that a negative orthogonal commonent is attended with the opposite effects.

1V. GENERAL SUMMARY OF THE EFFECTS OF A DISTURBIAND AND A STANDARD OF the effects of the several the many of the disturbing force.—

	_		_		_	_	_	_				_	_	- 1	_	
Flace of disturbed Body.	Radial.						Transversal.						Orthogonal.			
	+			3-5			+			1.2			+		-	
			π		•	π	a		π			π	v	•	*	1
At Perihelion	:	0	+	:	0	+	‡	+	0	Ξ	7	0	×	:	:	1
		-			+		+		+	-		-		0		1
		+	٠,		-		÷		-	-		+		,		
			-			+	٠			10						1
			+		8	-			÷	9				Ġ.		1
			0			0		0								
								+			-					١.
				÷	4	è		-			+	¥			٠	
Distance of disturbed body from ascend- ing node: 0° and Between 0° and							1							0	+	
90°								Ш	Į,				Ξ	<u>-</u>	‡	-
180° 180° Between 180°									V				Ξ	+	‡	-
and 2700- 2700- Between 2700													-	0	+	-
and 00								Μ,					\simeq	+	+	-

It will be convenient, then, to collect and arrange in juxtaposition, for the purpose of reference, the various effects produced by the three components of the disturbing force, as explained in the preceding paragraphs. We have accordingly done this in the above tabular statement. The sense in which the symbols + and — are applied to each of the components has been already explained. As applied to the semi-axis a, the eccentricity e, and the inclination I, + is used here to signify increase, and — diminution, and 0 the positions in which they are not affected by the disturbing force.

ASTRONOMY . .

to the motions of the perihelion (**) and the node (*); + progressive and — regressive motion. The sign 0 is pre there is no motion imparted to these points by the force.

CHAP. XX.

PROBLEM OF THREE BODIES.

Attraction independent of the mass of the attracted body. in clear and distinct ideas of the effects of the disturbing masses brought into proximity with bodies moving in ora centre of attraction, it is most necessary, in the first o comprehend clearly the law and conditions which deterattractions.

traction exerted by one body upon another depends solely mass of the attracting body, and its distance from the atdy, and is altogether independent of the mass of the latter, nore necessary to indicate this, inasmuch as students are an inch in one second of time. Now, if the mass of the earth were 10 or 100 times greater or less than it is, the sun's attraction exerted at the same distance would produce precisely the same effect

upon it.

3165. Hence the denomination "accelerating force."—This species of force, the effect of which is exclusively a certain velocity imparted to the body affected, is distinguished in physics from that other sort of force which varies in its effects with the mass of the body moved, by the term accelerating force; while the force which varies in its effect with the mass of the body moved, is called moving force, or momentum.

3166. Accelerating force of gravitation.—The accelerating force of gravitation is therefore measured by and proportional to the space through which a body is drawn in the unit of time by the attraction

of a given mass at a given distance.

Let the unit of accelerating force be the space through which a body would be drawn in the unit of time by the unit of mass placed at the unit of distance from it. The accelerating force exerted at the unit of distance by any other mass M, will therefore be expressed by the number of units in M; and since the attraction decreases in the same proportion as the square of the distance increases, the accelerating force exerted by M at the distance D being expressed by A, we shall have

$$A=\frac{M}{D^2},$$

-a formula, which, properly understood, expresses the law of

gravitation in its highest generality.

3167. Problem of two bodies. — When a lesser body P revolves in an elliptic orbit round a greater mass s, the place of s being the focus of the ellipse, it has been hitherto assumed that s is fixed, and not at all affected by P's attraction, the only attraction assumed hypothetically to be in operation being that of s upon P. Now if D be the distance between them, and A the space through which P would be drawn by s in the unit of time, we should have, according to what has been just explained,

$$\mathbf{A} = \frac{\mathbf{g}}{\mathbf{p}^2}.$$

But, by the universal reciprocity of the principle of gravitation, P acts upon s as well as s upon P; and if the accelerating force of P on s be expressed by A', we shall have

$$A' = \frac{P}{D^2}.$$

It remains, therefore, to consider in what manner this effect of P's

will modify the conclusions at which we have arrived supposition that the attraction alone of s was in operation. In that by P's attraction s is drawn towards P, while by ion P is drawn towards s.

one were supposed to act, the distance D would in the unit e decreased, supposing the bodies free to move towards , by the space A. But now that the action of P is admitistance D between P and s will be diminished by the sum ces through which s and P may be respectively moved in of time, each by the attraction of the other; so that we we the actual force of mutual attraction between the two

$$A + A' = \frac{S + P}{D^2}.$$

ars, therefore, that the mutual attraction of the two bodies than when s alone acted in the proportion of s to s + P; equently, that the relative motion of P round s will be the same as if the mass of s were increased by the addiof the mass of P and P were deprived of its reciprocal investigation of the effects of such a combination has acquired great celebrity in the history of science, from the difficulties which it presented, and the importance of the results which followed its solution. This question is generally denominated the PROBLEM OF THREE BODIES.

The three bodies involved in the problem are, 1st, the central body s; 2ndly, the revolving body P, which, if undisturbed, would describe an elliptic orbit round s as a focus; 3rdly, the disturbing

body M.

3169. Simplified by the comparative feebleness of the forces exerted by the third body. — In all the cases presented in the great phenomena of the universe, the mass of s is incomparably greater than that of P, and the attraction exerted by M is incomparably more feeble than the central attraction of s on P, either because of the comparative smallness of M's mass, or because of its great distance from the attracted body, or from both these causes combined.

3170. Attracting force of third body not wholly disturbing.— But whatever be the force exerted by M, it is most necessary to bear in mind two things respecting it: 1st, that its attraction does not necessarily produce a disturbing action at all upon P's orbit; and 2ndly, that when it does, the disturbing action is not identical with M's attraction upon P, either in intensity or direction. It is never equal to it in intensity, and very rarely identical with it in direction, often having a direction immediately opposed to that of M's attraction.

3171. Attracting force which would produce no disturbing effect.

— Such a force must be one which would cause s and P to be moved in parallel lines in the same direction through equal spaces in the same time. It is quite evident that such a force, while it would transport s and P with this common motion in a common direction, could not in the least degree derange their relative position or motion. If P, previously to the action of such a force, revolved round s, for example, in a circle with a uniform velocity, it would continue to revolve round it in the same circle with the same velocity when subject to the force here supposed; for the effect would be merely that the two bodies with their circular orbit would be transported in space as bodies would be which might be supposed to have any motion upon the deck of a ship in full sail.

8172. This would be the case if the third body were enormously distant compared with the second.—But in order to impart such a force to s and P, the body M must be at such a distance from them that the distance between S and P should subtend at M a visual angle so small as to be insensible; since otherwise the lines of M's attraction, being sensibly convergent, would not be parallel. If the distance, however, of M be enormously great compared with the dis-

between s and P, then the direction of M's attraction be sensibly parallel; and for the same reason, the intensity of M's attraction will be likewise incomit varies inversely as the square of the distance, an apposition, the distance of P from s is quite insigning with the distance of M from either of them.

73. Example of a force supposed to act on the soins, if we suppose that the solar system is subject on of some mass or collection of masses among the listance so prodigious that, compared with it, the wl of the system would shrink into a point, such an I have the character here described, and the wn would be moved by it with a common motion tion, all the bodies composing it describing parallel ame velocity, and consequently preserving, so far sed by this common motion, their relative positions.

74. Case in which the distance of third body is not great.—Let us now, however, suppose that the t placed at such a distance from P and s that it acts and in different directions, but with forces of different consequently imparts to them motions where the suppose of the property of the suppose of the supp

which now acts upon P, parallel to SM, and opposite to Pm, would impel P through a space parallel to s M in the unit of time, exactly equal to that through which M's attraction upon 8 impels 8. two forces, therefore, would carry P and s in parallel directions through equal spaces in the unit of time, and would therefore produce no disturbing effect (3170). All the disturbance, therefore, which can be produced upon P by the forces in operation must arise from the combined action of the two forces acting upon P: 1st M's attraction in the direction PM; and 2ndly, a force equal and contrary to M's attraction on s, acting in the direction Pm parallel to If, therefore, we take the line P m in the same proportion to PM as the attraction of M upon 8 has to the attraction of M upon P. and complete the parallelogram PmxM, the diagonal Px will express, in intensity and direction, the resultant of the forces expressed by the sides Pm and PM; in other words, the diagonal Px will express in quantity and direction the resultant of the only two forces which can produce a disturbing effect upon P. Since M's attraction on s, represented by M x, is to M's attraction on P, represented by MP, as the square of MP is to the square of Ms, it follows that

$$SM^{2}:PM^{2}::PM:Mx;$$

or, if we use the symbols already indicated, we shall have

$$r'^{2}:z^{2}::z:Mx;$$

and consequently

$$M x = \frac{z^3}{z^2} \dots (1.)$$

We shall obtain an expression for sx, the distance of the point x from the central body s, by subtracting mx from sm; consequently,

8
$$x = r' - \frac{z^3}{r'^2} = \frac{r'^3 - z^3}{r'^2}$$

But since

$$r'^3 - z^3 = (r' - z) \times (r'^2 + r'z + z^3),$$

we shall have

$$s x = (r'-z) \times \left(1 + \frac{z}{r'} + \frac{z}{r'^2}\right) \dots (2.)$$

By either of these formulæ (1) or (2), the direction of the disturbing force can always be determined. It is only necessary to take, upon the line joining the disturbing and central bodies, a space Mx or Sx, determined by one or the other formulæ (1) or (2).

8175. To determine the ratio of the disturbing to the central force. — For this purpose let

A = M's attraction on P. A' = M's attraction on S.

A"= s's attraction on M.

D =the disturbing force Px.

F = s's attraction on P.

ll then, according to what has been explained above,

$$= \frac{P x}{M x} = P x \times \frac{r'^2}{z^3}, \qquad \frac{A'}{A''} = \frac{M}{8}, \qquad \frac{A''}{F} = \frac{r^2}{r'^2}$$

iplying all these together we shall obtain

$$\frac{D}{P} = \frac{M}{S} \times \frac{r^2}{z^3} \times Px....(3.)$$

formula the ratio of the disturbing force D to the central F can always be calculated when the masses of the disturbed central bodies, and their distances from each other and bed body, are known; for in such cases the line Px can ted by the common principles of trigonometry; and con-

D., or the ratio of the disturbing to the central attraction,

therefore consider, in the first instance, the effects only of that component of the disturbing force which is in the plane of the disturbed orbit, and afterwards that of the orthogonal component.

3177. FIRST CASE. The component of the disturbing force in the plane of the orbit when the disturbing body is outside the orbit of the disturbed body. — Let s, fig. 838, be the central

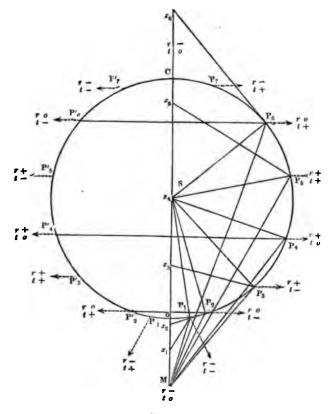


Fig. 838.

and m the disturbing body; and let P1, P2, P3, &c. be the disturbed body in a succession of its synodic positions.

It is evident from the formulæ (1) and (2), that as P moves from o, taking successively the synodic positions P₁, P₂, Sc., 111.

erefore M x, constantly increases; and consequently the ere the direction of the disturbing force meets the line antly approaches s. The angle s P, x1, obtuse at first, less and less so at P, and P2, until at a certain point reduced to 90°. There the direction P₂ x₂ of the discree is therefore that of the tangent to P's orbit; and on being opposed to P's motion, it is negative. passing this point P2, the angle formed by the disturbwith the direction PM becomes less than 90°. When nce PM becomes equal to SM, as at Po, the direction turbing force, according to what has been shown (3176), ough s, and accordingly x, coincides with s. P passes this position, the direction of the disturbing ses above s as at P, x, the angle MP x increasing. At point P6 this angle again becomes 90°; and the direcof the disturbing force being at right angles to sp, tangential. The point x continues to recede from s

rives at c.

P passes from c to o through the other half of its revolution, the direction of the disturbing force underchanges, but in a contrary order, being tangential at

and at P. constitutes the whole disturbing force, being then directed to s.

After passing P4, as for example at P5, the tangential component changes its sign, and becomes positive, so that both components of the disturbing force are positive, the radial component now decreasing.

When P arrives at P6, the radial component vanishes, the whole

disturbing force becoming tangential.

After passing P_6 the radial component again changes its sign, and becomes negative, as at P_7 , and increases continually to c, the positive tangential component at the same time continually decreasing, and becoming = 0 at c. At this point c, therefore, the disturbing force is wholly radial, and is negative, being therefore in antagonism not only with the central attraction of s, but with the immediate attraction of M, which is its cause.

It may be naturally asked, how it can happen that the attracting force of M produces a disturbing force in immediate opposition to its own direction? This, however, is easily explained. M's attraction on s being $\frac{M}{r'P}$ and M's attraction on P at C being $\frac{M}{(r'+r)^2}$, the former being greater than the latter, we shall have the disturbing force

$$D = \frac{M}{(r+r')^2} - \frac{M}{r^2},$$

which is negative: in fact, s is attracted towards M with a greater accelerating force than P, and, consequently, s and P are caused to separate from each other by a space equal to the difference of the two attractions, which is equivalent to a repulsion acting from s upon P, or, what is the same, a negative disturbing force.

The tangential component vanishing at C changes its sign; the radial component, however, continuing negative. From C to P₆', for example at P₇', therefore, both components are negative, and the radial component gradually diminishes until P arrives at P₆', when it vanishes, the whole disturbing action being a negative tangential

After passing P₆, as for example at P₅, the radial component changing its sign becomes positive, the tangential component continuing negative and decreasing gradually until it vanishes when P arrives at P₄, at which point the whole disturbing action is a positive radial force.

After passing P_4 , as for example at P_3 , the tangential component again changes its sign and becomes positive; both components are, therefore, positive to P_2 , where the radial component becomes nothing, and the whole disturbing action consists of a positive tangential force.

passing P2', as for example at P1', the radial component ages its sign and becomes negative; the tangential compoinuing, however, positive, until P arriving at o completes ion.

Diagram illustrating these changes of directions.—In m we have indicated in an obvious way these successive the directions of the components of the disturbing force, component being expressed by r, and the tangential by t, quality or value being expressed by the symbols +, -, h follow them. The diagram, though appearing at first licated, is really simple and easily understood; and the indiven will be found by the student to be extremely conveuseful.



3180. SECOND CASE, in which the disturbing body is within the disturbed orbit.—Let us now suppose that M is within P's orbit, as in fig. 839, and that its distance from the central body S is greater than half the radius of P's orbit. Taking, as before, the disturbed body P in a succession of positions P₁, P₂, P₃, P₄, &c., the direction of the disturbing forces P₁ x₁, P₂ x₂, P₃ x₃, &c., &c., is found in the same manner exactly as before.

Now it will be easy to perceive, by following the lines upon the diagram, how the direction of the disturbing force varies with relation to M and S. At a point such as P_1 it falls at x_1 , between M and S; at P_2 , where M P_3 = M S, it is directed to S, as has been already proved. At this point, therefore, the disturbing force is wholly radial. When P has advanced to the position P_4 , at which the direction of the disturbing force is at right angles to the radius vector S P_4 , it is wholly tangential, the radial force vanishing.

At c, where M's attraction is at right angles to the tangent, the tangential force vanishing, the disturbing force is wholly radial. In the semicircle described by P in passing from C to O, there are two points, P₄ and P₂, corresponding to the points P₄ and P₈, at the former of which the radial, and the latter the tangential, component vanishes.

3181. Changes of sign of the components in this case. — It will now be easy to trace the successive changes of direction of each of the components of the disturbing force to which P is subject in the successive positions which it assumes throughout its synodic period.

At o, M's attraction upon P is $\frac{M}{(r-r')^2}$, and M's attraction on S is

 $\frac{M}{r^2}$; and since both these attractions are directed towards M, the relative effect upon P and s will be their sum; and therefore P and s will be attracted towards each other by a disturbing force, the value of which will be,

$$D = \frac{M}{(r-r')^2} + \frac{M}{r'^2} = M \times \left(\frac{1}{(r-r')^2} + \frac{1}{r'^2}\right).$$

In this case it is obvious that the disturbing force will be wholly radial and positive, the tangential force being nothing, inasmuch as the direction of the disturbing force is at right angles to the tangent. When the body leaving 0 moves towards P₂, the radial force, being still positive, gradually decreases, and the tangential force being inclined below the radius, will act against P's motion, and therefore be negative. As P moves forward, the negative tangential force gradually decreases; and when P arrives at P₃, where its distance from M is equal to that of s from M₃, the disturbing force being wholly radial, the tangential force vanishes. After passing this

for example at P3, the tangential force, changing its sign. positive as well as the radial force, and both forces continue sitive, the radial force gradually decreasing until the body at P4, where the radial force vanishes, the disturbing force he direction of the tangent, and being still positive.

passing this point, the radial force, changing its sign, negative as at P5, the tangential force still being positive, lually decreasing. This latter vanishes when P arrives at C, he whole disturbing force is radial and negative. After this point, the negative radial force gradually diminishes, tangential component, changing its direction as at Pi, beike the radial component, negative. On arriving at P4, the omponent having gradually decreased, vanishes, the whole ng force being tangential and negative.

ng this point, the radial component changing its sign becomes as at P3', the tangential component being still negative. On at P2, the tangential component having gradually decreased, , and the whole disturbing force is radial and positive. ssing this point, as for example at Pi, the tangential comas well as the radial component, is positive; and, in fine, e body returns to o, the tangential component vanishes, and

collect here, and arrange in juxtaposition, the several changes of direction which the components of the disturbing force in the plane of the disturbed orbit undergo during a synodic period of P. This is done in the following table, the signs retaining the significations already given to them:—

Disturbing Body outside the Orbit of the disturbed Body. r' greater than r.			Disturbing Body within the Orbit of the disturbed Body.					
			r' less than r, but greater than 16 r.			r' not greater than 1/4 r.		
Place of P.	R	T	Place of P.	R	T	Place of P.	R	T
At 0 From 0 to P2 At P2 From P2 to P4 At P4 From P2 to P6 At P6 From P4 to C At C From C to P6 At P6 From P6 to P6 At P7 From P6 to P6 At P7 From P6 to P7 At P7	0+++0 0+++0	0 0+++0 0++	At 0 From 0 to P2 At P2 From P2 to P4 At P4 From P4 to C At C From C to P4 At P4 From P4 to C At P4 From P4 to P4 From P4 to P4 From P4 to P4 From P4 to P4	++++0 0+++	0 0 ++++0 0 +	At 0 From 0 to P4 At P4 From P4 to 0 At C From C to P4 At P4 From P4 to 0	+0 0+	0+++0

3183. Varying effects of the orthogonal component during a synodic revolution.—If a triangle be imagined to be formed by lines drawn joining the places of the central body s, the disturbed body P, and the disturbing body M, the plane of this triangle will in general be inclined at some angle to the plane of P's orbit. The direction of the disturbing force, according to what has been shown, will be that of a line drawn from P in the plane of this triangle, meeting the line M s either between M and s, at s, or beyond s, according to the relative magnitude of M s and M P. If M P be less than M s, then the direction of the disturbing force will meet M s between M and s; if M P = M s, its direction will be that of the line P s; and, in fine, if M P be greater than M s, its direction will meet the prolongation of M s beyond s.

On considering these various directions of the disturbing force, it will be evident that when MP is less than MS its direction will lie on the same side of the plane of P's orbit with the disturbing body M, and the orthogonal component being therefore directed towards that side, will have a tendency to bring the plane of the disturbed

orbit nearer to M.

When MP is greater than MS, on the contrary, the direction of the disturbing force meeting the prolongation of the line MS beyond a, must lie on the side of the plane of P's orbit, different from that at which M is ed; and the orthogonal component being in that case directed ... ie same side, would have a tendency to deflect the plane of P's orbit from M.

In the former case, the orthogonal component would decrease, and in the latter it would increase the angle at which the line

M s is inclined to the plane of P's orbit.

When MP = Ms, the disturbing force, being directed from P to s, would act in the plane of P's orbit, and would conse-

quently have no effect in changing that plane.

If M be situate any plane of P's orbit, which will be the case whenever it passes through the nodes of its own and P's orbit, the three bodies being in the same plane, the orthogonal component of the disturbing force will be nothing.

Thus it appears that the orthogonal component will vanish at each passage of M through P's nodes; and also at each of the points, if any such there be, at which M and P are equally dis-

tant from s.

3184. Periodic and secular perturbations. — From what he been explained in the present and the preceding chapter, it appears that the several components of the disturbing force produce contrary effects on the elements of the disturbed orbit when they have contrary signs, and that they are severally subject to a succession of changes of sign during the synodic revolution of the disturbed and the disturbing bodies. The several elements of the disturbed orbit will therefore be in a continual state of oscillation, from these alternate actions of the components of the disturbing force in one direction and the other.

If, in all cases, the sum of the effects produced by the action of each component while positive were equal to the sum of its effects while negative, the elements would oscillate round a fixed and invariable state. They would pass through all their variations when the disturbed and disturbing bodies would have assumed all their possible varieties of position with relation to the central body, and they would then recommence the same some

cession of changes.

The mean values of all the elements of the disturbed orbit would in this case be constant. Thus the major axis would alternately increase and decrease between fixed limits, but is mean value would be always the same. In like manner, to eccentricity and inclination would alternately increase and decrease having a constant mean value; and the like would be true of the other elements.

But if, on the contrary, it were found, on comparing the soft the positive with the sum of the negative effects of the components, that the sum of all the effects while pere not exactly equal to the sum of the effects while are

but that a certain minute difference or residual phenomenon always remains uneffaced, it is evident that this residuum, however small it may be, must accumulate until at length it will ttain a magnitude which will tell in a very sensible manner, nd, if a still longer series of periods be waited for, would totally

hange the elements of the disturbed orbit.

It must be observed that the interval which leaves this resiuum uncompensated, is one during which the disturbed and isturbing bodies pass through all possible varieties of configuation, taking into the account not merely their directions with elation to the central body, but their positions with relation to the apsides of their respective orbits. It is only after assuming Il the varieties of relative position and distance, arising as well com the relative changes of direction of M and P as viewed rom s, as from their changes of position in their respective ribits with relation to their points of perihelion and aphelion, hat the components of the disturbing force complete their round of effects, and recommence another series of actions. It is the esidual phenomena which remain uneffaced after this interval, which, accumulating for a long succession of ages, produce the litimate changes of the elements now referred to.

It appears, therefore, that there are two extremely different classes of INEQUALITIES as they are called, which arise from

he operation of the disturbing force.

lat. Those which vary with and depend on the configuration of the disturbed and disturbing bodies with relation to the central body, taking into the account not only their relative directions as seen from the central body, and their varying distance from each other, but also their varying distances from the central body, owing to the elliptic form of their orbits.

These inequalities necessarily pass through all their phases, somplete their periods, and recommence the same succession of thanges, when the disturbed and disturbing bodies have passed through all their possible varieties of configuration; and, consequently, their several periods must be less than the interval within which this succession of configurations is completed.

These are denominated PERIODIC INEQUALITIES.

2nd. Those which arise from the accumulation of the residual phenomena already mentioned, as being in some cases unextinguished by the opposite effects of the positive and negative composents of the disturbing force, acting during that interval of time within which the bodies assume all their possible varieties of configuration. It will appear hereafter that these residual phenomena are generally of very small value,—so small as to be rarely sensible to observation until they have been allowed to accumulate for a long uncoession of periods.

It is, therefore, evident that these latter inequalities are incomparably slower in their progressive development than the former, and consequently the intervals of time within which they complete their changes are proportionally more protracted. These have, accordingly, been denominated SECULAR INEQUALITIES.

It must not, however, be imagined that these are less really periodic than the former. The only difference in that respect between the two classes of phenomena is in the length of their periods. Where those of the former may be expressed by years, those of the

latter will be expressed by centuries.

CHAP. XXI.

LUNAR THEORY.

3185. Lunar theory an important case of the problem of three bodies.—The most remarkable example, and in many respects the most interesting, of the application of the principles explained in the last chapter for the solution of the problem of three bodies, is unquestionably that which is presented by the lunar theory, in which the central body s is the earth, the disturbed body P the moon, and the disturbing body M the sun.

This application of the theory of perturbation is interesting, not so much because of the physical importance of the moon, as because, by the proximity of that body, perturbations produced upon it become conspicuously observable, which in any other body of the solar system would be inappreciable by reason of its remote-

ness.

The lunar perturbations, moreover, present another feature of interest, as compared with those of the planets, by reason of the comparative shortness of their cycles,—phenomena, which, in the case of the planets, require a succession of ages to complete the periods, passing, in the case of the moon, through all their plass, and returning upon themselves, in the course of a few years.

3186. It supplies striking proof of the truth of the theory of gravitation.— But transcendantly the most interesting and important circumstance attending the lunar theory is, the remarkable of dence it has afforded in support of the theory of gravitation. In perturbations of the lunar motions being, for the most part, of considerable magnitude, and recurring after short intervals,

siderable magnitude, and recurring after short intervals, observed, and the laws of many of them ascertaine epoch in the progress of astronomical

discovery of gravitation had disclose of these phenomena were explained

some perfectly, others imperfectly; and those which remained ained or imperfectly explained by him have since been fully tisfactorily accounted for, upon the principles which form the tion of his physical theory.

7. The sun alone sensibly disturbs the moon.—The only body system, which produces a sensible disturbing effect upon the is the sun; for although several of the planets when in oppoor inferior conjunction, come within less distances of the their masses are too inconsiderable to produce any sensible sing effect upon the moon's motion. The mass of the sun, contrary is comparatively so prodigious that, although the of the moon's orbit bears so small a ratio to the sun's disand although lines drawn from the sun to any part of that may be regarded as sensibly parallel, the difference between rees exerted by the sun upon the moon and earth, so far from insensible, produces on the contrary those perturbations which

it is our purpose in the present

chapter to explain.

3188. Lines of syzygy and quadrature. — Let s, fig. 840, represent the place of the earth; P₁, P₂, P₃, &c., representing successive positions of the moon in its orbit, which, for the present, we shall consider to be circular. Let Co be that diameter of the lunar orbit which is directed to the sun, C being the point of conjunction, and o the point of opposition. Let P₄ s P'₄ be drawn through s at P'₄ right angles to 0 C; the points P₄ P'₄ will then be the points of quadrature.

The line O C is called the LINE OF SYZYGIES; and the line P₄ P'₄ the LINE OF QUADRATURES.

We shall, for the present, consider only that component of the sun's disturbing force which is in the plane of the moon's orbit; and shall, therefore, speak of the sun as if it were placed in the prolongatio of the line s c.

The moon being supposed to move synodically in the direction CP_1P_2 , &c., we shall distinguish

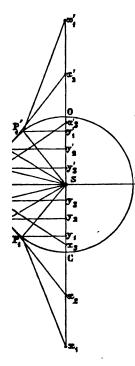


Fig. 840.

e first quadrant, P. o as the second, o P', as the third, and e fourth quadrant of the synodic revolution.

Direction of the disturbing force of the sun. — If we supmoon at any point, such as P_1 in the first quadrant, and w P_1 y_1 at right angles to s c, the direction of the sun's force acting at P_1 will be found by taking s x_1 , = 3 s y_1 , ng P_1 x_1 , which will then be the direction of the disturbing

ve this, we have to observe that P_1 and y'_1 may be consequally distant from the sun. Let their common distance sed by z, and let the sun's distance from s be expressed the moon's distance by r.

all then by the formula [2] (3174) have

$$sx_i = sy_i \times (1 + \frac{z}{r^2} + \frac{z^2}{r^{2i}}).$$

nce the moon's distance bears an insignificant proportion the sun, being only a 400th part of it, we may consider a consequently $\frac{z}{r'}=1$, and therefore we shall have

takes successively the positions P'_3 , P'_3 , P'_1 , &c., the disturbing force takes successively the directions P'_3 , P'_3 , P'_3 , P'_1 , P'_1 , &c.

Without pursuing these considerations further, it will be evident that, in moving through the first quadrant, the direction of the disturbing force intersects the line of syzygies below s; and in moving through the second quadrant, intersects it above s; and the same reasoning will show that, in moving through the fourth quadrant, the disturbing force intersects the line of syzygies below s in the same manner as in the first quadrant; and in moving through the third quadrant, it intersects it above s in the same manner as in the second quadrant; and it is further evident, that at corresponding points in the third and fourth quadrants the direction of the disturbing force intersects the line of syzygies at the same points as in the second and first quadrants.

3190. Points where the disturbing force is wholly radial and wholly tangential. — From what has been explained it appears, that the disturbing force at quadratures being directed to the

earth, is wholly radial and positive.

It is easy to show that at syzygies it is also wholly radial, but negative; for at this place the sun's attraction is obviously at right angles to the tangents of the moon's orbit at c and o, and as the whole attraction is thus perpendicular to the tangent, and the disturbing force is equal to the difference of the attracting force exerted by the sun upon the moon and upon the earth, it is clear that disturbing force is also perpendicular to the tangent, and therefore radial, since the moon's orbit is here assumed to be sensibly circular.

To determine the points at which the disturbing force of the sun assumes the direction of a tangent to the moon's orbit, let \mathbf{P}_1 be that point in the first quadrant. We shall then have the sagle $\mathbf{S} \mathbf{P}_2 \mathbf{x}_2 = 90^\circ$, and consequently

$$sy_2: P_2y_2:: P_2y_2: y_2x_2;$$

and consequently,

$$\frac{\mathbf{P}_{\mathbf{s}} \mathbf{y}_{\mathbf{s}}}{\mathbf{s} \mathbf{y}_{\mathbf{s}}} = \sqrt{\frac{\mathbf{y}_{\mathbf{s}} \mathbf{x}_{\mathbf{s}}}{\mathbf{s} \mathbf{y}_{\mathbf{s}}}} = \sqrt{2}.$$

$$\frac{P_2 y_3}{8 y_3} = \tan P_3 8 C = \sqrt{2}$$

And it appears by the trigonometrical tables that the angle whose tangent is $\sqrt{2}$ is 54° 44′ 7″.

Thus it follows that the synodic position of the moon in the first quadrant at which the disturbing force is wholly tangential,

the direction $P_1 x_2$ against the moon's motion, is at the 54° 44′ 7" from conjunction.*
follow in the same manner, that the disturbing force cond quadrant will be wholly tangential at a point P', stance from opposition o is 54° 44′ 7"; and in like t will be tangential at points in the third and first

which are at like distances from opposition and con-

t appears that in the synodic orbit of the moon there coints, viz., opposition, conjunction, and quadratures, at sun's disturbing force is wholly radial, being directed earth, and therefore negative at opposition and conand directed towards it, and therefore positive at quadand four other points at distances of 54° 44′ 7″ on e of opposition and conjunction, at which it is wholly, being in the direction of the moon's motion and therefore in the second and fourth quadrants, and contrary oon's motion and therefore negative in the first and trants.

Intensities of the disturbing forces at syzygies and

$$D = \frac{8}{r^3} \times \frac{r}{r'} = 8 \times \frac{r}{r'^3} = 8 \times \frac{1}{400^3}$$

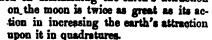
and, consequently,

$$D = 0.0000000156 \times s.$$

It appears from these values of D', D", and D, that the three radial disturbing forces exerted by the sun upon the moon at conjuction, opposition, and quadrature, are in the following proportion,

Thus it appears that the disturbing force at conjunction is greater than at opposition in the proportion of 63 to 62, and that the negative disturbing force at syzygies is about double the positive disturbing force at quadratures.

In other words, it appears that the disturbing force of the sun acts against the moon's attraction upon the earth at conjunction more energetically than at opposition, in the proportion of 68 to 62; and that, in both cases, its action in diminishing the earth's attraction



8192. The sun's disturbing force at equal angles with energy varies in the direct ratio of the moon's distance from the earth.—It is easy to show that if the moon's distance from the earth be supposed to vary, while the sun's distance remains the same, and still bears a high ratio to the moon's distance, the san's disturbing force will vary in the direct ratio of the moon's distance at equal angular distances from syzygy.

Let P and P', fig. 841, represent the moon at two different distances, s.P., and s.P', from the earth. To find the lines representing the disturbing force at P and P' draw Py and P' y' at right angles to the line drawn from s to the sun, and let sx = 3 sy, and sx' = 3 sy', and draw the lines Px and P'x'. These two lines will then represent in quantity and direction the disturbing forces of the

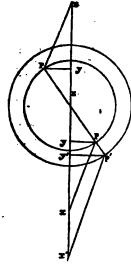


Fig. 841.

sun upon the moon at P and P'.

But it is evident, since sx is three times sy, and sx' is three times sy', that the lines Px and P'x' are parallel, and are therefore proportional to sP and sy'; that is, the disturbing forces at P and

portional to the distances of the moon from the earth at points.

be seen hereafter that this principle is attended with some

consequences in the lunar theory.

Analysis of the variations of sign of the components sturbing force during a synodic period. — From what has ained in the preceding paragraphs, it will be easy to trace ssive changes of direction and sign of the radial and tanomponents of the disturbing force of the sun, during an ation or synodic period of the moon.

fig. 842, represent the position of the moon in conjunction; ition in opposition; P_{21} its position in western, and P_{11} in

uadrature.



From what has been already explained it appears that, the disturbing force at c being at right angles to the tangent, the tangential component is nothing; and since, through the first quadrant c Ps, the direction of the disturbing force forms an obtuse angle with the direction of the moon's motion, its tangential component will be in a direction contrary to the moon's motion, and it will therefore be negative. This component vanishes at P2, where the whole disturbing force becomes radial, and therefore at right angles to the tangent, and after passing P2, the direction of the disturbing force forming an acute angle with the direction of the moon's motion, the tangential component is in the direction of the moon's motion, and therefore positive; and continues to be positive throughout the second quadrant until the moon arrives at opposition o, where the disturbing force again becomes radial, and being at right angles to the tangent, the tangential component vanishes. After passing o, the disturbing force forms an obtuse angle with the direction of the moon's motion, and its tangential component is therefore contrary in direction to the motion of the moon, and consequently negative.

It continues negative through the third quadrant until, the moon arriving at P₂, the direction of the disturbing force becomes radial and at right angles to the tangent, and the tangential component again vanishes. After passing this point the disturbing force forms an acute angle with the direction of the moon's motion, and its tangential component therefore being in the direction of such motion is positive, and continues positive throughout the fourth quadrant until

it vanishes at conjunction.

Thus it appears, that the tangential component is negative in the first and third quadrants, throughout which it has therefore a tendency to retard the moon's motion; and that it is positive in the second and fourth quadrants, throughout which therefore it has a tendency to accelerate the moon's motion.

Let us now trace the changes of direction and sign, which affect

the radial component of the disturbing force.

It has been already shown that at conjunction the radial component is negative, and therefore directed from the earth. This circumstance arises from the fact that the sun's attraction on the moon at C, is greater than its attraction upon the earth at S, and the disturbing force being the excess of the attraction towards the sun at C, above the attraction towards the sun at S, is directed from S. As the moon moves from C to P, the direction of the disturbing force lies outside the tangent, and consequently its radial component is directed from S and is therefore negative. It gradually decreases from C to P, because the angle under the disturbing force and the tangent gradually decreases. This angle vanishes at P, where the disturbing force coincides with the tangent, and where therefore its radial component vanishes. Thus it appears that the radial com-

ich is negative at c, continually decreases from c to \mathbb{F}_1 = 0.

assing P₁, the direction of the disturbing force falling tangent, its radial component is directed towards s, and re positive; and the angle which the direction of the force makes with the the tangent, increasing from P₁ to lial component continually increases until at P₂ the dithe disturbing force being at right angles to the tangent, disturbing force becomes radial. After passing P₂, the er the direction of the disturbing force and the tangent omes acute, and the radial component being positive, and continues to decrease until at P₃ the angle under the of the disturbing force and the tangent vanishes, and there y the radial component also vanishes, the whole disturbing g tangential.

assing P₃, the direction of the disturbing force falling outangent, the radial component is again directed from the
l is therefore negative; and the angle under the disturbing
the tangent continually decreases until the moon arrives at
o, where it becomes a right angle, and the whole disrce becoming radial, is directed from s, and is therefore
After passing opposition, the angle under the disturbing

After passing opposition, the angle under the disturbing

whole attraction, it must increase and decrease with such attraction. Now, since the sun's distance from the earth varies, being least when the earth is in perihelion, and greatest when it is in aphelion, and since the sun's attraction on the earth increases in the same proportion as the square of the earth's distance from it decreases, it follows, that the sun's attraction on the earth and moon, and therefore its disturbing force, is greatest when the earth is in perihelion, and least when it is in aphelion, and that it continually decreases while the earth passes from aphelion to perihelion.

Now, since, from what has been just explained, the mean apparent motion of the moon is diminished by every increase of the sun's disturbing force, it will follow that this mean apparent motion will be least when the earth is in perihelion, and greatest when it is in aphelion; and that it will gradually increase while the earth is passing from perihelion to aphelion, and gradually decrease while

the earth is passing from aphelion to perihelion.

If we suppose an imaginary moon to revolve round the earth uniformly in the same time as the real moon does variably, the spparent motion of this imaginary moon would be the mean apparent motion of the moon, and its place would be the mean place of the moon.

The difference between the places of this imaginary moon and the true moon, produced by the inequality of the moon's mean motion which has been just explained, is called the annual equation, because this difference must continually increase for one half year, and diminish for another half year, according as the true

motion exceeds or falls short of the mean motion.

This inequality or variation of the moon's mean apparent motion was discovered by observation at a very early period in the progress of astronomical science, and long before its physical cause was disclosed by the discovery of gravitation. Its discovery by observation was due to Tycho Brahe, about the year 1590. The greatest value of this annual equation, or, what is the same, the greatest difference between the mean and true places of the moon, so far as they are affected by this cause, is about 10'.

\$195. Acceleration of the moon's mean motion.—It might very naturally be expected that a mean between the greatest and least values of the moon's mean motion, as above explained, would be equal to the moon's mean motion when the earth is at its mean distance from the sun. Thus, if M' express the moon's mean apparent motion when the earth is in aphelion, and M' its mean apparent motion when in perihelion, and M be the mean between these, we shall have

$$M = \frac{1}{2}(M' + M'').$$

Now, if m express the mean motion of the moon, subject to

e radial components do not amount to more than one-half the negative radial components of the disturbing force entire synodic period.

sides this excess of intensity of the negative over the dial components, it is to be considered that while the adial components are in operation through four ares of " of the synodic revolution, the positive radial compoin operation only through the four arcs complementary -that is, through four arcs whose magnitude is 35°

al effect, therefore, of the radial components, during an odic period, must be to diminish the earth's central attracthe moon - first, because the intensity of the negative aponents is greater than that of the positive in the pronearly 2 to 1; and, secondly, because the total length cs, through which the former act, is greater than that of through which the latter act, in the proportion of 54 to The total effect, therefore, of the radial component of bing force is to diminish the earth's attraction upon the low it appears, from the general principles of central ch have been so fully explained in former chapters of this hat the angular motion of a body, revolving at a given round a centre of attraction, will be more or less rapid to the greater or less intensity of that attraction. Whatefore, diminishes the central attraction of the earth upon , must produce a corresponding diminution of the rate of s mean motion round the earth. Since, therefore, the

ole attraction, it must increase and decrease with such attraction.

w, since the sun's distance from the earth varies, being least
en the earth is in perihelion, and greatest when it is in aphelion,
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its mean distance from the sun. Thus, if M' express the con's mean apparent motion when the earth is in aphelion, id M" its mean apparent motion when in perihelion, and M be e mean between these, we shall have

$$\mathbf{M} = \frac{1}{2}(\mathbf{M}' + \mathbf{M}'').$$

Now, if m express the mean motion of the moon, subject to

angular motion round the earth, is greatest at syzygies, and least at

quadratures.

But if we take into account, also, the effect of the tangential component, this variation of the apparent motion will be still greater. This component, according to what has been shown, continually accelerates the moon's motion in approaching the syzygies, and continually retards it in approaching the quadratures, so that, so far as depends on it, the moon's velocity will be greatest at syzygies, and least at quadratures.

Thus the two components of the sun's disturbing force combine to render the moon's apparent motion greatest at con-

junction and opposition, and least at quadratures.

This inequality of the moon's apparent motion, which passes through all its phases in the synodic period, is called the variation, and was discovered about the same time with the annual

equation by Tycho Brahè.

If we suppose an imaginary moon to perform the synodic period with a uniform angular motion, while the motion of the true moon is subject to this alternate acceleration and retardation at syzygies and quadratures, the distance between the two moons will be the variation, and its greatest amount will be about 32'.

3198. Parallactic inequality. — In this explanation, however, we have assumed that the disturbing forces are equal at conjunction and opposition. Now, it has been already shown that, at these points, they are slightly unequal—the disturbing force at conjunction exceeding that at opposition, in the proportion of about 63 to 62. It follows, therefore, that the effect of the disturbing forces will not be exactly equal at the two syzygies; and a small inequality is thus, as it were, superposed upon the variation, or, so to speak, a variation of the variation is produced, which is called the parallactic inequality.

3199. Inequalities depending on the elliptic form of the lunar orbit.—In the preceding paragraphs we have omitted the consideration of the elliptic character of the moon's orbit. We shall now explain those inequalities which depend on the

varying length of the moon's radius vector.

3200. Equation of the centre. — The first inequality of this class which we shall notice is one which appertains to the problem of two bodies, rather than that of three bodies, and which has been already noticed in relation to elliptic motion in general. The equable description of areas by the moon in its elliptic orbit, causes its angular motion at perihelion to be greater than at other points; and, as it moves from perihelion, this angular motion gradually diminishes, and continues to diminish, until it arrives at aphelion, where it is least. From aphelion to peri-

ainishes the central attraction or increases the velocity, must iminish the curvature of the path of the body, and vice versa. Iow it has been shown that, throughout two arcs of the lunar rbit extending to 54° 44′ 7" at each side of the line of syzyies, the radial component of the disturbing force is negative, and therefore diminishes the central attraction, and consequently lso diminishes the curvature. But it has also been shown that he tangential component is positive while the moon approaches he syzygies, and negative after it passes them. The motion of the moon is therefore accelerated by this component until it rrives at syzygies, and retarded after it passes these points. The velocity of the moon, therefore, being most augmented at syzygies by the tangential component, the curvature of its path sthere diminished.

It appears, therefore, that throughout the arcs extending i4° 44′ 7" on either side of the syzygies, both components of he sun's disturbing force have a tendency to diminish the curva-

ure of the moon's path.

On the other hand, throughout the arcs which extend 35° 15′ 53″ meach side of the quadratures, the radial force, being positive, agments the central attraction of the earth, and therefore increases the curvature of the orbit; and at the same time the angential component of the disturbing force, being negative as he moon approaches the quadratures, diminishes the velocity, and consequently increases the curvature of the moon's path.

For these reasons, the curvature of the moon's orbit is greatest the quadratures and least at the syzygies, which is equivalent to tating that the lunar orbit has an oval form arising from these auses, the longer axis of the oval being in the direction of the qua-

ratures, and the lesser axis in the direction of syzygies.

8197. Moon's variation. — If the radial component be alone conidered, it is easy to see that the moon, moving in such an orbit, rould have a varying angular motion, which would be greatest at vzygies where the moon is nearest the earth, and least at quadraares where it is most distant from the earth. This will follow mmediately from the principle of the equable description of areas, rhich is never affected by a radial disturbing force, since that priniple rests on no other condition than that the revolving body be ffected only by a force directed to a fixed centre. It is clear, from that has been proved in (2614), that the angular velocity, varying aversely as the square of the moon's distance from the earth, will, a such an oval orbit as has just been described, be greatest where he distance is least, — that is, at syzygies; and least where the istance is greatest, — that is, at quadratures. So far, therefore, as elates to the radial component of the disturbing force, the moon's pparent motion, as seen from the earth, which is, in fact, its

otion round the earth, is greatest at syzygies, and

we take into account, also, the effect of the tangenti is variation of the apparent motion will be still conent, according to what has been shown, con the moon's motion in approaching the syzygies, a stards it in approaching the quadratures, so that s on it, the moon's velocity will be greatest at sy at quadratures.

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suppose an imaginary moon to perform the th a uniform angular motion, while the motion is subject to this alternate acceleration and syzygies and quadratures, the distance between till be the variation, and its greatest amount

helion, on the contrary, the angular motion gradually and continually increases. If we suppose an imaginary moon to move from perihelion through aphelion back to perihelion, with a uniform angular velocity, the motion of this moon would be the mean motion of the moon, its place the mean place, and its anomaly, or its distance from perihelion, the mean anomaly; and the distance between this imaginary moon and the true moon is called the equation of the castre.

Starting from perihelion, the motion of the true moon being greater than that of the imaginary moon, the true moon is in advance of the imaginary moon, and it continues to gain upon the imaginary moon to a certain point, after which the mean moon begins, in its turn, to gain upon the true moon, and overtakes it at aphelion; the distance between the two moons, mean and true, at any point, is the equation of the centre. From aphelion to perihelion, on the contrary, the mean moon precedes the true moon, and the distance between them increases to a certain point, after which the mean moon begins to overtake the true moon, and does overtake it on returning to perihelion.

The equation of the centre is, therefore, positive from perihelion

to aphelion, and negative from aphelion to perihelion.

3201. Method of investigating the variations of the elliptic elements of the lunar orbit. — After what has been explained in the present and preceding chapters, there will be no difficulty in tracing the effects produced by the sun's disturbing force upon the magnitude, form, and position of the moon's elliptic orbit. produced in general upon any elliptic orbit whatever, by positive and negative, radial and tangential disturbing forces (317 et seq.), and the successive changes of direction and intensity of the radial and tangential components of the sun's disturbing force acting on the moon, as explained above, being fully comprehended, it is only necessary to apply the general principles to the particular case of the moon in order to explain all the phenomena. For this purpose it will be necessary to consider successively the cases in which the moon's perigee assumes every variety of position with relation to the line of syzygies, and in each position to investigate the effects produced upon the elements of the instantaneous ellipse in the different positions which the moon assumes during an entire revolution in its orbit.

8202. Moon's mean distance not subject to secular variation.—
It may be stated, generally, that the effects of the disturbing force of the sun upon the moon's mean distance or major axis of its orbit neutralise each other; the increase which it produces on that element in some synodic positions being exactly compensated by the decrease it produces in others.

In the first place, it must be observed that since the eccentricity

of the lunar orbit is very small, the radial component produces no effect on the moon's orbital velocity, and, therefore, none upon the

magnitude of its major axis.

The tangential component being negative in the first and third, and positive in the second and fourth, quadrants, diminishes the axis in the former and increases it in the latter. If it can be shown that, on the whole, the increase is equal to the decrease, it will fallow that the magnitude of the mean distance or major semiexis

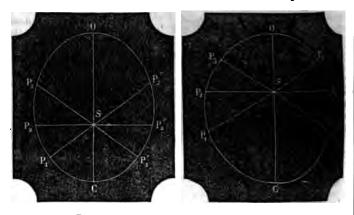


Fig. 843.

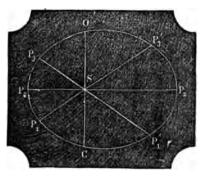


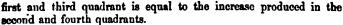
Fig. 845.

intensity of the disturbing force is the same at equal angular in tances from the apsides, it follows that in each case the diminute of the mean distance produced by the tangential component in the

Fig. 844.

suffers no ultimate change. For this purpose it will be necessary to examine the effects in different positions of the lunar orbit relatively to the syzygies and quadratures.

If the line of apsides be in syzygies, as represented in fig. 843, when perigee is in conjunction, and is fig. 814 when apogee is in conjunction, the elliptic 🕾 bit will be divided symmetrically by the four synoir quadrants; and, since the



If the apsides be in quadrature, as represented in fig. 845, the same will obviously be true.

In these cases, therefore, the major axis of the orbit suffers no ultimate change from the action of the disturbing force.

But if, as in fig. 846, the line of apsides p a be inclined at an oblique angle to the line of syzygies c o, the elliptic orbit will not



Fig. 846.

be symmetrically divided by the four synodic quadrants CP2, P2O, OP2, and Pc, C, and in that case the decrease and increase of the axis produced in the alternate quadrants will no longer be equal, and a complete compensation will not, as before, be effected in a single synodic revolution. But if the orbit be taken in two positions in which the line of apsides p a and p' a' is equally inclined on different sides of the line of syzygies, the effect of the disturbing force on the mean distance in a complete synodic revolution in one position will be compensated by

the equal and contrary effect produced in the other position. This will be apparent by considering that the intensities of the disturbing force at equal inclinations to the line of syzygies are proportional to the moon's distance from the earth. It follows from this that the effects of the disturbing force in the quadrants Cp P_2 and Cp' r'_2 , and in the quadrants P_2a P'_2 and P_2a' P'_2 are equal, and in the same manner that the effects are equal in the other corresponding quadrants. It will, therefore, be apparent that, taking the orbit in the two positions, the increase and decrease which the major axis suffers in two complete synodic periods are equal, and that, therefore, the major axis suffers no ultimate change of magnitude.

But since, in the revolution of the earth and moon round the sun, the line of apsides takes successively every inclination to the line of syzygies, it will necessarily assume, at regular intervals, the equal inclinations at which the effects of the disturbing force upon the axis of the orbit are mutually compensatory, and it follows, therefore, that no ultimate decrease of magnitude of the axis takes place.

It remains, therefore, to investigate the effects of the disturbing

ne sun on the other elements of the lunar orbit; that is, direction of the apsides, or, what is the same, on the longirihelion and the eccentricity.

se effects will vary according to the varying position of f apsides, with relation to the line of syzygies, we shall accessively the variation of each of the elements during a evolution of the moon, when the apsides are in syzygies, ares, and between these points.

FIRST CASE.

WHEN PERIGEE IS IN CONJUNCTION.

Motion of the apsides. — Let the lines P₁ P'₄ and P'₁ P₃ be aking angles of 54° 44′ 7" with the line of syzygies co, Let us consider, first, the effect of the radial, and,

the effect of the tangential component.

The radial component, being negative while the moon rough the arcs $P_1 \cap P_1$, and $P_3 \cap P_3 \cap P_3 \cap P_3$, a regressive ll be imparted to the apsides in the former and a progression in the latter (3193).

progressive motion considerably exceeds the regressive; and, there-

fore, on the whole, the apsides are moved forward.

Secondly. The tangential component being negative from C to P_2 and from 0 to P'_2 , and positive from P_2 to 0 and from 0 to P'_2 , it imparts a regressive motion to the apsides from P'_1 to P_1 , from P_2 to P_3 , and from P'_3 to P'_2 , and a progressive motion from P_3 to P'_3 , from P'_2 to P'_1 , and from P_1 to P_2 , (3193).

It may be shown, as in the former case, that the progressive motion in a complete synodic revolution exceeds the regressive motion, and, therefore, that on the whole the tangential component imparts

a progressive motion to the apsides.

It follows, therefore, that when perigee is in conjunction, the disturbing force of the sun, acting during a complete synodic revolution of the moon, causes the line of apsides to move forward in the direction of the sun's motion, so that, at the end of a synodic revolution, the longitude of perigee will be greater than it was at its commencement,—the longitude of that point, however, having, during such revolution, alternately increased and decreased.

3204. Effects on the eccentricity.—To ascertain the variation of the eccentricity of the lunar orbit, produced by the sun's disturbing force in the same position of the apsides, we shall, as before, consider first, the effect of the radial, and, secondly, that of the tangential

component.

First. The radial component being negative from P₁ to P₁ and from P₃ to P₃, and positive from P₁ to P₃ and from P₃ to P₁, it follows, that it will cause the eccentricity to increase from C to P₁ and from P₃ to 0, and to decrease from P₁ to P₃, while, in the other half of the synodic revolution, it will cause it to decrease from 0 to P₃, and from P₁ to C, and to increase from P₃ to P₁, (3193). Now it is evident that the effects of the disturbing force through the arcs CP₁, P₁ P₃, and P₃ O, are respectively equal to its effects through the arcs CP₁, P₁ P₃, and P₃ O, and, therefore, that the increments and decrements which the eccentricity receives during a complete synodic revolution are equal, and that so far as depends on the radial component of the disturbing force, it suffers no ultimate variation.

Secondly. Since the tangential component is negative in the first and third, and positive in the second and fourth quadrants, it will follow, from what has been proved (3156), that this component will cause the eccentricity to decrease throughout the first and second, and to increase throughout the third and fourth quadrants.

But it will be evident, from the same reasoning as has been used in the former case, that the intensity of the disturbing force in the first and second quadrants, being respectively equal to its intensity in the fourth and third, the decrease of the eccentricity in the first quadrant will be equal to its increase in the fourth, and its decrease

nd quadrant will be equal to its increase in the third; the
e of which will be that, in a complete revolution, the
y will suffer no change from the operation of the tangennent of the disturbing force.
's, therefore, that when the moon's perigee is in conjunccentricity of its orbit, at the end of each synodic revolube the same as at the beginning, but that during such
it will alternately increase and decrease within certain
hits.

SECOND CASE.

WHEN PERIGEE IS IN OPPOSITION.

Motion of the apsides. — As before, let the lines P₁ P'₁ and 844, be drawn, making angles of 54° 44′ 7″ with the tygies C O, and let us consider, first, as in the former case, of the radial, and, secondly, the effect of the tangential t.

The radial component being negative, while the moon m P'₁ to P₁, and from P₃ to P'₃, a progressive motion will

First. The radial component being negative from P'₁ to P₁ and from P₂ to P'₃ and positive from P₁ to P₃ and from P'₂ to P₁, it will cause the eccentricity to decrease from C to P₁ and from P₃, to O, and to increase from P₁ to P₃; while in the other half of the synodic revolution, it will cause it to increase from O to P'₃ and from P'₁ to C, and to decrease from P'₃ to P'₁ (3193); and it is evident, as before, that the effects in each half orbit being compensatory, no ultimate variation is produced by this component upon the eccentricity in a complete synodic revolution.

Secondly. The effects of the tangential component are, in like manner, shown to be compensatory in this case by reasoning so com-

pletely similar to the former that it need not be repeated.

THIRD CASE.

WHEN THE APSIDES ARE IN QUADRATURE.

3207. Motion of the apsides. — Let the lines P₁ P', and P'₁ P₂, fig. 845, as before, be drawn, making angles of 54° 44′ 7″ with the line of syzygies c o. We shall, as in the former case, consider first the effect of the radial, and second that of the tangential component.

First. The radial component being negative from P_1 to P_7 and from P_3 to P_3 , and positive from P_1 to P_3 and from P_3 to P_4 , it follows that a regressive motion will be imparted to the apsides while the moon moves from c to P_1 , from P_3 to 0, and from P_3 to P_4 , and that a progressive motion will be imparted to it in the intermediate arcs, that is from P_1 to P_3 , from 0 to P_3 , and from P_4 to c.

But, from the principle already so often referred to, in virtue of which the intensity of the disturbing force at equal inclinations to the line of syzygies is proportional to the distance of the moon from the earth, it will be evident that the total effect of the radial component in imparting a regressive motion to the apsides from P_1 to P_1 will be much greater than its total effect in imparting a progressive motion from P_1 to P_2 , while the difference of its effects in the other arcs will be comparatively small. It will follow, therefore, that after an entire revolution the effect of this component in imparting regression will greatly predominate over its effect in imparting progression, and that, on the whole, the apsides will be made to regress.

Secondly. The tangential component being, as before, negative in the first and third, and positive in the second and fourth quadrants, it will impart to the line of apsides a progressive motion through the arc op, o, and a regressive motion through the arc

o r', c (3163).

It is evident, as before, that in this case the regressive effects predominate over the progressive, and that, therefore, the effect of this component throughout a complete synodic revolution is to impart to the apsides a regressive motion.

Effect on the eccentricity. - We shall, as before, first coneffect of the radial, and secondly of the tangential com-

appear, from what has been already explained (3163), adial component being positive from P, to P, and from P, eccentricity will increase from P, to P, and from P', to P, ecrease from P2 to P3 and from P3 to P2; and the radial t being positive from P₃ to P'₃ and from P', to P₁, the y will increase throughout the former and decrease t the latter arc.

, the several arcs of the ellipse in which the eccentricity be compared with those in which it decreases, they will be be perfectly equal and symmetrical, so that the intensity dial components which produce increase will be equal on to those which produce decrease; consequently, the effects mponent on the eccentricity will be compensatory.

ly. Since the tangential component is negative in the first , and positive in the second and fourth quadrants, it will m what has been explained (3163), that the eccentricity nually increase through the same ellipse P2 O P2, so that the effects of the component are compensatory.

quadrature, the result will be a progression of the apsides amount-

ing to $11^{\circ} - 9^{\circ} = 2^{\circ}$.

Several circumstances attending the moon's motion combine in producing this difference in the effects of the apsides in the two positions. The synodic motion of the moon is slower at apogee than at perigee in the ratio of 9 to 13; that is to say, while the moon departs from the sun at perigee through 13°, it will depart at apogee through only 9°. The consequence of this is, that the slower synodic motion at apogee leaves a longer time for the operation of the sun's disturbing force upon the earth than at perigee. Thus, this force is not only more energetic at apogee than at perigee, since its intensity is proportional to the mean distance from the earth, but the more intense force acts for a longer time.

When perigee is in conjunction, the motion of the apsides being progressive, and at the rate of 11° in each synodic revolution, while the progressive motion of the sun in the same time is about 27°, it follows that, in each synodic revolution, the sun will depart from

perigee through a distance of $27^{\circ} - 11^{\circ} = 16^{\circ}$.

But when the sun is in quadrature, the regressive motion of the apsides in each revolution being 9° , while the progressive motion of the sun is, as before, 27° , the sun and perigee will depart from each other, in each synodic revolution, through $27^{\circ} + 9^{\circ} = 36^{\circ}$.

It appears, therefore, that the separation of the sun and perigee, in each synodic revolution when perigee is in syzygies, is greater than when it is in quadrature, in the proportion of 36 to 16, or 9 to 4.

It is evident from this, therefore, that another cause operates in favour of the more continued action of the disturbing force in producing a progressive motion in syzygies than in producing a regressive motion in quadratures, inasmuch as, from what has been just explained, the sun separates itself from the position favourable to the action of the disturbing force more than twice as rapidly in quadratures than in syzygies.

FOURTH CASE.

WHEN THE APSIDES ARE OBLIQUE TO THE LINE OF SYZYGIES.

3210. Motion of the apsides.—It has been shown that when the apsides are in syzygy the disturbing force imparts to them a progressive motion at the rate of about 11° in each synodic revolution, and that when they are in quadrature it imparts to them a regressive motion at the rate of about 9° in each synodic revolution. It might therefore be expected, that if the line of apsides assume successively increasing inclinations with the line of syzygies, from 0° to 90°, the progressive motion of 11° imparted to the apsides at syzygies would gradually decrease, and at some intermediate inclinations.

nation between 0° and 90° would become nothing, after which the motion imparted to the apsides becoming regressive, would gradually increase until it becomes 9° in each synodic revolution, when the line of apsides is in quadrature.

If the conditions which determine the effect of each component of the disturbing force upon the direction of the line of apsides, in relation to that of syzygies, be clearly fixed in the mind, the student will have no difficulty in seeing that this in fact will be the case. For this purpose, it is only necessary to draw the elliptic orbit with its major axis inclined to the line of syzygies at successively increasing angles, and to examine and compare carefully the different effects produced by each component of the disturbing force upon the moon at different elongations from the sun, in each position of the apsides in relation to syzygy. It will be found that when the line of apsides makes a very small angle with the line of ayzygies, the effect of the disturbing force is very little less than at syzygies, and that, accordingly, a progressive motion is imparted to the assides, very little less than 11°; and on the other hand, that when the line of apsides makes with that of syzygies an angle but little less than 90°, the regressive motion imparted to the apsides is little less than 9°.

It will not be necessary here to multiply the details of this analysis, by going through the particulars of all such cases; but it may be useful to illustrate the mode of investigating them, by showing the effects of the disturbing force on the line of apsides when that line is inclined to that of syzygies at the angle of 34 44 7", at which the effects of the disturbing force in imparting progressive and regressive motion to the apsides are compensatory, or nearly so, and where, therefore, the apsides at the end of a synolic revolution have the same direction as at its commencement.

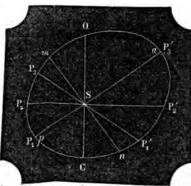


Fig. 847.

3211. When the mom's perigee is 54° 44' 7" bijor the point of conjunction. Let c o, fig. 847, be the line of syzygies, c being the point of conjunction when the moon's perigee p is 54°44' 7" before it, and when, orsequently, the apogee a is a the same angular distance from the point of opposite The line of apsides vil then coincide with the line which in the preceding dir grams has been marked ! V' 3, and the line mn passis

through s at right angles to the line of apsides, will lie in advance of the line P'₁ P₃, which is inclined to the line of syzygies on the other side of it at the angle 54° 44′ 7".

We shall consider, first, the effect of the radial, and secondly, of

the tangential component.

First. From what has been already proved (3163), it appears that a positive radial component will render the apsides regressive while the moon passes from m to n, and progressive while it passes from n to m, and, consequently, that a negative radial component will produce a contrary effect. By combining these with the conditions which determine the changes of sign of the radial component, explained in the present chapter, it may be easily inferred, that the apsides will be progressive, while the moon moves from p to p from p to p, and from p, and that they will be regressive while the moon moves through the arcs p, p, p, p, and p, and p, and it will be easy to perceive that the aggregate length of these arcs is not only nearly equal, but that their distances from p are nearly the same, consequently the extent of the orbit through which the radial component renders the apsides progressive, is nearly equal to that through which it renders it regressive. The effects of this component are therefore compensatory.

Secondly. It appears from what has been proved (3163) that a positive tangential component renders the apsides progressive while the moon moves from p to a, and regressive while it moves from a to p, and that a negative tangential component has contrary effects. By combining these with what has been proved in the changes of sign of the tangential component in the present chapter, it will be easy to infer that this component will render the apsides progressive from p to p, from p to p, from p to p, and from p to p, and regressive from p to p, from p to p, and from p to p, and the energy equal in length and at nearly equal distances from p, and that consequently the effects of this component of the disturbing force are also compensatory.

It follows therefore, generally, that in this position of the moon's perigee no motion is imparted to the line of apsides in a complete synodic revolution, but that alternate motions of progression and regression of equal total amount are imparted to it during each

revolution.

3212. When the moon's perigee is 54° 44′ 7" behind the point of opposition. — This case is represented in fig. 848, the moon's apogee being the same distance behind the point of conjunction c.

We shall, as in the former case, consider, first, the effect of the

radial, and secondly, that of the tangential component.

First. Upon the same principles as were applied in the preceding case, it will follow that, by the effect of the radial component, the apsides will be progressive while the moon moves from m to \mathbf{r}'_{∞}



Fig. 848.

from P'₁ to n, and from P'₁ to P'₃, and regressive while the moon moves from P₃ to m, from P'₃ to P'₁ and from n to P₁; and, as before, if these arcs be compared both as to length and distance from s, it will be found that the effects of this component on the lines of apsides are compensatory.

Secondly. By the same principles as before, it will follow that, by the effect of the tangential component, the apsides will be progressive while the moon moves from

om P'₂ to P'₁, and from C to P₂, and regressive while the res from m to P₂, from P'₁ to C, and from P₂ to P₃; and, it will be apparent by comparing these arcs that these the apsides are compensatory.

ws therefore, as before, that in this case the disturbing

mgential component the speides will be rendered progressive while moon moves from 0 to P's, from P's to C, and from P, to Pe, and 124 they will be regressive while it moves from P, to 0, from P, to and from 0 to P1; and it will appear as before that the effects re compensatory.

It follows, therefore, in general, as in the former cases, that in his position of perigee the line of apsides suffers no change of irection from the action of the disturbing force after a complete ynodic revolution, but that, during such revolution as before, it

scillates on either side of its mean position.

8214. When perigee is 54° 44' 7" behind conjunction.—In this



Fig. 850.

case, which is represented in fig. 850, the line of apogee is at the same angular distance behind the point of opposition.

First. By the effects of the radial component the apsides will be rendered progressive while the moon moves from Ps to n, from P's to P', and from m to P1, and regressive while it moves from P, to Pa, from n to P's, and from P', to m; and as before, it may be shown that the effects in these cases respectively are compensatory.

Secondly. By the effects of the tangential force it appears.

n like manner, that the apsides will be rendered progressive from o to f_{s} , from P_1 to C, and from P_2 to P_s , and regressive from P_2 to O, from f_{s} to f_{s} , and from G to f_{s} ; and that, in like manner, these effects ure compensatory.

It follows, therefore, that in this position of the moon's perigee 10 effect is produced by the disturbing force upon the direction of he line of apsides after a complete synodic revolution, but that line. s before, during such revolution oscillates on the one side and on

he other of its mean position.

3215. Summary of the motions of the apsides.—After what has een explained above, the motion of the line of apsides in all its ositions with relation to the line of syzygies may be easily inferred. t must be remembered that the lines of syzygies and apsides being oth affected with a mean progressive motion, that of syzygies, howver, being much more rapid than that of apsides, it will follow that he line of syzygies after each successive synodic revolution will ain upon the line of apaides, advancing constantly before it. III.

then imagine, first, that the moon's perigee is in con-

ne of apsides will then, according to what has been fter one synodic revolution be affected by a progressive After the next synodic revolution the line of syzygies will anced before that of apsides, and the progressive motion to the latter will be less than before, and after each sucnodic revolution the line of syzygies advancing further and advance of the line of apsides, the progressive motion imthe latter will become less and less until the line of syzyng advanced to the distance of 54° 44' 7" from the line of he progressive motion ceases, and the line of apsides stationary. his, the line of syzygies advancing to a still greater anguce from the apsides, the motion imparted after each revothe latter becomes regressive, and its regressive amount every successive synodic revolution until the line of apsides o quadrature, when the regressive motion of the apsides in a complete synodic revolution becomes a maximum.

s when the line of syzygies has advanced more than 90° line of apsides the regressive motion imparted in each resubject to no variation, it is plain that at these points it must be either a maximum or a minimum, since it is neither on the increase or decrease.

8217. When perigee is 54° 44' 7" before the point of conjunction.

We shall consider as before, first, the effects of the radial, and secondly, those of the tangential component upon the eccentricity.

It appears from what has been proved, that a positive radial component will cause the eccentricity to diminish, while the meon moves from perigee to apogee, and to increase while it moves from apogee to perigee, and that a negative radial component will have a contrary effect. It will follow, therefore, in this case by comhining this principle with the conditions determining the change of sign of the radial component explained in the present chapter, that is will cause the eccentricity to increase while the moon moves from B to F1, fig. 847, and to decrease while it moves from F1 to P2. But it will be evident by comparing the lengths of these two arcs, and their distances from s, that the effect of the disturbing force will be much greater in the former than in the latter, and consequently, that the increase of the eccentricity in the former must greatly exceed the decrease in the latter, and therefore, that the lect of the radial component in an entire synodic revolution will be to increase the eccentricity.

Secondly. It appears from what has been explained that the effect of a positive tangential component will be to decrease the eccentricity while the moon moves from m to n, and to increase it while it moves from n to m, and that a negative tangential component will have contrary effects. By combining this with the changes of sign explained in the present chapter, it will follow that the eccentricity will be increased while the moon moves from P₂ to m, from o to P₂, and from n to c, and that it will be decreased while it moves from c to P₂, from m to 0, and from P'₂ to n, and by comparing these ares both with relation to their extent and their distance from s, it will be apparent that the increase of the eccentricity must exceed the decrease, and that consequently the result of a whole synodic period will be to cause the eccentricity to increase.

It appears, therefore, that both components of the disturbing force in this position of the line of speides will cause the eccentricity to increase during each synodic revolution, being subject nevertheless

during such revolution to alternate increase and decrease.

8218. When periges is 54° 44′ 7" behind opposition. — First. By the effects of the radial component it may be shown, as before, that the eccentricity will constantly increase while the moon moves from P₁ to P₂, fig. 848, and will continually decrease while it moves from P's to P₁, and it will be obvious, from considering the magnitude of these area and their distances from s, that the decrease of the eccentricity will considerably exceed the increase; and that,

this component of the disturbing force will, during an plution, cause the eccentricity to decrease.

by. By the effects of the tangential force, it may be before, that the eccentricity will be increased while the ves from P₂ to 0, from m to P'₂, and from c to n, and that decreased while the moon moves from n to P₂, from 0 to m P'₂ to c, and by comparing these arcs it will be obvious otal decrease will exceed the total increase.

Its therefore from this, that both components of the disorce in this position of perigee causes the eccentricity to

n a complete synodic revolution.

When perigee is 54° 44′ 7" before opposition. — First.—
shown as before, that the radial component will cause the
ty continually to increase while the moon moves from r'
849, and to decrease continually while it moves from r
by comparing these arcs as before, it will be apparent
increase greatly exceeds the decrease, and therefore, so far
to the radial component, the eccentricity during each
evolution will suffer an increase.

ly. By the effects of the tangential component, the eccenli increase while the moon moves from c to P2, from n to 0 from periges, the eccentricity decreases, and continues to decrease until the point of conjunction is 90° from perigee, when the eccentricity again becomes stationary, its decrease ceasing. When the conjunction advances more than 90° from perigee, the eccentricity again increases and continues to increase until the point of conjunction has moved 180° before perigee, when the increase ceases. After this, the eccentricity again decreases, and continues to decrease until the point of conjunction gains another quadrant on perigee, when the increase ceases and the decrease commences, which is continued through another quadrant. It appears, therefore, that the eccentricity is a maximum when the apsides are in quadrature, and a minimum when they are in conjunction, and that consequently it gradually increases while the apsides move from conjunction to quadrature, and gradually decreases while they move from quadrature to conjunction.

If e' express the value of the eccentricity while the apsides are in quadrature, and e'' their value when in conjunction, the mean value being e, it is found that

$$e': e: e'' = 1.50: 1.25: 1.00;$$

so that the extreme range of variation of the eccentricity of the moon's orbit is as 3 to 2.

EFFECTS OF THE DISTURBING FORCE UPON THE LUNAR NODES AND INCLINATION.

From what has been proved in general (3158. et seq.), it will appear that when the moon is less distant than the earth from the san, the orthogonal component of the disturbing force will have a tendency to draw it out of the plane in which it is moving towards the side on which the sun is placed, and that when the moon is more distant than the earth from the sun, the orthogonal component will have a tendency to draw it out of the plane in which it moves to the side opposite to the sun.

But it has also been proved that the nodes will have a progressive or regressive motion, according to the direction of the orthogonal force in the successive quadrants of its orbit between node and node.

It will, therefore, be necessary to consider successively the effects of the disturbing force in the various positions which the lines of syzygies and quadratures may assume with relation to the line of nodes.

FIRST CASE.

8222. When the line of syzygies is in the line of nodes.—In this case, it is evident that the orthogonal component of the disturbing 51*

be nothing, since the whole attraction of the sun is in the he moon's orbit, and, consequently, no part of the attract at right angles to that plane.

SECOND CASE.

When the line of nodes is in quadrature. — Let ACOA, represent the moon's orbit, and ADA the ecliptic seen in

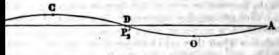


Fig. 851.

lane and projected into a straight line. Let A be the and D the descending node, and let the points of syzygies ed to be at c, and o the points of the moon's orbit most om the ecliptic, while the points of quadrature P₂ and P'₂ nodes A and D.

een already shown, that when the moon is in quadratures disturbing force is radial, and being directed to the sun plane of the moon's orbit, it can have no component per-

creases with the increase of the orthogonal force, until the moon arrives at c, when the regression is a maximum; it then decreases and continues to decrease until the moon arrives at D, where it vanishes; it again increases from D to O, where it is again a maximum, and decreases from O to A, where it vanishes.

The change of inclination produced by the disturbing force being nothing at A, the inclination decreases continually from A to C, and increases from C to D. It is, therefore, a minimum at C. After passing D, it decreases from D to O, and, consequently, is a maximum at D. After passing O, it increases from O to A, and is, consequently a minimum at O.

Thus it appears that the inclination is least at conjunction and opposition, and greatest at quadratures,—that is, in the present position of the lines of syzygies and quadrature, it is least when the moon's latitude is greatest, and greatest when the moon's latitude is nothing.

THIRD CASE.

8224. When the line of syzygies is less than 90° before the line of nodes. — This case is represented in fig. 852, where, as before, A

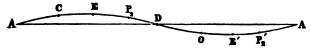


Fig. 852.

ascending and D the descending node, C and O being the extremities of the line of syzygies, and P₂ and P'₂ those of the line of quadratures, the points E and E' being those at which the moon's orbit is most distant from the ecliptic, and, therefore, the middle points of the semicircles AD and DA.

From what has been explained, it is evident that the orthogonal component at P₂ and P'₂ will be nothing, since at these points the disturbing force is radial; and it has been already shown that at the nodes A and D the orthogonal component is also nothing.

While the moon moves from P'₂ through A and C to P₂ the disturbing force tends to draw it from the plane of its orbit towards the ecliptic, and while it moves from P₂ through D and O to P'₂ the disturbing force tends to draw it up from the plane of her orbit; therefore in moving from P'₂ to A the disturbing force draws it from the plane of the ecliptic, and while it moves from A to P₂ through C and E the disturbing force draws it towards the plane of the ecliptic.

While the moon moves from P₂ to D it draws the moon from the plane of the ecliptic, and while it moves from D through o and F' to P₂ it draws it towards the plane of the ecliptic.

bining these results with what has been proved in 3161, low that while the moon moves from A to P₂ and from D gressive motion, and while it moves from P₂ to D and from a progressive motion, is imparted to the line of nodes. ill appear by inspection of the figure, that the arc A P₂ is an the arc P₂ D, and that the arc D P'₂ is greater than P'₁ A, equently, it follows that the sum of the arcs through etrograde motion is imparted is much greater than the sum as through which a progressive motion is imparted, and tly, after the synodic revolution has been completed, the des on the whole will have retrograded.

wes, also, from what has been stated that from P'2 to E and be' the inclination will decrease, and from E to P2 and from t will increase. But since the arcs P'2 E and P2 E' are regreater than E P2 and E' P'2, the sum of the former will r than the sum of the latter, and consequently the arcs which the inclination decreases being much greater than ough which it increases, there will be on the whole a dethe inclination after the synodic revolution has been

FOURTH CASE.

The same conclusions would follow if the moon's orbit were

supposed to be inclined to the ecliptic in the other direction.

Thus it appears in general that when the line of nodes is in syzygies no change takes place either in the position of that line or in the magnitude of the inclination. While it passes from syzygies to quadrature the line of nodes regresses and the inclination diminishes; when it is in the line of quadratures the line of nodes regresses, but the inclination is unchanged; and when it is between quadratures and syzygies the line of nodes still regresses and the inclination is increased. Thus when the sun has described in its apparent motion nearly one half a revolution of the ecliptic, there is, on the whole, a regression of the node and an alternate increase and decrease of the inclination; and during its motion through the other half of the ecliptic similar changes are produced in the same order. It follows, that the inclination is a maximum when the line of nodes is in syzygies, and a minimum when it is in quadratures.

8226. GENERAL SUMMARY OF THE LUNAR INEQUALITIES. —
From all that has been stated in the present chapter it appears that

the principal lunar inequalities are as follows:-

1°. THE ANNUAL EQUATION, which depends on the variation of the disturbing force due to the varying distance of the earth from the sun in its elliptic orbit.

2°. THE VARIATION, which depends on the difference of the

disturbing force arising from the synodic place of the moon.

8°. THE ACCELERATION OF THE MOON'S MEAN MOTION, depending on the effect produced upon the disturbing force by the secular variation of the eccentricity of the earth's orbit.

4°. THE PARALLACTIC INEQUALITY, depending on the difference between the disturbing forces of the sun in conjunction and oppo-

sition.

5°. THE EQUATION OF THE CENTRE, an inequality which, however, cannot properly be called a perturbation, inasmuch as it depends only on the elliptic form of the lunar orbit, which would subsist without any disturbing force.

6°. THE ALTERNATE PROGRESSION AND REGRESSION OF THE

APSIDES, depending on the synodic place of the moon.

7°. THE MEAN PROGRESSION OF THE APSIDES, being the excess of the progression over the regression during a synodic period.

8°. THE VARIATION OF THE ECCENTRICITY, depending on the

synodic place of the moon.

9°. THE ALTERNATE REGRESSION AND PROGRESSION OF THE MODES, arising from the effect of the orthogonal component of the disturbing force.

10°. THE MEAN REGRESSION OF THE NODES, arising from the excess of the regressive over the progressive motion during the synodic revolution.

HE ALTERNATE INCREASE AND DECREASE OF THE INmbined effects of the seventh and eighth of the preceding independing on the synodic position of perigee are called by

on name, evection. This is the greatest inequality to which 's place is subject, producing a variation in the moon's the extreme range of which is 21°. It was discovered by n about the year A. D. 140, by Ptolemy.

equality arising from the alternate regression and proof the nodes and the alternate increase and decrease of the a were discovered by Tycho, about the year 1590. This eatest of the inequalities which affect the moon's latitude. however, is limited to about 16'.

Other lesser inequalities.—The preceding inequalities, s as they may seem, are nevertheless only the principal lunar perturbations. There are many others which depend ences of intensity of the disturbing force, which have not a taken into account; for example, the rate of the proof the apsides, as well as the diminution of the lunar orbit, by the difference of the intensities of the disturbing force ction and opposition.

Jupiter's satellites, and that such disturbances do act and that like inequalities are produced cannot be doubted.

3229. Why the same inequalities are not manifested.—But when we come to calculate the quantities of these inequalities in the case of Jupiter, they are found to be so utterly insignificant in their numerical values, that they are altogether incapable of being appreciated by the nicest observation, except in the case of the fourth satellite, in whose motions inequalities of very minute amount, analogous to the moon's variation, evection, and annual equation are barely observable, the inequality corresponding to the annual equation in this case amounting to no more than 2', and the other inequalities being much less.

The cause of this insignificant amount of the disturbing force of

the sun will be easily understood.

The whole Jovian system subtends at the sun a visual angle less than one-half the apparent diameter of the sun as seen from the earth, and consequently, lines drawn from the sun to all points in that system will be practically parallel, and with the exception of the fourth satellite, as already mentioned, the variation of the distances of the different satellites from the sun is so utterly insignificant, compared with the whole distance, that the corresponding variation of the intensity of the sun's attraction upon the satellites and the central body is so minute as to produce no perceptible disturbing effect. In a word, the sun's attraction upon the Jovian system may be regarded as a force acting with equal intensities in parallel lines on all parts of the system, exactly as the force of gravitation would act upon any small group of heavy bodies placed near the surface of the earth.

3230. Mutual perturbations of the satellites.—In this secondary system, therefore, contrary to what might be expected, there is no analogy whatever to the lunar theory, and all the perturbations which are observable are those due to the mutual gravitation of the four satellites one upon another.

The investigation of these perturbations is greatly simplified by

the following conditions which prevail in the system:

First. That the undisturbed orbits of all the satellites are very nearly circular, those of the first and second being exactly so.

Secondly. That they are very nearly in the common plane of the

planet's equator; and

Thirdly. That the mean motions of the three inner satellites are commensurable in the remarkable manner already expressed, (2762.)

3231. Retrogression of the lines of conjunction of the first three satellites.—As some of the most remarkable consequences of the mutual disturbing forces in this system depend upon the relation between the mean motions of the three inner satellites just mean-

HE ALTERNATE INCREASE AND DECREASE OF THE IN-

mbined effects of the seventh and eighth of the preceding independing on the synodic position of perigee are called by on name, evection. This is the greatest inequality to which is place is subject, producing a variation in the moon's the extreme range of which is 2½°. It was discovered by

n about the year A. D. 140, by Ptolemy.
equality arising from the alternate regression and pro-

of the nodes and the alternate increase and decrease of the n were discovered by Tycho, about the year 1590. This eatest of the inequalities which affect the moon's latitude.

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3229. Why the same inequalities are not manifested.—But when we come to calculate the quantities of these inequalities in the mase of Jupiter, they are found to be so utterly insignificant in their numerical values, that they are altogether incapable of being apprenated by the nicest observation, except in the case of the fourth satellite, in whose motions inequalities of very minute amount, satellite, in whose motions inequalities of very minute amount, analogous to the moon's variation, evection, and annual equation are barely observable, the inequality corresponding to the annual squation in this case amounting to no more than 2', and the other inequalities being much less.

The cause of this insignificant amount of the disturbing force of

the sun will be easily understood.

The whole Jovian system subtends at the sun a visual angle less than one-half the apparent diameter of the sun as seen from the sarth, and consequently, lines drawn from the sun to all points in that system will be practically parallel, and with the exception of the fourth satellite, as already mentioned, the variation of the distances of the different satellites from the sun is so utterly insignificant, compared with the whole distance, that the corresponding variation of the intensity of the sun's attraction upon the satellites and the central body is so minute as to produce no perceptible disturbing effect. In a word, the sun's attraction upon the Jovian system may be regarded as a force acting with equal intensities in parallel lines on all parts of the system, exactly as the force of gravitation would act upon any small group of heavy bodies placed near the surface of the earth.

8230. Mutual perturbations of the satellites.—In this secondary system, therefore, contrary to what might be expected, there is no analogy whatever to the lunar theory, and all the perturbations which are observable are those due to the mutual gravitation of the four satellites one upon another.

The investigation of these perturbations is greatly simplified by

the following conditions which prevail in the system:

First. That the undisturbed orbits of all the satellites are very nearly circular, those of the first and second being exactly so.

Secondly. That they are very nearly in the common plane of the

planet's equator; and

Thirdly. That the mean motions of the three inner satellites are commensurable in the remarkable manner already expressed, (2762.)

3231. Retrogression of the lines of conjunction of the first three satellites.—As some of the most remarkable consequences of the mutual disturbing forces in this system depend upon the relation between the mean motions of the three inner satellites just mean-

tioned, we shall, in the first instance, explain the effect of this relation upon the successive positions assumed by their lines of conjunction.

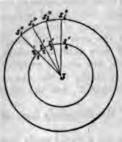


Fig. 854.

Let the three inner satellites be expressed by s', s", s", and their periods by P, P", P".

By the line of conjunction of any two satellites is to be understood that line which would be drawn through their e centre of Jupiter, where pla

they . same direction as seen from that c T

plan... the s with satellite

the direction of the arrows from of the first will be $\frac{360^{\circ}}{7}$ - and that o ig. 854, be the centre of the that of the first satellite, ellite will be in conjunction e at s". Now, if the two each in its proper orbit, in osition, the angular motion

second 390° p" and since p' is

less than P", the latter angular motion will be more rapid than the former, and the first satellite will continually gain upon the second, and after the lapse of the interval called their synodic period, the first will overtake the second, and they will be again in conjunction.

The new direction of their line of conjunction, relatively to the former, will depend upon the relation which subsists between their periodic times, and, consequently, between their mean motions. Now it appears that the mean motions of the first and second are very nearly, though not exactly, in the proportion of 2 to 1. By reference to the tabular synopsis of the elements of the Jovin system, in (2999), it will be seen that the proportion of their perodic times is as 1769 to 3551, that is, as 1000 to 2007. It follows, therefore, that the mean motion of the first satellite is a little more than twice as rapid as the mean motion of the second. If the mean motion of the first were exactly twice the mean motion of the second the first would make two complete revolutions while the second would make one; and, therefore, the second having revolved cost in its orbit, and returned to s", the first would have revolved twin and would also have returned to s',, and in this case, their lined conjunction would always have the same fixed direction J si fa But since the periodic time of the first is a little less than b

of the second, the first will overtake the second before it h completed two revolutions, and the consequence will be, the next line of conjunction J s', s'', will be behind the former; in a single synodic revolution, their line of conjunction wi

retrograded through the angle s", J s", and in the same manner, in another synodic period, it will have retrograded through an equal angle, and will assume the direction J s' s", and in the same manner at every successive conjunction it will have retrograded through an equal angle, the mean motion of the satellite being supposed to remain the same.

3232. Change of direction of line of conjunction in each synodic revolution. — To determine this, let φ be the angle formed by the line of conjunction at the termination of each revolution with the direction it had at the commencement, such angle being measured from the latter position, in the direction of the motion of the satellites, so that, in fact, o will express the increase of longitude which the line of conjunction may receive in the synodic period. Let T' express the synodic period of the satellites s' and s". We shall then have (2589.)

$$\frac{1}{T''} = \frac{1}{P'} - \frac{1}{P''}$$
 $T' = \frac{P''P'}{P'' - P'};$

and since s'' moves through $\frac{360^{\circ}}{p''}$ in the unit of time, and the advance of the line of conjunction in the time T' is equal to the angle through which s" moves in that time, we shall have

$$\phi' = \frac{360^{\circ}}{1''} \times T = 360^{\circ} \times \frac{P'}{P'' - P'}$$

In like manner, if \(\psi'' \) express the same angle for the line of conjunction of the satellites s" and s", we shall have

$$\phi'' = 360^{\circ} \times \frac{P''}{P''' - P''}$$

3233. Application to the three inner satellites. - Now in the case of these three satellites we have by (2999.) Table V.

$$\mathbf{p}':\mathbf{p}'':\mathbf{p}''' = 17691:35512:71546,$$

from which it appears that

$$\frac{\mathbf{p''}}{\mathbf{p''} - \mathbf{p'}} = 0.9927$$
 $\mathbf{p''} \frac{\mathbf{p''}}{\mathbf{p''}} = 0.9855$;

and consequently
$$\phi' = 357^{\circ} \cdot 37 \qquad \qquad \phi'' \ 354^{\circ} \cdot 78.$$

It appears, therefore, that in each synodic revolution of s' and s" their line of conjunction advances through 357° 37, and is, therefore, 2°.23 behind its first position; and that in the case of s" and s", the corresponding line advances through 354° 78, and is, therefore, 5°.12 behind its first position.

8234. Regression of the lines of conjunction of the three satel111.

ual. — But the synodic periods T and T', of s', s", 2577),

T' = 8.525 T'' = 7.050;

asequently the angles of regression of the two lines in in the same time are as

 $2.23 \times 7.050:5.12 \times 3.050::157:156,$

the rate of regression of the two lines of conjuncti . Line of conjunction of the first and second in a

of the second and third.—It follows from this that f conjunction, thus regressing at the same rate, mudined to each other at the same angle. Now it is ation, that this invariable angle is 180°, so that the ction of the first and second satellites is always in it ion to the line of conjunction of the second and the seen from the planet.

shall now see the remarkable consequences of these reflects upon the mutual perturbations of the satell

shall now see the remarkable consequences of these reflects upon the mutual perturbations of the satell b. Effects of their mutual perturbations upon the

bits. — The undisturbed orbits of the first and sec

in conjunction, the eccentricity of the disturbed orbit varies, if . : line of apsides be inclined to that of conjunction, and is only rariable when these lines coincide. Now, in the present case, the entricities of the disturbed orbits are subject to no variation; and follows, consequently, that the lines of apsides of the disturbed pits must always coincide with the lines of conjunction.

3239. Positions of the perijoves and apojoves of the three orbits. But this being admitted, the apsides may be presented in either two opposite directions. If we consider s' as disturbed by s", her the perijove or apojove of s' (as the apsides of the satellites ; called,) may be in conjunction with s". It results, however, m what has been proved, that if the perijove be in conjunction, e disturbing force of 8" will render the ansides of 8' regressive, d if the apojove be in conjunction, it will render that motion ogressive. But since the motion of the apsides of s' is regressive, a perijove must be in conjunction.

If we consider s" disturbed by s', we have the case of an exterior sturbed body, the latter being at a distance from the centre greater

than half that of the exterior body. this case, the motion imparted to the apsides of s" would be progressive, if s"s perijove were in conjunction, and regressive if its apojove were in that position. since the motion of the apsides is actually regressive, the apojove of s" must be in conjunction with s', In the same manner it may be shown,

that in consequenc of the disturbing forces mutually exerted by s" and s", the former must be in perijove and the latter in apo-

jove when in conjunction.

By combining these consequences with the relative positions of the lines of con-junction of s' s" and of s" s" already indicated (3235), it will be apparent that the perijove of s' and the apojove of s", when s' and s" are in conjunction, are in opposition with the perijove of s" and the apojove of s'", when s" and s" are in con-

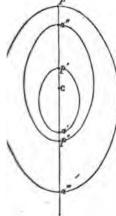


Fig. 855.

inction, so that the relative position of the three orbits in this case that which is represented in fig. 855, where p' is the perijove, and a' the apojove of s', p'' and a'' those of s'', and p''' and a'''ose of s'".

3240. Value of the eccentricity.—Since the motion of the apsides id the eccentricity are exclusively due to the disturbing force, hich in this case is given, the constant value of the eccentricity

pend on the motion of the apsides, that the latter being former may be determined. Now, the regressive motion ides being exactly equal to that of the line of conjunction and therefore the value of the eccentricity can be deter-

centricity which thus arises exclusively from the agency turbing forces, though less than the eccentricities of the ed orbits of the planets generally, is nevertheless not inle, exceeding, for example, that of the orbit of Venus. Remarkable precision in the fulfilment of these laws. parkable laws, of which there is no other example in the m, are fulfilled with such precision, that in the thousands ions of the satellites which have taken place since their not the smallest deviation from them has ever been obcept such as has arisen from the slight ellipticity of the ed orbit of the third satellite. The greatest and most perturbations of the planet or the satellites, provided they gradually, do not interrupt the play of these laws, nor e relation of the motions resulting from them. The effect ting medium will not affect them, though each of these uld alter the motions of all the satellites, and though being that of an interior upon an exterior body (3180), has on the whole the effect of increasing the effective attraction of the central body; and this effect is chiefly due to the action when s" and s" are at or near the line of conjunction; consequently, where that line is near the perijove of s""s undisturbed orbit, the disturbing force of s" is most effective, and, as that line revolves, the angle under it and that of the apsides of s""s undisturbed orbit continually varying, the effect of s"s disturbing force alternately increases and decreases. This is attended with an irregularity in the major axis, and consequently in the mean motion of s" which depends on its synodic position.

The disturbing force of an exterior exerted on an interior body tends, on the whole, to diminish the effective attraction of the central body (3177). It follows, therefore, that s'' exerts upon s' a disturbing force which produces an irregularity depending on the

synodic position of the perijove of s'"s undisturbed orbit.

Each of the small inequalities noticed above, depending on the eccentricity of s'''s undisturbed orbit reacting on the other satellites s' and s'', produce corresponding small inequalities, which if attempted to be introduced in the general theory of the system would render it extremely complicated. Their almost infinitely small amounts, however, render them comparatively unimportant.

3243. Perturbations of the fourth satellite. — The theory of the perturbations produced and sustained by the fourth satellite s''' has nothing in common with that of the three others, inasmuch as no such remarkable commensurability prevails between its mean motion and those of the others. As it sustains small inequalities from the action of the sun similar to the lunar disturbances, so it also produces and sustains a system of inequalities analogous to those of the planets. Thus this satellite s''' presents at once an example on a small scale of the application of the principles of both the lunar and the planetary theories.

To explain the theory of the fourth satellite, we shall first suppose that the undisturbed orbit of s''' is circular, while that of s''' has a sensible eccentricity. We shall assume (what will be more fully explained hereafter) that a slow progressive motion is imparted to its apsides by the spheroidal shape of Jupiter, this motion being such that the apsides make a complete revolution in about 11,000 revo-

lutions of s'".

Owing to the periods not being nearly commensurable, like those of the inner satellite, the line of conjunction of s'' and s''' will, after a few hundred revolutions of the satellites, have assumed every possible direction. Now, since the mutual disturbing action of the two satellites is greatest when the perijove of s''' is at or near conjunction, the question is what will be the form of orbit that will be

on s" by the disturbing force, subject to the condition

entricity being invariable. is evident, from all that has been explained, that if the of s" be in conjunction, the disturbing force of s" will apsides to regress, and the rate of this regression will be the eccentricity is smaller (3151). It may therefore be neutralize the progressive motion which is imparted to les by the spheroidal shape of the central planet, and thereas to render the actual progressive motion of s'"s apsides that s'"'s. But the motion of s'"'s apsides will be also hough in a very slight degree, by the action of s" in the

ssive motion. the increased progressive motion of the line of apsides of nal to the diminished progressive motion of the line of s", this state of the system will be permanent, and thus ressive motion of the apsides of s" will be somewhat and the orbit of s" will have a compression correspondection to the perijove, and an elongation in the same direc-

tion, and will receive from that action a small increase of

e apojove of s'". reasoning we have assumed that the undisturbed orbit of satellite is circular, but similar effects will ensue if it have

ecentricity. next suppose that the undisturbed orbit of s'" is circular, while has a small eccentricity. The disturbing force will be the t the apojove of s", and this will cause the line of apsides of gress; that is to say, it will increase the progressive motion reference to undisturbed circular orbits will be equally applicable to them.

Besides the eccentricity of the undisturbed orbit of s''', it has also an eccentricity impressed upon it by the disturbing force, opposite in kind to that of s'''s orbit; and besides the eccentricity of the undisturbed orbit of s''', it has impressed upon it an eccentricity of the same kind as that of s''''.

In the same manner, the orbits of s' and s" have small eccentricities impressed upon them, similar in their kind to those of s" and s"".

3244. Complicated perturbations of this system.—The inequalities which have been here briefly noticed as produced in the Jovian system, by the mutual perturbations of the satellites, and which are only the principal inequalities of this system, are so closely connected, and so completely entangled, that though they admit of being, for popular purposes, explained under the point of view here presented, it would not be possible to reduce them in this way to computation; a mathematical process of the most abstruse kind, which would, at the same time, include the motions of all the four satellites, would alone be sufficient for this purpose.

Enough, however, has been done if, in what has been said above,

Enough, however, has been done if, in what has been said above, a general idea may be obtained of the theory of these disturbances in the most curious and complicated system that has ever been reduced to calculation.*

CHAP. XXIII.

THEORY OF PLANETARY PERTURBATIONS.

3245. The theory simplified by those of the moon and the Jovian system. — The investigation and solution of the more general and complicated cases of perturbation presented by the mutual action of the planets, will be greatly simplified and facilitated by the previous exposition of the theories of the moon and the Jovian system. The inequalities developed in each of these, are reproduced in very slightly modified forms, in the case of the planets. Thus the terrestrial disturbed by the major planets, present a class of perturbations similar to those of the moon disturbed by the sun. In both cases the disturbing is exterior to the disturbed body; in both, the mass of the disturbing is incomparably greater than that of the

^{*} We are indebted for the substance of some parts of this chapter to the short but excellent tract on Gravitation by Professor Airy, to which we refer readers who may desire further details.

in both, the distance of the disturbing from the central rs a large ratio to that of the disturbed body; and if in theory the mass of the disturbing body be much larger to case of the planets, its distances from the disturbed and odies, bearing also a much larger ratio to the distance of es from each other, the intensity of its disturbing force is not brought into closer analogy with the cases referred to equalities incidental to the three inner satellites of Jupiter, on the near commensurability of their periods, have also rts among the perturbations of the planets, some of the arkable of the planetary inequalities arising from the circle of the periods being very nearly in the ratio of whole as will presently appear.

, other inequalities produced by the gravitation of planet are analogous to those found to prevail between the outer

of Jupiter.

Perturbations of the terrestrial by the major planets.—If se any one of the terrestrial to be disturbed by any one of planets, it will be easy to show that the points at which bed planet and the sun are equidistant from the disturbing at which, therefore, the tangential component of the force vanishes, are in all cases very near the points of

By the application of the same process of investigation as that already adopted in the case of the lunar theory, it will be found that the points P_1 , P_2 , P_3 and P_1 , will have positions very nearly the same as those assigned to them in the case of the moon.

It follows, therefore, that the several vanishing points of the components of the disturbing force, on the position of which the successive phases of the perturbations so mainly depend, are distributed around the synodic orbit of the terrestrial planets as disturbed by the major planets in a manner similar in all respects, to the corresponding points in the lunar theory and periodical inequalities, are accordingly developed in a like order and of a like character, differing only in their limiting magnitudes and the lengths of their periods.

Thus the disturbed orbit is less curved at c and o, and more so at P₂Q and P'₂Q', than elsewhere, so as to acquire an oval form, placed with relation to the line c o similarly to that of the moon, (3196). Its curvature at c is more flattened than at o, (3198). Inequalities affecting the place of the planet in approaching to and departing from syzygies, result from this, similar to the moon's vari-

stion, parallactic inequality, and annual equation.

The line of apsides is affected with a motion alternately progressive and regressive, but on the whole progressive (3215). The disturbed orbit is rendered a little more eccentric, when this line is in quadrature than when it is in syzygies. The effect of the disturbing force on the whole is, as in the case of the moon, to diminish the effective central attraction, and therefore to enlarge in a slight degree the orbit; and this effect is, of course, somewhat greater when the disturbing planet is near perihelion, while the disturbed planet is near aphelion.

It must, nevertheless, be observed, that these and other like periodical inequalities arising from similar causes, are not only smaller incomparably in magnitude, taken within their extreme limits, and slower in their rate of development, than in the case of the lunar perturbations, but that their absolute limits are so extremely parrow, that it is only those which are due to the predominant mass and greater proximity of Jupiter, which are productive of effects great

enough to be appreciable by common observations.

8247. Cases in which the disturbing is in closer proximity with the disturbed planet. — In such cases the same close analogy to the lunar inequalities does not prevail. Nevertheless, even when the disturbing planet, being exterior to the disturbed, lies in comparatively close proximity with it, several of the inequalities manifested in the lunar motions, may still be recognised in a modified form. The vanishing points of the components are somewhat differently distributed in relation to the lines of syzygy and quadrature. The points P2, P2, of equidistance from the disturbing body recode from

and approach the point c of conjunction, and the nts of the radial components P, P', approach conju P'a approach opposition o. The disturbing force, ho tendency to diminish the curvature of the orbit I to increase it near P2 and P2. The general effec diminish the effective central attraction, and conseq the orbit of the disturbed planet. Case in which the disturbing is within the orbit planet.—In these cases the general effect of the dist be traced without difficulty, by the method expla In these cases the general effect of the disturbing ! nt the effective central attraction, and conseque the magnitude of the orbit of the disturbed planet. Perturbation affected by the position of the apsid relation to the line of conjunction. - In the genera f the planetary perturbations it is necessary to c effect produced by the disturbing force in each

n relation to the lines of nodes and apsides, and wind position.

orbits of the disturbing and disturbed planets were do in a common plane, the effect produced by the dist

will necessarily depend on the position of the

inclined to the lines Ms and Ps would be always the same. All the conditions, therefore, which can affect the intensity and direction of the disturbing force, would be absolutely identical; and it follows consequently that, no matter what may be the directions of the lines of syzygy and quadrature, the disturbing force during each synodic revolution would pass through precisely the same changes of intensity and direction, and consequently produce precisely the same effects upon the orbit of the disturbed planet.

If, however, the orbits, being still in a common plane, be either or both of them ellipses, the same identity of effects of the disturbing force during a synodic revolution will no longer prevail.

Let it first be supposed that the orbit of the disturbing planet M, figs. 859, 860, is circular; and that of the disturbed, elliptical. Let p be the point of perihelion, and a that of aphelion, p' and a' being the places of M corresponding to these points; and let m, n be the points at right angles to p, m' and n' being the corresponding positions of M.

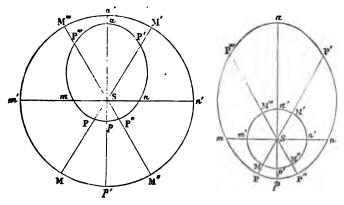


Fig. 859. Fig. 860

Upon comparing the varying distance of M, whether it be outside the orbit of P, as represented in fig.~850, or within it, as represented in fig.~860, it will be evident that the effects of the disturbing force, during a synodic revolution, will be subject to a variation with the varying angle formed by the radius vector Ms of the disturbing planet with the direction ps of the perihelion of the disturbed planet. Thus, when M, being outside P's orbit, is at a', it is evident that its distance from P, in any proposed synodic position, will be much less than its distance from P in the same synodic position when M is at p'; and consequently the effect of the dis-

ree during a synodic revolution when M is at a', is much an when M is at p'; and the same may be said of any two esitions, such as M and M', or M" and M", which the disanct can assume.

ovious, the like observations are applicable to the rase d in fig. 860, in which M is within the orbit of P. t only are the effects of the disturbing force different in nitude according as the radius vector of M takes different with relation to the line ps, but they are also different in ction. The position of the vanishing points of the comf the disturbing force, and the distribution of the mes hich they are alternately positive and negative round the he disturbed body, depend solely on the direction of the yzygy and quadrature; but the effects which these comroduce upon the different elements of the elliptic orbit of upon the position of these several arcs with relation to In some positions the effect of the disturbing apsides. complete synodic revolution, will be to augment, in others sh, one or other element; and in positions in which the ents are augmented or diminished, they will be augmented hed in different degrees, according to the angle which the njunction (that is, the line passing through P and M when

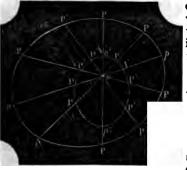


Fig. 861.

during each such revolution, will vary with the angle at which the line of conjunction is inclined to the line of nodes.

It will, therefore, be apparent that, in each position which the line of conjunction nay assume with relation as well to the line of apsides as to the line of nodes, the disturbing force will, in each synodic revolution, produce a certain change, either by progression or regression, by increase or diminution in the ele-

nents severally of the disturbed orbit, the magnitude of which will lepend on such position, so as to be always the same for the same position, but generally different for different positions; and when such positions are in extreme opposition, the effects of the elements severally are often also contrary in their character, so as mutually to lestroy or compensate each other either wholly or partially, the propression or increase resulting from the effect of the disturbing force none position being compensated, wholly or partially, by an equal representation or decrease in the opposite position of the ine of conjunction.

It follows from this that, if the motions of two planets were so elated that the line of conjunction should always have the same sosition with relation to the lines of apsides and nodes, the effect of he disturbing force on each of the elements, in each synodic revontion, would be always the same; and the consequence would be hat, after the lapse of a considerable number of such revolutions, he changes produced in each revolution accumulating, an alteration the form and position of the disturbed orbit would be produced to great as completely to disturb the physical conditions of the planet and derange the harmony and order of the system.

But even though the place of the line of conjunction should not be rigorously the same after each successive synodic revolution, if nevertheless it be subject only to a small change of position, it is evident that the change in the character and magnitude of the effects of the disturbing force on the elements will be proportionally small; and that, therefore, such effects will continue to accumulate and to augment the variation of each of the elements of the disturbed what in the same direction, until by the long continuance of the slow thange of position of the line of conjunction, that line at length bifts its direction so as to take up a position in which a contrary

be produced upon the elements. The variation of these then change; what was previously increase will become and vice versa; and this will continue until the line of n, still slowly shifting its position, again resumes the avourable to the former change of the elements.

manner inequalities may be produced, of which the period f great length, but which, nevertheless, depending essenbe direction of the line of conjunction, and therefore on uration of the disturbing and disturbed planets, are still and not secular variations. Since, however, the motions e of conjunction on which they depend, are, in all the his class presented in the solar system, extremely slow, quently the periods of these inequalities are incomparably racted than those which arise from the varying synodic of the disturbed and disturbing planets, they have been ted by astronomers as the "long inequalities;" and the of some of them by theory, before their detection by obbas constituted one among the many triumphs of physicoical science.

Method of determining the change of direction of the line ction. — From all that has been just explained it will be

- (2568), the angle e, which it describes in the time T, will be

$$\phi = \frac{860^{\circ}}{P'} \times T = 860^{\circ} \times \frac{P}{P' - P}$$

This is, then, the angle, measured in the direction of the planet's motion, through which the line of conjunction advances in each synodic revolution.

8251. Condition under which the direction of the line of conjunction is invariable. - If the line of conjunction has always the same direction, it is evident that in a synodic revolution both planets must have made a complete number of revolutions, and consequently the angle ϕ must either be 360° or some exact multiple of 360°. If $\phi = 360^\circ$ we shall have P = P' - P (2548), and, therefore, $\mathbf{p}' = 2 \, \mathbf{p}$. In that case, while the exterior planet makes a single revolution, the interior makes two; so that, after each revolution of the exterior planet, the two planets come into conjunction always at the same point. In this case it is evident also, that the synodic time is equal to the periodic time of the exterior planet. If $\phi = 2 \times 360^{\circ}$, we shall have P = 2 P' - 2 P, and, therefore,

8 P = 2 P'. In that case, while the exterior planet makes two complete revolutions, the interior makes exactly three, and the synodic period is equal to twice the periodic time of the exterior

planet.

If $\phi = 3 \times 360^{\circ}$, we shall have P = 3P' - 3P, and, therefore, 4 P = 8 P. In that case, therefore, the conjunctions are reproduced at the same point, after every three complete revolutions of the exterior planet.

In general, if $\phi = n \times 360^{\circ}$, $P = n \times P' - n \times P$, and, therefore, $(n+1) \times P = n \times P'$, and the conjunctions are reproduced constantly at the same point, after n revolutions of the exterior, and

+ 1 revolutions of the interior planet.

The general condition on which the line of conjunctions shall have one invariable position, therefore, is that the periodic times of the two planets shall be such as can be exactly expressed by two whole numbers, of which the greater exceeds the less by 1, such as 1 and 2, 2 and 3, 3 and 4, &c.

8252. To determine the condition under which the line of conjunction shall have a limited number of invariable positions. — Although the conjunctions may not be always reproduced at the same point, they may take place invariably at two, three, or more fixed points.

If $\phi = 180^{\circ}$, they will take place invariably at two points which are diametrically opposed to each other. In that case, we shall have 2P = P' - P (3250), and, therefore, P' = 8P and $T = \frac{1}{4}P'$. To comprehend the motions of the planets in this case, let E and I



Fig. 862.

(fig. 862) be their positions at any proposed conjunction. The angular motion of I being three times that of E, while the latter moves from E to E' through a semicircumference, I moves through three semicircumferences, and, therefore, through the whole circumference II'I, and after that through the semicircumference II', overtaking the exterior planet at i', where, therefore, the next con-junction takes place. In like manner, the succeeding conjunction will take place at SIE, and the next at s I' E', and so on, no conjunction

ible except in these two lines.

120°, or a third part of the circumference, the conjuncbe reproduced continually in three fixed directions, he circumference into three equal parts. In this case, 3 P = P' - P, and, therefore, P' = 4 P, and $T = \frac{1}{2} P'$. To explain the motion in this case, let SIE (fig. 863.) be the



in any proposed number n of fixed directions, it will be necessary that the period P shall be exactly n+1 times the period P. In that case the synodic time T will be n times P; and the fixed directions in which the conjunctions will succeed each other, will divide the circumference into equal arcs or angles, the magnitude of which 860°

will be $\frac{300}{n}$.

8258. Effects of the disturbing force in cases of commensurable periods. — It follows from what has been explained (8249), that in such cases the effects of the disturbing force would accumulate indefinitely, without compensation or with imperfect compensation, through an indefinite succession of synodic revolutions. If, for example, P'= 2 P, and therefore the conjunctions would always take place in the same line, the line of conjunctions being always inclined to the line of apsides at the same angle, the effect of the disturbing force on the several elements, in a synodic revolution would be always exactly the same, and would, therefore, accumulate indefinitely from revolution to revolution.

If r'=3 P, the lines of conjunction would have three, and only three, different positions in relation to the line of apsides; and although the effects of the disturbing force in a synodic revolution in these three positions would be different, and some of them would necessarily have contrary signs, and would produce, therefore, more or less compensation, such compensation would be imperfect; and after each series of three conjunctions, a residual inequality would remain, affecting each of the elements which, as before, would accumulate indefinitely during an indefinite succession of synodic revolutions.

In the same manner, if P' were any other exact multiple of P, the series of conjunctions which would take place in the directions of the fixed lines dividing the circumference into equal parts would still be imperfectly compensatory, and residual quantities would, as before, remain uneffaced, which would accumulate indefinitely.

In order that the conjunctions should take place always in certain fixed directions, it is not necessary that the periodic time of the exterior planet should be an exact multiple of that of the interior. The same will happen, if any exact multiple of one of the periods be exactly equal to an exact multiple of the other, or in other words, if the periods be commensurable. Thus, if 2 P' = 5 P, it is evident that, counting from the epoch of any one conjunction, another will arrive in exactly the same place after every two complete revolutions of E, and every five of E. But, between these others will take place at fixed intermediate positions, for we should have

$$\frac{\mathbf{P}}{\mathbf{P'}-\mathbf{P}}=\frac{2}{5-2}=\frac{2}{3};$$

quently,

$$\phi = 360^{\circ} \times \frac{2}{3} = 240^{\circ}$$
.

ase, the lines of conjunction would be distributed in the mer as when P' = 4P, but the conjunctions would not precisely the same manner. After the conjunction which he in the line SIE (fig. 858), would succeed that which he line SI'E', and the third of the series would take the line SI'E'; the fourth, or the first of the next series, are in the line SIE.

see in the line S T E.

suing this method of reasoning, it will be easily seen that,
es in which the periods of the two planets would be in the
io of two whole numbers m and n, the conjunctions would
succeed each other in certain fixed lines. We should, in

$$\frac{\mathbf{P'}}{\mathbf{P}} = \frac{m}{n}, \ \frac{\mathbf{P}}{\mathbf{P'} - \mathbf{P}} = \frac{n}{m - n};$$

quently,

Suppose, for example, that in the case of exact commensurability the positions of the lines of conjunction after each series of three synodic revolutions were SIE, SI'E', and SI'E', as represented in fig. 863, and suppose that the deviation of the periods from exact commensurability is such that the second conjunction, instead of taking place at E', shall take place at α' . If $\alpha'' E'' = 2 \alpha' E'$, the third conjunction will take place at α'' ; and if $E \alpha''' = 8 E' \alpha'$, the next conjunction will take place at α''' , and so on.

If, then, the distance of E be very small, which it will be if the periods are very nearly commensurable, the lines of conjunction, though not rigorously in fixed directions will, for a considerable number of successive synodic revolutions, crowd about those fixed directions which they would have rigorously assumed if the commensurability had been exact, and during that interval, which, when the synodic time is of much length, will be of great duration, nearly the same inequality will be produced by the want of compensation in the effects of the disturbing force as if the directions of the line of conjunction were fixed.

But, however small the advance a' E' of the line of conjunction in each synodic revolution may be, its continued accumulation through a long succession of synodic revolutions will carry that line at length round the whole circumference, causing it in slow but regular and inevitable succession to take all directions with relation to the lines of apsides of the two orbits. When it has made half a revolution, or revolved through 180° , it will have precisely the opposite position with relation to these lines, and the disturbing force will produce contrary effects upon the elements of the disturbing the orbit; and while the line of conjunction revolves through the other half revolution, the disturbing force, for like reasons, produces a series of effects on the elements which are the opposite to those it produced during the first half revolution.

3255. Long inequalities. — Hence, obviously arise a group of inequalities, affecting the elements severally of the disturbed orbit, the periods of which will correspond with the revolution of the line of conjunction.

What has been said of the varying position of the line of conjunction in relation to the line of apsides, will affect the inequalities of the major axis, the motions of the apsides, and the eccentricity. The varying position of the same line with relation to the line of nodes, will in like manner affect the motion of that line and the variation of the inclination.

Having thus explained in general the principle which determines the successive phases of the LONG INEQUALITIES of the planets, we shall now briefly notice some of the most remarkable of these phenomena.

Long inequality of Jupiter and Saturn.—By (2984) it will be seen that the periodic times of Saturn and

 $p' = 10759 \cdot 2198$. $p = 4332 \cdot 5848$, quently,

$$\frac{P'}{P} = 2.48325 = \frac{5}{2} - 0.01675,$$

th it appears that five times the period of Jupiter exceeds of Saturn by a small fraction. Now, if 2 p' were exactly 5 p, the conjunctions would invariably take place in three ngles of 120°, (3253). But since

$$\phi = 360^{\circ} \times \frac{P}{P'-P} = 242.7^{\circ},$$

that in the series of three successive conjunctions in line would assume the three directions at angles of 120°, eriods were exactly commensurable, it advances beyond ections successively by the angles, $2 \cdot 7^{\circ}$, $2 \cdot 7^{\circ} \times 2 = 5 \cdot 4^{\circ}$, $3 = 8 \cdot 1^{\circ}$, so that, after making a single revolution in odic periods, it advances $8 \cdot 1^{\circ}$ beyond its first position;

series of inequalities will be produced upon the elements of the two orbits, which will go on increasing or decreasing for a period of 440 years, and will undergo the contrary variation, decreasing or increasing during the succeeding 440 years.

As already observed, however, it must not be assumed, in this or any like case, that the compensation produced by the contrary effects in the two intervals is necessarily complete, and that the increase effaces completely the decrease, or vice versit. Such a perfect equilibrium between the effects of the perturbations rarely takes

place.

8258. Its effect upon the major axis and periods. — One of the long inequalities resulting from this relation between the mean motions of the planets, affects the major axes of their orbits, and consequently their periodic times. The major axis of one orbit increases, and that of the other decreases, continually for 440 years, and during the next 440 years the former decreases and the latter increases. The consequence of this is that the mean motion of one planet continually increases, and that of the other continually decreases, during periods of 440 years. Although the changes produced upon the axes from this cause are so minute as to be scarcely appreciable, that of Saturn's orbit amounting when greatest to only the 1350th, and that of Jupiter's to the 8550th part of its length, the effects produced upon the motions of the planets are very considerable, the place of Saturn being affected to the extent of 48', and that of Jupiter to 21'. The greatest inequality of any other planet does not affect its place to a greater extent than 8'; and those which are within Jupiter's orbit are much less affected, being never removed from their mean place by so much as half a minute.

3259. Its effects upon the eccentricities. — It appears that, during the interval in which the line of conjunction moves through 120°, the eccentricity of each of the two orbits increases, attains a maximum magnitude, and then decreases. The effect produced upon the planet's distance from the sun by the change of eccentricity is much more considerable than the effect produced by the change in the magnitude of the major axis. In the case of Jupiter it amounts to the 1230th part of the entire distance, and in the case of Saturn to the 314th part.

8260. Effect on the direction of the apsides. — The effect upon the motion of the apsides is subject to a like period. A progressive motion is imparted to them for 440 years, and a regressive motion for the next 440 years. Between this motion of the apsides and the variation of the eccentricity of each orbit, there is a necessary relation; the eccentricity of each orbit having its mean value, when the progressive or regressive motion of the apsides has attained its

ad when the eccentricity is at its maximum or minimum, es arrive at their mean places.

ong inequality of Jupiter and Saturn is a phenomenon of ble historical celebrity and interest, owing to the apparent ty which it explained, having been observed long before was discovered, and having given great perplexity to as a lts cause was demonstrated and the whole character of the phenomenon explained by Laplace, in 1785.

Long inequality of Venus.—Next to that which has been ced, the most remarkable inequality of this class is the uality of Venus, arising from the near commensurability eriods of that planet and the Earth. If P and P express iods, we shall have (2984,)

$$\frac{P'}{P} = \frac{365 \cdot 256}{224 \cdot 701} = 1 \cdot 6255 = \frac{13}{8} - 0 \cdot 0005.$$

P exceeds 8 P by 0.004 P, that is, by the 250th part of P. ermine the value of \$\phi\$, we have

$$=360^{\circ} \times \frac{1}{0.6255} = 575.53^{\circ} = 576^{\circ} - 0.47^{\circ}.$$

p' were exactly equal to 13 p. each successive conjunction

to which our knowledge of the planetary motions has been carried by the application of the principles of the theory of gravitation.

3262. Other long inequalities. — There are several other inequalities of this class, incidental to the other planets, which need only be indicated here, their investigation and exposition being precisely similar to these already explained. Thus in the case of Mercury and the Earth

$$\frac{\mathbf{r'}}{\mathbf{P}} = \frac{365 \cdot 256}{87 \cdot 969} = 4 \cdot 15 = 4 + 0 \cdot 15;$$

so that the one period is but a little more than four times the other. This produces an inequality whose period is about seven years.

In the case of Venus and Mercury we have

$$\frac{\mathbf{r}'}{\mathbf{p}} = \frac{224.701}{87.969} = 2.55 = \frac{5}{2} + 0.05.$$

In the case of Mars and Venus

$$\frac{\mathbf{P'}}{\mathbf{P}} = \frac{686.979}{224.701} = 3.057 = 3 + 0.057.$$

In the case of Uranus and Saturn

$$\frac{\mathbf{r'}}{\mathbf{P}} = \frac{30687}{10769} = 2.85 = 3 - 0.15.$$

In the case of the Earth and Mars

$$\frac{\mathbf{p'}}{\mathbf{p}} = \frac{686.979}{365.256} = 1.88 = 2 - 0.12.$$

In each of these cases long inequalities are produced, the periods of which may be determined by the method already explained.

\$263. Long inequalities of the nodes and inclination.—The variation of the motion of the line of nodes and of the magnitude of the inclination, consequent upon the changes of position of the line of conjunction, in all cases of near commensurability of the periods, are so exactly similar to the changes already explained, of the line of apsides and the eccentricity, that it is only necessary here to observe that, mutatis mutandis, all that has been explained of the one is applicable to the other.

8264. Secular inequalities. — The inequalities noticed in the preceding paragraphs, have been exclusively those whose periods are determined by the variation of the relative positions of the disturbing and disturbed planets, or by what has been called their configuration; and which are denominated periodical inequalities, not because all other inequalities are not also periodical, but because the periods of the former are of much more limited length, and excepts

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of the long inequalities, such as may be in general comhin the limits of astronomical records. The other class of s are those which are from the continual accumulation of hal phenomena, which remain uncompensated after the and disturbed bodies have passed through all their phases ration, and recommence to pass through a like series of sitions; these are the SECULAR INEQUALITIES.

Secular constancy of the major axes.— No result of the of mathematicians in physical astronomy has excited so so just an admiration, as the discovery of the fact that, the major axes of the orbits of the planets are subject to iodical variations, which cause their periodic times and tions to oscillate within narrow limits round certain mean t that the mean values of these axes are, in the long run, invariable and subject to not the slightest variation from , and cannot be subject to any, so long as the solar system erfered with by any agencies, save those which have play a bodies, great and small, which compose it.

portance of this theorem, and the interest with which its demonstration must be regarded, will be understood when sidered that, upon the magnitude of the major axis of can it would be in the absence of the disturbing force; but in oth cases, so long as the mean effective central attraction remains see same, the mean value of the major axis of the orbit will be intriable.

If we take an interval of time so great that each of the planets ill have assumed, with relation to the other, every possible relave position, it will follow that the mean value of the radial comment of the disturbing force corresponding to any proposed point, , of the orbit of the disturbed planet, during such interval, will be and by taking a mean of the radial components of all the disturbig forces exerted by the disturbing planet in all the points M of s orbit upon the disturbed planet at the proposed point; for at one me or other in the assumed interval, provided it be sufficiently reat, the disturbing planet must have been found at each of the oints of its orbit, the disturbing planet being at the same moment If, then, we imagine the radial components of the disturbig force exerted by the planet M, at each of the points of its orbit pon the disturbed planet at the point P, and if we take the mean f all these components by dividing their sums by their number, ne mean will be the mean value of the radial component of all ne disturbing forces exerted by the disturbing planet upon the disarbed planet, when the latter was found at the point P during the Now, it is quite evident that this mean value saumed interval. nust always be the same.

In the same manner, the mean value of the radial component for very other position of the disturbed planet may be found, and it will be apparent that the mean effect of the disturbing force estimated in the direction of the radius vector at each point of the rbit of the disturbed planet, is always the same, and consequently he effect produced by this component on the major axis is always he same. So far, therefore, as relates to this component of the isturbing force, the mean value of the major axis taken in an inserval of time so great that the two planets will have assumed with elation to each other every possible position in it, is subject to no altimate variation.

Secondly. The effects of the tangential components are most asily explained, by considering the whole attractive forces which he disturbing planet exerts upon the sun and upon the disturbed lanet. It will be remembered, that the disturbing force exerted by M on P, is the resultant of the attractive force exerted by M on P and a force exerted on P, equal and opposite to the attractive force which M exerts on S. Now, if we take M successively at every coint of its orbit, and find its attractive force on S, it will be apparent that the resultant of all these forces directed from S towards M, will be in equilibrium, and therefore, compensatory. It follows.

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III.

that the forces equal and opposite to those which are act on P, must also be compensatory.

ins, therefore, only to investigate the total effects of M's on P, in all the positions which the two bodies can

be supposed to be at any given point of its orbit, and let P t every point of its orbit. These are positions which are sively assumed in the motions of the two bodies; but they ns which at some times in the assumed interval they must nat interval be assumed of sufficient length; and as our ject is to obtain the aggregate effect of the forces during interval, the order in which they are exerted is immatew, if P be thus supposed to make a complete revolution paintains its position, it will follow, from a general prinphysics, that, when it returns to its primitive place, after g a revolution, it will have exactly the same orbital when it started from that place. It follows, therefore, ffects of the tangential component of M's attraction in acit during its revolution must have been precisely equal ects of the same component in retarding it. wn (3154.) that every such acceleration produces an ind every such retardation a diminution, of the major axis bit. It follows, therefore, that in such a revolution, the s and decrements of the major axis would be equal, and a compensation would be effected.

he same will be true for every position whatever which M he in its orbit, and it will therefore follow, that if, while M be realised in the actual motions which have been here shown to take place in the supposed motions.

It will doubtless be objected to this reasoning, that we have supposed each planet to make its revolution in an orbit of fixed magnitude and form, without allowing for the displacement which the disturbing force itself must inevitably produce during each revolution, which, though very small, is not quite inappreciable. however, has been taken into the account in some mathematical

researches, and it does not appear to affect the conclusion.

What is true in this reasoning of the effect of the disturbing force of any one planet upon another, will be equally true of all the planets, primary and secondary, on that other; and it may, therefore, be inferred, in general, that the major axes of the planetary orbits are not subject to any secular variation, and that in the course of ages the periods and mean motions, which by the harmonic law depend on the major axis, can never suffer any per-

manent change.

3266. Secular variation of the apsides. — It has been shown that the change of position of the apsides in a synodic revolution, depends on the position of the line of conjunction with relation to the perihelion of the disturbed orbit, but in an interval of time so long as to allow the line of conjunction to assume all possible positions, all possible effects will be produced upon the apsides. magnitude of these effects will vary with the varying distance of the disturbing planet from the disturbed orbit. The greatest effect will obviously be produced at those parts of the disturbed which are nearest to the disturbing orbit; and in taking a mean of all the variations of the apsides during the entire interval these effects will predominate, so that it may be assumed that the final residual effect upon the apsides, will be identical in its character with the effect produced in those conjunctions which take place at the points where the two orbits are nearest to each other.

The position of these points will evidently depend upon the relative magnitude of the two major axes, their relative position, and

the eccentricities of the two orbits.

If that half of the disturbed orbit, in the middle of which aphelion is placed, be nearer than the other half to the orbit of the disturbing planet, the secular motion of the apsides will be progressive; if it be more remote, the motion will be regressive. the position of the orbits be such that both halves are equidistant from the orbit of the disturbing planet, there will be no secular variation of the apsides.

The secular motion of the apsides will continue to have the same direction, until their change of relative position shall alter the conditions and render them stationary, or reverse the direction

of the motion.

Secular variation of the eccentricity.—The secular effect turbing force upon the eccentricity of the disturbed orbit, at of the apsides, similar in character to the effect produced oints of the disturbed orbit, which are nearest to the distribit. The eccentricity will accordingly, on the whole, rease or decrease, or suffer no change, according to the of the perihelion of the disturbed orbit at those points a two orbits are in greatest proximity, and it will continue cted in the same manner, until the conditions are changed cular change of the apsides.

place where the two orbits are in closest proximity, both re in general moving either from aphelion to perihelion, or ary, so that one eccentricity is increasing and the other de-

cular variation of the eccentricities, if it continued to take the same way, either always increasing or always decreasing, ter a period of time of great length, but still definite, so s to derange in a serious degree the economy of the system, xpose the planets to such vicissitudes of temperature as incompatible with their well-being, not to mention other derangement which would attend such changes. It is therefore, that the nodes of P's orbit must secularly regress upon m's orbit.

It is necessary, nevertheless, to bear in mind that this secular regression on the orbit of the disturbing planet does not infer its regression on other places. A regression on one place may cause a progression of the nodes of the same orbit with another plane.

3269. Secular variation of the inclination.—If the orbits of both planets were absolutely circular, the periodical inequalities of the inclination would be exactly compensatory, and there would, therefore, be no secular variation of that element; for in such case at points equally distant from the point which is most remote from M, M exerts equal disturbing forces on the inclination, one tending to increase it, and the other to decrease it.

But if the orbits be elliptic, a certain point can be determined where the effect of the orthogonal component of the attracting force of M on P is greater than at any other point, and the total effect produced on the inclination by M taken in every part of its orbit, on P taken in every part of its orbit, in all positions of the line of conjunction with relation to the line of nodes, will be similar in character to this maximum effect; and such will be the character of the secular variation of the inclination.

The observations, however, which have been made (3267), respecting the limits within which the secular variation of the eccentricities are confined, are equally applicable to the inclinations. These also, though they may severally increase continually (subject to their periodical oscillations), for thousands of years, will necessarily decrease continually for periods of like duration, and the limits within which this secular oscillation is confined are in all cases extremely narrow.

3270. Laplace's theorems of the relations between the eccentricities and inclinations of the planetary orbits.—The researches of Laplace have led to the discovery of a beautiful mathematical relation which prevails between the eccentricities and inclinations of the planetary orbits, which may be easily comprehended without any profound mathematical knowledge, although its demonstration does not admit of exposition on principles sufficiently elementary to allow of its introduction here.

THEOREM.

"IF THE NUMBERS WHICH EXPRESS THE SQUARE OF THE ECCENTRICITY AND THE SQUARE ROOT OF THE SEMI-AXIS MAJOR OF EACH OF THE PLANETARY ORBITS BE MULTIPLIED TOGETHER, AND THEIR PRODUCT BE MULTIPLIED BY THE NUMBER WHICH EXPRESSES THE MASS OF THE PLANET, THE SUM OF ALL SUCH PRODUCTS FOR ALL THE PLANETS WILL ALWAYS BE THE SAME, NOTWITHSTANDING THE SECULAR VARIATION OF THE ECCENTRICITY."

This celebrated theorem may be conveniently and very concisely

the supposed satellite is close to the surface, its distance centre is the earth's semi-diameter; and since the moon's sixty semi-diameters of the earth, we shall have

$$\frac{r^3}{r'^3} = \frac{1}{60^3};$$

m = 655.73 hours (2470), it follows that p = 3.613

'satellite would be subject to the disturbing action of the a would produce in its orbit inequalities similar in kind to, ent in magnitude from, those produced by the sun's discree on the moon's orbit. Its nodes, that is, the equinoctial asmuch as its orbit is by the supposition the plane of the would receive a slow regressive motion; and its inclinatis, the obliquity of the ecliptic, would be subject to a varie period would depend on that of the successive returns to the same equinoctial point.

tellite would also be subject to the disturbing action of which would affect it in a manner nearly similar; since, se, also, the disturbing body would be exterior to the dis-It would impart to the line of nodes of the supposed that is, to the intersection of the plane of its orbit with

CHAP. XXIV.

THEORY OF SPHEROIDAL PERTURBATIONS.

3272. Attraction of planets would be central if their forms were exactly spherical.—In the preceding investigations of the effects of the reciprocal attractions of the bodies composing the solar system, the attraction exerted by each of these upon the others, is considered to emanate from its centre in all directions around it, as luminous rays would from a radiant point. This would be strictly true if the gravitating bodies were all spherical; since it is a property of a sphere that the matter composing it, supposing it to be either uniformly dense, or to have a density varying according to some fixed law depending on the distance from the centre of the mass, exercises on all distant bodies exactly the same attraction as if its entire mass were concentrated at its centre.

But if the attracting body be not spherical, this will not be true; and accordingly the attraction exerted by any such body, must be

investigated with especial reference to its form.

3273. Disturbing forces consequent on spheroidal forms. — Now, although the planets generally, including the earth, are very nearly, they are not exactly, spherical, as has been already explained. The ellipticity of these spheroids, though too inconsiderable to produce any sensible effect upon their mutual attractions, or to require to be taken into account in any analysis of their perturbations, is nevertheless sufficient to produce very sensible effects on the mutual attractions of the spheroidal planets and their satellites, and even upon the phenomena resulting from the central attraction of the sun exerted upon them.

These effects are manifested in the motions of the planets themselves by periodical changes in the position of their axes of rotation, and in their satellites by similar changes in the elements of their

orbits.

It is these effects that we denominate SPHEROIDAL INEQUALI-

TIES; the name indicating their physical cause.

3274. Effects which would be produced if a satellite were attached to the surface of the earth at the equator. — If the earth were attended by a second satellite, revolving close to its surface and in the plane of its equator, its periodic time would be less than that of the moon, in a ratio which is easily ascertained by the harmonic law. Let m express the moon's period, r' its distance, p the period of such a satellite as is here supposed, and r its distance from the earth's centre. We should then have

$$\frac{p^2}{m^2}=\frac{r^3}{r'^3}.$$

 $\frac{50\cdot 1}{147\cdot 8''} = 0.33898 = 20 \quad 20\cdot 3,$

leting its revolution.

quinoctial and sidereal year. — Hence is explained the appears in (2984), Table II., that while the sidereal nal revolution of the earth round the sun, is

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of M

days days hrs. min. sec. 365.25637 = 365 6 9 10.38,

tial revolution, or the time between two successive equie same name, is

 $\frac{\text{days}}{365 \cdot 242255} = \frac{\text{days}}{365} = \frac{\text{brs}}{5} = \frac{\text{min.}}{5} = \frac{\text{sec.}}{5}$

peing less than the former by 20^m· 20ⁿ·.

cessive returns of the sun to the same equinoctial point

efore, always *precede* its return to the same point of the

20^m· 20ⁿ of time, and by 50·1" of space.

Period of precession.—To determine the period in which ctial points moving backwards constantly at this mean make a complete revolution of the ecliptic, it is only to find how often 50.1" must be repeated to make up what is the same, to divide the number of seconds in 360°

This gives

included between them will obviously be equal to the angle under the equator and ecliptic; and since the extremities of these diameters are the poles of the equator and ecliptic, it follows that the arc of the heavens included between these poles is equal to the obliquity of the ecliptic.

But since a plane passing through these diameters is at right angles both to the equator and ecliptic, the line of equinoxes or the intersection of the planes of the equator and ecliptic, will be at right angles to that plane. If, therefore, the equinoctial points revolve round the ecliptic in a retrograde direction, it follows that the plane passing through the diameters above mentioned, and through the poles of the two circles to which the line joining these points is at right angles, will revolve with a like motion, round that diameter of the sphere which is at right angles to the plane of the ecliptic, and which therefore terminates in its poles. But since the pole of the ecliptic equal to the obliquity of the ecliptic, it follows that the pole of the equator will be carried round the pole of the ecliptic, in a lesser circle parallel to the plane of the ecliptic, with a retrograde motion exactly equal to that of the equinoctial points.

3282. Distance of pole of equator from pole of ecliptic varies with the obliquity.—And since the distance of the pole of the equator from that of the ecliptic must always be exactly equal to the obliquity of the ecliptic, it follows that every change which may take place from whatever cause, in the position of the plane of the equator, whether the change affect the angle at which it is inclined to the ecliptic, or the position of the equinoctial points, must be attended with a corresponding change, either in the apparent distance of the pole of the equator from that of the ecliptic, or in the rate or direction of the motion of the latter round the former.

3283. Pole star varies from age to age.—As the pole of the equator is carried with this slow motion round the pole of the ecliptic, its position for all popular, and even for some scientific, purposes is usually indicated by the nearest conspicuous star, for it rarely happens that any such star is found to coincide with its exact place. Such star is the pole star, for the time being; and it is clear from this motion of the pole, that the pole star must necessarily change from age to age.

The present polar star is a star of the second magnitude in the constellation called the "Lesser Bear," and its present distance

from the exact position of the pole is 1° 24'.

The motion of the pole as above described, however, is such that this distance is gradually diminishing, and will continue to diminish until it is reduced to about half a degree; after which it will increase, and after the lapse of a long period of time, the pole will

om this star, and it will cease to bear the name, or serve

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oses, of a pole star.

Former and future pole stars. - If upon any star-map a traced round the pole of the ecliptic at a distance from it such circle will pass through all positions which the pole uator will have in time to come, or has had in time past; ll then be easily seen which are the conspicuous stars in ighbourhood it will pass in after ages, and near which it d in past ages, and which will become in future, or have ast times, the pole star of the age. 000 years from the present time, for example, it will be

it the pole will pass within a few degrees of the star of the nitude in the constellation of "Lyra," called a Lyrae. cing back in the same manner the position of the pole e stars, it is found that at an epoch 3970, or nearly 4000 fore the present time, the pole was 55° 15' behind its osition in longitude; and at this time the nearest bright was the star y, in the constellation of "Draco." The of this star, at that time, from the pole must have been

Remarkable circumstance connected with the pyramids.searches which have been made in Fount

change of place produced by the disturbing forces of the sun and moon upon the protuberant matter of the equator in long periods of time. But this regression is not produced at a uniform rate. The disturbing forces vary in their action according to the general principles already explained, with the angles formed by lines drawn from the sun and moon to the centre of the earth with the plane of the equator. So far as relates to the sun, this variation in its effect goes through all its changes within a year. In the case of the moon, it will obviously vary from month to month and from year to year, with the change of position of the moon's nodes; and as these nodes have a regressive motion making a complete revolution in about nineteen years, the variation of the effect of the moon's disturbing force will pass through all its changes within that period. The regressive motion imparted to the equinoctial points, and also to the pole of the equator in moving round the pole of the ecliptic. as already described, by the sun and moon, is therefore subject to an alternate increase and decrease, whose period is a year for the sun, and nineteen years for the moon.

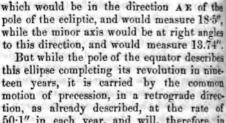
But these are not the only effects produced upon the position of the pole of the equator by the disturbing action of the moon and sun. According to what has been explained in general of the effects of the orthogonal component of the disturbing force, it will be easily understood that the protuberant matter of the equator being regarded as a satellite disturbed by the sun and moon, the inclination of the plane of the equator to the ecliptic will be subject to a variation proceeding from the disturbing force of the sun, whose period will be a year; and its inclination to the plane of the moon's orbit will be subject to a like variation, whose period is about nineteen years. These changes of the inclination of the plane of the equator to that of the ecliptic and the moon's orbit will be attended with a corresponding motion of the pole of the equator to and from the pole

of the ecliptic.

This alternate approach and recess of the pole of the equator to and from the pole of the ecliptic, combined with the alternate increase and decrease of its regressive motion, is called the Nutation; that part of it due to the sun being called the solar nutation; and that due to the moon, the lunar nutation.

The solar nutation is an inequality of so small amount as altogether to escape observation, and therefore must be looked upon to have a merely theoretical existence.

It is otherwise, however, with the lunar nutation. alternate increase and decrease of the regressive motion of the pole, combined with its alternate approach and recess to and from the pole of the ecliptic, the pole is moved in such a manner that, if it were affected only by the disturbing force of the moon, it would describe an ellipse such as ABCD, fig. 864; the major axis of



then years, it is carried by the common motion of precession, in a retrograde direction, as already described, at the rate of 50·1" in each year, and will, therefore, in nineteen years be carried through 15·5' in its motion round the pole of the equator. Now, by combining this motion with the elliptic motion already described, it will be easily seen that the pole of the equator would, in revolving round the pole of the ecliptic, alternately approaching to it and receding from it through 9·25", describe an undulating line such as is represented in fig. 865, where P represents the pole of the ecliptic.

3287. Equation of the equinoxes. - Since

. 864.

precession in a given time be expressed by 7, the part due to the moon will be 5, and that due to the sun will be 2.

3289. Like effects produced in the case of other planets. — These disturbing effects produced upon the plane of the planet's equator, are not confined to the case of the earth. All the planets which have the spheroidal form, are subject to similar effects from the sun's attraction on their equatorial protuberance, the magnitude of these effects being, however, less as the distance from the sun is increased. In the case of the major planets, the sun's disturbing action on the planet's equator, proceeding from this cause, will be altogether insensible.

The disturbing forces of the satellites exerted upon the plane of the equator, in the cases of the major planets, however, must be considerable in magnitude, especially so far as relates to the inner satellites, and very complicated in its character, the precession and nutation of each of the satellites separately being combined in affecting the actual position of the pole of the planet.

Since, however, these phenomena are necessarily local, and manifested only to observers on the planet, they offer merely speculative

interest to the terrestrial astronomer.

3290. Effects of spheroidal perturbation on the motions of the moon generally minute. — The protuberant matter of the terrestrial spheroid disturbs the lunar orbit, in the same manner as would a satellite placed at the surface of the earth and in the plane of the equator. From what has been explained of the general effects when the disturbing body is within the disturbed orbit, it will follow that the terrestrial spheroid must impart a progressive motion to the moon's apsides, and a regressive motion to the nodes. These inequalities have, however, a theoretical existence only, being so minute, compared with the progression of the apsides and regression of the nodes due to the disturbing force of the sun, that they do not produce any observable change in these motions.

3291. Spheroidal inequality of the inclination of the moon's orbit observable. — A case, however, exists, in which the disturbing force of the terrestrial spheroid does produce sensible effects on the

lunar orbit.

It has been already shown, that the moon's nodes move round the ecliptic with a retrograde motion, in about nineteen years. Twice in this period they must, therefore, coincide with the equinoctial points; and when they do so, the line of nodes must coincide with the inclination of the planes of the equator and ecliptic. In one of the two positions which they thus assume, the plane of the moon's orbit must lie between the planes of the ecliptic and equator as represented in fig. 866, where ACDC'A' represents the equator, ACDC'A' the ecliptic, and AdDd'A' the moon's orbit. In the other position the moon's orbit will make a greater angle with the



which would be in the direction AE of the pole of the ecliptic, and would measure 18.5", while the minor axis would be at right angles to this direction, and would measure 13.74".

But while the pole of the equator describes this ellipse completing its revolution in nineteen years, it is carried by the common motion of precession, in a retrograde direction, as already described, at the rate of 50.1" in each year, and will, therefore, in nineteen years be carried through 15.5' in its motion round the pole of the equator. Now, by combining this motion with the elliptic motion already described, it will be easily seen that the pole of the equator would, in revolving round the pole of the ecliptic, alternately approaching to it and receding from it through 9-25", describe an undulating line such as is represented in fig. 865, where P represents the pole of the ecliptic.

Fig. 864.

3287. Equation of the equinoxes. - Since

the regression of the equinoxes does not take place at a uniform rate, but is subject to variations, alternately increasing and decreasing during every nineteen years, its true place will differ from its mean place. If we conceive an imaginary con-

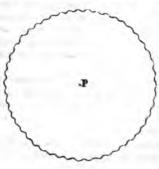


Fig. 865.

If we conceive an imaginary equinoctial point moving backward, with a uniform motion at the rate of 50° 1", the place of such point would be the mean place of the equinoctial point. The true place would vary from this, preceding it when the disturbing force augmenta the rate at which the equinoctial point moves, and falling behind it when it decreases that rate.

The distance between the true and imaginary equinoctial points is called the equation of the equinors.

The mean place of the equinar for any proposed time is given by tables; and the equation of the

equinoxes for the proposed time gives the quantity to be added to, or subtracted from, the mean place, to find the true place.

3288. Proportion of the mean precession due to the disturbing forces of the moon and sun. — If the entire amount of the mean

precession in a given time be expressed by 7, the part due to the moon will be 5, and that due to the sun will be 2.

3289. Like effects produced in the case of other planets. — These disturbing effects produced upon the plane of the planet's equator, are not confined to the case of the earth. All the planets which have the spheroidal form, are subject to similar effects from the sun's attraction on their equatorial protuberance, the magnitude of these effects being, however, less as the distance from the sun is increased. In the case of the major planets, the sun's disturbing action on the planet's equator, proceeding from this cause, will be altogether insensible.

The disturbing forces of the satellites exerted upon the plane of the equator, in the cases of the major planets, however, must be considerable in magnitude, especially so far as relates to the inner satellites, and very complicated in its character, the precession and nutation of each of the satellites separately being combined in affecting the actual position of the pole of the planet.

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nan the ecliptic does, and will lie above the ecliptic, as d at A b D b' A'.

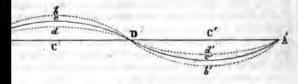


Fig. 866.

no disturbing force acted upon the plane of the moon's obliquity to the plane of the ecliptic would remain invad, therefore, in both positions here represented, the angles make with the ecliptic would be the same, that is to say, which is the mean inclination of the moon's orbit. it be admitted that the spheroidal protuberance of the, as it has been shown to do, as a satellite would situate ane of the equator, this attraction would likewise tend to moon towards that plane, and it would act more energeting the plane of the moon's orbit makes a less, than when

and while it has the apparent position AbD its apparent motion is less, than its mean motion. This difference is found to produce a variation of the moon's place in its orbit or of its longitude amounting to 8", by which it gets in advance of its mean place when the orbit has the position AdD, and lags behind it when the orbit has the position AdD.

Since the interval between the epochs at which the moon's orbit has the two positions indicated in the figure, is one half the period of the regression of the nodes, that is about nine years and a half, it follows that the moon's inclination to the ecliptic gradually increases during that interval of nine years and a half, from its position AdD to its position ADD, and that, during the next nine years and a half, it gradually decreases from its position ADD to its position ADD; therefore, it follows that the moon's angular motion is continually greater than its mean value during nine years and a half, and continually less during the next nine years and a half.

Now, this inequality in its exact quantity depends altogether upon the oblateness of the terrestrial spheroid, or, what is the same, on the ratio of the equinoctial, to the polar diameter of the earth. If this ratio were greater than 301 to 300, its actual value, the inequality of the moon's motion consequent upon it would be greater, and accordingly its apparent place would be more than 8" in advance of the true place in the one interval of nine years and a half, and less so in the succeeding nine years and a half; and, on the contarry, if the ratio of the equatorial to the polar diameter were less than 301 to 300, the variation of the moon's apparent motion would be less than 8". Thus it appears, that this uninute inequality of the moon's motion, developed in the protracted periods of nineteen years, supplies a measure of the spheroidal form of the earth, the result of which completely verifies the other methods already explained, of determining the ellipticity of the terrestrial spheroid.

3292. Spheroidal inequalities of the Jovian system. — The oblateness of Jupiter, still greater than that of the earth, produces inequalities of the motion of the satellites, similar to those produced by the spheroidal protuberance of the earth upon the moon, but greater in degree and more rapid in their development, in proportion to the greater ellipticity of the planet and the greater proportional proximity of the satellites. Thus, a progressive motion is imparted to the apsides, and a regressive motion to the nodes of each of the satellites; and these motions are so much the more considerable the nearer the satellite is to the planet. The effect of this spheroidal perturbation on the inner satellites is so predominant, that the motion of these satellites is nearly the same as it would be if no other disturbing force whatever affected them.

It will be obvious that a very complicated system of inequalities must thus be produced upon the satellites of Jupiter, insumuch as

bing effect of the spheroidal protuberance of the planet elements of each of the orbits, is necessarily mixed up disturbing effects of the satellites upon each other. Spheroidal inequalities of the Saturnian system. - The forces produced by the spheroidal form of Saturn, are in a similar to those developed in the Jovian system. The the ring is nearly the same as if the oblateness of the ere augmented, - with this difference, however, that the being attached to the planet, is not clogged with the inertia spherical mass within it, hanging upon it, as is the case spheroidal protuberance of the planet. sequence of this, the combined effects of the ring and the l protuberance of the planet, is to impart a very rapid re motion to the apsides, and a regressive motion to the the orbits of the several satellites. These effects must be greater on the inner, than on the more remote satellites. eory of the perturbations of this system is rendered very wing to the fact, that the sun, in consequence of its reand of the small visual angle which the whole system at it, can produce no sensible perturbation. vever, been so imperfectly observed that no data have been by which the results of the theoretical reasoning respect-

CHAP. XXV.

THE FIXED STARS .- STELLAR PARALLAX AND DISTANCE.

3294. Creation not circumscribed by the solar system. The region of space, vast as it is, which is occupied by the solar system, forms but a small portion of that part of the material universe to which scientific inquiry and research have been extended. The inquisitive spirit of man has not rested content within such limits. Taking its stand at the extremities of the system, and throwing its searching glance toward the interminable realms of space which extend beyond them, it still asks—What lies there? Has the Infinite circumscribed the exercise of his creative power within these precincts—and has He left the unfathomable depths of space that stretch beyond them, a wide solitude? Has He whose dwelling is immensity, and whose presence is everywhere and eternal, remained inactive throughout regions compared with which the solar system shrinks into a point?

Even though scientific research should have left us without definite information on these questions, the light which has been shed on the Divine character, as well by reason as by revelation, would have filled us with the assurance that there is no part of space, however remote, which must not teem with evidences of exalted power,

inexhaustible wisdom, and untiring goodness.

But science has not so deserted us. It has, on the contrary, supplied us with much interesting information respecting regions of the universe, the extent of which is so great that even the whole dimensions of the solar system supply no modulus sufficiently great

to enable us to express their magnitude.

3295. The solar system surrounded by a vast but limited void.—
We are furnished with a variety of evidence, establishing incontestably the fact, that around the solar system, to a vast distance on every side, there exists an unoccupied space; that the solar system stands alone in the midst of a vast solitude. It has been shown, that the mutual gravitation of bodies placed in the neighbourhood of each other, is betrayed by its effects upon their motions. If, therefore, there exist beyond the limits of the solar system, and within a distance not so great as to render the attraction of gravitation imperceptible, any mass of matter, such as another sun like our own, such a mass would undoubtedly exercise a disturbing force upon the various bodies of the system. It would cause each of them to move in a manner different from that in which it would have moved if no such body existed.

Thus it appears that, even though a mass of matter in our

chood should escape direct observation, its presence would ably betrayed by the effects which its gravitation would pon the planets. No such effects, however, are discoverne planets move as they would move if the solar system ependent of any external disturbing attraction. These are such, and such only, as can be accounted for by the of the sun and the reciprocal attraction of the other the system. The inference from this is, that there does any mass of matter in the neighbourhood of the solar ithin any distance which permits such a mass to exercise by discoverable disturbing influence; and that if any body is to our sun exists in the universe, it must be placed at a so great, that the whole magnitude of our system will to a point, compared with it.

The stars must be placed beyond the surrounding void.—
of sensible parallax.—Yet when, on any clear night, we
ate the firmament, and behold the countless multitude of
hat sparkle upon it, remembering what a comparatively
mber are comprised among those of the solar system, and
these how few are visible at any one time, we are naturally
to the inquiry, Where in the universe are these vast num-

hierts placed?

of our own change of position; and the greater that change of position is, the greater will be the relative change of these appearances. Let us suppose, however, that we are moved to a much greater distance from the shipping; any change in our position will produce much less effect upon the relative position of the masts; perhaps it will require a very considerable change to produce a perceivable effect upon them. In fine, in proportion as our distance from the masts is increased, so in proportion will it require a greater change in our own position to produce the same apparent change in their position.

Thus it is with all visible objects. When a multitude of stationary objects are viewed at a distance, their relative position will depend upon the position of the observer; and if the station of the observer be changed, a change in the relative position of the objects must be expected; and if no perceptible change is produced, it must be inferred that the distance of the objects is incomparably

greater than the change of position of the observer.

Let us now apply these reflections to the case of the earth and the stars. The stars are analogous to the masts of the ships, and the earth is the station on which the observer is placed. It might have been expected that the magnitude of the globe, being eight thousand miles in diameter, would produce a change of position of the observer sufficient to cause a change in the relative position of the stars, but we find that such is not the case. The stars, viewed from opposite sides of the globe, present exactly the same appearance; we must, therefore, infer that the diameter of the earth is

absolutely nothing compared to their distance. But the astronomer has still a much larger modulus to fall back upon. He reflects, as has been already observed, that he is enabled to view the stars from two stations separated from each other, not by 8000 miles, the diameter of the earth, but by 200 millions of miles, that of the earth's orbit. He, therefore, views the heavens on the 1st of January, and views them again on the 1st of July, the earth having in the meanwhile passed to the opposite side of its orbit, yet he finds, to his amazement, that the aspect is the same. He thinks that this cannot be — that so great a change of position in himself cannot fail to make some change in the apparent position of the stars; — that, although their general aspect is the same, yet when submitted to exact examination a change must assuredly be detected. He accordingly resorts to the use of instruments of observation capable of measuring the relative positions of the stars with the last conceivable precision, and he is more than ever confounded by the fact that still no discoverable change of position is

For a long period of time this result seemed inexplicable, and accordingly it formed the greatest difficulty with astronomers, in

the annual motion of the earth. The alternative offered it was necessary, either to fall back upon the Ptolemain which the earth was stationary, or to suppose that the change of position of the earth in the course of half a year, duce no discoverable change of appearance in the stars; a involves the inference that the diameter of the earth's to be a mere point compared with the distance of the nearest ach an idea appeared so inadmissible that for a long period any preferred to embrace the Ptolemaic hypothesis, best with difficulties and contradictions.

ed means of instrumental observation and micrometrical ent, united with the zeal and skill of observers, have at urmounted these difficulties; and the parallax, small at still capable of measurement, of several stars has been

Annual parallax. — Parallactic ellipse. — To render these and the processes by which they have been attained intelements resume the explanation of the general effects of rallax, already briefly given (2442).

ual ray by which a star is seen, and which is its apparent is carried by the annual motion of the earth round the



Fig. 867.

through the star; and let AA' be the diameter of the circle of parallax which is at right angles When the longitude of the sun to that plane. is the same as that of the star, the apparent place of the star will be at B', that extremity of the diameter BB' which is most remote from the sun; and when the longitude of the sun exceeds that of the star by 180°, it will be at B, the extremity of the same diameter which is nearest to the sun. When the longitude of the sun exceeds that of the star by 90°, the apparent place of the star will be at A', the eastern extremity of the diameter AA'; and when it exceeds that of the star by 270°, it will be at A, the western extremity. It appears therefore,

that while the sun makes a complete revolution of the ecliptic from the point at which it has the longitude of the star until its return to the same point, the star appears to move round the circle of the parallax from B' in the direction indicated by the arrows, taking successively the positions p and the angle B'sp or the arc B'p, being always equal to the difference of the longitudes of the sun and star measured from the star in the order of signs.

But the plane of this circle A B' A' B being parallel to that of the celiptic, will be inclined to the surface of the celestial sphere, at an angle equal to the complement of the latitude of the star; and by the common principles of projection it will, when projected optically on that surface, become an ellipse, of which the major axis is the projection of the diameter A A', and is parallel to the celiptic, and the minor axis that of B B', and which is perpendicular to the celiptic, and therefore coincident with the circle of latitude of the star. The diameter A A' being parallel to the surface on which it is projected, is not altered in apparent magnitude by projection; but the diameter B B' is diminished by projection, in the ratio of the sine of the star's latitude to 1.

In the figure, this ellipse is represented above the circle of parallax.

It will be apparent that, when the star is projected on B or B', its longitude is not affected by parallax, but its latitude is increased by S B at B, and diminished by S B' at B'. In like manner, when the star is seen at A or A', its latitude is not affected by parallax; but its longitude is increased by S A' at A', and diminished by S A at A.

When the star is seen at any of the intermediate points p of the parallactic ellipse, it is affected by parallax both in latitude and longitude, s n being the parallax in longitude, and p n the parallax in latitude.

mere inspection of the figure it will be apparent, that the in longitude s n is not affected by projection, being the he parallactic circle as in the ellipse; but that the parallax e p n is reduced in the ratio of the sine of the star's lati-

sy, and in some respects clearer, to express these relations mbols of arithmetic. Let ω be the excess of the sun's above that of the star, let α be the angle which the radius rele of parallax subtends at the earth, and let λ be the f the star. The angle B's p in the parallactic circle will ω , and the parallax in longitude s n will be $\alpha \times \sin \omega$. Llax in latitude which is p n in the parallactic ellipse will be $\omega \times \sin \omega$.

the star is at B or B', $\cos \omega = 1$, and $\sin \omega = \omega \times \sin \omega$, and $\sin \omega = 1$, and $\sin \omega = 1$, and $\sin \omega = 1$.

Eccentricity of parallactic ellipse depends on star's latiThe eccentricity of the parallactic ellipse increases as the
tude decreases. If the star be at the pole of the ecliptic,
of the circle of parallax being parallel to the surface of
ial sphere, it is not altered by projection; and the apparent
the star is in a circle, of which the centre is the true

from the extreme minuteness of its magnitude. It is quite certain that the quantity we have designated by a in the preceding paragraphs, does not amount to so much as 1" in the case of any of the numerous stars which have been as yet submitted to the course of observation which is necessary to discover the parallax. Now, since in the determination of the exact uranographical position of a star geocentrically and heliocentrically considered, there are a multitude of disturbing effects to be taken into account and eliminated, such as precession, nutation, aberration, refraction, and others, besides the proper motion of the star, which will be explained hereafter: and since besides the errors of observation, the quantities of these are subject to more or less uncertainty, it will astonish no one to be told that they may entail upon the final result of the calculation, an error of 1"; and if they do, it is vain to expect to discover such a residual phenomenon as parallax, the entire amount of which is less than 1".

8300. How the distance is inferred from the parallax—parallactic unit.—If in any case the parallax or the quantity which in the preceding paragraphs has been expressed by a, and which is the semi-axis major of the parallactic ellipse, could be determined, the distance of the stars could be immediately inferred. For, if this value of a be expressed in seconds or in decimals of a second, and if B express the semidiameter of the earth's orbit, and D the distance of the star, we shall have

$$D = R \times \frac{206265}{\pi}$$

If, therefore, w = 1'' the distance of the star would be 206265 times the distance of the sun, and since it may be considered satisfactorily proved that no star which has ever yet been brought under observation has a parallax greater than this, it may be affirmed that the nearest star in the universe to the solar system is at a distance at least 206265 times greater than that of the sun.

Let us consider more attentively the import of this conclusion. The distance of the sun expressed in round numbers (which are sufficient for our present purpose) is 95 millions of miles. If this be multiplied by 206265, we shall obtain—not indeed the distance of the nearest of the fixed stars—but the minor limit of that distance, that is to say, a distance within which the star cannot lie. This limit expressed in miles is

 $D = 206265 \times 95,000,000 = 19,595,175,000,000$ miles,

or nearly twenty trillions of miles.

3301. Motion of light supplies a convenient unit for the stellar distance.—In the contemplation of such numbers the imagination is lost, and no other clear conception remains, except of the mere arithmetical expression of the result of the

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on. Astronomers themselves, accustomed as they are the stupendous numbers, are compelled to seek for units ionate magnitude to bring the arithmetical expression of ities within moderate limits. The motion of light supof the most convenient moduli for this purpose, and has, on consent, been adopted as the unit in all computations ect is to guage the universe. We have shown that light the rate of 192000 miles per second. If, then, the disbove computed be divided by 192000, the quotient will ne, expressed in seconds, which light takes to move over acc. But since even this will be an unwieldy number, it educed to minutes, hours, days, or even to years.

manner we find that, if any star have a parallax of 1", it at such a distance from our system that light would take ars, or three years and eighty-five days, to come from it to

space through which light moves in a year be taken, therene unit of stellar distance, and w be the parallax expressed s or decimals of a second, we shall have

$$p = \frac{3.235}{1}$$

was carried on through the year; and if the earth's change of position, by reason of its annual motion, should produce any effect upon the apparent position of the stars, it was anticipated that such effect would be discovered by these means. After, however, making all allowance for the usual causes which affect the apparent position of the stars, no change of position was discovered which could be assigned to the earth's motion.

8303. Professor Henderson's discovery of the parallax of a Centauri.—Notwithstanding the numerous difficulties which beset the solution of this problem, by means of observations made with the ordinary instruments, Professor Henderson, during his residence as astronomer at the Royal Observatory at the Cape of Good Hope, succeeded in making a series of observations upon the star designated a in the constellation of the Centaur, which, being afterwards submitted by him to the proper reductions, gave a parallax of 1". Subsequent observations made by his successor, Mr. Maclear, at the same observatory, partly with the same instrument, and partly with an improved and more efficient one of the same class, have fully confirmed this result, giving 0.9128, or \(\frac{1}{2} \) ths of a second as the parallax.

It is worthy of remark, that this conclusion of Messrs. Henderson and Maclear is confirmed, in a remarkable manner, by the fact that like observations and computations applied to other stars in the vicinity of a Centauri, and therefore subject to like annual causes of apparent displacement, such as the mean annual variation of temperature, gave no similar result, showing thus that the displacement found in the case of a Centauri could only be ascribed to

parallax.

Since the limits of error of this species of observation affecting the final result cannot exceed the tenth of a second, it may then be assumed as proved, that the parallax of a Centauri is 1", and consequently that its distance from the solar system is such that light

must take 3.235 years to move over it.

3304. Differential method. — In the practical application of the preceding and all similar methods of ascertaining the stellar parallax, it must not be imagined that every apparent deviation from a fixed position that may be observed, is to be immediately placed to the account of parallax. There are a great number of other causes of apparent displacement, which must first be allowed for; and it is only after eliminating these, and discovering the quantity and direction of the residual displacement, that we are in a position to pronounce upon the existence and quantity of the parallax. But in account and previously eliminated, are subject to errors, small in magnitude it is true, but still great enough on the whole to absorb the entire amount of a residual phenomena so minute as the stellar

must in some cases be. All such methods of observation plation are therefore liable to be rendered abortive by the they are subject to sources of ultimate error, the amount may be greater than the quantity sought. endent of this class of errors, there are others which do not ede the discovery of a quantity so exceedingly minute as llax, and which have a very different origin. All astroinstruments are exposed to uncertain and variable changes rature, which cause the materials of which they are comundergo equally uncertain and variable expansions and ons. The piers of stone-work to which they are attached, very foundation on which these piers rest, is liable to these which more especially affect the result of the comparison vations made at intervals of six months, and therefore at seasons of the year when the effects of difference of temare the most aggravated. "Hence," as Sir John Herserves, "arise slow oscillatory movements of exceedingly mount, which levels and plumb-lines afford but very inacneans of detecting, and which being also annual in their (after rejecting what is merely casual and momentary,) mix res intimately with the matter of our inquiry," and give hich are especially liable to be mistaken for those of stellar included with s in the field of the telescope; and let s" be another situate in the same circle of latitude, and therefore having the same longitude as s, and also so near to s as to be included in the field of view of the telescope.

Let us suppose for the present, that the stars s' and s'' have no sensible parallax, and therefore undergo no apparent change of position throughout the year. From what has been already explained, it will be evident that the apparent place of s will be A', when the sun's longitude exceeds that of the star by 90°; it will be B, when it exceeds it by 180°; A, when it exceeds it by 270°; and B', when the sun's longitude is the same as that of the star. The semi-axis major s A of the parallactic ellipse is the actual parallax, or the angle which the semi-diameter of the earth's orbit subtends at the star. Let this be expressed by s. s B the somi-axis minor will be found by multiplying this last by the sine of the star's latitude, as has been already explained. Let this latitude be expressed by x; we shall therefore have

$$BA = \emptyset$$
, $BB = \emptyset \times \sin \lambda$.

Let s' A = D, s' A' = d, and $s' s = \Delta$. Since $s A = s A' = \sigma$, we shall have

$$\Delta = \frac{1}{2}(D+d), \quad \alpha = \frac{1}{2}(D-d);$$

that is, the true distance between the stars s and s' is half the sum of their apparent distances at the times when the difference between their longitude and that of the sun is 270° and 90°, and the parallax of s is half the difference between the same apparent distances.

In like manner, let s'' B' = D', s'' B = d', and $s'' S = \Delta$, and we shall have

$$\Delta' = \frac{1}{2}(D' + d'), \quad \alpha \times \sin \alpha = \frac{1}{2}(D' - d');$$

that is, the true distance is half the sum of the apparent distances when the difference of longitude of the sun and star is 0° and 180°, and the parallax is half the difference of the same distances divided by the sign of the star's latitude.

It is evident, therefore, that under the supposition here made of the absence of all sensible parallax in the subsidiary stars s' and s", the actual parallax of the star s would be found by measuring with the micrometer the distance between the stars s and s', at the epochs when the sun's longitude differs from that of the star by 90° and 270°.

In like manner, the parallax would be found by comparing the star s with the star s" at the epoch when the difference between the longitude of the sun and that of the star is 0° and 180°.

It is evident, that the four observations here indicated, two upon each of the stars, will be made at intervals of three months, deter-

mined by the epochs at which the longitude of the syn excels that of the star by 0°, 90°, 180°, and 270°.

The precision with which micrometrical measurements can be effected, when applied to two or more objects which are simulaneously present in the field of view of the telescope, renders this method of observation susceptible of extraordinary exactness. It is also attended with the obvious advantage of being totally independent of all disturbing causes which, in this case, equally affect all the objects present simultaneously in the field of view; thus all the uncertainties attending the effects of refraction, aberration, precession, nutation, &c., may be here discarded, as not interfering

in any way with the final result of the observations.

8305. Position micrometer, its application to this problem.—But these are not the only indications of the stellar parallax presented by this method of observation. An arrangement provided in the micrometers applied on the eye-piece of the astronomical instrument, supplies the observer with the means, not only of measuring the apparent distance between two or more points which are present simultaneously in the field of view, but also the direction of the line joining these two points with relation to some fixed direction, such, for example, as a parallel or a perpendicular to the ecliptic. Thus, when the star s is seen at A, the direction of the line joining it with the star s', is parallel to the ecliptic; but when it is seen at B, the line B s' joining it with the star s' is inclined to the ecliptic at the angle B s' s.

The micrometric apparatus just indicated, which from its use is called the position micrometer, enables the observer to measure with the greatest precision the angle B s' s, and in like manner to measure the equal angle B' s' s when the star s is seen at the lower

point B' of the parallactic ellipse.

The same apparatus enables the observer to measure the angle A s" s, which the line joining the stars s s' when the sun's losgitude exceeds that of the star by 90° makes with a perpendicular the ecliptic, that is, the angle A s" s, and in like manner he can measure the angle A' s" s.

Let the angle B s's == +, and let the angle A s" s = +'; we shall

then have

$$a \times \sin \lambda = \frac{1}{2} (D + d) \times \tan \lambda \phi$$
,
 $a = \frac{1}{2} (D' + d') \times \tan \lambda \phi'$.

If, therefore, the angles ϕ and ϕ' be ascertained, they supply further data by which the results of the combined observations and be verified.

If the subsidiary stars s' and s' be not in the exact position is assumed, but have latitudes and longitudes differing more or in from those of the star s, the question will be somewhat modificulty.

3306. Case of two stars having equal parallax.— If the two stars seen at once in the field of view of the telescope have equal parallaxes, both being sensible, they will appear to describe similar parallactic ellipses, and will from time to time occupy similar positions in these ellipses, since their position will be determined by the difference of longitudes of the sun and the stars. It follows from this, that the lines drawn from the centres of the parallactic ellipses to any simultaneous positions of the stars in these ellipses, will be parallel and equal; and consequently the line joining the stars will always be parallel to the major axis of the ellipse and always equal to the true distance between the stars. This will easily be comprehended by reference to fig. 870, where s and s are the true positions

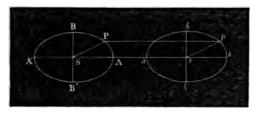


Fig. 870.

of the stars, and ABA'B', and aba'b', the two parallactic ellipses, and P and p simultaneous positions of the stars in these ellipses. The semi-diameters sP and sp being parallel, it is evident, that Pp will be equal to ss, that is to say, the apparent distance between the stars will be equal to the true distance between them; and the line Pp, joining the simultaneous positions of the stars will be constantly parallel to the line ss, that is, to the ecliptic. But if the stars be not, as here supposed, in the same parallel to the ccliptic with the star s, the same will nevertheless be true, the line joining the apparent places of the two stars being always parallel to the line joining their true places. It is evident, therefore, that if the two stars thus compared had exactly equal parallaxes, which they would have if they were at exactly equal distances from the solar system, this method of observation would not supply any means of determining the common value of their parallax.

3307. Case in which they have unequal parallaxes.—But if while the parallax of the subsidiary star is, on the one hand, not absolutely insensible, as first supposed, nor, on the other, equal to that of the principal star, but it is much less than that of the principal star, then the subsidiary star will appear to move in a parallactic ellipse proportionally smaller than that of the principal star.

Let A B A' B', fig. 871, be the parallactic ellipse of the principal

t a b a' b' be the parallactic ellipse of the subsidiary star, implify the explanation we will suppose, as before, to be

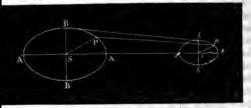


Fig. 871.

ne parallel to the ecliptic with the principal star. Since are have the same latitude, their parallactic ellipses will be not their minor axes will consequently bear the same ratio ajor axes, as represented in the figure. The simultaneous the two stars in the parallactic ellipses, will also be such emi-diameter of the ellipses s P and s p which pass through I always be parallel. But since, in this case, s p will less than s p, the line p p, which joins the simultaneous

the great multitude of stars to which instruments of observation of unlooked-for perfection, in the hands of the most able and zealous observers, have been directed, the results of all such labours have hitherto been rather negative than positive. The means of observation have been so perfect, and their application so extensive, that it may be considered as proved by the absence of all measureable displacement consequent upon the orbital motion of the earth that, a very few individual stars excepted, the vast multitude of bodies which compose the universe and which are nightly seen glittering in the firmament, are at distances from the solar system greater than that which would produce an apparent displacement amounting to the tenth of a second. This limit of distances is, therefore, ten parallactic units, or about two million times the space between the earth and sun.

Within this limit, or very little beyond it, nine stars have been found to be placed, the nearest of which is that already mentioned, of which Professor Henderson discovered the parallax. Those of the others are due to the observations of Messrs. Bessel, Struve, and Peters. In the following Table the parallaxes of these stars are given with their corresponding distances expressed in parallactic units, and also in the larger unit presented by the distance through which light moves in a year.

TABLE.

Nine Stars, with their ascertained Parallax and corresponding Distances.

Star.	Parallax.	Distance.		Observer.
		Sun's dist. = 1".	Ann. mot. of light=1.	Outsives.
a Centauri	0-913"	225916	8-54325	Henderson.
61 Cygni	0-848	592712	9-29580	Bestel.
a Lyra	0-261	790280	12:39400	Struve.
Birius	0-230	896780	14-0650	Henderson.
1830 Groombridge	0.226	912660	14-3140	Peters.
(Uras	0-138	1550800	24-3230	Peters.
Areturus	0-127	1624100	25-4725	Peters.
Polaris	0-067	8078400	48-2838	Peters.
Capells	0-046	4484000	78-6400	Poters.

rallax of the first seven of these stars may be considered; been ascertained with tolerable certainty and precision. small amount of that of the last two is such as to render oubtful. What is certain, however, in relation to these is, actual amount of their parallax is less than the tenth of a

CHAP. XXVI.

MAGNITUDE AND LUSTRE OF THE STARS.

Orders of magnitude of the stars. — Among the multitars dispersed over the firmament, we find a great variety dour. Those which are the brightest and largest, and a said to be of the first magnitude, are few; the next in brightness, which are called of the second magnitude, numerous; and as they decrease in brightness their numly increases. umber of stars of the first magnitude does not exceed ur; the second, fifty; the third, two hundred; and so on; per of the smallest visible without a telescope being from placed at the same distance; or objects generally of the same of magnitude, placed at a great diversity of distances.

these two suppositions, the latter is infinitely the more proand natural; it has, therefore, been usually adopted: and we lingly consider the stars to derive their variety of lustre it entirely from their places in the universe being at various less from us.

11. Stars as distant from each other generally as they are the sun. — Taking the stars generally to be of intrinsically brightness, various theories have been proposed as to the posiwhich would explain their appearance; and the most natural probable is, that their distances from each other are generally, or nearly so, and correspond with the distance of our sun the nearest of them. In this way the fact that a small numf stars only appear of the first magnitude, and that the numnereases very rapidly as the magnitude diminishes, is easily red intelligible.

12. Why stars increase in number as they decrease in magni--If we imagine a person standing in the midst of a wood, unded by trees on every side and at every distance, those 1 immediately surround him will be few in number, and by mity will appear large. The trunks or stumps of those which y a circuit beyond the former, will be more numerous, the t being wider, and will appear smaller, because their distance eater. Beyond these again, occupying a still wider circuit, appear' a proportionally augmented number, whose apparent itude will again be diminished by increased distance; and thus rees which occupy wider and wider circuits at greater and ar distances will be more and more numerous, and will appear sually smaller. It is the same with the stars; we are placed e midst of an immense cluster of suns, surrounding us on side at inconceivable distances. Those few which are placed diately about our system, appear bright and large, and we call stars of the first magnitude. Those which lie in the circuit id, and occupy a wider range, are more numerous and less t; and we call them stars of the second magnitude. is thus a progression increasing in number and distance and sishing in brightness, until we attain a distance so great that ars are barely visible to the naked eye. This is the limit of 1. It is the limit of the range of the eye in its natural con-; but an eye has been given us more potent still, and of iny wider range - the eye of the mind. The telescope, a creaof the understanding, has conferred upon the bodily eye an ely augmented range, and, as we shall presently see, has ed us to penetrate into realms of the universe, which, without l, would never have been known to us. But let us pause for the present and dwell for a moment upon that range of space which comes within the scope of natural vision.

8818. What are the fixed stars? — The extent of the stellar universe visible to the naked eye, and the arrangement of stars in it and their relative distances, have just been explained. But currently will be awakened to discover, not merely the position and arrangement of those bodies, but to ascertain what is their nature, and what parts they play on the great theatre of creation. Are they analogous to our planets? Are they inhabited globes, warmed and illuminated by neighbouring suns? Or, on the other hand, are they themselves suns, dispensing light and life to systems of surrounding worlds?

2814. Telescopes do not mognify them like the planets. — When a telescope is directed to a star, the effect produced is strikingly different from that which we find when it is applied to a planet. planet, to the naked eye, with one or two exceptions, appears like a common star. The telescope, however, immediately presents it w us with a distinct drouler disk similar to that which the moon offer to the naked eye, and in the case of some of the planets a powerful telescope will render them apparently even larger than the most. But the effect is very different indeed when the same instrument is directed even to the brightest star. We find that instead of magnifying, it actually diminishes. There is an optical illusion preduced when we behold a star, which makes it appear to us to be surrounded with a radiation which causes it to be represented when drawn on paper, by a dot with rays diverging on every side from it The effect of the telescope is to cut off this radiation, and present to us the star as a mere lucid point, having no sensible magnitude; nor can any augmented telescopic power which has yet been reserted to, produce any other effect. Telescopic powers amounting to it thousand were occasionally used by Sir William Herschel, and be stated that with these the apparent magnitude of the stars seemed less, if possible, than with lower powers.

8315. The absence of a disk proved by their occultation by in moon. — We have other proofs of the fact that the stars have me sensible disks, among which may be mentioned the remarkable effect called the occultation of a star by the dark edge of the most. When a moon is a crescent or in the quarters, as it moves over the firmament, its dark edge successively approaches to, or recedes from the stars. And from time to time it happens that it passes between the stars and the eye. If a star had a sensible disk in this case, the edge of the moon would gradually cover it, and the star, instant of being instantaneously extinguished, would gradually disapper. This is found not to be the case; the star preserves all its latter until the moment it comes into contact with the dark edge of the

moon's disk, and then it is instantly extinguished, without the

slightest appearance of diminution of its brightness.

3816. Meaning of the term magnitude as applied to stars. — It may be asked then, if such be the case, if none of the stars, great or small, have any discoverable magnitude at all, with what meaning can we speak of stars of the first, second, or other orders of magnitude? The term magnitude thus applied, was used before the invention of the telescope, when the stars, having been observed only with the naked eye, were really supposed to have different We must accept the term now to express, not the magnitudes. comparative magnitude, but the comparative brightness of the stars. Thus a star of the first magnitude, means of the greatest apparent brightness; a star of the second magnitude, means that which has the next degree of splendour, and so on. But what are we to infer from this singular fact, that no magnifying power, however great, will exhibit to us a star with any sensible magnitude? must we admit that the optical instrument loses its magnifying power when applied to the stars, while it retains it with every other visible object? Such a consequence would be eminently absurd. therefore driven to an inference regarding the magnitude of stars, as astonishing and almost as inconceivable as that which was forced upon us respecting their distances. We saw that the entire magnitude of the annual orbit of the earth, stupendous as it is, was nothing compared to the distance of one of those bodies, and consequently if that orbit were filled by a sun, whose magnitude would therefore be infinitely greater than that of ours, such a sun would not appear to an observer at the nearest star of greater magnitude than I"; consequently would have no magnitude sensible to the eye, and would appear as a mere lucid point to an observer at the star! We are then prepared for the inference respecting the fixed stars which telescopic observations lead to. The telescope of Sir William Herschel, to which he applied a power of six thousand, did undoubtedly magnify the stars six thousand times, but even then their apparent magnitude was inappreciable. We are then to infer that the distance of these wonderful bodies is so enormous compared with their actual magnitude, that their apparent diameter, seen from our system, is above six thousand times less than any which the eye is capable of perceiving.

3317. Why stars may be rendered imperceptible by their distance.—It appears, therefore, that stars are rendered sensible to the eye, not by subtending a sensible angle, but by the light they emit. It has been already explained (1131) that an illuminated or luminous object, such, for example, as the sun, has the same apparent brightness at all distances, and, consequently, that the quantity of light which the eye of an observer receives from it being in the exact ratio of the apparent area of its visual disk, is inversely as the

III. 5

its distance. It remains, however to explain how it can ter it ceases to have a disk of sensible diameter, it does to be visible. This arises from the fact that the luminous tituting the image on the retina, is intrinsically as bright nat image has a large and sensible magnitude. The eye e sensible to the light, though not sensible to the magthe image; and it continues to be sensible to the light, crease of distance the light which enters the pupil and is on the retina, though still as intense in its brilliancy as so small in its quantity, that it is insufficient to produce

Classification of stars by magnitudes arbitrary and t.— The distribution of the stars visible to the naked eye orders of magnitude, has been so long and so generally and is referred to so universally in the works of astronent and modern, that it would be impossible altogether to it, and if possible, such a change would be attended with prevenience. Nevertheless, this classification is open to ections, and is, from its looseness and want of definiteness ion, in singular discordance with the actual state of astronence. The stars which abound in such countless num-

sun, which is itself only an individual of the same class of bodies, the importance of the expedients for the more exact estimation of their relative lustre, and a more precise basis of classification as to apparent magnitude, cannot fail to be felt and acknowledged. The importance of this is rendered still greater by the consideration that the parallax of a very small number of stars being found to have appreciable magnitude, the comparative lustre of these bodies taken in the mass, is the only ground upon which any estimate of their relative distances can be determined; and when the large number which are subject to observation is considered, and the improbability of their differing greatly in intrinsic magnitude taken collectively in classes, it must be admitted that their relative apparent brightness cannot fail to be a tolerably exact exponent of their comparative distances.

8320. Astrometer contrived and applied by Sir J. Herschel. — During his residence at the Cape, Sir J. Herschel contrived an apparatus for the more exact determination of the relative lustre of the stars, and applied it with great advantage to the determination of the relative brightness of a considerable number of these objects. This apparatus consisted of a rectangular glass prism, and a lens so mounted that two celestial objects might be seen in juxta-position, one directly, and the other by reflection and transmission through the prism and lens, the apparent brightness of the latter being capable of being varied at pleasure by the observer, so that, by proper adjustments, the two objects thus seen may be rendered sensibly equal in brightness. When this is accomplished, the arrangements of the apparatus are such, that by measuring the distance of the eye of the observer from the focus of the lens, a measure may be obtained by which the comparative lustre of any objects to which the apparatus may be successively directed may be determined.

To render this intelligible, let r, fig. 872, represent the rectangular prism, one of the faces of which is placed so as to receive a pencil

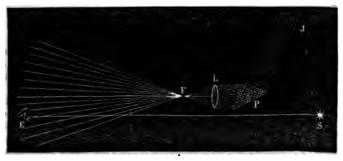


Fig. 872.

of rays passing from a distant object J perpendicularly. These rays are totally reflected (1006,) by the back of the P, and emerging from the other face of the prism, are receithelens L, and brought to a focus F, as if they came from tion PF. The parallel pencil is thus converted into a pencil, of which F is the focus, and the point F will appaye, placed any where, as at E, within the limits of the pencil as a star, the apparent brightness of which will bless according as the eye is nearer to or more distant for results from the principles of optics, that the apparent of the focal point F will be inversely as the square of the ustre of F when the eye is at the unit of distance from it, by D² will express its apparent lustre when the eye is a tance D.

Let us now suppose the apparatus so arranged in its pos while the eye, placed within the divergent pencil, sees th it may also see, in juxta-position with it, a star s, whose it be determined. Let the eye be moved to or from F until of the star becomes sensibly equal to that of F. If, then, of the star be expressed by s, we shall have In this manner, Sir J. Herechel ascertained numerically the commerative brightness of a considerable number of stars under the barth magnitude, and has given, in his "Cape Observations" a metalogue, exhibiting the relative magnitudes to two places of lecturals.

8321. Principle on which the successive orders of stellar magnitude should be based. — Astronomers are not agreed as to the sptical conditions by which the successive orders of stellar magnitudes should be fixed. It might appear, at first view, that a star of the second magnitude ought to have one half the brightness of the first magnitude, that a star of the third magnitude ought to have one third of the brightness, and so on.

But such a proportion would not be at all in accordance with the

common classification of magnitudes.

The more generally received condition has been a succession of magnitudes, such as a star of a given intrinsic lustre would have if memoved to a series of distances increasing in arithmetical progression. Thus, stars of the first magnitude would be at the unit of the stellar distance; those of the second magnitude would have a lastre due to twice this distance; those of the third magnitude, to three times this distance, and so on. Now, since the apparent lustre of an object is in the proportion of the inverse square of the distance, it would follow that, in this system, the succession of brightness would be as the numbers 1, 1, 1, 1, 1, 1, 1, and so on.

Meanwhile, whatever may be the principle adopted for this classication, the astrometric expedient contrived by Sir John Herschel, being sufficient for the numerical estimation of the relative brightnesses of different stars, it will be sufficient to determine a variety of interesting and important problems respecting the absolute lustre and magnitudes of those objects, not only compared with each other,

but with the sun.

3322. Comparative lustre of a Centauri with that of the full moon.—By means of the instrument described above, Sir J. Herschel compared the full moon with certain fixed stars, and ascertained, by a mean of eleven observations, that its lustre bore to that of the star a Centauri, which he selected as the standard star of the first magnitude, the ratio of 27408 to 1; in other words, he showed that a cluster consisting of 27408 stars equal in brightness to that of a Centauri would give the same light as the full moon.

3323. Comparison of the lustre of the full moon with that of the sun. — Dr. Wollaston by certain photometric methods which are considered to have been susceptible of great precision, compared the light of the sun with that of the full moon, and found that the ratio was 801072 to 1; or in other words, that to obtain moon-light as intense in its lustre as sun-light, it would be necessary that 801072

full moons should be stationed in the firmament together.

Comparison of the sun's light with that of a Centauri.—
ombination of these observations by Herschel and Wolare supplied with means of bringing into direct numerical
n the sun and the star a Centauri. Since it appears that
of a Centauri is 27408 times less than that of the full
ile the light of the full moon is 801072 times less than
e sun, it will evidently follow, that if we express by s the
e sun, and by s that of a Centauri, we shall have

= $27408 \times 801072 \times s = 21955,000,000 \times s$; say, the light of the sun is very nearly 22,000,000,000 re intense than that of a Centauri.

eralise these results, m express the ratio of the light of moon to that of any star, as determined by Herschel's r, we shall then have,

 $s = 801072 \times m \times s;$

quently,

 $s = \frac{8}{801072 \times m}.$

Comparison of the intrinsic splendour of the sun and a r. — Since all analogy and observation lead to the con-

the sun, so that it shall present to the eye the same apparent lustre as the star, for in that case the visual magnitude of the sun, which could be calculated by means of its real magnitude and distance, would necessarily be equal to the visual magnitude of the star. In this manner, a visual angle too small to be ascertained by direct instrumental measurement, would be determined by indirect means.

Let d = the real diameter of the sun, D = the distance to which it would be necessary to remove it from the observer, so that it might present to the eye the same appearance as a given star, and let $\phi =$ its visual diameter at that distance. We should then have,

$$\phi'' = 206265 \times \frac{d}{D}$$

and ϕ would then be the visual angle subtended by the star, if the star be supposed to have the same intrinsic lustre as the sun. But if the star be supposed to have a greater or less intrinsic lustre than the sun, then the visual magnitude of the star will be greater or less than ϕ .

Although the sun cannot be removed to increased distances, the same optical effect may be produced by the following expedient.

Let A B C D be a tube like that of a telescope, furnished with a

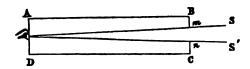


Fig. 873.

disphragm at BC, so constructed that by sliding pieces a circular aperture, having a diameter variable at pleasure within practical limits, may be made in its centre. Let a sliding tube having an eye-hole in a disphragm at the end of it, like that in the eye-piece of a telescope, be attached to the other end AD of the tube, so that the distance of the eye-hole from the variable aperture m n may be varied at pleasure within practical limits. It is evident, that the diameter of the aperture m n, and the distance from E to m n, being known, the visual angle subtended by m n at E will be determined.

If the tube thus constructed and arranged be directed to the disk of the sun, a circular part of that disk having any desired visual diameter, can be made visible to an eye placed at E. This can always be accomplished within limits by the variation of the diameter m n of the aperture, and the variation of the distance of E from m n.

ASTRONOMY,

a well-understood principle of optics (1132), the circular e sun's disk visible through the aperture, has exactly the arance both in apparent magnitude and brightness, as the would have if it were removed to such a distance from er, that it would subtend the same visual angle as that by the aperture m n at the eye E.

, the apparatus be so adjusted, that the apparent lustre of of the sun seen through the aperture, shall be equal as can be determined by an observation of this kind, to the brightness of any star, it will follow, that the visual angle by the aperture seen from E, will be equal to the visual tended by the star; and as the former can be calculated og the real diameter of the aperture and its distance from ter can be inferred.

practical application of this method, the difficulty arises being able to bring the luminous point seen in the tube, ediate juxtaposition with the star with which it is comhe observer must rely upon his judgment and memory of ent brightness of the stars, to determine when that of the point seen in the tube is equal to it.

Comparison of the sun and a Centauri - There will be

star is four times that of a Centauri. For the Dog-star we shall have, therefore,

$$L = \frac{s}{5,488,750,000};$$

and since it appears, by the observations of Peters, that the parallax of this star is 0.230", its distance will be 896800 semidiameters of the earth's orbit. We shall consequently have, for Sirius,

$$1 \times M = \frac{896800^{8}}{5,488,750,000} = 146.53.*$$

From which it appears that Sirius is a sun, whose lustre is such as, if placed in the centre of the solar system, would diffuse a light to the surrounding planets 146.53 times more intense than that afforded by the actual sun. If, therefore, the intensity of the lustre of the surface of this stupendous sphere be equal to that of the sun, it must have a diameter 12.11 times greater than that of our sun; and since the diameter of the latter is 882,000 miles, that of Sirius would be.

$$882000 \times 12.11 = 10,676,600$$
 miles.

8329. Astrometric table of 190 principal stars. — In the following table (see pp. 682-3,) are collected the results of the observations of Sir J. Herschel, for the determination of the relative lustre of 190 principal stars. In addition to their astrometric magnitudes, as determined by Sir J. Herschel, we have computed from the data supplied by him, their relative brightness compared with that of the star a Centauri as a standard, and also their light in billiouths of the light of the sun.

3330. Use of the telescope in stellar observations.—Since no telescope, however great might be its power, has ever presented a fixed star with a sensible disk, it might be inferred that, for the purposes of stellar investigation, the importance of that instrument must be inferior to that which it may claim in other applications. Nevertheless it is certain, that in no department of physical science has the telescope produced such wonderful results as in its application to the analysis of the starry heavens.

Two of the chief conditions necessary to distinct vision are, first, that the image on the retina shall have sufficient magnitude; or, what is equivalent to this, that the object or its image shall subtend at the eye a visual angle of sufficient magnitude (1116); and, secondly, it must be sufficiently illuminated (1100). When, by reason of their distance from the observer, visible objects fail to

[•] Sir J. Herschel makes the proportion 68-02 which is certainly incorrect, that being the ratio of the intrinsic brightness of Sirius to that of a Centauri and not that of Sirius to the sun. See Astronomy, p. 558, edit. 1849.

TABLE.

List of 190 stars, from the first to the third magnitude inclusive, with nitudes, according to the astrometric scale proposed by Sir John and their apparent brightness compared with each other, and with

في والشير ورسالم	Astrometric Magnitude.	Star*	Light.	tion but in	Astrometric Magnitude.	81
Stars.	a Centauri = f.	a Cen- taŭri = 1.	Billionths of Suo's Light.	Stars.	a Centauri = 1.	a Cer
I. First Mag. Sirius Argus Canopus Centauri Arcturus Rigel Capella Lyra Procyon Orionis	1·00 1·18 1·23 1·4 1·4 1·4 1·4	4·165 	189·7 92·97 45·55 32·71 30·11 23·24 23·24 23·24 22·27 20·24	II. 2 Mag. β Gruis a Arietis σ Sagitt δ Argus ζ Ursæ maj β Androm β Ceti λ Argus β Aurigæ γ Androm	2·84 2·86 2·87 2·87 2·89	0·13 0·12 0·12 0·12 0·12 0·12 0·12 0·12 0.12 0.12
Aldebaran . Aldebaran . β Centauri Crucis Antares Aquilæ	1.5 1.58 1.6 1.6	0.44 0.40 0.39 0.39 0.35	20-24 18-24 17-79 17-79 15-95	III. 3 Mag. γ Cassiope a Androm θ Centauri a Cassiope	2·95 2·95	0·11 0·11 0·11 0·11

MAGNITUDE AND LUSTRE OF THE STARS.

	Astro- metric Magni- tude.	Star's	Light.		Astro- metric Magni- tude.	Starfe)	Light.
•	a Cen- tauri = 1.	a Con- tauri 	Bil- lienths of Star's Light.	Stare.	a Cen- tauri = 1,	s Cen- tauri == 1.	Bil. liouth of Sun' Light
eg.				III. 3 Mag.			
tis		0.0902	4.11	β Arae	3-72	0.0723	3-29
•••••		0.0891 0.0891	4.06	a Toucani β Capric	3·73 3·73	0-0719 0-0719	3.27
		0.0886	4.03	e Argus	3.73	0.0719	3.27
		0.0881	4.01	ξ Aquilse	3.73	0.0719	3.27
ri		0.0881	4.01	βCygni	8.74	0.0715	3-26
bi		0.0875	3.99	γ Persei	3.75	0-0711	3.24
I	3.38	0.0875	3.99	μ Ursæ maj	3.76	0.0707	3.22
		0.0870	3-95	β Triang, bor.	3.76	0-0707	3.22
		0.0870	3.95	# Scorp	3.76	0.0707	3.22
······		0.0865	3.94	β Leporis	3.76	0.0707	3-22
ri		0.0865 0.0860	3.94	γ Lupi	3·77 3·77	0.0704	3.21
ı bi		0.0860	3-92	δ Persei	3.77	0.0704	3·21 3·21
rii		0.0855	3.89	φ Ursæ maj ε Aurig	V. 3.78	0.0700	8-19
		0.0855	3.89	s Scorp	3.78	0.0700	3.19
is		0.0850	3.87	(Orion	3.78	0.0700	3.19
hi		0.0835	3.80	y Lyncis	3.80	0.0693 -	3.15
is		0.0830	3.78	ξ Drac	3.81	0.0689	3.14
		0.0826	3.76	« Aræ	3.81	0.0689	3.14
s		0.0821	3.74	π Sagitt	3.81	0.0689	3.14
•••••	7	0-0821	3.74	π Herc	3 82	0-0685	3.12
••••••		0.0816	3.72	β Can min.?	3.82	0.0685	3.12
•••••••••• 		0.0807 0.0807	3·68 3·68	ξ Tauri	8·83 3·83	0.0682	3·10
rii		0-0802	3.65	d Drac μ Gemin	3.83	0.0682	3.10
		0-0798	3.63	y Boot.	3.84	0.0678	3-09
		0.0793	3.61	e Gemin	3.84	0.0678	3.08
s 7		0.0793	3.61	a Muscse	3.84	0.0678	3.09
bee		0.0789	3.59	a Hydri?	8.85	0.0675	3.07
		0.0780	3.22	τ Scorp	3.85	0.0675	3-07
is		0.0776	3.23	δ Herc	3.85	0.0675	3.07
ri		0.0767	3.49	δ Gemin	3.85	0.0675	3.07
orni		0.0769	3.49	ø Orion	3.86	0.0671	3.06
venat	3.63	0·0759 0·0759	3.46	β Cephei θ Ursæ maj	3·86 3·86	0.0671	3-06
hi		0.0755	3.44	{ Hydrae	3.86	0.0671	3.00
		0.0751	3.42	y Hydræ	3.87	0.0668	3.04
********		0.0742	3.38	β Triang. aus.	3.87	0.0668	8-04
	1 - 11	0.0742	3.38	· Ursæ maj	3.87	0.0668	8-04
1		0.0742	3.38	η Aurig	3.87	0.0668	3.04
•••••	. 3.67	0.0742	3.38	γ Lyrae	3.88	0.0664	3.03
,,,,,,,,,		0.0738	3.36	η Gemin	8.89	0.0661	3-01
•••••		0.0738	3.36	γ Ceph	3.89	0.0661	3.01
4		0.0734	3.34	к Ursæ maj	3.90	0-0657	2.99
•••••	3.69	0.0734	3·34 3·33	ε Cassiop	3-90	0.0657	2-99
) nin		0.0730 0.0726	3.33	d Aquil	3-91 3-91	0-0654 0-0654	2-98
nin		0.0728	3.31	σ Scorp	3.81	0.0654	2.88

er or both of these conditions, the telescope is capable of ng them. It augments the visual angle by substituting stant object, which the observer cannot approach, an age of it close to his eye, which he can approach; and it the illumination by collecting, on each point of such many rays as can enter the aperture of the object glass, the more limited number which can enter the pupil of the ; allowance, nevertheless, being made for the light lost by from the surfaces of the lenses, and by the imperfect acy of their material.

crease of the visual angle is determined by the ratio of the th of the object glass to that of the eye glass (1212), and se of illumination is determined by the ratio of the area erture of the object glass to that of the pupil, which areas rtional to the squares of the diameters of the object glass pupil. The illumination will, therefore, vary in the ratio areas of the aperture of the telescope.

blain the effect of the telescope applied to stellar observahe sun or any similar object be imagined to be transferred hally increased distance from the observer. The effect will adual decrease of its visual diameter, and a corresponding of the image on the retina. The brightness or intensity greater and greater distances, the image on the retina will be proportionally diminished in magnitude; but as its magnitude has already ceased to be sensible because of its minuteness, this decrease of magnitude will necessarily also be insensible. But the total quantity of light falling upon the retina will also be decreased, and this decrease will be in the ratio of the increase of the square of the distance. Now, since the apparent brightness of the luminous point to which the sun would be in this case reduced, must depend altogether on the total quantity of light falling on the retina this brightness will be in the inverse ratio of the square of the distance.

Let L' be the total quantity of light falling on the retina, or the apparent brightness of the object at the distance D' at which it ceases to have a sensible disk, and let L be its apparent brightness, at any greater distance D. We shall then, according to what has just been explained, have

$$L : L' :: D'^2 : D^2;$$

and consequently,

$$L = L' \times \frac{D'^2}{D^2},$$

from which it appears again that L will decrease as D2 increases.

By the continual increase of D, therefore, the apparent brightness of the luminous point to which the object has been reduced, would be continually diminished, and it would successively assume the appearance of stars of less and less magnitude, until at length the quantity of light falling on the retina would become so small that it would be insufficient to produce a sensible impression on the organ, and the object would cease to be seen. Let the distance at which this would take place be D".

It appears, then, that in the gradations of the optical impression produced by such a continually receding object, there are two limiting distances, the lesser D' at which it ceases to have sensible magnitude but continues to be visible as a lucid point, and the greater D' at which it ceases to be seen altogether; and that at intermediate distances D it appears as a lucid point of all degrees of brightness, less than that which it has at the distance D'.

If this reasoning be applied to different objects, it is evident that the distance D' will vary with the real diameter of the object, and will be exactly proportional to it. The distance D" for objects having the same real diameter, will vary with their intrinsic lustre, or the relative quantities of light which they emit from their visible hemispheres, and will be greater in the ratio of the square root of the absolute quantity of light emitted.

If a telescope be directed to a star at any distance D greater than D", its magnifying power will be incapable, however great it may 111.

menting the visual angle to such an extent as to render it an it would be, if the star were at the distance D', at which angle becomes so small as to be inappreciable by the eye. he same case, the power of the telescope to increase the of light which enters the pupil, will produce effects which nly very sensible, but which may be increased almost ly, by augmenting the aperture of the telescope. In this ough the magnifying power is altogether inefficacious so ites to the visual angle of the object, its power, so far as the increase of light or increase of apparent brightness of , becomes of the greatest importance. Thus it is evident, escope of a certain aperture directed to a star of the sixth e, the light of which, according to the estimate of Sir J. is about the 100th part of the light of such a star of the nitude as a Centauri, would render it equal in apparent s to the latter, and would, therefore, have the effect of it so much nearer to the observer, as the distance of an tar of the first magnitude is less than an average star of magnitude. But since the apparent brightness decreases pare of the distance increases, it follows that a star of the gnitude, being 100 times less bright than a star of the first e, will be 10 times more distant. The telescope, thereThe star is, therefore, brought nearer to the observer in the ratio of \sqrt{m} to 1.

3331. Space-penetrating power.—This number \sqrt{m} which expresses the power of the telescope to bring a star nearer to the observer, or what is the same, to enable the observer to see distant stars with the same degree of distinctness or brightness as if they were at less distances, is called the SPACE PENETRATING POWER.

Thus, if the light of a star of the sixth magnitude be 100 times less than that of a star of the first magnitude, a telescope which would augment the light 100 times, would exhibit it with the same apparent brightness as a star of the first magnitude; and for such a telescope we should have m = 100, and therefore $\sqrt{m} = 10$, so that the star of the first magnitude would be ten times more distant than the stars of the first magnitude.

Thus, for example, the reflecting telescope used by Sir William Herschel in some of his principal etellar researches, had an aperture of eighteen inches, and twenty feet focal length with a magnifying power of 180. The pace-penetrating power of this instrument was found to be seventy-five, the meaning of which is, that when directed to a star of any given brightness, it would augment its brightness so as to make it appear the same as it would be if at seventy-five times less distance, or what is the same, that a star which to the naked eye would appear of the same brightness as that star does when seen in the telescope would require to be removed to seventy-five times the actual distance, so that when seen through the telescope it would have the brightness it has when seen with the naked eye. Thus a star of the sixth magnitude, if removed to seventy-five times the actual distance, would appear in such an instrument still as a star of the simh magnitude would to the naked eye, and if we assume with Sir John Herschel, that a star of the sixth magnitude has a hundred times less light than a Centauri, and is therefore at ten times a greater distance, it will follow that a Centauri would require to be removed to seven hundred and fifty times its actual distance, so that when viewed through such a telescope it would be seen as a star of the sixth magnitude is to the naked eve.

If, then, it be assumed, as it may fairly be, that among the innumerable stars which are beyond the range of unaided vision, and brought into view by the telescope, a large proportion must have the same magnitude and intrinsic brightness, as the average stars of the first magnitude, it will follow that these must be at distances 750 times greater than the distance of an average star of the first magnitude, such as a Centauri. But it has been already shown (3308,) that the distance of a Centauri is such that light would require 3.54325 years to come from it to the earth. It would,

follow that the distance of the telescopic stars just referred be such that light would take to come from them to the

 $3.54325 \times 750 = 2657.4375$ years.

e desired to ascertain the distance of such stars, taking the

 $225916 \times 750 = 169,437,000.$

ears, therefore, that the distance of such a star would be a hundred and seventy million times the distance of the since the distance of the sun expressed in round numbers and red millions of miles, it will follow that the distance of r is seventeen thousand billions of miles. ive, therefore, at the somewhat astonishing conclusion that nee of these objects, the existence of which the telescope disclosed to us, must be such that light, moving at the 92000 miles per second, takes upwards of 2600 years to a them to us, and consequently that the objects we now of those which now exist, but those which did exist 2600 yand it is within the scope of physical possibility that have changed their conditions of existence, and consequence.

between the members composing each group, or is the result of the fortuitous relation of the visual lines directed to them, the principal collections of the more conspicuous stars, thus placed in near apparent vicinity, have been recognised from the most remote antiquity, and such groups have been commonly denominated CONSTELLATIONS.

Although in certain cases, it is probable that some physical relation may exist between the more close neighbours in these constellations, it is certain that the apparent juxta-position and relative arrangement of the component stars generally is altogether for-Imagination has, however, connected them together, and invested such constellations with the forms of mythological figures, animals, such as bears, dogs, lions, goats, serpents, and so on, from which they severally take their names. Unreasonable as such a system must be allowed to be, it is not without its use as a means of reference and an artificial aid to the memory. That a better system of signs and symbols might have been devised for these purposes, may be admitted; but when it is considered that the names and forms of the most conspicuous constellations have had their origin in remote antiquity—that they were handed down from the Chaldeans to the Egyptians, from the Egyptians to the Greeks, and from these to the moderns — that they are referred to in the works of every past astronomer, and registered in the memory of every living observer—that they are associated with the productions of art, and supply illustrations to the orator and the poet — it will be readily admitted that, even though a general change of the stellar nomenclature and symbols were practicable, it would neither be advantageous nor advisable.

As an example of a constellation, the group of seven conspicuous stars, arranged nearly in the form of a note of interrogation, visible in the northern part of the firmament, and in these latitudes always above the horizon, may be referred to. This constellation is called Ursa major (the great bear). The seven stars are only the more conspicuous of those which compose the constellation, the entire number being eighty-seven, most of them, however, being telescopic; of the seven chief stars one only is of the first magnitude,

three of the second, and three of the third.

The seven principal stars of this constellation being all less than forty degrees from the north pole, will be always above the horizon in latitudes greater than forty degrees. Hence it is that this constellation is so familiarly known. They may serve as standards or moduli by which the astronomical amateur may estimate the orders of magnitudes of the stars generally. It is in the quarter of the heavens opposite to that in which the sun is in the month of March, and is therefore visible at midnight near the meridian above the pole at that season. In the month of September it is visible at midnight below the pole.

58*

The stars which compose a constellation are designated usually by the letters of the Greek alphabet, the first letters being generally assigned to the most conspicuous. The order of the letters, however, does not always follow strictly the order of magnitudes. When the stars are not designated by letters, they are distinguished by numbers, and this is mostly the case with the smaller stars.

It is usual to express the constellations by their Latin names, and to designate the individual stars by the letter or number and the constellation, as a Lyree, 3 Ursee majoris, 61 Ophiuchi, 24

Comæ, &c.

In the cases of some of the more conspicuous stars, such as have been objects of observation in remote ages, they are also frequently distinguished by proper names. Thus, a Canis major. is more commonly called Sirius, and sometimes the Dog-star, and is known as the most resplendent of the fixed stars. In like manner a Piscis is always called Fomalhaut, a and β Gemini are called Castor and Pollux, β Orionis is known as Rigel, a Tauri as Aldebaran, a Virginis as Spica, a Bootis as Arcturus, and so on.

The practical usefulness of the imaginary figures which give names to the constellations, will thus be understood. If we desire to express the position of the star η Ursæ majoris, for example, we say that it is at the tip of the tail of the Great Bear. We indicate, in like manner, the place of three remarkable stars, by saying that they form the belt of Orion, and another Rigel by saying that it is on his foot. The star Sirius is on the nose of Canis major, and the bright star β on his right thigh.

3334. Use of pointers. — Those who desire to obtain an acquaintance with the stars, will find much advantage in practising the method of pointers, by which the position of conspicuous stars with which the observer is well acquainted is used to ascertain the places of others which are less known and less easily identified. This method consists in assigning two conspicuous stars so placed, that a straight line imagined to be drawn between them, and continued if necessary in the same direction, will pass through or near the star whose position it is desired to ascertain.

The most useful example of the application of this method, is the case of the pole star, which is a Ursæ minoris, a star of the third magnitude. Let the observer direct his eye to the two conspicuous stars, a and β Ursæ majoris, and supposing a straight line drawn from β to a, let him carry his eye along that line beyond a to a distance about six times the space between a and β , he will arrive

at the Pole Star.

3335. Use of star maps. — To comprehend the preceding paragraphs, and profit by the instructions given in them, it will be necessary for the student to have in his hands a set of star maps.

The GUIDE TO THE STARS* will be found to be one of the most convenient works for this purpose. In the maps there given, will be found indications of the most useful applications of this method

of pointing.

3336. Use of the celestial globe.—A celestial globe may be defined to be a working model of the heavens. It is mounted like a common terrestrial globe. The visible hemisphere is bounded by the horizontal circle in which the globe rests. The brass circle at right angles to this, is the celestial meridian. The constellations with outlines of the imaginary figures from which they take their

names, are delineated upon it.

The globe will serve, not merely as an instrument of instruction, but will prove a ready and convenient aid to the amateur in astronomy, superseding the necessity of many calculations which are often discouraging and repulsive, however simple and easy they may be to those who are accustomed to such inquiries. Most of the almanacs contain tables of the principal astronomical phenomens, of the places of the sun and moon, and of the principal planets as well as the times when the most conspicuous stars are on the meridian after sunset. These data, together with a judicious use of the globe and a tolerable tolescope, will enable any person to extend his acquaintance with astronomy, and even to become a useful contributor to the common stock of information which is now so fast increasing by the zeal and ability of private observers in so many quarters of the globe.

To prepare the globe for use, let small marks (bits of paper gummed on will answer the purpose) be placed upon it, to indicate the positions of the sun, moon, and planets, at the time of observing the heavens. The place of the sun on the ecliptic is usually marked on the globe itself. If not, its right ascension (that is, its distance from the vernal equinoctial point, measured on the celestial equator), and its declination, (that is, its distance north or south of the equator), are given in the almanac, for every day. The moon's

right ascension and declination are likewise given.

3337. To find the place of an object on the globe when its right ascension and declination are known.— Find the point on the equator where the given right ascension is marked. Turn the globe on its axis till this point be brought under the meridian. Then count off an arc of the meridian (north or south of the equator, according as the declination is given) of a length equal to the given declination, and the point of the globe immediately under the point of the meridian thus found, will be the place of the object. By this rule, the position on the globe of any object of which the right

Twelve Planispheres, forming a Guide to the Stars for every Night in the Year, with an Introduction. — Taylor and Walton, London.

leclination are known, may be immediately found,

ding mark put upon it.

e globe so as to use it as a guide to the position of objects on the heavens, and as a means of identifying the stars and learning their names, let the lower clamping-screw of the meridian be loosened, and let the north pole of the globe be elevated by moving the brass meridian until the arc of this meridian between the pole and the horizon be equal to the latitude of the place of observation. Let the clamping-screw be then tightened, so as to maintain the merid

placed that the brass r the pole being turned u will correspond with the meridian, and the r

To ascertain the as it is now only necessary . mark indicating the place of the same position as the sun tion. To effect this, let th cating the position of the Observe the hour marked on the . Let the globe be then so directed due north and south, This being done, the globe r as relates to the poles, the

nent at any hour of the night, globe upon its axis until the shall be under the horizon in ually is at the hour in questurned until the mark indirought under the meridian. of the equator which is then

under the meridian. Add to this nour the hour at which the observation is about to be taken, and turn the globe until the point of the equator on which is marked the hour resulting from this addition is brought under the meridian. The position of the globe will then correspond with that of the firmament. Every object on the one will correspond in its position with its representative mark or symbol on the other. If we imagine a line drawn from the centre of the globe through the mark upon its surface indicating any star, such a line, if continued outside the surface toward the heavens, would be directed to the star itself.

For example, suppose that when the mark of the sun is brought under the meridian, the hour 5h. 40m. is found to be on the equator at the meridian, and it is required to find the aspect of the heavens at half-past ten o'clock in the evening.

To		
	_	
•	16	10

Let the globe be turned until 16h. 10m. is brought under the meridian, and the aspect given by it will be that of the heavens.

CHAP. XXVII.

PERIODIC, TEMPORARY, AND MULTIPLE STARS.—PROPER MOTION OF STARS.—MOTION OF THE SOLAR SYSTEM.

Telescopic observations on individual stars. — Besides kinging within the range of observation objects placed beyond the phere which limits the play of natural vision, the telescope has greatly multiplied the number of objects visible within that sphere, by enabling us to see many rendered invisible by their minuteness, er confounded with others by their apparent proximity. Among the stars also which are visible to the naked eye, there are many, respecting which the telescope has disclosed circumstances of the highest physical interest, by which they have become more closely allied to our system, and by which it is demonstrated that the same material laws which coerce the planets, and give stability, uniformity, and harmony to their motions, are also in operation in the most remote regions of the universe. We shall first notice some of the most remarkable discoveries respecting individual stars, and shall afterwards explain those which indicate the arrangement, dimensions, and form of the collective mass of stars which compose the visible firmament, and the results of those researches which the telescope has enabled astronomers to make in regions of space still more remote.

I. PERIODIC STARS.

3339. Stars of variable lustre. — The stars in general, as they are stationary in their apparent positions, are equally invariable in their apparent magnitudes and brightness. To this, however, there are several remarkable exceptions. Stars have been observed, sufficiently numerous to be regarded as a distinct class, which exhibit periodical changes of appearance. Some undergo gradual and alternate increase and diminution of magnitude, varying between determinate limits, and presenting these variations in equal intervals Some are observed to attain a certain maximum magnitude, from which they gradually and regularly decline until they altogether disappear. After remaining for a certain time invisible, they re-appear and gradually increase till they attain their maximum splendour, and this succession of changes is regularly and periodically repeated. Such objects are called periodic stars.

3340. Remarkable stars of this class in the constellations of Cetus and Perseus.— The most remarkable of this class is the star called Omikron, in the neck of the Whale, which was first observed by David Fabricius, on the 13th August, 1596. This star retains its greatest brightness for about fourteen days, being then equal to

a large star of the second magnitude. It then decreases continually for three months until it becomes invisible. It remains invisible for five months, when it re-appears, and increases gradually for three months until it recovers its maximum splendour. This is the general succession of its phases. Its entire period is about 332 days. This period is not always the same, and the gradations of brightness through which it passes are said to be subject to variation. Hevelius states that, in the interval between 1672 and 1676, it did not appear at all.

Some recent observations and researches of M. Argelander, render it probable that the period of this star is subject to a variation which is itself periodical, the period being alternately augmented and diminished to the extent of 25 days. The variations

of the maximum lustre are also probably periodical.

The star called Algol, in the head of Medusa, in the constellation of Perseus, affords a striking example of the rapidity with which these periodical changes sometimes succeed each other. This star generally appears as one of the second magnitude; but an interval of seven hours occurs at the expiration of every sixty-two, during the first three hours and a half of which it gradually diminishes in brightness till it is reduced to a star of the fourth magnitude, and during the remainder of the interval it again gradually increases until it recovers its original magnitude. Thus, if we suppose it to have attained its maximum splendour at midnight on the first day of the month, its changes would be as follows:—

D. H. M. D. H. M. D. H. M.

0 0 0 to 2 14 0 It appears of second magnitude.

2 14 0 to 2 17 24 It decreases gradually to fourth magnitude.

2 17 24 to 2 20 48 It increases gradually to second magnitude.

2 20 48 to 5 10 48 It appears of second magnitude.

5 10 48 to 5 14 12 It decreases to fourth magnitude.

5 14 12 to 5 17 36 It increases to second magnitude.

&c. &c. &c.

This star presents an interesting example of its class, as it is constantly visible, and its period is so short that its succession of phases may be frequently and conveniently observed. It is situate near the foot of the constellation Andromeda, and lies a few degrees north-east of three stars of the fourth magnitude which form a triangle.

Goodricke, who discovered the periodic phenomena of Algol in 1782, explained these appearances by the supposition that some opaque body revolves round it, being thus periodically interposed between the earth and the star, so as to intercept a large portion of

its light.

The more recent observatious on this star indicate a decrease of

its period, which proceeds with accelerated rapidity. Sir J. Herschel thinks that this decrease will attain a limit, and will be followed by an increase, so that the variation of the period will prove itself to be periodic.

The stars δ in Copheus and β in Lyra are remarkable for the regular periodicity of their lustre. The former passes from its least to its greatest lustre in thirty-eight hours, and from its greatest to its least in ninety-one hours. The changes of lustre of the latter, according to the recent observations of Argelander, are very complicated and curious. Its entire period is 12 days 21 hrs. 53 min. 10 sec., and in that time it first increases in lustre, then decreases, then increases again, and then decreases, so that it has two maxima and two minima. At the two maxima its lustre is that of a star of the 3.4 magnitude, and at one of the minima its lustre is that of a star of the 4.3, and at the other that of a star of the 4.5 magnitude.

In this case also the period of the star is found to be periodically variable.

3341. Table of the periodic stars. — In the following Table the stars periodically variable, discovered up to 1848, are given, with their periods and extremes of lustre. This Table has been collected from various astronomical records by Sir J. Herschel.

No.	Star.	Period.	Cha b	inge of	Discovered by
_		d. dec.	from	to	
1	β Persei (Algol)	2.8673	2	4	Goodricke, 1782.
2	λ Tauri	4 土	4	5.4	Baxendell, 1848.
3	* Cephei	5.3664	3.4	5	Goodricke, 1784.
4	7 Aquiles	7.1763	3.4	4.5	Pigott, 1784.
5	* Cancri R. A. (1800))		-		
-	$= 8^{h} 32.5^{m} N. P.$	9.015	7.8	10	Hind, 1848.
	D. 70° 15′		1		,
6	ζ Geminorum	10.2	4.3	4.5	Schmidt, 1847.
7	β Lyra	12.9119	3.4	4.5	Goodricke, 1784.
8	a Herculis	63 士	3	4	Herschel, 1796.
9	59 B. Scuti R. A.(1801))		1		
	= 18h 37m N. P.	71.200	5	0	Pigott, 1795.
	D. = 95° 57')				
10	& Aurige	250 	3	4	Heis, 1846.
11	o Ceti (Mira)	331.63.	2	0	Fabricius, 1596.
12	* SerpentisR A (1828))		1		
	== 15h 46m 45 P. }	335 土	7?	0	Harding, 1826.
	D. 74° 20′ 30″)		ł		
13	χ Cygni	396.875	6	11	Kirch, 1687.
14	v Hydræ (B. A. C. 4501)	494 士	4	1.0	Maraldi, 1704.
15	Cephei (B. A. C. 7582)	5 or 6 years	3	6	Herschel, 1782.
16	34 Cyni (B. A. C. 6990)	18 years ±	6	0	Janson, 1600.
17	* Leonis (B. A. C. 3345)		6	0	Koch, 1782.
18	g Sagittarii	Ditto	3	6	Halley, 1676.
19	↓ Leonis		6	0	Montanari, 1667.
20	η Cygni	Ditto	4.5	5.6	Herschel, jun., 1842?

Star.	Period.	Chan	ige of	Discovered by
A 5 7 (d. dec,	from	to	1
rginis R.A.(1840) = 12 ^h 3 ^m N. P. D. 82° 8′	145 days	6.7	0	Harding, 1814.
ronæ Bor. (B. A.) C. 5236)	101 months	6	0	Pigott, 1795.
detis (B. A. C. 581) gus ionis ssæ majoris ssæ majoris ssæ minoris sssiopeiæ ydræ A. (1847) = 22 ^h	5 years? Irregular Irregular Some years Ditto 2 or 3 years? 225 days? 29 or 30 days?	6 1 1 1·2 1·2 2 2 2·3	8 4 1·2 2 2 2·3 2·3 3	Piazzi, 1798. Burchell, 1827. Herschel, jun., 1836. Ditto, 1846. Ditto, 1846. Struve, 1838. Herschel, jun., 1838. Ditto, 1837.
58 ^m 57·9° N. P. D. = 80° 17′ 30″	Unknown	8.7	0	Hind, 1848.
A. (1848) = 7 ^b 33 ^m 55·2 ^s N. P. D. = 66° 11′ 56″	Ditto	9	0	Ditto, 1848.
A. $(1848) = 7^h$ $40^m 10 \cdot 3^s \text{ N. P. D.}$ $= 65^\circ 53' 29''$	Ditto	9	0	Ditto, 1848.
© R. A. 22 ^h 21 ^m) 0·4 ^s (1848) N. P. } D. 100° 42′ 40″	Ditto	7.8	0	Rümker.

marcely perceivable, but they become suddenly so great that the star wholly disappears. The variations of No. 25 were very conspicuous from 1836 to 1840, and again in 1849, being much less to in the intermediate time.

8342. Hypotheses proposed to explain the phenomena,—Several

explanations have been proposed for these appearances.

1. Sir W. Herschel considered that the supposition of the existence of spots on the stars similar to the spots on the sun, combined with the rotation of the stars upon axes, similar to the rotation of the sun and planets, afforded so obvious and satisfactory an explanation of the phenomena, that no other need be sought.

2. Newton conjectured that the variation of brightness might be produced by comets falling into distant suns and causing temporary sonflagrations. Waiving any other objection to this conjecture, it is put aside by its insufficiency to explain the periodicity of the

phenomena.

3. Maupertuis has suggested that some stars may have the form of thin flat disks, acquired either by extremely rapid rotation on an axis, or other physical cause. The ring of Saturn affords an example of this, within the limits of our own system, and the modern discoveries in nebular astronomy offer other examples of a like form. The axis of rotation of such a body might be subject to periodical change like the nutation of the earth's axis, so that the flat side of the luminous disk might be present more or less towards the earth at different times, and when the edge is so presented, it might be too thin to be visible. Such a succession of phenomena are actually exhibited in the case of the rings of Saturn, though proceeding from different causes.

4. Mr. Dunn* has conjectured that a dense atmosphere surrounding the stars, in different parts more or less pervious to light, may explain the phenomena. This conjecture, otherwise vague, indefinite, and improbable, totally fails to explain the periodicity of the

phenomena.

5. It has been suggested that the periodical obscuration or total disappearance of the star, may arise from transits of the star by its attendant planets. The transits of Venus and Mercury are the

basis of this conjecture.

The transits of none of the planets of the solar system, seen from the stars, could render the sun a periodic star. The magnitudes, even of the largest of them, are altogether insufficient for such an effect. To this objection it has been answered that planets of vastly greater comparative magnitude may revolve round other suns. But if the magnitude of a planet were sufficient to produce by its transit these considerable obscurations, it must be very little inferior to the

magnitude of the sun itself, or at all events, it must bear a very considerable proportion to the magnitude of the sun; in which case it may be objected that the predominance of attraction necessary to maintain the sun in the centre of its system could not be secured. To this objection it is answered, that although the planet may have a great comparative magnitude, it may have a very small comparative density, and the gravitating attraction depending on the actual mass of matter, the predominance of the solar mass may be readed consistent with the great relative magnitude of the planet by supposing the density of the one vastly greater than that of the etter. The density of the sun is much greater than the density of Seture.

6. It has been suggested that there may be systems in which the central body is a planet attended by a lesser sun revolving round is as the moon revolves round the earth, and in that case the periodical obscuration of the sun may be produced by its passage once in each

revolution behind the central planet.

Such are the various conjectures which have been proposed to explain the periodic stars; and as they are merely conjectures, scarcely deserving the name of hypotheses or theories, we shall leave them to be taken for what they are worth.

II. TEMPORARY STARS.

Phenomena in most respects similar to those just described, but exhibiting no recurrence, repetition, or periodicity, have been observed in many stars. Thus, stars have from time to time appeared in various parts of the firmament, have shone with extraordinary splendour for a limited time, and have then disappeared

and have never again been observed.

3343. Temporary stars seen in ancient times.—The first star of this class which has been recorded, is one observed by Hipparches, 125 B. c., the disappearance of which is said to have led that astronomer to make his celebrated catalogue of the fixed stars; a work which has proved in modern times of great value and interest. In the 389th year of our era, a star blazed forth near a Aquilæ, which shone for three weeks, appearing as splendid as the planet Venus, after which it disappeared and has never since been seen. In the years 945, 1264, and 1572, brilliant stars appeared between the constellations of Cepheus and Cussiopeia. The accounts of the positions of these objects are obscure and uncertain, but the intervals between the epochs of their appearances being nearly equal, it has been conjectured that they were successive returns of the same periodic star, the period of which is about 300 years, or possibly half that interval.

The appearance of the star of 1572 was very remarkable, and having been witnessed by the most eminent astronomers of that day,

the account of it may be considered to be well entitled to confidence. Tycho Brahe, happening to be on his return on the evening of the 11th November from his laboratory to his dwelling-house, found a crowd of peasants gazing at a star which he was sure did not exist half an hour before. This was the temporary star of 1572, which was then as bright as the Dog-star, and continued to increase in splendour until it surpassed Jupiter when that planet is most brilliant, and finally it attained such a lustre, that it was visible at midday. It began to diminish in December, and altogether disappeared in March, 1574.

On the 10th October, 1604, a splendid star suddenly burst out in the constellation of *Serpentarius*, which was as bright as that of 1572. It continued visible till October, 1605, when it vanished.

3344. Temporary star observed by Mr. Hind. — A star of the fifth magnitude, easily visible to the naked eye, was seen by Mr. Hind in the constellation of Ophiuchus, on the night of the 28th April, 1848. From the perfect acquaintance of that observer with the region of the firmament in which he saw it, he was quite certain that, previous to the 5th April, no star brighter than those of the ninth magnitude had been there, nor is there any star in the catalogues at all corresponding to that which he saw there on the 28th. This star continued to be seen until the advance of the season and its low altitude rendered it impossible to be observed. It, however, constantly dimfnished in lustre until it disappeared, and has not since been seen.

3345. Missing stars. — To the class of temporary stars may be referred the cases of numerous stars which have disappeared from the firmament. On a careful examination of the heavens, and a comparison of the objects observed with former catalogues, and of catalogues ancient and modern with each other, many stars formerly known are now ascertained to be missing; and although, as Sir John Hersehel observes, there is no doubt that in many instances these apparent losses have proceeded from mistaken entries, yet it is equally certain that in numerous cases there can have been no mistake in the observation or the entry, and that the star has really existed at a former epoch, and as certainly has since disappeared.

When we consider the vast length of many of the periods of astronomical phenomena, it is far from being improbable that these phenomena which seem to be occasional, accidental, and springing from the operation of no regular physical causes, such as those indicated by the class of variable stars first considered, may after all be periodic stars of the same kind, whose appearances and disappearances are brought about by similar causes. All that can be certainly known respecting them is, that they have appeared or disappeared once in that brief period of time within which astronomical observations have been made and recorded. If they be periodic stars,

n of whose period exceeds that interval, their changes have been once exhibited to us, and after ages have rolled time has converted the future into the past, astronomers as the next occurrence of their phases, and discover that lar, harmonious, and periodic, which appears to us accicasional, and anomalous.

III. DOUBLE STARS.

the stars are examined individually by telescopes of a wer, it is found that many which to the naked eye appear le stars are in reality two stars placed so close together appear as one. These are called double stars.

Researches of Sir W and Sir I Herschel — A year

Researches of Sir W. and Sir J. Herschel. — A very umber of these objects had been discovered before the had received the vast accession of power which was given he labour and genius of Sir William Herschel. That asobserved and catalogued 500 double stars; and subsequent among whom his son, Sir John Herschel, holds the forest, have augmented the number to 6000.

Stars optically double.—The close apparent juxta-position are on the firmament is a phenomenon which might be

admitted; and such may, in fact, be the cause of the phenomenon in some instances. The chances against such proximity of the lines of direction are however so great as to be utterly incompatible with the vast number of double stars that have been discovered, even were there not, as there is, other conclusive proof that this proximity and companionship is neither accidental nor merely apparent, but that the connection is real, and that the objects are united by a physical bond analogous to that which attaches the planets to the sun.

But apart from the proofs of real proximity which exist respecting many of the double stars, and which will presently be explained, it has been shown that the probability against mere optical juxtaposition, such as that described above, is almost infinite. Professor Struve has shown that, taking the number of stars whose existence has been ascertained by observation down to the 7th magnitude inclusive, and supposing them to be scattered fortuitously over the entire firmament, the chances against any two of them having a position so close to each other as 4" would be 9570 to 1. But when this calculation was made, considerably more than 100 cases of such duple juxtaposition were ascertained to exist. The same astronomer also calculated that the chances against a third star falling within 32" of the first two would be 173524 to one; yet the firmament presents at least four such triple combinations.

Among the most striking examples of double stars may be mentioned the bright star Castor, which, when sufficiently magnified, is proved to consist of two stars between the third and fourth magnitudes, within five seconds of each other. There are many, however, which are separated by intervals less than one second; such as a Arietis, Atlas Pleiadum, γ Coronæ, η and ζ Herculis, and τ and γ Ophiuchi.

3349. Argument against mere optical double stars derived from · their proper motion.—Another argument against the supposition of mere fortuitous optical juxtaposition, unattended by any physical connection, is derived from a circumstance which will be fully explained hereafter. Certain stars have been ascertained to have a proper motion, that is, a motion exclusively belonging to each individual star, in which the stars around it do not participate. some of the double stars have such a motion. If one individual of the pair were affected by a proper motion, in which the other does not participate, their separation at some subsequent epoch would become inevitable, since one would necessarily move away from the Now, no such separation has in any instance been witnessed. It follows, therefore, that the proper motion of one equally affects the other, and, consequently, that their juxtaposition is real and not merely optical. 59 *

Struve's classification of double stars. - The systematic n of double stars, and their reduction to a catalogue with descriptions, commenced by Sir W. Herschel, has been with great activity and success by Sir J. Herschel, Sir and Professor Struve, so that the number of these objects n, as to character and position, amounts to several thouindividuals of each pair being less than 32" asunder. been classed by Professor Struve according to their disinder, the first class being separated by a distance not 1", the second between 1" and 2", the third between 2" e fourth between 4" and 8", the fifth between 8" and 12", between 12" and 16", the seventh between 16" and 24" ghth between 24" and 32". Selection of double stars. - The double stars in the followhave been selected by Sir J. Herschel from Strave's as remarkable examples of each class well adapted for ns by amateurs, who may be disposed to try by them the of telescopes. (See next page.) Coloured double stars. - One of the characters observed e double stars is the frequent occurrence of stars of differs found together. Sometimes these colours are comple-

1059); and when this occurs, it is possible that the fainter

y Coronas Bor. y Circini. a Placit y Centauri. d Cygral. g Hydr y Lupi. c Chamaleontis. y Ceti. a Arietis. S Bootis. y Leoni g Heroulis. t Casniopeise. y Cor. 1 y Oronas. t 2 Cancril. y Virgii y Heroulis. E Urse maj. d Serpe	e Piseium. β Hydre. tis. γ Ceti. γ Leontis. γ Virginis. δ Serpentis.	a Cracis. a Herculis. a Gennin. d Gennin.	β Orionia. γ Arietia. γ Delphini. ζ Antile.	e Centeuri.	e Can. Von.	1 Hamelle
	β Hydræ. γ Ceti. γ Leontis. γ Cor. Aus. γ Virginis. δ Serpentis.	a Herculla. a Gemin. δ Gemin. ζ Cor. Bor. θ Phænicia.	y Ariotia. y Delphini. \$ Antilæ.			o Meloures
	ids. y Cect. y Leonds. y Cor. Aus. y Virginis. d Serpentis.	a Gemin. δ Gemin. ζ Cor. Bor. θ Phenicis.	y Delphini. \$ Antilæ.	B Cephei.	s Norms.	* Lyre.
		 d Gemin. ζ Cor. Bor. θ Phænicis. 	\$ Antiles.	β Scorpii.	Ylectum.	. Canori.
		ζ Cor. Bor. θ Phænicis.		y Volantis.	9 Serpentls.	k Herculis.
	y Virginia. d Serpentia.	9 Phenicis.	, Cassiopeise.	• Lapi.	R Cor. Aus.	« Cephi.
	d Serpentis.		9 Bridant.	CUrsa maj.	r Teari.	↓ Draoonis.
	. Bootis	« Cephel.	e Orionis.	R Bootis.	24 Comm.	* Oygni.
λ Cassiopeise. π Aquilse.		λ Orionis.	f Bridani.	8 Monocerotis.	41 Draconis.	23 Orionis.
A Ophinchi. c Coro. Bor.	s Draconis.	r Cygni.	2 Cen. Ven.	61 Cygni.	61 Ophiuchi.	
r Lupi. 2 Camelopar.	. s Hydra.	& Bootis.				
7 Ophluchi. 32 Orionia.	\$ Aquarii.	€ Cephei.				
♦ Draconia. 52 Orionia.	Corlonis.	r Bootis.				
♦ Urse maj.	t Leonis.	e Capricor.				
X Aquilas.	. Trianguli.	, Argue.			,	
. Leonis.	r Leporis.	. Aurigm.				
Atlas Pleiad.	k Draconia.	r Eridani.				
4 Aquarii.	p Canis.	70 Ophiuchi.				
42 Comss.	e Hereulia.	12 Eridant				
52 Arietis.	e Cassiopeise.	32 Eridani.				
66 Piseium.	44 Bootis.	44 Hereulis.				

third star is much smaller than the principal ones, for n the cases of ζ Cancri, ξ Scorpii, 11 Monocesos, and 12 In others, as in θ Orionis, the four component stars are mous.

Attempts to discover the stellar parallax by double stars, the attention of astronomers was first attracted to double as thought they would afford a most promising means of

determining the annual parallax, and thereby discovering the distance of the stars. If we suppose the two individuals composing a double star, being situate very nearly in the same direction as seen from the earth, to be at very different distances, it might be expected that their apparent relative position would vary at different seasons of the year, by reason of the change of position of the earth.

Let A and B, fig. 875, represent the two individuals composing a double star. Let c and D represent two positions of the earth in its annual orbit, separated by an interval of half a year, and placed therefore on opposite sides of the sun s. When viewed from c, the star B will be to the hands to resolve finally the great problem of the stellar parallax, and Sir William Herschel accordingly engaged, with all his characteristic ardour and sagacity, in an extensive series of observations on the numerous double stars, for the original discovery of which science was already so deeply indebted to his labours. He had not, however, proceeded far in his researches, when phenomena unfolded themselves before him, indicating a discovery of a much higher order and interest than that of the parallax which he sought. He found that the relative position of the individuals of many of the double stars which he examined were subject to a change, but that the period of this change had no relation to the period of the earth's motion. It is evident that whatever appearances can proceed from the earth's annual motion, must be not only periodic and regular, but must pass annually through the same series of phases, always showing the same phase on each return of the same epoch of the sidereal year. In the changes of position which Sir William Herachel observed in the double stars, no such series of phases presented themselves. Periods, it is true, were soon developed; but these periods were regulated by intervals which neither agreed with each other nor with the earth's annual motion.

3356. His discovery of binary stars. - Some other explanation of the phenomena must, therefore, be sought for; and the illustrious observer soon arrived at the conclusion, that these apparent changes of position were due to real motions in the stars themselves; that these stars, in fact, moved in proper orbits in the same manner as the planets moved around the sun. The slowness of the succession of changes which were observed, rendered it necessary to watch their progress for a long period of time before their motions could be certainly or accurately known; and accordingly, although these researches were commenced in 1778, it was not until the year 1803 that the observer had collected data sufficient to justify any positive conclusion respecting their orbital motions. In that and the following year, Sir William Herschel announced to the Royal Society, in two memorable papers read before that body, that there exist sidereal systems consisting of two stars revolving about each other in regular orbits, and constituting what he called binary stars, to distinguish them from double stars, generally so called, in which no such periodic change of position is discoverable. Both the individuals of a binary star are at the same distance from the eye in the same sense in which the planet Uranus and its attendant satellites are said to be at the same distance.

More recent observation has fully confirmed these remarkable discoveries. In 1841, Mädler published a catalogue of upwards of 100 stars of this class, and every year augments their number. These stars require the best telescopes for their observation, being generally so close as to render the use of very high magnifying powers indispensable.

8857. Extension of the law of gravitation so the stars.—The moment the revolution of one star round another was accertained, the idea of the possible extension of the great principle of gravitation to these remote regions of the universe naturally suggested itself. Newton has proved in his Principia, that if a body revolve in an ellipse by an attractive force directed to the focus, that fine will vary according to the law which characterises gravitation. Thus an elliptical orbit became a test of the presence and sway of the law of gravitation. If, then, it could be accortained that the orbits of the double stars were ellipses, we should at once arrive at the fact that the law of which the discovery conferred such calculation the name of Newton, is not confined to the solar system; by prevails throughout the universe.

3358. Orbit of star around star elliptic. — The first distinct system of calculation by which the true elliptic elements of the orbit of a binary star were ascertained, was supplied in 1830, by M. Savery, who showed that the motion of one of the most remarkable of these stars (§ Ursæ majoris), indicated an elliptic orbit described in 584 years. Professor Encké, by another process, arrived at the fact that the star 60 Ophiuchi moved in an ellipse with a period of 74 years. Several other orbits were ascertained and computed by Sir John Herschel, MM. Mädler, Hind, Smyth, and others.

The following Table is given by Sir J. Herschel, as containing the principal results of observation in this part of stellar astronomy of to 1850.

Star's Name.	Apparent Semi-axis.	Eccentricity.	Position of Node.	Peribetion from Node or Orbit.	Inclination.	Period in Years.	Periheljon Pasage,	Pr whole the
1. Herculis	1·189′ 1·088	0.44154	39°26′ 24 18	261 21	50°53′		1829-50 1810-23	Madler, Direc
4. a. E Ursse ma-	1.292	0.23486	1 28	266 0	63 17		1853 87	Ditto.
joris	3.857	0-41640	95 22		50 40	58-202	1817-28	Savare.
4 b. Ditto	3:278	0.37770	97 47	134 22	56 6	60:720	181072	Bornchel, &
4. c. Ditto	2-417	0.41350	98 52	130 48	54 56	61:464	1816-44	Misdlet.
5. w Leonis		0.64338	135 11	185 27	46 33	82 533	1849 76	Ditto
6. a. p. Ophiuchi			147 12	125 22	46 25		1806'88	Eneka.
6, b. Ditto		0.46670	137 2	145 46	48 5		1807-06	Horschin,
6. c. Ditto 7. Σ 3062		0.44380	126 55	142 53	64 51		181272	Middlet
	1.255	0-44958	15 3	137 27	35 31	94-765	1837-41	Ditto
		0.59374	359 59	100 59	80 5		1779-88	Herschill.
	1.811	0.60667	24 54	243 24	46 23 23 36	178-700		Hind.
1. a. Castor	3.580 8.086	0.87952	5 33	313 45 97 29	23 36 70 3		1830-43	Herache P
1. b. Ditto	7:008	0.75820	58 6 23 5	87 37	70 58	252-660		Ditte
Le. Ditto	6.300	0.24050	23 5 11 24		43 14		1913-90	Mödler.
2. a. o Coronae B.		0.69978	25 7	64 38	29 29	632-270		Flind
2. b. Ditto		0.72560	21 3		25 39		1826-00	Maidler.
L µ 2 Bootis					46 57		1826-48	Hind
Le m sonofficial		0.95000			47 56	77:000		Ditto. Jacob

The elements Nos. 1, 2, 3, 4, c, 5, 6, c, 7, 11 b, 12, a, are extracted from M. Mädler's synoptic view of the history of double stars, in vol. ix. of the Dorpat Observations: 4 a, from the Connoiss. des Temps, 1830: 4 b, 6 b, and 11 a, from vol. v. Trans. Astron. Soc. Lond.: 6 a, from Berlin Ephemeris, 1832: No. 8, from Trans. Astron. Soc. vol. vi.: No. 9, 11 c, 12 b, and 13 from Notices of the Astronomical Society, vol. vii. p. 22, and viii. p. 159, and No. 10 fron Sir John Herschel's "Results of Astronomical Observations, &c., at the Cape of Good Hope," p. 297. The \(\mathcal{E}\) prefixed to No. 7 denotes the number of the star in M. Struve's Dorpat Catalogue (Catalogus Novus Stellarum Duplicium, &c., Dorpat, 1827), which contains the places for 1826 of 3112 of these objects.

The "position of the node" in col. 4 expresses the angle of position of the line of intersection of the plane of the orbit, with the plane of the heavens on which it is seen projected. The "inclination" in col. 6 is the inclination of these two planes to one another. Col. 5 shows the angle actually included in the plane of the orbit, between the line of nodes (defined as above) and the line of apsides. The elements assigned in this table to "Leonis, & Bootis, and Castor must be considered as very doubtful, and the same may perhaps be said of those ascribed to # 2 Bootis, which rest on so small an are of the orbit, and that too imperfectly observed, to afford a

secure basis of calculation.



Fig. 876.

3359. Remarkable case of y Virginis. — The most remarkable of these, according to Sir John Herschel, is y Virginis; not only on account of the length of its period, but by reason also of the great diminution of apparent distance and rapid increase of angular motion about each other, of the individuals composing it. It is a bright star of the fourth magnitude, and its component stars are almost exactly equal. has been known to consist of two stars since the beginning of the eighteenth century, their distance being then between six and seven seconds; so that any tolerably good telescope would resolve it. Since that time they have been constantly approaching, and are at present hardly more than a single second asunder; so that no telescope that is not of very superior quality, is competent to show them otherwise than as a single

what lengthened in one direction. It fortunately happens ley, in 1718, noticed and recorded, in the margin of one servation-books, the apparent direction of their line of as being parallel to that of two remarkable stars a and b of constellation, as seen by the naked eye. They are entered stinct stars in Mayer's catalogue; and this affords also cans of recovering their relative situation at the date of his ns, which were made about the year 1756. Without pargindividual measurements, which will be found in their positories, it will suffice to remark, that their whole series nted by an ellipse.

Singular phenomena produced by one solar system thus round another. — To understand the curious effects which nd the case of a lesser sun with its attendant planets round a greater, let the larger sun, fig. 876, with its e represented at s, in the focus of an ellipse, in which the accompanied by its planets moves. At a this latter sun erihelion, and nearest to the greater sun s. Moving in its course to B, it is at its mean distance from the sun s. At phelion, or its most distant point, and finally returns through erihelion A. The sun s, because of its vast distance from

ferent times. During a part of the day both will be seen at once in the heavens, occupying different places, and reaching the meridian at different times. There will be two noons. In the morning for some time, more or less, according to the season of the year, one sun only will be apparent, and in like manner, in the evening, the sun which first rose will be the first to set, leaving the dominion of the heavens to its splendid companion.

The diurnal and annual phenomena incidental to the planets attending the central sun s will not be materially different, except that to them the two suns will have extremely different magnitudes. and will afford proportionally different degrees of light. The lesser sun will appear much smaller, both on account of its really inferior magnitude and its vastly greater distance. The two days, therefore, when they occur, will be of very different splendour, one being probably as much brighter than the other as the light of noonday is to that of full moonlight, or to that of the morning or evening twilight.

But these singular vicissitudes of light will become still more striking, when the two suns diffuse light of different colours. us examine the very common case of the combination of a crimson with a blue sun. In general, they will rise at different times. When the blue sun rises, it will for a time preside alone in the heavens, diffusing a blue morning. Its crimson companion, however, soon appearing, the lights of both being blended, a white day will follow. As evening approaches, and the two orbs descend toward the western horizon, the blue sun will first set, leaving the crimson one alone in the heavens. Thus a ruddy evening closes this curious succession of varying lights. As the year rolls on, these changes will be varied in every conceivable manner. At those seasons when the suns are on opposite sides of the planet, crimson and blue days will alternate, without any intervening night; and at the intermediate epochs all the various intervals of rising and setting of the two suns will be exhibited.

8361. Magnitudes of the stellar orbits.—It is evident that in any case in which the parallax of a binary star, and consequently its distance from our system, has been or may be discovered, the magnitude of the orbit of one described round the other can be determined with a precision and certainty proportional to those with which the parallax is known. For, in that case, the linear value of 1" at the star will be found by dividing the earth's distance from the sun by the parallax expressed in seconds.

The binary stars 61 Cygni and a Centauri supply examples of the application of this principle. The parallax of these stars has been ascertained (2605). That of 61 Cygni is 0.348, and the semi-axis of the elliptic orbit of one star round the other is 15.5". The semi-diameter of the earth's orbit being D, therefore, the linear

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III.

I" at the star is $\frac{D}{0.348}$, and the semi-axis a of the stellar

$$a = D \times \frac{15.5}{0.348} = 44.54 D.$$

s, therefore, that the semi-axis of the orbit is greater than eptune's orbit in the ratio of 3 to 2.

agle subtended by the semi-axis of the elliptic orbit of ri is not so certainly known, but is taken to be about ne parallax of this star being 0.913", we should then

$$a = D \times \frac{12}{0.913} = 13.14 D.$$

axis of the stellar orbit would, therefore, be about one-half an the orbit of Saturn.

Masses of binary stars determined by their parallax and. Since by (2634) the relation of the semi-axis of the orbits eriodic times determines the relative masses of the central are enabled to compare the mass of the central star of a stem with that of the sun, in all cases in which the real of the orbit and the periodic time are known. Thus, let mass of the central star, a' the semi-axis of the orbit, and riodic time, and let M be the mass of the sun, a the semi-acceptance earth's orbit, and P the earth's period, and we shall

of apparent position on the surface of the heavens. The stars, on the contrary, so far as the powers of the eye unaided by art can discover, never change their relative position in the firmament, which seems to be carried round us by the diurnal motion of the sphere, just as if the stars were attached to it, and merely shared in its apparent motion.

But the stars, though subject to no motion perceptible to the naked eye, are not absolutely fixed. When the place of a star on the heavens is exactly observed by means of good astronomical instruments, it is found to be subject to a change from month to month and from year to year, small indeed, but still easily observed

and certainly ascertained.

3364. The sun not a fixed centre. — It has been demonstrated by Laplace, that a system of bodies, such as the solar system, placed in space and submitted to no other continued force except the reciprocal attractions of the bodies which compose it, must either have its common centre of gravity stationary or in a state of uniform rectilinear motion.

8365. Effect of the sun's supposed motion on the apparent places of the stars.—The chances against the conditions which would render the sun stationary, compared with those which would give it a motion in some direction with some velocity, are so numerous that we may pronounce it to be morally certain that our system is in motion in some determinate direction through the universe. Now, if we suppose the sun attended by the planets to be thus moved through space in any direction, an observer placed on the earth would see the effects of such a motion, as a spectator in a steamboat moving on a river would perceive his progressive motion on the stream by an apparent motion of the banks in a contrary direction. The observer on the earth would, therefore, detect such a motion of the solar system through space by the apparent motion in the contrary direction with which the stars would be affected.

Such a motion of the solar system would affect different stars differently. All would, it is true, appear to be affected by a contrary motion, but all would not be equally affected. The nearest would appear to have the most perceptible motion, the more remote would be affected in a less degree, and some might, from their extreme distance, be so slightly affected as not to exhibit any apparent change of place, even when examined with the most delicate instruments. To whatever degree each star might be affected, all the changes of position would, however, apparently take place in the same direction.

The apparent effects would also be exhibited in another manner. The stars in that region of the universe toward which the motion of the system is directed, would appear to recede from each other. The spaces which separate them would seem to be gradually augmented, while, on the contrary, the stars in the opposite quarter

n to be crowded more closely together, the distances beand star being gradually diminished. This will be more apprehended by fig. 877.



Fig. 877.

e line ss' represent the direction of the motion of the nd let s and s' represent its positions at any two epochs. stars ABC would be separated by intervals measured by ASB, and BSC, while at s' they would appear separated ser angles ASB, and BSC. Seen from s', the stars ABC em to be closer together than they were when seen from s. reason the stars abc, towards which the system is here to move, would seem to be closer together when seen from hen seen from s'. Thus, in the quarter of the heavens

Herculis. About the same time, Prevost came to a like conclusion, assigning, however, the direction of the supposed motion to a point

differing by 27° from that indicated by Sir W. Herschel.

Since that epoch, the proper motions of the stars have been more extensively and accurately observed, and calculations of the motion of the sun which they indicate, have been made by several astronomers. The following points have been assigned as the direction of the solar motion in 1790:--

B. A.	N. P. D.	•
260° 84′	63° 43′	Sir W. Herschel.
256° 25′	51° 23′	Argelander.
255° 10′	51° 26′	Ditto.
261° 11′	59° 2′	• Ditto.
252° 53′	75° 84′	Luhndahl.
261° 22′	62° 24′	Otto Struve.

The first estimate of Argelander was made from the proper motions of 21 stars, each of which has an annual motion greater than 1"; the second from 50 stars having annual proper motions between 1" and 0.5", and the third from those of 319 stars having motions between 0.5" and 0.1". The estimate of M. Luhndahl is based on the motions of 147 stars, and that of M. Struve on 392 stars.

The mean of all these estimates is a point whose right ascension is 259° 9', and north polar distance 5° 23', which it will be seen differs very little from the point originally assigned by Sir W. Herschel.

All the preceding calculations being based on observations made on stars in the northern hemisphere, it was obviously desirable that similar estimates should be made from the observed proper motions of southern stars. Mr. Galloway undertook and executed these calculations; and found that the southern stars gave the direction of the solar motion for 1790, to be towards a point whose right ascension is 260° 1', and north polar distance 55° 87'.

No doubt therefore, can remain that the proper motion of the stars is produced by a real motion of the solar system, and that the direction of this motion in 1790 was towards a point of space which seen from the then position of the system had the right ascension

of about 260°, and the north polar distance of about 55°.

3367. Velocity of the solar motion.—It follows from these calculations, that the average displacement of the stars requires that the motion of the sun should be such as that if its direction were at right angles to a visual ray, drawn from a star of the first magnitude of average distance, its apparent annual motion would be 0.3392"; and taking the average parallax of such a star at 0.209", if D express the semi-axis of the earth's orbit, the annual motion of the sun would be

 $\frac{3392}{2090} \times D = 1.623 D.$

, therefore, that the annual motion of the sun would be $1.623 \times 95,000,000 = 154,200,000$ miles; aily motion

 $\frac{154,200,000}{8651} = 422,000 \text{ miles};$

equal to something more than the fourth of the earth's

The probable centre of solar motion.—The motion of the h has been computed in what precedes, is that which it particular epoch. No account is taken of the possible or changes of direction of such motion. To suppose that the em should move continuously in one and the same directly deep equivalent to the supposition that no body or collecties in the universe would exercise any attraction upon it ously more consistent with probability and analogy, that no f the system is orbital, that is to say, that it revolves he remote centre of attraction, and that the direction of its ust continually change, although such change, owing to

pression will be corrected, and it will, on the contrary, be found that the distribution of the stars over the surface of the celestial sphere follows a distinct and well-defined law; that their density, or the number of them which is found in a given space of the heavens, varies regularly, increasing continually in certain directions and decreasing in others.

Sir W. Herschel submitted the heavens, or at least that part of them which is observable in these latitudes, to a rigorous telescopic survey, counting the number of individual stars visible in the field of view of a telescope of certain aperture, focal length, and magnifying power, when directed to different parts of the firmament. The result of this survey proved that, around two points of the celestial sphere diametrically opposed to each other, the stars are more thinly scattered than elsewhere; that departing from these points in any direction, the number of stars included in the field of view of the same telescope increases first slowly, but at a greater distance more rapidly; that this increase continues until the telescope receives a direction at right angles to the diameter which joins the two opposite points where the distribution is most sparse; and that in this direction the stars are so closely crowded together that it becomes, in some cases, impracticable to count them.

3370. Galactic circle and poles.—The two opposite points of the celestial sphere, around which the stars are observed to be most sparse, have been called the GALACTIC POLES; and the great circle at right angles to the diameter joining these points, has been denominated the GALACTIC CIRCLE.

This circle intersects the celestial equator at two points, situate 10° east of the equinoctial points, and is inclined to the equator at an angle of 63°, and, therefore, to the ecliptic at an angle of 40°.

In referring to and explaining the distribution of the stars over the celestial sphere, it will be convenient to refer them to this circle and its poles, as, for other purposes, they have been referred to the equator and its poles. We shall, therefore, express the distance of different points of the firmament from the galactic circle, in either hemisphere, by the terms north and south GALACTIC LATITUDE.

3371. Variation of the stellar density in relation to this circle.

The elaborate series of stellar observations in the northern hemisphere made during a great part of his life, by Sir W. Herschel, and subsequently extended and continued in the southern hemisphere by Sir J. Herschel, has supplied data by which the law of the distribution of the stars, according to their galactic latitude, has been ascertained at least with a near approximation.

The great celestial survey executed by these eminent observers, was conducted upon the principle explained above. The telescope used for the purpose had 18 inches aperture, 20 feet focal length, and a magnifying power of 180. It was directed indiscriminately

oint of the celestial sphere visible in the latitude of the bservation.

by means of a vast number of distinct observations thus the position of the galactic poles was ascertained. The the stars, measured by the number included in each (as the field of view was called), was nearly the same for galactic latitude, and increased in proceeding from the gap and the same for the poles of the same for galactic latitude, and increased in proceeding from the gap are poles of the same for galactic latitude, and increased in proceeding from the gap are poles of the same for galactic latitude, and increased in proceeding from the gap are poles of the same for galactic latitude was much diminished.

Struve's analysis of Herschel's observations. — An analysis ervations of Sir W. Herschel, in the northern hemisphere,

by Professor Struve, with the view of determining the sity of the stars in successive zones of galactic latitude; e analysis has been made of the observations of Sir J.

in the southern hemisphere.

magine the celestial sphere resolved into a succession of
the measuring 15° in breadth, and bounded by parallels to
tic circle, the average number of stars included within a
ose diameter is 15′, and whose magnitude, therefore, would
the fourth part of that of the disk of the sun or moon,
at which is given in the second column of the following

of whitish nebulous light. This appearance extends over a vast extent of the celestial sphere, deviating in some places from the exact direction of the galactic circle, bifurcating and diverging into two branches at a certain point which afterwards reunite, and at other places throwing out off-shots. This appearance was denominated the Via Lactea, or the galaxy, by the ancients, and it has retained that name.

The course of the milky way may be so much more easily and clearly followed by means of a map of the stars, or a celestial globe, upon which it is delineated, that it will be needless here to describe it.

8874. It consists of innumerable stars crowded together.—When this nebulous whiteness is submitted to telescopic examination with instruments of adequate power, it proves to be a mass of countless numbers of stars, so small as to be individually undistinguishable, and so crowded together as to give to the place they occupy, the whitish appearance from which the milky way takes its name.

Some idea may be formed of the enormous number of stars which are crowded together in those parts of the heavens, by the actual number so distinctly visible as to admit of being counted or estimated, which are stated by Sir W. Herschel to have been seen in spaces of given extent. He states, for example, that in those parts of the milky way in which the stars were most thinly scattered, he sometimes saw eighty stars in each field. In an hour, fifteen degrees of the firmament were carried before his telescope, showing successively sixty distinct fields. Allowing eighty stars for each of these fields, there were thus exhibited, in a single hour, without moving the telescope, four thousand eight hundred distinct stars! But by moving the instrument at the same time in the vertical direction, he found that in a space of the firmament, not more than fifteen degrees long, by four broad, he saw fifty thousand stars, large enough to be individually visible and distinctly counted! The surprising character of this result will be more adequately appreciated, if it is remembered that this number of stars thus seen in the space of the heavens, not more than thirty diameters of the moon's disk in length and eight in breadth, is fifty times greater than all the stars taken together, which the naked eye can perceive at any one time in the heavens, on the most serene and unclouded night!

On presenting the telescope to the richer portion of the via lactea, Herschel found, as might be expected, much greater numbers of stars. In a single field he was able to count 588 stars; and for fifteen minutes, the firmament being moved before his telescope by the diurnal motion, no diminution of number was apparent, so that he estimated that in that space of time, 116,000 stars must have passed in review before him; the number seen at any one time

^{*} From the Greek word yake yakeares, milk.

ater than can be seen by the naked eye, on the entire

, except on the clearest nights.

The probable form of the stratum of stars in which the ced.—It may be considered as established by a body of evidence, having all the force of demonstration, that the are self-luminous bodies, similar to our sun; and that they may differ more or less from our sun and from each agnitude and intrinsic lustre, they have a certain average ; and that, therefore, in the main, the great differences apparent in their brightness, are to be ascribed to difference Assuming, then, that they are separated from each listances analogous to their distances from the sun, itself e general phenomena which have been described above, the rapid increase of stellar density in approaching the lane, combined with the observed form of the milky way, llowing the galactic plane in its general course departs ess from it at some points, bifurcates, resolving itself into ging branches at others, and at others throws out irregular conducted Sir W. Herschel to the conclusion, that the ur firmament, including those which the telescope renders well as those visible to the naked eye, instead of being indifferently in all directions around the solar system

will be the direction of the north, and z D that of the south galactic role. Let z H represent the two branches which bifurcate from the hief stratum at B. Now, if we imagine visual lines to be drawn from z in all directions, it will be apparent that those z C and z D, which are directed to the galactic poles, pass through a thinner bed of stars than any of the others; and since z is supposed to be nearer to the northern than to the southern side of the stratum, z C will mass through a less thickness of stars than z D. As the visual lines are inclined at greater and greater angles to z A, their length rapidly lectroses, as is evident by comparing z A, z E, and z F, which explains the fact that while the stars are as thick as powder in the lirection z A, they become less so in the direction z E, and still less a the direction z F, until at the poles in the directions z C and z D, hey become least dense.

On the other side, z B being less than z A, a part of the galactic sirele is found at which the stars are more thinly scattered; but in we directions, z H intermediate between z B and the galactic poles,

hey again become nearly as dense as in the direction z A.

This illustration must, however, be taken in a very general sense. No attempt is made to represent the various off-shoots and variations of length, breadth, and depth of the stratum measured from the position of the solar system within it, which have been indicated by the telescopic soundings of Sir W. Herschel and his illustrious on, whose wondrous labours have effected what promises in time, by the persevering researches of their successors, to become a complete analysis of this most marvellous mass of systems. Meanwhile the may be considered as demonstrated that it consists of myriads of determinated together:

"A broad and ample road, whose dust is gold,
And pavement stars, as stars to us appear;
Seen in the galaxy, that Milky Way,
Like to a circling zone powder'd with stars."—Millton.

The appearance which this mass of stars would present if viewed from a position directly above its general plane, and at a sufficient listance to allow its entire outline to be discerned, was represented by Sir Wm. Herschel as resembling the starry stratum sketched a Plate XXVI.

He considered that it was probable that the thickness of this bed of stars was equal to about eighty times the distance of the nearest of the fixed stars from our system; and supposing our sun to be near the middle of this thickness, it would follow that the stars on its surface in a direction perpendicular to its general plane would be at the fortieth order of distance from us. The stars placed in the more remote edges of its length and breadth he estimated to be in some places at the nine-hundredth order of distance from us, we

extreme length may be said to be in round number mes the distance of the nearest fixed stars from our space light would take 20,000 years to move over t time at the rate of nearly 200,000 miles betweeks of a common clock!

CHAP. XXIX.

STELLAR CLUSTERS AND NEBULÆ.

b. The stars which form the firmament a stellar by suggests the probable existence of others.—It appears units an individual star, forming only a single or mass of many millions of other similar stars; has limited dimensions, has ascertainable length, ickness, and in short, forms what may be expresse of solar systems. The mind, still unsatisfied, is re in its questions regarding the remainder of in er vast the dimensions of this mass of suns be

the naked eye, would, to telescopes of adequate power, present the same whitish nebulous appearance; and that we might look forward without despair to such augmentation of the powers of the telescope as may even enable us to perceive them to be actual clusters of stars.

3377. Such clusters of stars innumerable. — Such anticipations have accordingly been realised. In various parts of the firmament objects are seen which, to the naked eye, appear like stars seen through a mist, and sometimes as nebulous specks, which might be, and not unfrequently are mistaken for comets. With ordinary telescopes these objects are visible in very considerable numbers, and were observed nearly a century ago. In the Connoissance des Temps, for 1784, Messier, then so celebrated for his observations on comets, published a catalogue of 103 objects of this class, of many which he gave drawings, with which all observers who search for comets ought to be familiar, to avoid being misled by their resemblance to them. The improved powers of the telescope speedily disdoeed to astronomers the nature of these objects, which, when examined by sufficient magnifying powers, prove to be masses of stars elustered together in a manner identical with that cluster in which cour sun is placed. They appear as they do, mere specks of whitish **Eght**, because of their enormous distance.

***378. Distribution of clusters and nebulæ on the firmament.—

***These objects are not distributed fortuitously and indifferently on

***Parts of the heavens. They are wholly absent from some regions,

***some rarely found, and crowded in amazing profusion in others.

***This disposition, however, is not like that of the stars in general,

***Thermined by a great circle of the sphere and its poles. It was

***posed that they showed a tendency to crowd towards a zone at

***that angles to the galactic circle, but a careful comparison of their

***Initial comparison of their

**This disposition has been added to the sphere and its poles. It was

***posed that they showed a tendency to crowd towards a zone at

***that angles to the galactic circle, but a careful comparison of their

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The North Galactic Pole.

Leo major.

Leo minor.

Ursa major.

5 Canes Yenatici. 6 Coma Berenici.

7 Bootes (precedingly).

8 Virago (head, wings and shoulder).

parts of the heavens, on the other hand, where they are found the smallest numbers, are:—

Aries. Taurus

8 Hercules.
(head and shoulders). 9 Serpentarius (northern part).

Orion (head and shoulders). Auriga.

Perseus. Camelopardus. 10 Serpens (tail). 11 Aquila (tail).

7 Draco.

12 Lyra.

the southern hemisphere their distribution is more uniform.

Constitution of the clusters and nebulæ. — What those and of what they severally consist, admits of no reason. So far as relates to the stellar clusters, their constituent visible. They are, as their name imports, masses of stars together at certain points in the regions of space which youd the limits of our own cluster, and are by distance so a the visual magnitude that an entire cluster will appear ted eye, if it be visible at all, as a single star, and when the telescope will be included within the limit of a single sw.

nt clusters exhibit their component stars seen with the mifying power more or less distinctly. This may be exither by difference of distance, or by the supposition that consist of stars of different real magnitudes, and crowded ess closely together. The former supposition is, however,

more natural and probable.

pearance of the stars composing some of the clusters is geous. Sir J. Herschel says, that the cluster which sur-Crucis in the southern hemisphere, occupies the 48th part re degree, or about the tenth part of the superficial magthe moon's disk, and consists of about 110 stars from the itude downwards, eight of the more conspicuous stars being 3380. Nebular hypothesis.—A theory was put forward to explain these objects, based upon views not in accordance with what has just been related. It was assumed hypothetically that the nebulous matter was a sort of luminous fluid diffused through different parts of the universe; that by its aggregation on certain laws of attraction solid luminous masses in process of time were produced, and that these nebulæ grew into clusters.

It would not be compatible with the limits of this work, and the objects to which it is directed, to pursue this speculation through its consequences, to state the arguments by which it is supported and opposed; and it is the less necessary to do so, seeing that such an hypothesis is not needed to explain appearances which are so much more obviously and simply explicable by the admission of a

gradation of distances.

3381. Forms apparent and real of the clusters.—The apparent forms of these objects are extremely various, and subject to most extraordinary and unexpected changes, according to the magnifying power under which they are viewed. This ought, however, to excite no surprise. The telescope is an expedient by which a welldefined and strongly illuminated optical image of a distant object is formed so close to the observer, that he is enabled to view it with microscopes of greater or less power, according to the perfection of its definition, and the intensity of its illumination. Now, it is known to all who are familiar with the use of the microscope, that the apparent form and structure of an object change in the most remarkable and unexpected way when viewed with different microscopic powers. The blood, for example, which viewed with the naked eye, or with low powers, is a uniformly red fluid, appears as a pellucid liquid, having small red disks floating in it, when seen with higher powers (46). Like effects are manifested in the cases of the nebulæ, when submitted to examination with different and increasing magnifying powers, of which we shall presently show many striking examples.

The apparent forms of the stellar clusters are generally roundish or irregular patches. The stars which compose them are always much more densely crowded together, in going from the edges of the cluster towards the centre, so that at the centre they exhibit a per-

fect blaze of light.

The apparent form is that of a section of the real form, made by a plane at right angles to the visual ray. If the mass had a motion of rotation, or any other motion by which it would change this plane, so as to exhibit to the eye successively different sections of it, its real form could be inferred as those of the planets have been. But there are no discoverable indications of any such motion in these objects. Their real forms, therefore, can only be conjectured from comparing their apparent forms with their structural appearance.

usters having round apparent forms, and of which the rapidly more dense towards the centres, are inferred to be obular or spheroidal masses of stars, the greater apparent passing from the edges to the centre being explained by it thickness of the mass, in the direction of the visual line of irregular outline which show also a density increasing are also inferred, for like reasons, to be masses of stars, nensions in the direction of the visual rays correspond with ensions in the direction at right angles to those rays.

Forms apparent and real of the nebulæ.—These objects orms much more various than those presented by the clustere are circular, with more or less precision of outline elliptical, the oval outline having degrees of eccentricity various, from one which scarcely differs from a circle, to h is compressed into a form not sensibly different from a line. In short, the minor axis of the ellipses bears all no to the major axis, until it becomes a very small fraction ter.

er the real from the apparent forms of these objects with inty, there are no sufficient data. But in the cases in brightness increases rapidly towards the centre, which it trally does it may be probably conjectured that their forms

These double nebulæ are generally circular in their apparent, and therefore probably globular in their real form. In some cases they are resolvable clusters.

That such pairs of clusters are physically connected does not admit of a reasonable doubt, and it is highly probable that, like the binary stars, they move round each other, or round a common centre of attraction, although the apparent motion attending such revolution is rendered so slow by their immense distance that it can only be ascertained after the lapse of ages.

3384. Planetary nebulæ. — This class of objects derive their name from their close resemblance to planetary disks. They are in general either circular or very slightly oval. In some cases the disk is sharply defined, in others it is hazy and nebulous at the edges. In some the disk shows a uniform surface, and in some it has an appearance which Sir J. Herschel describes by the term curdled.

There is no reason to doubt that the constitution of these objects is the same as that of other nebulse, and that they are in fact clusters of stars which, by mutual proximity and vast distance, are reduced

to the form of planetary disks.

These objects, which are not numerous, present some remarkable peculiarities of appearance and colour. It has been already observed that, although the companion of a red individual of a double star appears blue or green, it is not certain that this is its real colour, the optical effect of the strong red of its near neighbour being such as would render a white star apparently blue or green, and no example of any single blue or green star has ever been witnessed. The planetary nebulæ, however, present some very remarkable examples of these colours. Sir J. Herschel indicates a beautiful instance of this, in a planetary nebula situate in the southern constellation of the Cross. The apparent diameter is 12", and the disk is nearly circular, with a well-defined outline, and a "fine and full blue colour verging somewhat upon green." Several other planetary nebulæ are of a like colour, but more faint.

The magnitudes of these stupendous masses of stars may be conjectured from their probable distances. One of the largest, and therefore probably the nearest of them, is situate near the star β Ursæ majoris (one of the pointers). Its apparent diameter is 2' 40'. Now, if this were only at the distance of 61 Cygni, whose parallax is known (2603), it would have a diameter equal to seven times that of the extreme limit of the solar system; but as it is certain that its distance must be many times greater, it may be conceived its di-

mensions must be enormous.

3385. Annular nebulæ. — A very few of the nebulæ have been observed to be annular. Until lately there were only four. The telescopes of Lord Rosse have, however, added five to the number, by showing that certain nebulæ formerly supposed to be small round.

e really annular. It is extremely probable, that he smaller class of round nebulæ will prove to be a nitted to further examination with telescopes of a efficiency.

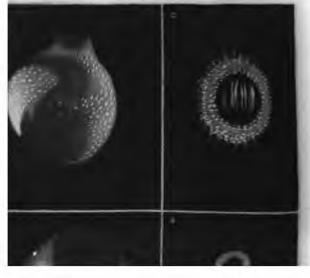
efficiency. Spiral nebulæ. — The discovery of this class of xtraordinary and unexpected which modern resea sed in stellar astronomy, is due to Lord Rosse. rm and character may be conceived by referring d in Plate XXII. figs. 1 and 3, and Plate XXIII raordinary forms are so entirely removed from all of the phenomena presented either in the motions em, or the comets, or those of any other objects t n has been directed, that all conjecture as to the of the masses of stars which could assume sucl vain. The number of instances as yet detected, in prevails, is not great; but it is sufficient to prove on, whatever be its cause, is the result of the oper eral law. It is pretty certain, that when the same I ts which have rendered these forms visible in object dy been so long under the scrutiny of the most of the last hundred years, including Sir W. and nided by the vast telescopic nowers at their dist



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ences of form and structure, which the same object presents when viewed with telescopes of different powers. The drawings of the same nebulæ, which have appeared in the Philosophical Transactions by Sir J. Herschel and the Earl of Rosse, supply numerous and instructive examples of this.

Plate XX. fig. 6. RA 15h 29m 9. MPD 33° 27'. Diameter, 9. RA.-Drawn by Sir J. Herschel, who describes it as a faint large round nebula, which, by attentive examination, may be seen to be composed of excessively minute stars,

appearing like points rubbed out. It is, in fact, a globular cluster.

Plate XXL fig. 2. RA 21 24 40 NPD 91 34. Diameter, & RA.—Drawn by Sir J. Herschel, who describes it as a most superb cluster of stars of the 15th magnitude, compressed towards the centre to a perfect blaze. It resembles a mass of fine luminous sand. It is resolvable with a six-inch aperture. The stars just visible with a nine-inch aperture (reflector).

Plate XXL fig. 1.—The same object as shown by the larger telescope of the Earl of Rosse. Lord Rosse thinks that no increased power is likely to alter materially its appearance. It would merely render the component stars brighter

and less closely crowded.

Plate XXI. fig. 4. RA 5^h 24^m 16^s. NPD 68° 7'. Length 4', breadth 3', ral form.—A fine object. (Sir J. Herschel.)

Plate XXI. fig. 3.—The same object as shown by Lord Rosse's telescope. A

oval form.-

considerable change of appearance is here produced by increased power, the oval resolvable nebula being changed into what the drawing represents. It is studded with stars mixed with a nebulosity, which a still higher power would evidently resolve into stars.

Plate XXII. fig. 2. RA 13h 32m 39. NPD 41° 56'. — This is, in many respects, one of the most remarkable and interesting of its class, and has been submitted to elaborate examination by all the eminent observers. The distance of the centre of the small nebula from that of the large one, is given by Messier, as 4'35", which may serve as a modulus for its other dimensions. It was described by Sir W. Herschel as a bright round nebula, surrounded by a halo or glory, and attended by a companion. Sir J. Herschel observed this object, and represented it as in the figure. He noticed the partial division of the ring as if it were split, as its most remarkable and interesting feature, and inferred that, supposing it to consist of stars, the appearance it would present to an observer, placed on a planet attached to one of them eccentrically situate towards the north preceding quarter of the central mass, would be exactly similar to that of the milky way as seen from the earth, traversing in a manner precisely similar the firmament of large stars, into which the central cluster would be seen projected, and, owing to its greater distance, appearing like it to consist of stars much smaller than those in other parts of the heavens. "Can it be," asks Sir much smaller than those in other parts of the heavens. J. Herschel, "that we have here a brother system, bearing a real physical resemblance and strong analogy of structure to our own?" Sir J. Herschel further argues, that all idea of symmetry caused by rotation must be relinquished, considering that the elliptical form of the inner subdivided portion indicates with extreme probability, an elevation of that part above the plane of the rest; so that the real form must be that of a ring split through half its circumference, and having the split portions set asunder at an angle of 45°.

Plate XXIL fig. 1. — The same object as shown by Lord Rosse's telescope. This shows, in a striking manner, how entirely the appearances of these objects are liable to be varied by the increased magnifying power and greater efficiency of the telescope through which they are viewed. It is evident that very little resemblance or analogy is discoverable between fig. 2 and fig. 1. Lord Rosse, however, says that if Sir John Herschel's be placed as it would be seen with a Newtonian telescope, the bright convolutions of the spiral shown in his own would be recognised in the appearance which Sir J. Herschel supposed to be that which would be produced by a split or divided ring. Lord Rosse further

at with each increase of optical power, the structure of this object re complicated and more unlike anything which could be supposed alt of any form of dynamical law of which we find a counterpart in The connection of the companion with the principal nebula, of is not the least doubt, and which is represented in the sketch, ada, see's opinion, if possible, to the difficulty of forming any conceivable. That such a system should exist without internal movement, he is the last degree improbable. Our conception may be aided by the idea of motion the effects of a resisting medium: but it is immagine such a system, in any point of view, as a case of mere statical Measurements he therefore considers of the highest interest, but iculty.

III. fig. 1.— This object is the 99th in Messier's catalogue. The of the nebula, represented in Plate XXII. fig. 1, was discovered by in the early part of 1845. In the spring of 1846, that represented ent figure was discovered. The spiral form is here also presented, erent character. Lord Rosse conjectures, that the nebula No. 2370, Herschel's southern catalogue, are very probably objects of a similar As Herschel's telescope did not reveal any trace of the form of this not surprising that it did not disclose the spiral form presumed to be others, and it is not, therefore, unreasonable to hope, according to p, that whenever the southern hemisphere shall be re-examined with of greater power, these two remarkable nebulæ will yield some intelts.

see has discovered other spiral nebulæ, but they are comparatively be seen, and the greatest powers of the instrument are required to the details.

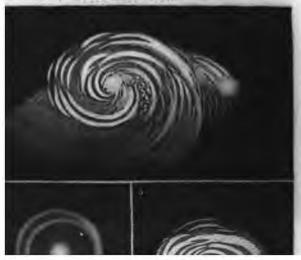
II. fig. 6. RA 9h 22m 32*. NPD 67° 45'. Length, 3'. - This is



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tails and curved filaments issued. The existence of an annulus surrounding the two nebulæ was suspected.

Plate XXIII. fig. 14. RA 11 10 2. NPD 75° 59'. Length 4'.—Described by Sir John Herschel, as large, elliptical in form, with a round nucleus, and

growing gradually brighter towards the middle.

Plate XXIII. fig. 3.—The same object as shown by Lord Rosse's telescope, 31st March, 1848. Described as a curious nebula, nucleus resolvable, having a spiral or annular arrangement about it. It was also observed with the same

results on the 1st and 3d April.

Plate XXIII. fig. 5. RA 15 1= 47. NPD 33° 35'. Length 50", breadth 20". — This nebula was not figured by Sir John Herschel, but is described by him as an object very bright, and growing much brighter towards the middle. The drawing fig. 5, represents the object as seen in Lord Rosse's telescope, in April, 1848. It is described by Lord Rosse as a very bright resolvable nebula, but that none of the component stars could be distinctly seen even with a magnifying power of 1000. A perfectly straight longitudinal division appears in the direction of the major axis of the ellipse. Resolvability was strongly indicated towards the nucleus. According to Lord Rosse, the proportion of the major axis to the minor axis was 8 to 1; much greater than the estimate of Sir John Herschel.

Plate XXIII. fig. 10. RA 12h 33m 54°. NPD 56° 30'.—Described by Sir John Herschel as a nebula of enormous length, extending across an entire field of 15', the nucleus not being well defined. It was preceded by a star of the tenth magnitude, and that again by a small faint round nebula, the whole forming a fine and very curious combination.

Plate XXIII. fig. 4.—The same object as shown by Lord Rosse's telescope on 19th April, 1849. The drawing is stated to be executed with great care, and to A most extraordinary object, masses of light appearing be very accurate.

through it in knots.

Plate XXII. fig. 10. RA6h 29m 53°. NPD 81° 74- Described by Sir John Herschel as a star of the 12th magnitude, with a bright cometic branch issuing from it, 60'' in length, forming an angle of 60° with the meridian, passing through it. The star is described as ill defined, the apex of the nebula coming exactly up to it, but not passing it.

Plate XXII. 19. 9. — The same object as seen with Lord Rosse's telescope on 16th January, 1850. Lord Rosse observed that the two comparatively dark spaces, one near the apex and the other near the base of the cone, are very

remarkable.

Plate XXII. fig. 12. RA 11^h 49°. NPD 34° 3'. Diameter 19" time.— Described by Sir John Herschel as a large uniform nebulous disk, very bright and perfectly round, but sharply defined, and yet very suddenly fading away into

darkness. A most extraordinary object.

Plate XXII. fig. 11. — The same object as shown by Lord Rosse's telescope. Two stars considerably apart, seen in the central part of the nebula. A dark penumbra around each spiral arrangement with stars as apparent centres of attraction. Stars sparkling in it and in the nebula resolvable. Lord Rosse saw two large and very dark spots in the middle, and remarked that all around its

edge the sky appeared darker than usual.
Plate XXIII. fig. 11. RA7 34m 2. NPD 104° 20' 25". Diameter 3.75" time. - Described by Sir John Herschel as a planetary nebula, of a faint equal light, and exactly round, having a very minute star a little north of the centre. Very velvety at the edges. In the telescope of Lord Rosse, however, it appears as an

annular nebula as represented in the figure, with two stars within it.

Plate XXIII. fig. 7. RA 23 17 42. RPD 48° 24' 24". Diameter 12".—Figured by Sir John Herschel, who describes it as a fine planetary nebula. With a power of 240 it was beautifully defined, light, rather mottled, and the edges the least in the world unshaped. It is not nebulous, but looks as if it had a double outline, or like a star a little out of focus. It is perfectly circular.

Plate XXIII. fig. 6. — The same object as shown in Lord Rosse's telescope, 16th-19th December, 1848. A central dark spot surrounded by a bright annulus. Plate XXIII. Ag. 9. BA 20 54 5. NPD 1020 2' 46". Diameter 10" to 12"

Herschel, but 25" by 17" according to Struve, who gives it a more.

This figure is that given by Sir John Herschel, who describes it as tary nebula with equable light and blueish white colour.

III. fig. 8.— The same object as shown by Lord Rosse's telescope.

III. jg. 8.— The same object as shown by Lord Rosse's telescope e surrounded by a ring such as that of Saturn, the usual line being of the fing.

III. fig. 13, RA 7^h 19^m 8^h. NPD 68° 45'. — Described by Sir Jeha a star exactly in the centre of a bright circular atmosphere 25' in e star being quite stellar, and not a mere nucleus, and is a most rebject.

III. fig. 12.—The same object as shown by Lord Rosse's telescope graary, 1849; described by him as a most astonishing object. It was n January, 1850, with powers of 700 and 900, when both the dark rings seemed unequal in breadth.

III. fig. 15. RA 5° 27" 7'. NPD 96° 2' 18". — The star i Orionis infeeble nebula 3' in diameter. (Sir J. Herschel.) The drawing shows with Lord Rosse's telescope.

. fig. 3. n A 19^h 52^m 12^s. N P D 67° 44′—Drawn by Sir John Herschel, bes it as a nebula shaped like a dumb-bell, double-headed shot, or the elliptic outline being completed by a more feeble nebulous light. I symmetry through the centres of the two chief masses inclined at meridian. Dismeter of elliptic light from 7′ to 8′. Not resolvable, are are visible on it of the 12th, 13th, and 14th magnitude. The ad is denser than the northern. This extraordinary object was also y Sir W. Herschel, who recognised the same peculiar form. Sir J. onsiders that the most remarkable circumstances attending it is the besity which fills up the lateral concavities of its form, and in fact coninto protuberances, so as to render the whole outline a regular ellipse, like shorter axis the compounts of the two height mass. If it is shorter axis the compounts of the two height mass.

would be as perfect as, and nearly identical with, that obtained with the greater

telescope, Plate XX. fig. 1., a lower power being used.

It will be observed that the general outline of this remarkable object which is so geometrically exact as seen with the inferior power used by Sir John Herschel, is totally effaced by the application of the higher powers used by Lord Rosse, and consequently Sir John Herschel's theoretical speculations based upon this particular form, must be regarded as losing much of their force, if not wholly inadmissible; and this is an example proving how unsafe it is to draw any thecretical inferences from apparent peculiarities of form or structure in these objects, which may be only the effect of the imperfect impressions we receive of them, and which, consequently, disappear when higher telescopic powers are applied. The case of the nebula represented in Plate XXII. figs. 1. and 2. pre-

sents another striking example of the force of these observations. Plate XX. fig. 4. RA 8^h 47^m 13^s. NPD 57° 11'. — This object, drawn by Sir J. Herschel, is the annular nebula between β and γ Lyræ. He estimates its diameter at 6.5" RA. The annulus is oval, its longer axis being inclined at 57° to the meridian. The central vacuity is not black, but filled with a nebulous light. The edges are not sharply cut off, but ill defined; they exhibit a curdled and confused appearance, like that of stars out of focus. He considers it not well represented in the drawing.

Plate XX. fig. 2. — The same object as shown in the telescope of Lord Rosse.

This drawing was made with the smaller telescope, three feet aperture, before the great telescope had been erected. The nebula was observed seven times in 1848, and once in 1849. With the large telescope, the central opening showed considerably more nebulosity than it appeared to have with the smaller instrument. It was also noticed, that several small stars were seen around it with the large instrument, which did not appear with the smaller one, from which it was inferred that the stars seen in the dark opening of the ring may possibly be merely accidental, and have no physical relation to the nebula. In the annulus near the

extremity of the minor axis, several minute stars were visible.

Plate XX. fig. 5. RA 13 28 53 NPD 107 0' 50". Diameter of faint nebula,

2'. Diameter of bright part, 10" or 15". — Described as a faint large nebula

Plate XX. fig. 7. RA 17^h 44^m 42^s. NPD 66° 52' 41". Perceptible disk 1", or 1.5" diameter. Surrounded by a very faint nebula.—A curious object. (Herschel.)

Plate XX. fig. 8. RA 19h 40m 19h. NPD 39° 54'.—A most curious object. A star of the 11th magnitude, surrounded by a very bright and perfectly round planetary nebula of uniform light. Diameter in R a 3.5", perhaps a very little

hazy at the edges. (Herschel.) Plate XX. fig. 9. RA 10^h 28^h Plate XX. fig. 9. RA 10 28 7. NPD 35° 36' 32".—A bright round nebula, forming almost a disk 15" diameter, surrounded by a very feeble atmosphere.

(Herschel.)

3389. Large and irregular nebulæ. — All the nebulæ described above, are objects generally of regular form and subtending small visual angles. There are others, however, of a very different character, which cannot be passed without some notice. These objects cover spaces on the firmament, many nearly as extensive as, and some much more extensive than, the moon's disk. Some of them have been resolved. Of those which are larger and more diffused, some exhibit irregularly shaped patches of nebulous light, affecting forms resembling those of clouds, in which tracts are seen in every stage of resolution, from nebulosity irresolvable by the largest and most powerful telescopes, to stars perfectly separated like parts of the milky way, and "clustering groups sufficiently insulated and condensed to come under the designation of irregular and, in some

ty rich clusters. But, besides these, there are also nebulæ nce, both regular and irregular; globular clusters in every condensation, and objects of a nebulous character quite which have no analogy in any other part of the heavens."* Rich cluster in the Centaur.—The star ω Centauri presents ne most striking examples of the class of large diffused It is nearly round, and has an apparent diameter equal irds of that of the moon. This remarkable object was n Mr. Dunlop's catalogue (Phil. Trans. 1828); but it is observations of Sir John Herschel, at the Cape, that the e of its splendid character is derived. That astronomer es it, beyond all comparison, the richest and largest object nd in the heavens. The stars composing it are literally ble; and as their collective light affects the eye hardly n that of a star of the fifth magnitude, the minuteness of hem may be imagined. The apparent magnitude of this such that, when it was concentric with the field of Sir J. s 20 ft. telescope, the straggling stars at the edges were e limit of the field. In stating that the diameter is twothe moon's disk, it must be understood to apply to the of the condensed cluster, and not to include the straggling ne edges. When the centre of the cluster was brought to

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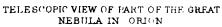
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rence to Sir J. Herschel's "Cape Observations," accompanied by

the interesting details of his observations upon it.

Sir J. Herschel describes the brightest portion of this nebula as resembling the head and yawning jaws of some monstrous animal, with a sort of proboscis running out from the snout. The stars scattered over it probably have no connection with it, and are doubtless placed much nearer to our system than the nebula, being visually projected upon it. Parts of this nebula, when submitted to the powers of Lord Rosse's telescopes, show evident indications of resolvability.

3392. The great nebula in Argo.—This is an object of the same class, and presenting like appearances; it is diffused around the star , in the constellation here named, and formed a special subject of observations by Sir J. Herschel, during his residence at the Cape. An engraving of it on a large scale, giving all its details, may be seen in the "Cape Observations." The position of the centre of the nebula is, BA 10° 38' 38", NPD 148° 47'.

This object consists of diffused irregular nebulous patches, extending over a surface measuring nearly 7' (time) in right ascension, and 68' in declination; the entire area, therefore, being equal to a square space, whose side would measure one degree. occupies, therefore, a space on the heavens about five times greater than the disk of the moon.

A part of the nebula immediately surrounding the central star is represented in Plate XXV. The space here represented measures about one-fourth of the entire extent of the nebula, in declination, and one-third in right ascension, and about a twelfth of its entire

magnitude.

No part of this remarkable object has shown the least tendency to resolvability. It is entirely compressed within the limits of that part of the milky way which traverses the southern firmament, the stars of which are seen projected upon it in thousands. Sir J. Herschel has actually counted 1200 of these stars projected upon a part of this nebula, measuring no more than 28' in declination, and 32' in right ascension, and he thinks that it is impossible to avoid the conclusion, that in looking at it we see through and beyond the milky way, far out into space through a starless region, disconnecting it altogether with our system.

3393. Magellanic clouds. — These are two extensive nebulous patches also seen on the southern firmament, the greater called the nubecula major, being included between RA 4h 40m, and 6h 0m and NPD 156° and 162°, occupying a superficial area of 42 square degrees; and the other called the nubecula minor, being included between RA 0h 21m and 1h 15m and between NPD 162° and 165a,

covering about 10 square degrees.

These nebulæ consist of patches of every character, some irre-111. 62

nd others resolvable in all degrees, and mixed with clusne, having all the characters already explained in the e large diffused nebulæ described above. So great is the distinct nebulæ and clusters crowded together in these he firmament, that 278, besides 50 or 60 outliers, have nerated by Sir J. Herschel, within the area of the nabecula e.

CHAP. XXX.

ES OF REMARKABLE ASTRONOMICAL INSTRUMENTS.

Classification of the instruments of observation. — In the pter of this book, an explanation of the principle of the on, the form, and application of the most necessary instruan observatory, is given, such as was deemed sufficient to telligible the succeeding parts of the work. The instruected for that purpose were those which seemed best o illustrate the theoretical principles afterwards developed,

THE CLUSTER IN WRIGH THE CUNIC PLACES





greatest practicable magnifying and illuminating powers, and so mounted as to enable the observer with all the requisite facility to present them to those parts of the heavens in which the objects of his observation are placed.

To attain the latter, it is necessary to provide an apparatus by which the direction of the visual line of the object of observation relatively to some fixed line and some fixed plane can be ascertained. The visual line being the straight line drawn from the eye of the observer to the object, at the moment of the observation, and having, therefore, no material tangible or permanent existence, by which it can be submitted to measurement, it is necessary to contrive some material line with which the visual line shall coincide. The telescope supplies an easy and exact means of accomplishing this. When it is directed so that the object or its centre, if it have a disk, is seen upon the intersection of the middle wires in the eye-piece, the visual direction of the object is the line drawn from the centre of the object-glass of the telecsope to the intersection of the middle wires.

Now the telescope being attached to a graduated circle is so placed, that the line joining the centre of the object-glass with the intersection of the wires is parallel to a diameter of the circle. This diameter will, therefore, be the direction of the visual line. If the circle thus arranged be so mounted that a line drawn from the observer to the fixed point of reference, whatever that point be, shall be parallel also to a diameter of the circle, and if the circle be so mounted that, however its position may otherwise be changed, one of its diameters shall always pass through the fixed point of reference, the angular distance of the object of observation from the fixed point of reference will always be equal to the angle formed by the two diameters of the circle, one of which is parallel to the line joining the centre of the object-glass, with the intersection of the wires at the moment of the observation, and the other parallel to the line drawn from the observer to the fixed point of reference.

But this is not yet enough to determine in a definite manner the position of the object on the heavens. A great many different objects may have the same angular distance from the fixed point of reference. If a plane be imagined to pass at right angles to a line drawn from the observer to the fixed point of reference, it will intersect the celestial sphere in a certain circle, every point of which will obviously be at the same angular distance from the point of reference. To render the position of the object of observation determinate, it is therefore necessary to know the position of the plane of the graduated circle, with relation to a circle whose plane is at right angles to that diameter of the celestial sphere which passes through the fixed point of reference.

The plane of the graduated circle may be fixed or moveable.

position with relation to the fixed point of reference is d once for all; after which, the position of the object of m will be determined merely by its angular distance from of reference. If moveable, it is necessary to provide raduated circle, the plane of which is perpendicular to the upon which some fixed direction is marked. The position ane of the moveable circle, which carries the telescope, ion to this latter fixed direction, is then ascertained by the second graduated circle, which is included between the circle and such fixed direction.

struments of observation for determining the position of the celestial sphere are constructed and mounted on one of these principles; and they differ one from another in the point adopted as the fixed point of reference, and the right angles to the diameter of the sphere passing through t with relation to which the position of the circle, if it be, is determined.

ed point of reference is, in all cases, either the zenith or and the plane of reference, consequently, either that of on or the equator.

the plane of the graduated circle carrying the telescope is



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ASTOR, LENOX AND

SIR W. HERSCHEL'S GREAT TELESCOPE.



THE LESSER ROSSE TELESCOPE.

XXVIII.

Focal length 27 f. Aperture 3 f.



ries made with it by its illustrious inventor and constructor, is represented in Plate XXVII. It will be seen in the drawing that the instrument is mounted on a platform which revolves in azimuth on a series of rollers. The telescope is placed between four ladders, which serve the double purpose of a framework for its support and a convenient means of approaching the superior end of the great These ladders are united at the top by being bolted to a By one system of cross bar, to which the pulleys are attached. pulleys, the telescope is raised or lowered; and by another the gallery or balcony in which the observer stands is also raised or lowered, so as to enable him to look into the tube. These pulleys are each worked by a windlass established on the platform below. The framing is strengthened by another system of diagonal ladders, as well as various masts and braces which appear in the figure. The telescope is so mounted that it can be raised until its axis is vertical, so that an object in the zenith can be observed with it. server's gallery rests in grooves upon the ladders, and slides up and down easily and smoothly by the operation of the pulley, so that when the telescope tube is elevated, even to the zenith, the observer can ascend and descend at pleasure by signals given to the man at the windlass. A small staircase is placed near the foot of one of the principal ladders, by which observers can mount into the gallery when it is let down to its lowest point.

The total length of the telescope tube is 39 ft. 4 in., and its clear diameter 4 ft. 10 in. It is constructed entirely of iron. The great speculum is placed in the lower end of the tube, the apparatus for adjusting it being protected by the wooden structure which appears in the figure. The diameter of the speculum is 4 ft., and the magnitude of its reflecting surface is consequently 12.566 square feet.

It contains 1050 lb of metal.

The axis of the speculum, when placed in the tube, is so inclined to the tube that its focus is at about two inches from the lower edge of the upper mouth of the tube, so that the observer, standing in the gallery with his back to the object, and looking over the edge of the tube towards the speculum, can direct an eye-piece conveniently mounted at that point upon the image of the object of observation formed by reflection in the focus.

Three persons are employed in conducting the observations: the observer, who stands in the gallery; his amanuensis, who may either be in the gallery or in the wooden house below, receiving the dictation of the observer by a speaking tube; and the person

who works the windlass.

3396. The lesser Rosse telescope. — This instrument, with its mounting, is represented in Plate XXVIII. The arrangements are so similar to those of the Herschelian instrument described above, that they will be easily understood from the Plate without

scription. The speculum is 3 feet aperture, and it reflecting surface. The length of the telescope is erected upon the pleasure-grounds at Parsonstown it its illustrious constructor. The weight of metal is about 13 cwt.

The greater Rosse telescope.—This stupendous instill investigation, by far the largest and most powerful, is represented in Plates XXIX. and XXX. from for this work under the superintendence of his Letter Plate XXIX. presents a North, and Plate X. wof the instrument.

ear aperture is 6 ft., and consequently the magnit ing surface is 28.274 square feet, being greater the el's great telescope in the ratio of 7 to 3.

ers great telescope in the ratio of 7 to 5.

Instrument is at present used as a Newtonian tell hat is to say, the rays proceeding along the axis ulum are received at an angle of 45° upon a second

by which the focus is thrown towards the side of the eye-piece is directed upon them. Provision is, he se the instrument also as an Herschelian telescope, at tube is supported at the lower end upon a n joint of cast-iron, resting on a pier of stone-work bu



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THE GREAT ROSSE TELESCOPE,









also attained, and with greater precision, by a 20-inch circle attached to the instrument.

Two specula have been provided for the telescope, one of which contains 31, and the other 4 tons of metal, the composition of which

is 126 parts in weight of copper to 571 of tin.

The great tube is of wood hooped with iron, and is 7 feet diameter, and 52 in length. The side-walls, 12 feet distant from the tube, are 72 feet in length, 48 feet in height on the outside, and 56 feet in the inside. These walls are built in the plane of the meridian.

The observer stands in one or other of four galleries, the three highest of which are drawn out from the western wall, while the fourth or lowest has for its base an elevating platform, along the surface of which a gallery is moved from wall to wall by a mechanism at the command of the observer.

3398. The Oxford heliometer. — This class of instrument, which derives its name from having been first applied to the measurement of the diameter of the sun, consists of a telescope equatorially mounted, the object-glass of which is divided along a plane passing through its optic axis, each half of the lens being capable of being moved in its own plane, so that the axes of the two semi-lenses, being always parallel to each other and to the axis of the telescope, may be within certain limits separated from each other, more or less, at the pleasure of the observer.

From what has been explained in general of the structure of an equatorial instrument (2336), and from the drawing of this instrument given in Plate XXXI., the provisions for the direction of the telescope in right ascension and declination will be easily comprehended. The polar axis, round which the instrument turns in right ascension, is fixed upon the face of a block of Portland stone, and the graduated circle measuring right ascension is seen at the top and at right angles to the polar axis. This circle receives its motion in the usual way, from clockwork, which is attached to the stone pier, and which, with its impelling suspended weight, is seen in the drawing. Rods are provided by which the observer can, at pleasure, set the clock going, or stop it, and connect it with, or disengage it from, the equatorial circle.

The circle for indicating polar distance or declination is placed upon the horizontal axis of the instrument, and also appears in the drawing at the side opposite to that at which the telescope is attached.

The object-glass of this instrument, sometimes called the "divided object-glass micrometer," supplies a very accurate method of measuring angles which do not exceed a certain limited magnitude.

It appears by the principles of optics, that when the image of a distant object is produced by a lens, each point of such image is formed by rays which proceed from every point of the lens. If,

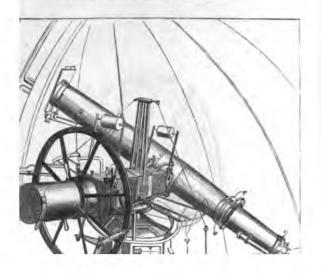
a part of the lens be covered by an opaque body or cut point of the image will still be formed by the rays which m every point of the lens which is not covered or cut away. difference which will be observed in the image will be, be less strongly illuminated, being deprived of the rays eceived from the part of the lens covered or cut away, and be less distinct in consequence of certain effects of difnich need not be noticed here. vs, therefore, that half a lens will produce at the focus an a distant object, and if two halves of the same lens be icentrically, they will form two images, the exact superwhich will, in fact, constitute the image formed by the ens. But if the two halves be not concentrical, the imnot be superposed, but will be separated by a space corwith, and proportional to, the distance between the the two half lenses. Thus, if the lenses be directed to wo images of the solar disc will be produced at the focus ses, and these images may be shifted in their positions, the proaching to, or receding from, one another, according as s of the two half lenses approach to, or recede from, each d if the angular distance through which either image he known it is easy to see how by this means the an



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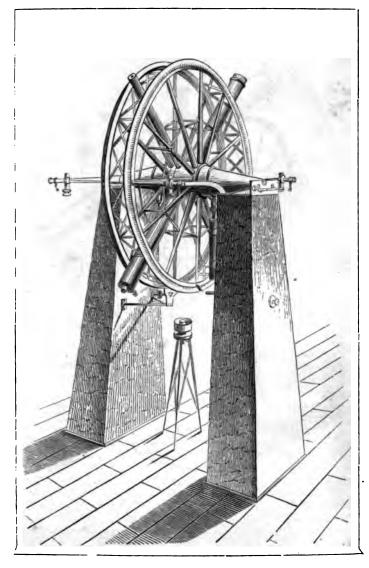
THE OXFORD HELIOMETER.





TROUGHTON'S TRANSIT CIRCLE.

XXXII.





the centres of the semi-lenses, and consequently the angular distance between the two images, is measured according to a known scale by the number of turns and parts of a turn of the screw which are necessary to produce the separation or to bring back the semi-lenses to a concentrical position, if they are separated.

It is obvious, that the same principle will be applicable to measure the apparent angular distance between any two objects, such as two stars, which are so near each other that they may be seen together in the field of view of the telescope. For this purpose, let the semi-lenses be first placed concentrically. The two stars s and s' will then be seen in their proper positions in the field. Let the semi-lenses be then moved so that two images of each star will be visible. Let the motion be continued until the image of the star s by one semi-lens coincides with the image of the other star s' by the other semi-lens. The angular distance corresponding to the separation of the lenses will then be the angular distance between the stars.

In this heliometer a very ingenious contrivance is introduced to enable the observer to read the scale by which the angular magnitude corresponding to the separation of the centres of the semilenses is indicated. This is accomplished by placing a scale behind the object-glass in the interior of the telescope tube, so that it can be read by means of a long microscope, the eye-glass of which is placed near the eye-piece of the telescope. This interior scale is illuminated by a piece of platinum wire placed near it, which is rendered incandescent by a galvanic current transmitted upon it at pleasure by the observer. This current is produced by a Smee's battery placed in a room below that containing the heliometer.

A very splendid instrument of this class has been erected at the

Pultowa observatory.

3399. The transit circle, by Troughton. — This instrument, which is represented in Plate XXXII., unites the functions of the mural circle and the transit instrument. The telescope is fixed between two parallel flat metallic circles or rings, the exterior face of each of which is graduated to 5'. These flat rings are connected with the horizontal axis, by two sets of radial hollow cones, so as to form two wheels, and they are connected with each other by various bars, crossing each other so as to form rhomboidal figures, as well as by a system of perpendicular rods, which appear in the figure. Each of these rings is 4 feet in diameter. The horizontal axis, which receives the spokes of each of the wheels, is cylindrical between the wheels, the parts projecting beyond them being strong cones, which rest in Ys fixed on two piers of solid stone-work, 5 feet 6 inches in height, and a little less than 3 feet apart. The length of the horizontal axis is 3 feet.

The faces of the stone piers coincide with the plane of the me-

he Ys are provided with adjustments, one of which is raising and lowering the Y, and the other of moving it ly through small spaces. When the instrument is placed upports, the line of collimation of the telescope will play the meridian, and it will be made to do so exactly, by the adjustments, according to the method explained in the e transit instrument (2398), et seq.

aduated faces of the two circles are surrounded by four or roscopes, by which the observation is read off in the same and subject to the same conditions as have been already

in the case of the mural circle (2408), et seq.

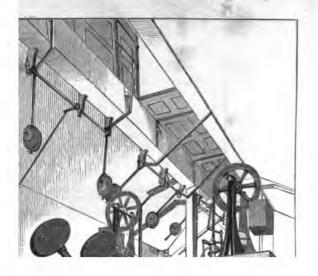
The Greenwich transit circle. — The great mural circle ansit instrument have lately been superseded at the Royal ry, Greenwich, by an instrument upon the principle of described, but constructed upon a vast scale of magnitude, ined with a variety of accessories by which its stability and ary precision of its indications are secured.

pective view of this instrument is presented in Plate, made from original drawings taken by permission of the er Royal.

found, by the results of observations made with the great

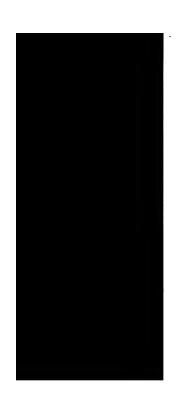


GREENWICH TRANSIT CIRCLE.



POLTOWA PRIME VERTICAL INSTRUMENT.

XXXIV.





es of the telescope, when it was found that this quantity did not eed the thousandth of an inch.

The parallel circles between which the telescope is fixed, are each eet in diameter, and are firmly attached to cylindrical bands, one each side of the central cube of the telescope. The clamping paratus is applied to the eastern circle, and the western circle is duated. The reading-off is effected by means of six microscopes,

h 45 inches in length.

The graduation of the circle is such as to show approximately iith distances; while a pointer fixed to a block projecting from lower part of the pier, directed to another graduated band on outer or eastern side of the circle, is used for setting the telepe, and gives approximately north polar distances. A small der, with a large field of view, is attached to the side of the cone or the eye-piece, as well as sights for directing the telescope to rs by the naked eye.

A large gas-light conveniently placed illuminates, by means of lectors, the graduated are of the circle at the points where the eral microscopes are fixed, and also the field of the telescope.

A variety of other provisions and adjustments are attached to the trument, which it would be impossible to render clearly intellile without reference to the instrument itself, or very detailed and borate drawings of its several parts, which our limits do not mit us to introduce here.

3401. The Pultowa prime vertical instrument.—This instrument y be summarily described as a transit, whose line of collimation ves in the plane of the prime vertical, instead of that of the meian. Nevertheless, its astronomical uses are essentially distinct

m those of the transit instrument (2397).

The first instrument made on this principle was erected, in the ginning of the last century, under the direction of the celebrated emer, whose name is rendered memorable by the discovery of the bility of light (2959). It was applied by that astronomer chiefly observations on the sun near the equinoxes; but none of the rposes to which it has more recently subserved appear to have en contemplated, and the instrument was allowed to fall into Its revival, and the idea of its application to various imrtant classes of observations in the higher departments of practical ronomy, and more especially to replace the zenith sector in obsertions having for their object the more exact determination of erration and nutation, and for researches in stellar parallax, is due Many of the improved details of construction Professor Bessel. hibited in the Pultowa instrument are, however, due to Professor rave, who, besides, has obtained such remarkable results by the stem of observations which he has made with it.

The Pultows prime vertical instrument was constructed, under

on of Professor Struve, by Messrs. Repsold, of Hamburg. It piers being erected in planes at right angles to the vertical chairs are fixed upon the summits in such a nat the line joining them is in the plane of the meridianirs are the supports of the cylindrical extremities of the axis of the instrument, which is, therefore, also in the meridian. The extremities of this axis project beyond and the piers on each side, and the transit telescope is to one of them, while a counter-weight is keyed on to the he telescope, having its line of collimation adjusted at es to the horizontal axis, revolves with this axis outside, in the same manner exactly as the transit telescope between its piers; and as the line of collimation of the ves in the plane of the meridian, that of the transit telesche present instrument moves in the plane of the prime

ments are provided in connection with the two chairs, one raises and lowers the axis, and the other moves it in azinilar exactly to those described in the case of the transit (2399), et seq. By these means, and by proper levels, is rendered truly horizontal, is brought exactly into the the meridian, and the line of collimation is brought to with the plane of the prime vertical by other expedients, a principle to those adopted in the case of the transit at.

strument, mounted on the piers, is represented in Plate

the telescope, and a counterpoise to it is represented on the inside. The process of reversion of the horizontal axis, which in the transit instrument is only used for the purpose of adjustment (2400), constitutes, in the case of the prime vertical instrument, an essential part of every observation. It was, therefore, of the greatest importance that an easy, expeditious, and safe apparatus for reversion should be provided. This was contrived with great ingenuity by the makers, and attended with the most successful results—results to which M. Struve ascribes a great share of the advantage obtained A part of this apparatus, by which the horiby this instrument. zontal axis, with the telescope, counterpoise, and their accessories. is elevated from the chairs, is represented in the drawing above the instrument. The two cords of suspension being attached by hooks to two points on the axis at equal distances from its centre, so as to maintain the equilibrium, the instrument is elevated by means of a windlass established on the floor below it and between the piers. When raised to the necessary height, it is turned through half a revolution in azimuth, so that the ends of the axis are brought

directly over the chairs, into which they are then let down. perfect is the performance of this apparatus, that notwithstanding the magnitude and weight of the instrument, the whole process of reversion is completed in sixteen seconds; and the interval, from the moment the observer completes an observation with the telescope on the north side, to the moment he commences it on the south side, including the time of rising from the observing-couch, disengaging the clamps, withdrawing the key from the micrometer, reversing, directing the instrument on the south side to the object by means of the finder, closing the clamps, returning the key to the micrometer, and placing himself on the observing-couch, is only 80

seconds. How essential to the practical use of the instrument this celerity is, will be understood when it is stated, that the same object which has been observed on one side must be also observed on the other The reversion, therefore, must be completed in the same transit. in less time than that which the object takes by the diurnal motion to pass over the space commanded by the field of the telescope in the two positions.

To comprehend the method of applying this instrument to the purposes of practical observation, it is necessary to remember that it is only applicable to objects moving in parallels of declination which intersect the prime vertical. Such objects must have northern declination (the instrument being supposed to be established in a place having a north latitude), and a polar distance greater than that of the zenith of the observatory, that is to say, greater than its colatitude. The parallels over which such objects are carried by the

ПI.

tion, all intersect the prime vertical at two points of equal in on the eastern, and the other on the western, quadrant ide. In passing from the east point of intersection to the the object passes over the meridian, and it is evident noment of its meridional transit is precisely the middle rval between its two prime vertical transits. If, therexact times of the latter be observed, the time of the meansit can be deduced by a simple arithmetical process. are the instruent for observation, let the polar distance are the instruent for observation, let the polar distance oct about to be observed be taken from the Tables. Let ressed by \$\alpha\$; let the co-latitude of the observatory, or, a same, the polar distance of the zenith, be \$\alpha\$; and let the tance which the object must have when it comes on the ical, be \$\alpha\$. These three arcs, \$\alpha\$, \$\alpha\$, and \$\alpha\$, form a righterical triangle, the right-angle being included by \$\alpha\$ and \$\alpha\$. gle at the pole, or the hour angle, be \$\alpha\$. We shall then, mentary principles of trigonometry, have

cos.
$$z = \frac{\cos \cdot \alpha}{\cos \cdot \lambda}(1);$$
 cos. $h = \frac{\tan \cdot \lambda}{\tan \cdot \alpha}(2).$

formula (1), the zenith distance of the points at which

prime vertical will be found by taking a mean between the times of the transits over all the wires at both sides. If this time be expressed by T', we shall then have

$$\mathbf{r}' = \frac{\mathbf{r}_1 + \mathbf{r}_2 + \ldots + \mathbf{r}_7 + t_7 + t_6 + \ldots + t_1}{14}.$$

These observations being completed, the observer awaits the transit of the object over the western quadrant of the prime vertical, when he makes a similar series of observations on the transits, first with the telescope on the south side, in the position it had at the last observation, and then, after reversion, at the north side. The true moment of the transit is found, in this case, in the same manner as in the former.

By taking a mean of these two means, or, what would be equivalent, a mean of the times of all the twenty-eight transits, the time of a meridional transit will be obtained.

The total length of the interval, necessary to observe the transits over the wires, north and south, in each quadrant of the prime vertical, is found to be about eleven minutes, less than 1½ minute of which is employed in the reversion of the instrument and attendant arrangements.

The time which elapses between the observations on the eastern and western quadrants of the prime vertical, will necessarily vary with the polar distance of the object, and will be less in proportion as excess of that distance above the co-latitude is less. The observations which have been made with this instrument at Pultowa, have been chiefly confined to stars whose polar distance exceeds the co-latitude by less than 2°. In that case, the interval between the observations, east and west, would be less than three hours.

Professor Struve notices, in strong terms, the advantage which this instrument possesses over others in respect to the errors arising from the variation of the inclination of the line of collimation to the axis of rotation. In the prime vertical instrument, the deviation of the line of collimation from true perpendicularity to the axis of rotation, is assumed to be invariable only during the short interval of a single observation, whereas, in other instruments, its invariability is assumed for twelve hours, and in some cases for months, and even years. It has the further great advantage, that, by reversion in each quadrant, east and west, all optical imperfections which affect the precision of the image of the star are absolutely annihilated.*

[•] For a detailed account of the Pultowa prime vertical instrument, see Description de l'Observatoire Astronomique de Pultowa, par F. G. W. Struve. Also Astronom. Nachrichten, No. 488, et seq.

roughton's altitude and azimuth circle. — The form of best adapted to render the principle of altitude and astruments in general intelligible, is that which is repre-Plate XXXV. This circle was originally constructed by for the Royal Academy of St. Petersburg; but, at the e invasion of Russia by the French, the fear that Peterst be exposed to the same disasters as Moscow, induced a authorities to relinquish their claim on the instrument, seed into the hands of Dr. Pearson, at whose private y, at Kilworth, it was erected. Owing to the indispolation, the graduation of the limbs was executed by

wing presents the circle so that all the important parts is is is. The instrument is supported on the capstone of a ne pedestal. Upon this, the fixed parts of the instruous which it revolves in azimuth, are firmly established, ist of a solid vertical cone, terminating below in an hexad mass of metal, each vertical face of which measures 3 are. From this proceed four radial cones, three of which, of 120° with each other, are supported on the stone by feet supplied with adjusting screws, by means of which ment is levelled. The fourth radial cone, which forms an 50° with two of the others, carries a clamp, which will be noticed.

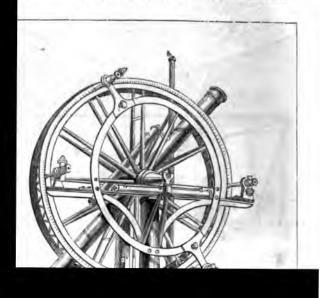


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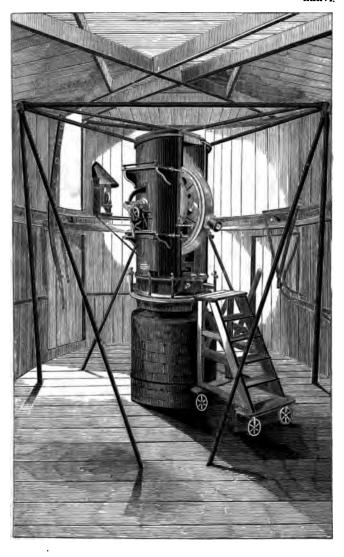
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IGHTON'S ALTITUDE AND AZIMUTH CIRCLE.



GREENWICH ALTAZIMUTH INSTRUMENT.

XXXVI.





inserted in a square hole of corresponding magnitude, connected by an universal joint with a rod of convenient length, which the observer holds at the moment of the observation, and by turning which the whole instrument is moved slowly in azimuth.

The vertical circle consists of two parallel limbs, having the telescope between them, constructed and connected in a manner exactly similar to the transit circle already described; and this circle is supported on the two vertical pillars in the same manner exactly, as already described in the case of the transit circle (3399).

One only of the two vertical circles is graduated, being divided as well as the horizontal circle to 5'. The clamp, with its tangent screw, is placed on the side not graduated. The focal length of the

telescope is 44.4 inches, and its aperture 31 inches.

The observations of altitude are read off by four microscopes, the supports of which are shown in the figure. Two are supported by arms attached to the vertical pillar on the graduated side of the circle, and the other two to a hoop screwed on the pillar and to the arms which carry the two former.

The instrument is provided with a plumb-line and four levels, by which its proper position with relation to the vertical direction can

be always verified.

3403. The Greenwich alt-azimuth instrument. - This, as the name imports, is an altitude and azimuth circle in principle similar to that just described, but in its construction and application different from any instrument of its class hitherto constructed. purpose chiefly to which it is applied, and with the view to which it was conceived by the Astronomer Royal, is the improvement of the lunar theory by multiplying in a large ratio the observations which can be made from month to month on the moon, without in any degree impairing their precision. Such observations were always made with the mural circle and the transit, until this instrument was brought into operation, and they were consequently confined to the meridional transits of the moon. Now, these transits cannot be observed, even when the firmament is unclouded, for four days before and four days after the new moon, in consequence of the proximity of that body to the sun; an interval amounting to little less than one-third of the month. Besides this, it happens, in this climate, that, at the moment of the meridional transits at other parts of the month, the observation is frequently rendered impracticable by a clouded sky. It was, therefore, highly desirable to contrive some means of making the observations in extra-meridional positions of the moon.

This could obviously be accomplished by means of an altitude and azimuth circle, such as that described above; but such an instrument, however perfect might be its construction, is not susceptible of the necessary precision. The Astronomer Royal, there-

ASTRONOMY.

lived the idea of an instrument on the same principle, ile it would be capable of shifting its azimuth, would still ible of as much precision in each vertical in which it placed, as the mural circle has in the meridian. He acproposed to attain this object by adopting adequate engineedients to produce the necessary solidity and invariability He adopted, as fundamental principles of construction,—

oroduce as many parts as possible in a single casting; use no small screws for combining the parts; illow no power of adjustment anywhere.

ng out these principles, the instrument represented in LXVI. was constructed, under his superintendence, by ansome and May, engineers, of Ipswich; the graduation cuted by Messrs. Troughton and Simms: and the first n with it was made by Mr. Hugh Breen, jun., one of the nt the Observatory, on the 16th of May, 1847, which was be as good as any succeeding observation.

strument is mounted in a tower, raised to such a height as nd the horizon in all directions above the other buildings servatory, except on the side of the south-east dome and to the instrument so as to revolve with it. Their reflectors are

illuminated by a lamp properly placed.

The lower pivot on which the instrument turns, is supported on a point in the stone pillar at the centre of the azimuthal circle. To support the upper pivot, an iron triangle is established on the three-rayed pier. On each side of this is erected another iron triangle, whose plane is vertical, and whose sides unite in a vertex which forms one of the angles of a corresponding triangle above. This upper triangle supports three radial bars, which carry at their point of union the Y in which the upper pivot plays. The bars of the lateral triangles, which are apparent in the drawings, pass the holes in the floor without touching it.

The frame, revolving in azimuth and carrying the instrument with it, consists of a top and bottom connected by vertical cheeks, all of cast iron. The supports of the four microscopes for reading off the azimuth on the lower circle are cast in the same piece with

these vertical cheeks.

The vertical circle carrying the telescope is 3 feet in diameter, and, like the azimuth circle, is made of hard gun-metal. The aperture of the object-glass is 3\frac{3}{2} inches. The top and bottom of the instrument each carries two levels, parallel to the plane of the vertical circle.

The dome over the instrument is cylindrical, with double sides, between which the air passes freely. Its diameter is 10 feet.

The drawing represents the instrument as in use. The ladder revolves in azimuth, with the instrument, round the central pier,—to facilitate which motion, rollers are placed under it. Two boards are attached to the revolving frame, having their edges in a plane parallel to that of the vertical circle. The eye being directed along these to view the object, the instrument is placed very nearly in the proper azimuth, and the telescope is then accurately directed to the object by the ring-finder. These boards are omitted in the drawing.

The drawing has been reduced from an engraving prefixed to the "Greenwich Observations for 1847," which, however, was originally

published in the "Illustrated London News."

The results of the observations made with this instrument are stated to have fulfilled all the anticipations of the Astronomer Royal, as well as to the number of observations as to their excellence. At least twice the number have been made, and of equal goodness with those formerly made with the meridional instruments. Some have been made even with a day of conjunction; and Mr. Main, the chief assistant at the Observatory, has expressed his conviction that in a few years observations with this instrument will remove all the deficiencies which still remain in the lunar theory.

ASTRONOMY.

The Northumberland telescope — Cambridge observatory. e Duke of Northumberland, who filled during the latter s life the high and honourable office of Chancellor of the of Cambridge, presented to that university this instruch, successively in the hands of the Astronomer Royal ssor Challis, has contributed so effectually to the advancestronomical science. strument, of which a perspective view is given in Plate ., together with a view of the building in which it is usists of a refracting telescope of 19½ feet focal length, nobes aperture equatoreally mounted. The polar axis, as the drawing, consists of a system of framing composed ong deal poles, attached at the ends to two hexagonal cast iron, the centres of which support the upper and ots on which the telescope revolves. These poles at the e braced by transverse iron bands, and by a system of ods of deal abutting near the middle of the poles. sess to the entire framing of the polar axis, and maintain onal frames square to it. Efficient means are provided to city to the supports of the pivots and smoothness to the motion.

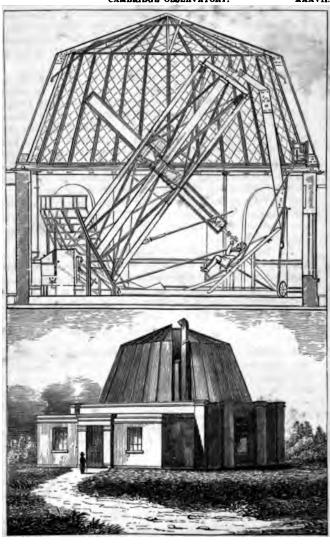
be of the telescope is made of well-seasoned deal, and



NORTHUMBERIAND EQUATORIAL.

CAMBRIDGE OBSERVATORY.

XXXVII.





through a limited space upon the hour circle. The rate of motion given to the hour circle by the clock is not affected by this movement. The hour circle, therefore, going according to sidereal time, small differences of right ascension can be measured by reading off the angles pointed to by the moveable index before and after the changes of position.

The dome which covers the instrument, and which, as well as the other details of its erection, was constructed under the direction of the Astronomer Royal, who was then the Cambridge astronomer, is supported so as to revolve on free balls between concave channels, holdfasts of peculiar construction being provided to obviate the eventuality of the dome being dislodged or blown off by wind or any other unusual disturbance. The winch which acts on the machinery for turning the dome, is carried to the observer's chair, so that he can, while engaged in a long observation, turn the dome slowly without removing from his position.

The magnitude of the instrument, and the consequent extensive motion of the eye-piece, rendered it necessary to contrive adequate means by which the observer could be carried with the eye-piece by a common motion without any personal derangement which might disturb the observation. This is accomplished by means of an ingenious apparatus consisting of a frame, of which the upper edge is nearly a circular arc whose centre is the centre of the telescope. which frame travels horizontally round a pin in the floor exactly below the centre of the telescope, the observer's chair sliding on the The observer can, by means of a winch placed beside his chair, turn round the frame on which the chair is supported, and by means of a lever and ratchet wheel he can raise and lower the chair on the frame. He has also means of raising and depressing the back of the chair so as to give it the inclination he may at the moment find most convenient.





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